

# Reliability of Marine Structures Program

**WAVEMAKER 2.0:**

## **SIMULATION AND IDENTIFICATION OF SECOND-ORDER RANDOM WAVES**

**Alok K. Jha  
Steven R. Winterstein**

*Civil Engineering Department, Stanford University*

**Supported by**  
*Office of Naval Research · Stanford RMS Program*

**June 1996  
Report No. RMS-22**

**DISTRIBUTION STATEMENT A**  
Approved for Public Release  
Distribution Unlimited

**20011123 056**



**Department of CIVIL ENGINEERING  
STANFORD UNIVERSITY**

**WAVEMAKER 2.0:**  
**SIMULATION AND IDENTIFICATION OF**  
**SECOND-ORDER RANDOM WAVES**

**Alok K. Jha**  
**Steven R. Winterstein**

*Civil Engineering Department, Stanford University*

**Supported by**  
*Office of Naval Research · Stanford RMS Program*

**June 1996**  
**Report No. RMS-22**

# Acknowledgments

These simulation and identification analysis capabilities have been developed by the first author during the course of his ongoing Ph.D. studies. Early portions of these studies were supported principally by the industry sponsors of the Reliability of Marine Structures Program of Stanford University.

Most recent developments have been funded by the Office of Naval Research, grant N00014-95-1-0366, under the supervision of Dr. Peter Majumdar, and grant N00014-96-1-0641, under the supervision of Dr. Roshdy S. Barsoum. These developments have included spatial modeling of nonlinear waves, for application to stochastic ship load and response calculation, and identification analysis capabilities, for application to offshore structural analysis.

We gratefully acknowledge these sources of support.



# Table of Contents

<b>Acknowledgments</b>	<b>iii</b>
<b>List of Figures</b>	<b>vii</b>
<b>Abstract</b>	<b>viii</b>
<b>1 Introduction to WAVEMAKER 2.0</b>	<b>1</b>
<b>2 Simulation of Second-Order Random Waves</b>	<b>3</b>
2.1 Introduction . . . . .	3
2.2 Methodology . . . . .	4
2.2.1 Underlying Theory and Assumptions . . . . .	4
2.2.2 Implementation . . . . .	6
2.2.3 Multiple Spatial Locations . . . . .	7
2.3 Input Specification . . . . .	8
2.3.1 Wave Spectrum Specification . . . . .	10
2.4 Output Format . . . . .	11
2.4.1 Time History Output . . . . .	12
2.4.2 Wave Statistics Output . . . . .	12
2.5 Example . . . . .	13
<b>3 Identification of First-Order Waves</b>	<b>17</b>
3.1 Introduction . . . . .	17
3.2 Methodology . . . . .	18
3.2.1 Newton-Raphson Scheme . . . . .	21
3.2.2 Convergence Criteria . . . . .	21
3.2.3 Implementation . . . . .	22
3.3 Input Specification . . . . .	23
3.4 Output Format . . . . .	25
3.5 Examples . . . . .	25
3.5.1 Example 1 . . . . .	26
3.5.2 Example 2 . . . . .	27

<b>4</b>	<b>Distribution</b>	<b>31</b>
4.1	Copying the Diskette . . . . .	31
4.2	Compiling the Source . . . . .	32
4.3	Executing the Routine . . . . .	33
	<b>List of References</b>	<b>35</b>
<b>A</b>	<b>Output Files for Simulation Example</b>	<b>37</b>
<b>B</b>	<b>Input/Output Files for Identification Example</b>	<b>41</b>
<b>C</b>	<b>Random Models of Second-Order Waves and Local Wave Statistics</b>	<b>45</b>

# List of Figures

2.1	Simulated wave time histories at specified spatial locations . . . . .	4
2.2	Simulated first- and second-order wave histories at location 0.0 . . . .	15
2.3	Simulated second-order wave histories at location 0.0 and 60.0 . . . .	15
3.1	Identification of first-order wave components is done in contiguous win- dows of the observed history . . . . .	23
3.2	Wave spectrum: observed vs. identified first- and second-order . . . .	28
3.3	Wave history: observed vs. identified first- and second-order . . . . .	28
3.4	Identified first-order vs. actual first-order wave history . . . . .	29
3.5	Wave history in wave tank: observed vs. identified first- and second-order	30
3.6	Wave spectrum in wave tank: observed vs. identified first- and second- order . . . . .	30

## Abstract

WAVEMAKER is a FORTRAN subroutine to simulate random non-Gaussian ocean wave histories. It generates a first-order (Gaussian) wave process with an arbitrary power spectrum, and applies nonlinear corrections based on second-order hydrodynamics. Inputs to the routine include the first-order spectrum, the water depth, and a set of locations in the along-wave direction at which wave elevation histories are desired. It may thus provide useful input to estimate loads on spatially distributed ocean structures and ships.

The WAVEMAKER package also includes a separate driver program, which facilitates input/output and generates several analytical spectral models. Its input is specified in command-line format, similar to that of the TF-POP program for hydrodynamic post-processing also developed in the Stanford RMS program. An example problem is included to demonstrate the use of WAVEMAKER and its driver.

In terms of methodology, WAVEMAKER first uses standard frequency domain methods to generate first-order Gaussian histories at each location. For each of these, WAVEMAKER then evaluates the full set of second-order corrections according to hydrodynamic theory. Thus the first-order wave process, with  $N$  components at frequencies  $\omega_n$ , gives rise to a total of  $N^2$  corrections, spread over all sum frequencies  $\omega_n + \omega_m$ , and to another  $N^2$  corrections over all difference frequencies  $\omega_n - \omega_m$ .

WAVEMAKER also includes the ability to identify the underlying first-order Gaussian history from a given observed time history. This feature is particularly attractive for use in situations where the second-order non-linearity in the waves is built-in into the structural response calculations. To avoid double-counting therefore, the input waves should be filtered to remove any second-order nonlinearity. WAVEMAKER takes in an input wave history and identifies its first- and second-order wave components. This identification, an inverse feature to simulation, is based on a Newton-Raphson scheme to solve  $N$  simultaneous nonlinear equations to identify the first-order waves which, when run through the second-order wave predictor, matches the observed waves.

## Chapter 1

# Introduction to WAVEMAKER 2.0

This release of WAVEMAKER software incorporates a major recent development achieved at the Reliability of Marine Structures Program. This is the ability to successfully identify the underlying first-order wave components for given target observed wave histories. WAVEMAKER 2.0 is fully backward compatible, that is, results from a run of earlier versions of WAVEMAKER can be exactly obtained with this new release. The input files to earlier versions can be directly used in this new version. A version history of WAVEMAKER follows:

- **Version 1.0:** Released in April 1995 and documented in Jha and Winterstein, 1995, Report RMS-17, contains simulation capabilities for second-order random waves.
- **Version 1.1:** Released in August 1995, includes modification of temporary intermediate output file to use less disk space and to reduce program execution time by approximately 50%. Additionally, a DOS executable of WAVEMAKER was included in this release.
- **Version 2.0:** Released June 1996, includes identification capabilities so that underlying first-order wave history can be retrieved from an observed wave history.

In this report, Chapter 2 includes a documentation of the simulation capabilities and is largely taken from Report RMS-17. Chapter 3 documents the newly developed identification analysis capabilities, and the appendices include sample input and output files for the simulation and identification examples presented in this report.



## Chapter 2

# Simulation of Second-Order Random Waves

### 2.1 Introduction

It is common in many ocean engineering problems to seek to simulate a time trace of the wave elevation process,  $\eta(t)$ , at one or more locations in the along-wave direction. It is most typical to use a *Gaussian* model of  $\eta(t)$  for this simulation, which is consistent with linear wave theory. This is due primarily to the ease of simulating Gaussian processes, e.g. with FFT (Fast Fourier Transform) methods for an arbitrary wave spectrum (e.g., Borgman, 1969).

We seek here to demonstrate and facilitate a similar frequency-domain simulation capability for *nonlinear* random waves at a set of spatial locations (e.g., Figure 2.1). These simulations split the wave elevation into a random first-order (linear) wave history,  $\eta_1(t)$ , and a corresponding nonlinear history  $\eta_2(t)$  which includes second-order corrections. FFT techniques are used to generate  $\eta_1(t)$  with an arbitrary (first-order) wave spectrum,  $S_{\eta_1}(\omega)$ . Physical principles are used to generate  $\eta_2(t)$  from  $\eta_1(t)$ , based on second-order perturbation analysis of the underlying nonlinear hydrodynamic problem. Thus if the first-order wave process has  $N$  components, at frequencies  $\omega_n$ ,  $\eta_2(t)$  includes  $N^2$  second-order corrections, spread over all sum frequencies  $\omega_n + \omega_m$ , and another  $N^2$  corrections over all difference frequencies  $\omega_n - \omega_m$ .

Note that these second-order wave models are not novel; they date back at least to the early 1960s (e.g., Longuet-Higgins, 1963). More novel, however, is their recent confirmation with respect to various statistics of field measurements (Marthinsen and Winterstein, 1992; Vinje and Haver, 1994) and wave tank studies of still more severe

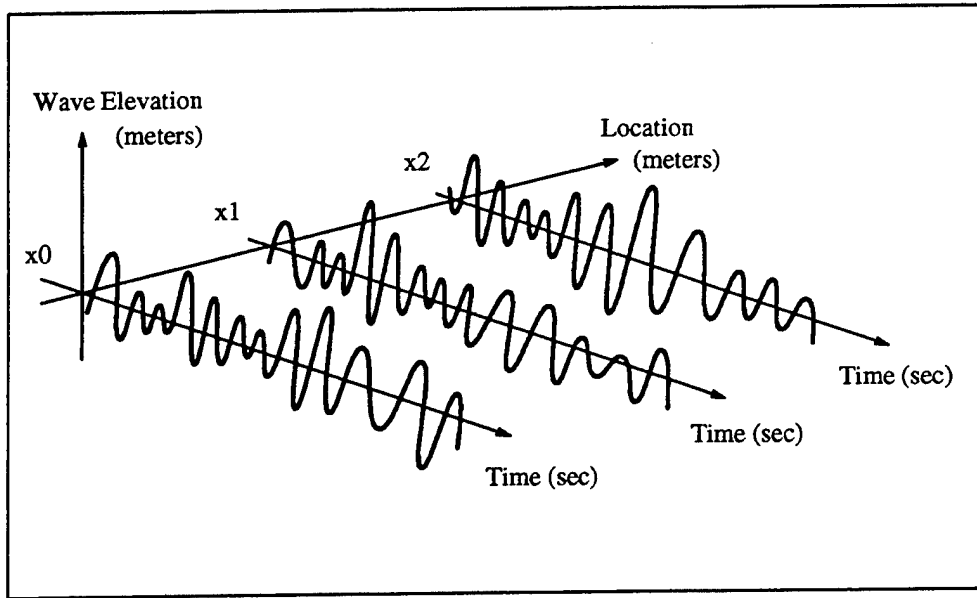


Figure 2.1: Simulated wave time histories at specified spatial locations

seas (Winterstein and Jha, 1995; preprint included in Appendix C). Such second-order wave models also form the basis of state-of-the-art nonlinear diffraction analysis of floating structures (e.g., SWIM, 1995; WAMIT, 1995). Note also that the model of  $\eta_2(t)$  used here varies explicitly with water depth, as predicted by second-order theory, to reflect increasing nonlinearity as we proceed to shallower water depths.

## 2.2 Methodology

### 2.2.1 Underlying Theory and Assumptions

We first consider  $\eta_1(t)$ , the first-order wave elevation, at a specific reference location (say  $x=0$ ). For either frequency-domain analysis or time-domain simulation, it is convenient to write  $\eta_1(t)$  as a discrete Fourier sum over positive frequencies  $\omega_k$ :

$$\eta_1(t) = \sum_{k=1}^N A_k \cos(\omega_k t + \theta_k) = \text{Re} \sum_{k=1}^N A_k e^{i(\omega_k t + \theta_k)} \quad (2.1)$$

To randomize Eq. 2.1, the phases  $\theta_k$  are taken to be uniformly distributed, mutually independent of each other and of the amplitudes  $A_k$ . Furthermore, we assign

random amplitudes  $A_k$  with Rayleigh distributions, and mean-square value

$$E[A_k^2] = 2S_\eta(\omega_k)d\omega \equiv \sigma_k^2; \quad d\omega = \omega_k - \omega_{k-1} \quad (2.2)$$

Finally, for purposes of simulation the lowest frequency interval  $d\omega$  is governed by the total period  $T$  of the simulation:

$$d\omega = \frac{2\pi}{T} \quad (2.3)$$

Together, Eqs. 2.1–2.2 ensure that each of the  $N$  frequency components in Eq. 2.1 is itself Gaussian. We also caution against the common use of choosing *deterministic* amplitudes,  $A_k = \sigma_k$ , particularly when interest lies in preserving higher moments of  $\eta_1(t)$ —or, similarly, the rms of second-order waves, loads, and responses. Use of deterministic amplitudes can give unconservative estimates; e.g., second-order rms values that are on average too small (Ude, 1994).

The resulting second-order wave at this elevation,  $\eta_2(t)$ , is calculated from  $\eta_1(t)$  as

$$\eta_2(t) = \eta_1(t) + \Delta\eta_2(t) \quad (2.4)$$

in which  $\Delta\eta_2(t)$  includes second-order corrections at sums and differences of all wave frequencies:

$$\Delta\eta_2(t) = q\text{Re} \sum_{m=1}^N \sum_{n=1}^N A_m A_n [H_{mn}^- e^{i[(\omega_m - \omega_n)t + (\theta_m - \theta_n)]} + H_{mn}^+ e^{i[(\omega_m + \omega_n)t + (\theta_m + \theta_n)]}] \quad (2.5)$$

In general, the functions  $H_{mn}^-$  and  $H_{mn}^+$  are known as quadratic transfer functions (QTFs), evaluated at the frequency pair  $\omega_m, \omega_n$ . Similar expressions arise in describing loads and responses of floating structures; in this case  $H_2^-$  and  $H_2^+$  are calculated numerically from nonlinear diffraction analysis (e.g., WAMIT, 1995). The leading factor  $q$  is included in Eq. 2.5 to alert readers to different QTF definitions in the literature: various diffraction analyses use  $q=1$  (WAMIT, 1995) or  $q=1/2$  (Molin and Chen, 1990).

In predicting motions of floating structures, in view of the relevant natural periods interest commonly lies with either  $H_2^-$  (slow-drift) or  $H_2^+$  (springing) but not both. In contrast, in the nonlinear wave problem both sum and difference frequency effects play a potentially significant role. Fortunately, unlike QTF values found numerically from numerical diffraction, closed-form expressions are available for both the sum- and difference-frequency QTFs for second-order waves (e.g., Langley, 1987; Marthinsen

and Winterstein, 1992). Including the effect of a finite water depth  $d$ , for example, the sum-frequency QTF can be written as

$$H_{mn}^+ = \frac{\frac{gk_mk_n}{\omega_m\omega_n} - \frac{1}{2g}(\omega_m^2 + \omega_n^2 + \omega_m\omega_n) + \frac{g}{2} \frac{\omega_mk_n^2 + \omega_mk_n^2}{\omega_m\omega_n(\omega_m + \omega_n)}}{1 - g \frac{k_m + k_n}{(\omega_m + \omega_n)^2} \tanh(k_m + k_n)d} - \frac{gk_mk_n}{2\omega_m\omega_n} + \frac{1}{2g}(\omega_m^2 + \omega_n^2 + \omega_m\omega_n) \quad (2.6)$$

in which the wave numbers  $k_n$  are related to the frequencies  $\omega_n$  by the linear dispersion relation. Note that this QTF definition assumes  $q=1/2$  in Eq. 2.5. This is the convention assumed in WAVEMAKER. The corresponding difference-frequency transfer function,  $H_{mn}^-$ , is found by replacing  $\omega_n$  by  $-\omega_n$  in Eq. 2.6.

## 2.2.2 Implementation

On input the simulation method requests the desired number of simulated points,  $npts$ , and the total duration  $T$  to be simulated. To take advantage of discrete FFT (Fast Fourier Transform) techniques, it assumes a regular spacing  $dt=T/npts$  between points. Eq. 2.1 is then rewritten as

$$\eta_1(t) = \sum_{k=1}^{npts/2} A_k \cos(\omega_k t + \theta_k) = \text{Re} \sum_{k=1}^{npts} X_k e^{i\omega_k t} \quad (2.7)$$

Here the  $X_k$  are complex Fourier coefficients. The lower half of these directly reflect both the random amplitude  $A_k$  and phase  $\theta_k$  at frequency  $\omega_k=k \cdot d\omega$ :

$$X_k = \frac{1}{2} A_k e^{i\theta_k}; \quad k = 1 \dots npts/2 \quad (2.8)$$

The upper half are in turn taken as the complex conjugates (the symbol “\*”) of the lower half:

$$X_{npts-k} = X_k^*; \quad k = 1 \dots npts/2 \quad (2.9)$$

This reflects that unique information is contained only the lower-half frequencies; indeed, any information in the upper half frequencies (above the Nyquist) is obscured by aliasing.

Thus, the first-order wave process is generated by assigning random  $A_k$  and  $\theta_k$ , defining  $X_k$  from Eqs. 2.8–2.9, and finally taking the inverse Fourier transform to recover the discretized time history  $\eta_1(t_j)$ . To see this, note that since  $dt \cdot d\omega = 2\pi/npts$ ,

Eq. 2.7 can be evaluated at  $t=t_j$  to give

$$\eta_1(t_j) = \text{Re} \sum_{k=1}^{npts} X_k e^{2\pi ijk/npts} \quad (2.10)$$

This is precisely the definition of the discrete FFT.

As a minor technical issue, note that the conjugate symmetry here ensures that the "Real Part" operation in Eq. 2.1 is superfluous; i.e., no imaginary component is generated. Also, to conform with the FFT routine used the array of  $X_k$  values is shifted by one index: i.e.,  $X_1$  corresponds to the frequency zero (the steady term, defined as zero),  $X_2$  to frequency  $\omega_1=d\omega$ ,  $X_3$  to frequency  $\omega_2=2 \cdot d\omega$ , and so forth.

The second-order correction is generated similarly. Starting with Eq. 2.5, substituting  $q=1/2$ ,  $N=npts/2$  (Eq. 2.7) and  $X_k$  from Eq. 2.8:

$$\Delta\eta_2(t) = 2\text{Re} \sum_{m=1}^{npts/2} \sum_{n=1}^{npts/2} X_m X_n H_{mn}^+ e^{i(\omega_m+\omega_n)t} + X_m X_n^* H_{mn}^- e^{i(\omega_m-\omega_n)t} \quad (2.11)$$

The leading factor reflects the product of  $q=1/2$  and a net factor of 4 (since  $A_n A_m$  is  $4 |X_m X_n|$ ). The program then seeks to rewrite both the sum and difference frequency contributions in a Fourier sum analogous to Eq. 2.10. For example, the sum-frequency is assumed of the form

$$\Delta\eta_2^+(t_j) = \text{Re} \sum_{k=1}^{npts} Y_k e^{2\pi ijk/npts} \quad (2.12)$$

The output Fourier coefficients,  $Y_k$ , are evaluated by equating Eqs. 2.11 and 2.12. This implies a sum over all wave frequency pairs  $(\omega_m, \omega_n)$  in Eq. 2.11 that give rise to output sum frequency  $\omega_k$ . The difference frequency Fourier coefficients are constructed in a similar way, and added on the sum frequency  $Y_k$  coefficients. Once these combined  $Y_k$  coefficients are found a (one-dimensional) inverse FFT is performed to recover the second-order time history.

### 2.2.3 Multiple Spatial Locations

The linear dispersion relation can be used to generalize Eq. 2.4, which generates a first-order wave at reference location  $x=0$ , to any other spatial location  $x$  in the along-wave direction. The linear dispersion relation is first used to find the wave number  $k_n$  associated with each frequency  $\omega_n$  in Eq. 2.4. The modified first-order simulation then merely replaces  $\omega_n t + \theta_n$  in Eq. 2.4 by  $\omega_n t - k_n x + \theta_n$ . Equivalently, the original phases  $\theta_n$  are first shifted to  $\theta_n - k_n x$  before applying Eq. 2.8 to define the wave Fourier amplitude  $X_n$ . These appropriately modified  $X_n$  are also used in Eq. 2.11 to find the corresponding second-order correction at this new location.

## 2.3 Input Specification

This section describes the various inputs required by the program and the syntax of the input to the driver routine for WAVEMAKER. This input is provided in the following format:

**keyword** *args*

where **keyword** is a reserved word and *args* are its arguments. A typical input file is in the following format:

```
# Typical input file: syntax description

simulate duration npts seed
depth value
psd psdtype psd_parameters
define varlimit value
define gravity value
write history filename1 filename2
write statistics filename3 filename4
location nloc
value1
value2
:
valuenloc
```

Each of these lines in a typical input file is explained below:

### # Typical input file: syntax description

Any line beginning with a “#” is treated as a comment line in the input file and is ignored by the program. Blank lines are also ignored by the program.

### simulate *duration npts seed*

The keyword **simulate** indicates to the program that the following three arguments in sequence are:

- *duration*: Total desired duration (in seconds) of each of the simulated wave histories (a real number).

- *npts*: Number of points required in each of the simulated wave histories (an integer).
- *seed*: A real number (131071.0 for example) for generation of random numbers. The seed may be changed by the user in order to generate a different set of wave histories. The number should be between 1.0 and  $2^{31}$ .

The resulting *dt* (time step) in the simulated histories is  $duration/npts$ . The *mxgrd* variable in the driver program controls the maximum number of points allowed (Maximum  $npts = 2 \times mxgrd$ ) in a simulation. The released driver program has  $mxgrd = 4096$ , so that specified *npts* can go up to 8192. The user may increase or decrease *mxgrd* to suit his/her needs.

#### **depth value**

This line specifies the water depth at the site of interest. The keyword is **depth** and *value* is a real number indicating the water depth. The units (meters, feet, etc.) of this value should be consistent with the units of other input parameters.

#### **psd psdtype psd\_parameters**

This line specifies the spectrum type to be used. The keyword is **psd** followed by its arguments. *psdtype* may be one of the following: jonswap, bimodal, or boxcar. If any other word is specified for *psdtype*, then it indicates to the program that an input spectrum is specified in a file whose name is same as the word specified in place of *psdtype*. More details regarding this input specification are given in the following subsection.

#### **define varlimit value [optional command]**

If included, this line defines a constant **varlimit** whose value is a real number (between 0.0 and 1.0) equal to *value*. A warning is issued by the simulation routine, if the estimated second-order power above Nyquist frequency is more than *value* times the first-order power. If this line is not provided in the input file, then a default value of 0.01 is assigned to **varlimit**.

#### **define gravity value [optional command]**

If included, this line specifies the acceleration due to gravity in consistent units. *value*, a real number, is assigned to **gravity**. If not included, a default value of 9.807 meters/sec<sup>2</sup> is assumed.

**write history** *filename1 filename2* [optional command]

If included, this line specifies the files which contain the simulated time histories at each location. The keyword is **write history**. The file *filename1* contains the underlying first-order (Gaussian) histories, and *filename2* contains the corresponding second-order wave histories. The format of the output is presented in the following section. If this line is not provided in the input file then default names of **gauss.hist** and **ngauss.hist** are assigned to the output first- and second-order histories, respectively.

**write statistics** *filename3 filename4* [optional command]

This line specifies the files to which the statistics (mean, standard deviation, skewness, kurtosis, minimum, and maximum value) of the simulated histories should be written. The keyword is **write statistics**. The statistics for the simulated first-order histories at each spatial location is written out in *filename3* and the statistics for the total second-order histories are written in *filename4*. If this line is not provided in the input file then default names of **gauss.stat** and **ngauss.stat** are assigned to the output files for the first- and second-order history statistics, respectively.

**location** *nloc*

This line specifies the number of spatial locations at which both the first- and total second-order wave histories should be simulated in time. The keyword is **location**. *nloc* (an integer) specifies the number of locations (maximum location allowed is 50). *value1, value2, ..., valuenloc* are the spatial values (real numbers) in consistent units. The number of values should be equal to *nloc*. The user is forewarned that the specification of the spatial locations should be at the end of all other inputs required.

### 2.3.1 Wave Spectrum Specification

The input wave spectrum can be specified in various ways: spectrum values in an input file, or spectrum type with related parameters from a default library.

**psd** *filename*

This specifies that the input spectrum be read from an input file named *filename*. The format of this file is two free-formatted values per line, specifying a natural frequency in radians per second and the one-sided PSD (power spectral density) ordinate for that frequency in consistent units of squared amplitude (feet<sup>2</sup>, meters<sup>2</sup>, etc.) per

rad/sec. Lines beginning with a “#” are regarded as comments and ignored. The input spectrum may be specified on an irregular mesh. This is internally linearly interpolated to a spectrum on a regular mesh specified by *duration* and *npts*. The spectral ordinates below the minimum frequency and above the maximum frequency specified in the irregular mesh are assumed to be zero.

Spectral models from the library are called upon using any one of the following reserved names followed by their parameters (that are real numbers):

```
psd jonswap  $H_s$   $T_p$   $\gamma$ 
psd bimodal  $H_s$   $T_p$ 
psd boxcar  $\sigma_\eta$   $\omega_{lo}$   $\omega_{hi}$ 
```

The keyword **jonswap** invokes a JONSWAP spectrum parameterized by the significant wave height  $H_s$  (defined as four times the standard deviation of the wave elevation process), spectral peak period  $T_p$  (in seconds), and the peakedness factor  $\gamma$ .

The keyword **bimodal** invokes a spectral model proposed by Torsethaugen (Bitner-Gregerson and Haver, 1991). This subdivides the  $H_s$ - $T_p$  scattergram into three regions, and assigns bimodal spectral shapes in several of these regions. Therefore, the only input required for this **bimodal** option is  $H_s$  and  $T_p$ .

Finally, the keyword **boxcar** invokes a simple band-limited white-noise model of the first-order wave spectrum. Its parameters are the rms  $\sigma_\eta$ , lower cutoff frequency  $\omega_{lo}$ , and upper cutoff frequency  $\omega_{hi}$  of the first-order wave spectrum. As in other cases (e.g., the user-defined spectrum at various frequencies), the frequencies  $\omega_{lo}$ , and  $\omega_{hi}$  here are assumed to be in units of rad/sec. Note also that non-zero values of the PSD at zero frequency are not allowed in either file input or library model selections.

## 2.4 Output Format

A total of four output files are produced by the driver program. Two output files contain the time histories: one for the underlying first-order wave histories and the other for the total second-order histories. The other two output files contain wave statistics: first four moments, minimum and maximum. Again, results for the first- and second-order wave histories are separated into two files.

### 2.4.1 Time History Output

As noted in the previous section, by default the first- and second-order histories are written to the files `gauss.hist` and `ngauss.hist`. Other choices of output filenames can be specified by the optional `write history` command. The format of this output depends on the number of spatial locations specified. If the number of locations ( $nloc$ ) is less than or equal to 8 then the output is in **Format1** otherwise the output is in **Format2**. Both of these formats write out 3 header lines beginning with a “#” sign. These are to be treated as comment lines in the output file. In order to explain the two format styles, say that the spatial locations specified are  $x_1, x_2, x_3, \dots, x_{nloc}$ .

**Format1** outputs data in  $nloc+1$  columns. The length of each column is equal to the number of points desired in each simulation. The first column contains the time increments in seconds going from 0 to  $T$  with  $dt = T/npts$ . Columns 2 through  $nloc+1$  contain the simulated history values at the specified locations  $x_1, x_2, x_3, \dots, x_{nloc}$ , respectively. Thus, column 2 contains the wave elevation at location  $x_1$ , column 3 contains wave elevation at location  $x_2$ , and so on.

**Format2** is for handling  $nloc$  greater than 8. The output begins with the time increment  $T_i$  in seconds on a line by itself. The time history values for the specified spatial locations at time  $T_i$  are written in the next line onwards, in sets of 10. So if 9 locations were specified (i.e.,  $nloc = 9$ ) then the time increment is printed on a line by itself followed by a line containing 9 time history values at that time increment. The next line contains the next time increment followed by another set of 9 values, and so on. If, on the other hand say 28 locations were specified, then a time increment is written on a line followed by 28 time history values (corresponding to 28 locations at that time increment) in the next 3 lines. The first line of the 3 lines contains 10 time history values for the first 10 locations specified. The next line contains 10 history values for locations 11 through 20 and the following line which is the third line of the set will contain only 8 history values for location 21 through 28.

### 2.4.2 Wave Statistics Output

The statistics of the simulated histories are also estimated by the driver program. These statistics include the mean, standard deviation, skewness, kurtosis, minimum, and maximum. As noted in the previous section, first- and second-order simulation results are written by default to the files `gauss.stat` and `ngauss.stat`, respectively. The optional command `write statistics` can alter this choice of output filenames.

The output format in both of these files begins with 2 header lines, each of which

begins with a “#” sign. The output is in seven columns. The first column specifies the spatial location. The following six columns contain statistics of the wave history at the spatial location specified in column 1. Columns 2 through 7 contain, the mean, standard deviation, skewness, kurtosis, minimum, , and maximum value in that order.

The next section presents some sample output files, to illustrate use of the WAVEMAKER routine.

## 2.5 Example

In this section, we present a sample problem (copies of input and output files are enclosed on disk). To illustrate, consider a simulation which samples the wave process at regular intervals of length  $dt=0.5$  [sec] over a total duration of  $T=2048$  [sec]; i.e.,  $npts=4096$  points. We assume here the first-order wave spectrum to be of JONSWAP form, with  $H_s = 12$  [m],  $T_p = 14$  [sec] and a peakedness factor  $\gamma = 3.3$ . We further seek to generate wave histories at 2 spatial locations: 0 and 60 [m]. Our input file for simulating waves using WAVEMAKER should be:

```
# Gaussian and Nongaussian Wave Input File

simulate 2048.0 4096 8123872.0
depth 70.0
psd jonswap 12.0 14.0 3.3
write history gauss.hist ngauss.hist
write statistics gauss.stat ngauss.stat
define varlimit 0.01
define gravity 9.807
location 2
0.0
60.0
```

Alternatively, if we intend to use the default definitions in the program then our input file could be (this will produce the same output as the extended version of the input file):

```

# Gaussian and Nongaussian Wave Input File
# (Alternative format)

simulate 2048.0 4096 8123872.0
depth 70.0
psd jonswap 12.0 14.0 3.3
location 2
0.0
60.0

```

The output files created are: **gauss.hist**, **ngauss.hist**, **gauss.stat**, and **ngauss.stat**. The contents of these are listed in the following table:

Output File	Contents
<b>gauss.hist</b>	First-Order Time History
<b>ngauss.hist</b>	Second-Order Time History
<b>gauss.stat</b>	First-Order History Statistics
<b>ngauss.stat</b>	Second-Order History Statistics

Each of these output files is given in the Appendix A.

Figures 2.2 and 2.3 show a comparison of the simulated histories. Figure 2.2 compares the simulated first- and second-order wave time histories at the same location (the first of the two requested, defined arbitrarily as  $x=0$  [m]). The file **ngauss.stat** includes the estimated skewness of the second-order waves. At this location the second-order wave history has a skewness of about 0.2. This positive skewness (compared to zero skewness of Gaussian waves) indicates the systematic nonlinear effects. This also gives rise to an asymmetry between peaks and troughs; in particular, the extreme wave crest in the second-order simulation systematically exceeds the corresponding extreme trough in absolute value. This tendency may be significant for potential deck impact problems, particularly in older jacket structures with relatively low deck levels.

Figure 2.3 compares the second-order wave histories predicted by simulation at the two spatial locations, separated by 60 [m]. The phase lag at these two locations is evident in the plot. It can be seen that a crest height at 0 [m] does not necessarily imply a crest of the same height at 60 [m].

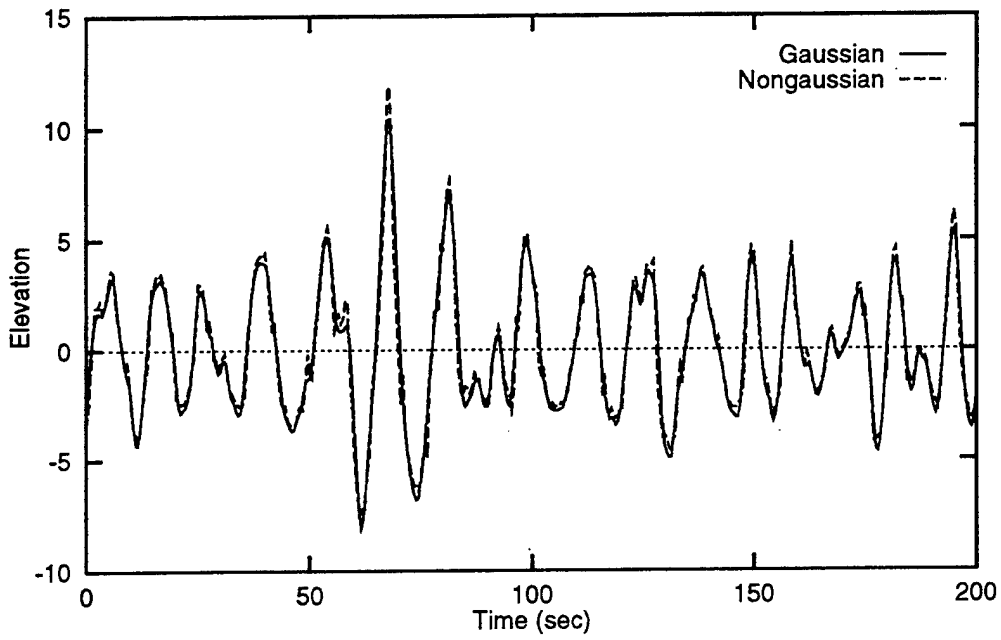


Figure 2.2: Simulated first- and second-order wave histories at location 0.0

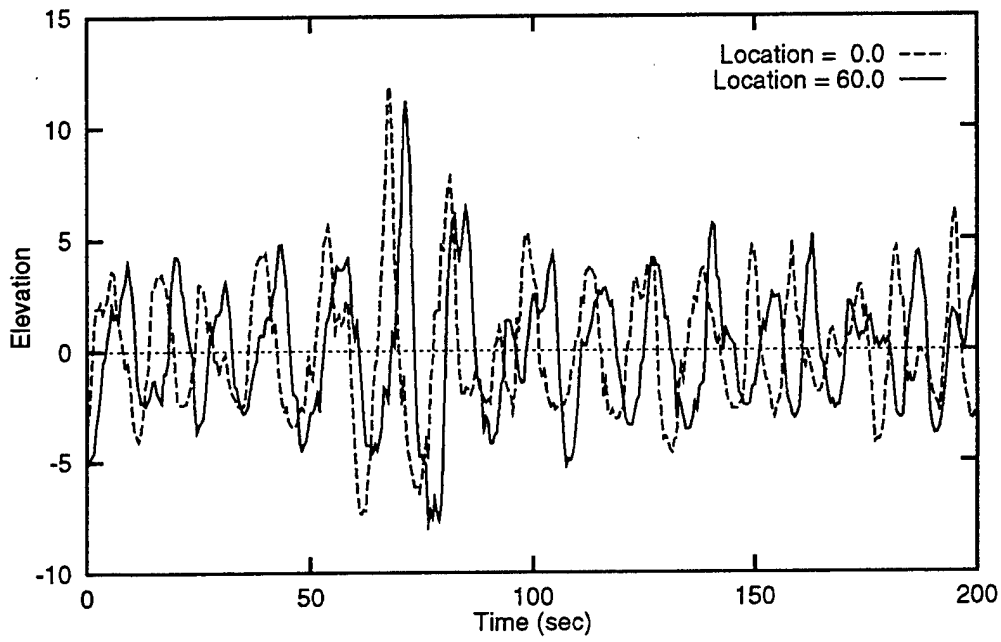


Figure 2.3: Simulated second-order wave histories at location 0.0 and 60.0



## Chapter 3

# Identification of First-Order Waves

### 3.1 Introduction

In ocean engineering practice it is common to assume the waves to be Gaussian and any nonlinearity in the waves is embedded in the structural response analysis (e.g., WAMIT, 1995). It has been shown in Winterstein and Jha, 1995 that observed time histories generally contain nonlinearities, it is thus imperative to remove any second-order effects in the incident waves so that we do not double-count these effects in the resulting response estimation. Recent studies (Ude and Winterstein, 1996) have demonstrated the impact of double-counting such second-order effects on various structural response characteristics.

The methodology to identify the underlying first-order waves is to seek the implied first-order wave history which, when run through the second-order wave predictor, yields an incident wave that agrees with the target observed history at each time point. This identification is performed using a Newton-Raphson scheme to achieve simultaneous convergence at each complex Fourier component. If the observed history has  $N$  components, we iteratively solve  $N$  simultaneous nonlinear equations to identify the first-order components.

Due to computer memory limitations, the identification of the first-order history is performed on short contiguous windows of the observed history. This window size ( $m_{len}$ ) can be made equal to the observed history length in WAVEMAKER if the computer has sufficient RAM and swap space.

## 3.2 Methodology

The idea here is to identify the implied first-order history  $\eta_1(t)$  (of an observed history  $\eta_{\text{obs}}(t)$ ) which, when run through the second-order predictor, yields an incident wave that agrees with  $\eta_{\text{obs}}(t)$ . In the first-order wave process  $\eta_1(t)$  (see Eq. 2.7), written as a Fourier sum of  $N$  frequencies,

$$\eta_1(t) = \sum_{k=1}^{N/2} A_k \cos(\omega_k t + \theta_k) = \sum_{k=1}^N X_k e^{i\omega_k t} \quad (3.1)$$

we need to identify only the lower half  $X_k$  components, since the upper half values are complex conjugates of the lower half. Let us denote  $X_k = U_k + iV_k$ , where  $U_k, V_k$  are the real and imaginary parts of the complex Fourier component  $X_k$ , respectively.

The predicted second-order wave process (see Eq. 2.11) as evaluated from the QTFs is

$$\Delta\eta_2(t) = 2\text{Re} \sum_{m=1}^{N/2} \sum_{n=1}^{N/2} X_m X_n H_{mn}^+ e^{i(\omega_m + \omega_n)t} + X_m X_n^* H_{mn}^- e^{i(\omega_m - \omega_n)t} \quad (3.2)$$

This may be rewritten in the form of a Fourier sum as

$$\Delta\eta_2(t) = \sum_{k=1}^N Y_k e^{i\omega_k t} \quad (3.3)$$

where  $Y_k = Y_k^+ + Y_k^-$  are the combined sum and difference frequency components. Here again,  $Y_k$  possesses conjugate symmetry so that only the lower half contains unique information.  $Y_k^+$  can be shown to be

$$\begin{aligned} Y_k^+ &= \sum_{m+n,k} X_m X_n H_{mn}^+ \\ &= \sum_{m+n,k} [(U_m U_n - V_m V_n) + i(V_m U_n + U_m V_n)] H_{mn}^+ \end{aligned} \quad (3.4)$$

where the summation symbol indicates a double summation

$$\sum_{m+n,k} = \sum_{m=1}^{N/2} \sum_{n=1}^{N/2} \quad \text{such that } \omega_m + \omega_n = \omega_k \quad (3.5)$$

and

$$\begin{aligned} Y_k^- &= \sum_{m-n,k} X_m X_n^* H_{mn}^- \\ &= \sum_{m-n,k} [(U_m U_n + V_m V_n) + i(V_m U_n - U_m V_n)] H_{mn}^- \end{aligned} \quad (3.6)$$

where

$$\sum_{m=n,k} = \sum_{m=1}^{N/2} \sum_{n=1}^{N/2} \quad \text{such that } |\omega_m - \omega_n| = \omega_k \quad (3.7)$$

The combined predicted wave process is

$$\eta_{\text{pred}}(t) = \eta_1(t) + \Delta\eta_2(t) \quad (3.8)$$

The identification scheme strives to simultaneously match  $\eta_{\text{pred}}(t)$  to the observed wave history  $\eta_{\text{obs}}(t)$  at every value of  $t$ . Alternatively, we can perform the identification in the frequency domain and strive to simultaneously match the predicted Fourier components to the observed Fourier components at all frequencies.

$\eta_{\text{obs}}(t)$  can be represented in the frequency domain as

$$\eta_{\text{obs}}(t) = \sum_{k=1}^N Z_k e^{i\omega_k t} \quad (3.9)$$

where  $Z_k$ 's also possess conjugate symmetry. If the first-order components are identified exactly, from Eq.s 3.1, 3.3 and 3.9 we will have

$$Z_k = X_k + Y_k \quad ; \quad \text{for all } k = 1 \dots N/2 \quad (3.10)$$

Note that the upper half values can be obtained from conjugate symmetry of the lower half values. In the Newton-Raphson identification scheme we will try to simultaneously minimize  $X_k + Y_k - Z_k$ ; for  $k = 1 \dots N/2$  to achieve convergence. Now, this scheme requires a Jacobian of  $X_k + Y_k - Z_k$  with respect to the unknowns  $X_k$ —such a complex differentiation will lead to numerical discontinuities so we will minimize an equivalent real function  $\sqrt{\sum_1^N f_k^2/N}$  instead, where for  $k = 1 \dots N/2$

$$\begin{aligned} f_k &= \text{Re}(X_k + Y_k - Z_k) \\ f_{k+N/2} &= \text{Im}(X_k + Y_k - Z_k) \end{aligned} \quad (3.11)$$

The identification of the lower half  $X_k$  values requires a simultaneous solution of the nonlinear equations in 3.11 such that  $f_k \rightarrow 0$  for all  $k = 1 \dots N$ , or alternately  $\sqrt{\sum_1^N f_k^2/N} \rightarrow 0$ . We will formulate the Newton-Raphson scheme in vector form as

$$\mathbf{f} = \begin{bmatrix} \text{ReX} \\ \text{ImX} \end{bmatrix} + \begin{bmatrix} \text{ReY} \\ \text{ImY} \end{bmatrix} - \begin{bmatrix} \text{ReZ} \\ \text{ImZ} \end{bmatrix} \quad (3.12)$$

where bold face letters denote vectors, and vectors  $\mathbf{X}, \mathbf{Y}, \mathbf{Z}$  contain the complex Fourier components  $X_k, Y_k, Z_k, k = 1 \dots N/2$ , respectively. Here,  $\begin{bmatrix} \text{ReX} \\ \text{ImX} \end{bmatrix}$  is a vector containing the real part of  $\mathbf{X}$  in the upper half and the imaginary part of  $\mathbf{X}$  in the lower half.

Let us denote

$$\begin{aligned} \mathbf{A} &= \begin{bmatrix} \text{ReX} \\ \text{ImX} \end{bmatrix} = \begin{bmatrix} \mathbf{U} \\ \mathbf{V} \end{bmatrix} \\ \mathbf{B} &= \begin{bmatrix} \text{ReY} \\ \text{ImY} \end{bmatrix} \\ \mathbf{C} &= \begin{bmatrix} \text{ReZ} \\ \text{ImZ} \end{bmatrix} \end{aligned} \quad (3.13)$$

Note that the vector  $\mathbf{A}$ , of length  $N$ , is constructed such that lower half values are the real parts of  $X_k$ ;  $k = 1 \dots N/2$  and the upper half is the imaginary part of  $X_k$ ;  $k = 1 \dots N/2$ . Similarly,  $\mathbf{B}$  and  $\mathbf{C}$ , each of length  $N$ , contain real and imaginary parts of the lower half of the second-order correction and the observed Fourier components, respectively. The elements of  $\mathbf{A}$  and  $\mathbf{B}$  are denoted by  $a_l$  and  $b_k$ , respectively, where  $l, k = 1 \dots N$ . The objective function in vector notation now is

$$\mathbf{f}(\mathbf{A}) = \mathbf{A} + \mathbf{B} - \mathbf{C} \quad (3.14)$$

A first-order Taylor approximation of  $\mathbf{f}(\mathbf{A})$  about a given  $\mathbf{A}^{(0)}$  is

$$\mathbf{f}(\mathbf{A}) = \mathbf{f}(\mathbf{A}^{(0)}) + [\mathbf{J}] (\mathbf{A} - \mathbf{A}^{(0)}) \quad (3.15)$$

where  $[\mathbf{J}]$  is a  $N \times N$  Jacobian matrix denoting the derivatives of the elements  $f_k$  in vector  $\mathbf{f}(\mathbf{A})$  with respect to each of the unknowns  $a_l$  in  $\mathbf{A}$  where  $k, l = 1 \dots N$ . The Newton-Raphson scheme at iteration  $p + 1$  is then formulated as

$$\mathbf{A}^{(p+1)} = \mathbf{A}^{(p)} + \mathbf{h} \quad (3.16)$$

where  $\mathbf{h}$ , a vector of length  $N$ , is found from a Cholesky decomposition followed by a back-substitution scheme from

$$[\mathbf{J}]\mathbf{h} = -\mathbf{f}(\mathbf{A}^{(p)}) \quad (3.17)$$

It can be easily shown from Eq. 3.14 that the entries  $J_{k,l}$  of the matrix  $[\mathbf{J}]$  are

$$J_{k,l} = \frac{\partial f_k}{\partial a_l} = \delta_{kl} + \frac{\partial b_k}{\partial a_l} \quad (3.18)$$

where  $\partial b_k / \partial a_l$  indicates the partial derivative of  $b_k$  with respect to  $a_l$ , and

$$\delta_{kl} = \begin{cases} 1 & \text{if } k = l \\ 0 & \text{otherwise} \end{cases} \quad (3.19)$$

To find  $\partial b_k / \partial a_l$ , recall from notation in 3.13

$$\begin{aligned} b_k &= \text{Re}Y_k & \text{and} & & b_{k+N/2} &= \text{Im}Y_k & \text{for } k &= 1 \dots N/2 \\ a_l &= \text{Im}X_l = U_l & \text{and} & & a_{l+N/2} &= \text{Im}X_l = V_l & \text{for } l &= 1 \dots N/2 \end{aligned}$$

so that from Eq.s 3.4 and 3.6 we have

$$\begin{aligned}
\frac{\partial \text{Re}Y_k}{\partial U_l} &= \sum_{m+n,k} (U_n \delta_{ml} + U_m \delta_{nl}) H_{mn}^+ + \sum_{m-n,k} (U_n \delta_{ml} + U_m \delta_{nl}) H_{mn}^- \\
\frac{\partial \text{Re}Y_k}{\partial V_l} &= \sum_{m+n,k} -(V_n \delta_{ml} + V_m \delta_{nl}) H_{mn}^+ + \sum_{m-n,k} (V_n \delta_{ml} + V_m \delta_{nl}) H_{mn}^- \quad (3.20) \\
\frac{\partial \text{Im}Y_k}{\partial U_l} &= \sum_{m+n,k} (V_m \delta_{nl} + V_n \delta_{ml}) H_{mn}^+ + \sum_{m-n,k} (V_m \delta_{nl} - V_n \delta_{ml}) H_{mn}^- \\
\frac{\partial \text{Im}Y_k}{\partial V_l} &= \sum_{m+n,k} (U_n \delta_{ml} + U_m \delta_{nl}) H_{mn}^+ + \sum_{m-n,k} (U_n \delta_{ml} - U_m \delta_{nl}) H_{mn}^-
\end{aligned}$$

Schematically,

$$[J] = [I] + \begin{bmatrix} \frac{\partial \text{Re}Y_k}{\partial U_l} & \frac{\partial \text{Re}Y_k}{\partial V_l} \\ \frac{\partial \text{Im}Y_k}{\partial U_l} & \frac{\partial \text{Im}Y_k}{\partial V_l} \end{bmatrix} \quad (3.21)$$

where  $[I]$  is the identity matrix.

### 3.2.1 Newton-Raphson Scheme

The algorithm for the Newton-Raphson scheme followed in WAVEMAKER is

- 
1. Estimate  $\mathbf{C}$  from observed history (Eq.s 3.9, 3.13)
  2. Initial Guess  $\mathbf{A} = \mathbf{C}$
  3. Estimate  $\mathbf{B}$  from  $\mathbf{A}$  (Eq.s 3.4, 3.6, 3.13)
  4. Find  $\mathbf{f}(\mathbf{A})$  (Eq. 3.14)
  5. Find  $[J]$  (Eq.s 3.20, 3.21)
  6. Solve  $[J]\mathbf{h} = -\mathbf{f}(\mathbf{A})$  to find  $\mathbf{h}$
  7. Update  $\mathbf{A} = \mathbf{A} + \mathbf{h}$
  8. Check Convergence (see next section):  
If converged terminate else go to 3
- 

### 3.2.2 Convergence Criteria

The Newton-Raphson iteration scheme is terminated based on the following conditions:

- **Program Converged:** If the rms of the increment vector  $\mathbf{h} = \sqrt{\sum_1^N h_k^2/N}$  is less than a specified tolerance, the program is said to have converged. This convergence tolerance is specified as a fraction  $\alpha$  ( $= 0.0001$  in WAVEMAKER) of the standard deviation of the observed wave history  $\sigma_{\eta, \text{obs}}$ .
- **Program Diverging:** If the rms of the identified first-order history  $\sigma_{\eta, 1}$  at any iteration  $p$  is larger than a specified fraction  $\beta$  ( $= 200$  in WAVEMAKER) of  $\sigma_{\eta, \text{obs}}$  then the identification scheme is restarted with a smaller initial guess which is a truncated and scaled down version of  $\mathbf{C}$ . The truncation point is at twice the peak spectral frequency of  $\eta_{\text{obs}}(t)$  and the scaling factor is  $\text{factnu}^r$  ( $= 0.9^r$  in WAVEMAKER), where  $r$  is the number of restarts needed so far. Thus the restart guess in complex Fourier notation is

$$X_k = \begin{cases} \text{factnu}^r Z_k & ; \omega_k < 2\omega_{\text{peak}} \\ 0 & ; \text{otherwise} \end{cases} \quad (3.22)$$

- **Maximum Iterations Reached:** If the maximum allowed iterations, specified by the variable  $mxiter$  ( $= 10$  in WAVEMAKER), is reached and the program has still not converged, then the program restarts the Newton-Raphson identification scheme with a smaller initial guess  $= \text{factnu}^r \mathbf{C}$ .
- **Maximum Restarts Reached:** If the maximum allowed restarts, specified by the variable  $nuiter$  ( $= 5$  in WAVEMAKER), is reached then the program terminates the identification scheme in the present window and proceeds to identify in the next observed history window.

### 3.2.3 Implementation

The first-order components for the observed wave history, of length  $N_{\text{obs}}$ , are identified in contiguous windows, each of length  $N \leq N_{\text{obs}}$ . The identification analysis is performed in this way to minimize the computer memory usage by WAVEMAKER. Recall that the Jacobian matrix  $[J]$  is a  $N \times N$  matrix and the memory usage is directly governed by the matrix size of this variable. In principle, if there is sufficient memory we could set  $N = N_{\text{obs}}$  and identify the first-order component for the entire observed history in one window, however, this is not usually not the case and we resort to identifying in contiguous windows, as shown in Fig. 3.1.

The first-order component is identified independently in each of the windows in sequence. The last window is skipped if its contains points less than  $N$ .

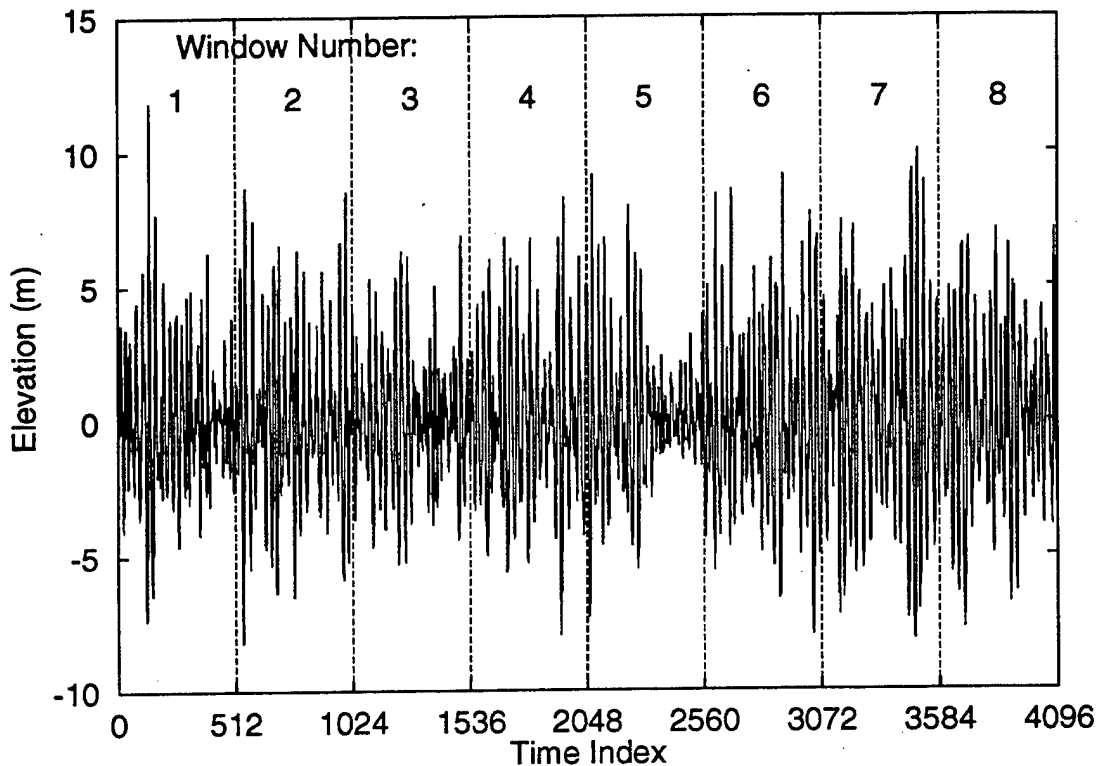


Figure 3.1: Identification of first-order wave components is done in contiguous windows of the observed history

### 3.3 Input Specification

The input specification for the identification of first-order wave process is in a command-line format similar to the simulation input. A typical input file for identification is:

```
# Typical input file: syntax description

identify filename dt winsize
depth value
define varlimit value
define gravity value
write history filename1 filename2
```

**# Typical input file: syntax description**

Any line beginning with a “#” symbol is treated as a comment line and is ignored.

Blank lines in the input file are ignored, as well.

**define varlimit** *value*

**define gravity** *value*

The keywords **varlimit**, **gravity** have the same meaning as in the simulation section and the user is referred to this section to understand the usage of these commands.

**depth** *value*

The keyword **depth** as in the simulation section indicates the water depth at which the identification analysis is to be performed.

**identify** *filename dt winsize*

The keyword **identify** indicates to the program that the user intends to identify the underlying first-order wave history for a given observed wave history. This command requires three arguments which in sequence are:

- *filename*: The name of the file, a character string, containing the observed wave time history for which the underlying first-order wave history is to be identified. The data in the **first** column in *filename* is read as the observed wave time history. Any blank lines in *filename* or lines that do not begin with a number are ignored.
- *dt*: This value, a real number, indicates the time resolution of the wave history provided in *filename*. In other words, *dt* is the time difference between two successive elevation values in the observed wave history.
- *winsize*: An integer value indicating the window size or the number of points of the provided wave history to be used in each Newton-Raphson iteration. The first-order wave components are identified in windows (of size *winsize*) in sequence for the provided time history. If the last window contains number of points less than *winsize* then this window is ignored and the first-order components are not identified in this window.

The maximum value of *winsize* is *m1en* set to 512 points in WAVEMAKER and can be changed according to the user's needs or according to the computer's limitations. Note that we require  $m1en < 2 \times m1xgrd$  in the program. These dimension values are set in this way so as to minimize the memory requirements of WAVEMAKER.

**write history** *filename1 filename2*

The command **write history** is used to specify the file names where the identified histories are to be written. The identified first-order wave history is written in file *filename1* and the identified second-order, combined first- and second-order, and the observed wave histories are written in file *filename2*. Default values assigned to *filename1* and *filename2* are **gauss.hist** and **ngauss.hist**, respectively.

## 3.4 Output Format

The output file names are governed by the command

**write history** *filename1 filename2*

with default names being **gauss.hist** and **ngauss.hist** for *filename1* and *filename2*, respectively.

*filename1* contains the identified first-order wave history in a column of real numbers. Each line of this file contains one real number indicating the elevation of the first-order wave history (see example output files in Appendix B). The time resolution of this first-order history is *dt*, equal to the *dt* provided in the input file using the command **identify**. This file also contains comment lines that begin with a “#” symbol as the first character on the line. The first comment line contains information on the contents of the file, and the following comment lines contain 3 integers: the first is the window number being identified, the second is the number of iterations required for convergence, and the third is the number of restarts needed for convergence.

*filename2* contains the second-order correction, the combined first- and second-order waves, and the observed wave time history. The second-order correction is found from the identified first-order waves, and these two are added together to yield the combined second-order wave history. These histories are provided in three columns in *filename2*, or in other words each line contains three real numbers: the first is the second-order wave elevation, the second is the combined identified wave elevation, and the third is the observed wave history (see example output file in Appendix B). A match of the total identified and the observed wave histories will verify successful identification by WAVEMAKER. The time resolution of each of these histories is *dt*. This file also contains comment lines beginning with a “#” symbol that provides information similar to the comment lines in *filename1*.

## 3.5 Examples

In this section we present two sample problems to illustrate the use of the identification capabilities of WAVEMAKER. Example 1 is based on the example presented in the simulation chapter. Sample input and output files of this identification example are included in the distribution diskette. Example 2 presented here demonstrates the identification of first-order components of a measured wave tank history. Note that sample input or output files of this second example are not included in the distribution.

### 3.5.1 Example 1

The example of the simulation capabilities of WAVEMAKER involved simulating a second-order wave history characterized by a JONSWAP spectrum with  $H_s = 12$  [m],  $T_p = 14$ s and  $\gamma = 3.3$  in 70 [m] water depth. We will use the combined second-order simulated history and try to identify its first-order wave component and compare it to the input first-order component used to simulate the combined wave history. The input file for the identification run is

```
# Wave Identification Input File

identify hist.dat 0.5 512
depth 70.0
write history gauss.ide ngauss.ide
define varlimit 0.01
define gravity 9.807
```

Alternatively, if we intend to use the default definitions in the program then our input file could be (this will produce the same output as the extended version of the input file):

```
# Wave Identification Input File
# (Alternative format)

identify hist.dat 0.5 512
depth 70.0
write history gauss.ide ngauss.ide
```

The input file **hist.dat** contains a column of real numbers (see sample files listed in the appendix) which will be read in as the observed wave history. The first-order components will be identified for this observed history and placed in the file **gauss.ide**. The corresponding second-order components, the combined identified history and the observed wave history are written in the file **ngauss.ide**.

Output File	Contents
<b>gauss.ide</b>	Identified First-Order Time History
<b>ngauss.ide</b>	Corresponding Second-Order Time History

Figure 3.2 shows the observed wave spectrum and the identified first-order spectrum along with the corresponding second-order wave spectrum. We see that small second-order contribution to the power spectrum, roughly a decade below the first-order spectrum even at frequencies twice the peak spectral frequency, suggests the difficulty in identifying these components. Figure 3.3 shows the observed wave history and the identified first-order wave history in cycles around the maximum crest height. Compare this to the simulation example where we solve the forward problem of finding the combined (first- plus second-order) history from a given underlying first-order wave spectrum. The identified first-order component in Fig. 3.3 is almost the same as the underlying first-order component (denoted Gaussian) in Fig. 2.2 and these two are shown together in Fig. 3.4. Note how close the two first-order components are, and any numerical differences can probably be further reduced by using a larger window size (greater than 512, for example) in the identification scheme.

### 3.5.2 Example 2

In this example we will identify the underlying first-order wave component for a measured wave tank history that reflects a water depth of about 300m. For this example the measured history is located in file `wave.dat` and has a  $dt = 0.424264$  seconds. We will use windows of  $winsize = 512$  to identify the first-order components. The input to `WAVEMAKER` is:

```
# Wave Identification Input File
# using default definitions

identify wave.dat 0.424264 512
depth 300.0
```

Figure 3.5 shows a portion where the maximum crest height occurs in the measured wave tank history. The figure also shows the identified first-order and the corresponding second-order wave histories. Note how the second-order wave component affects the first-order peaks, amplifying the crests and moderating the troughs. Figure 3.6 shows the wave spectra for the measured history along with the first-order and the second-order spectra. Again, observe that the second-order energy is significantly small compared to the first-order, however, phase locking of the first- and the second- component (Fig. 3.5) leads to larger crests and flatter troughs.

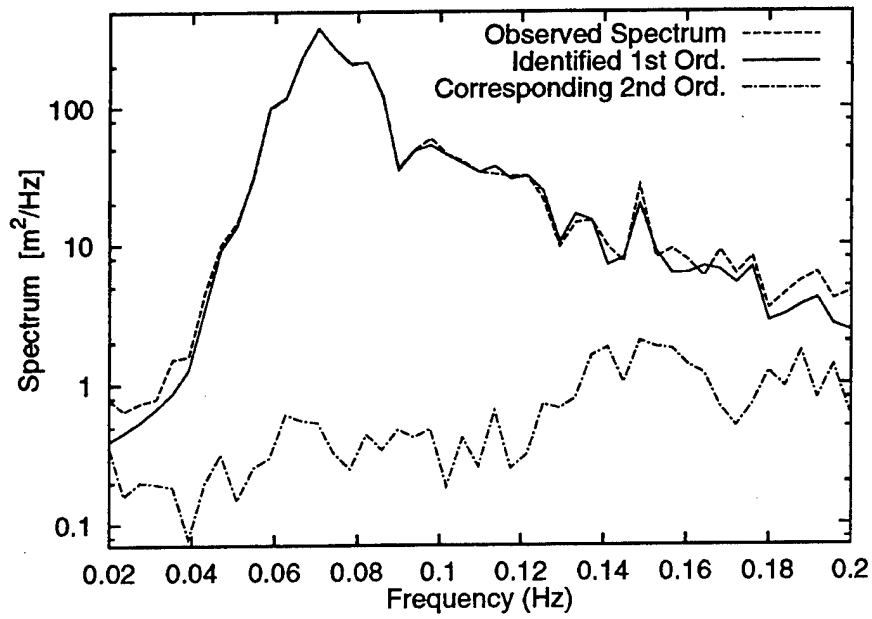


Figure 3.2: Wave spectrum: observed vs. identified first- and second-order

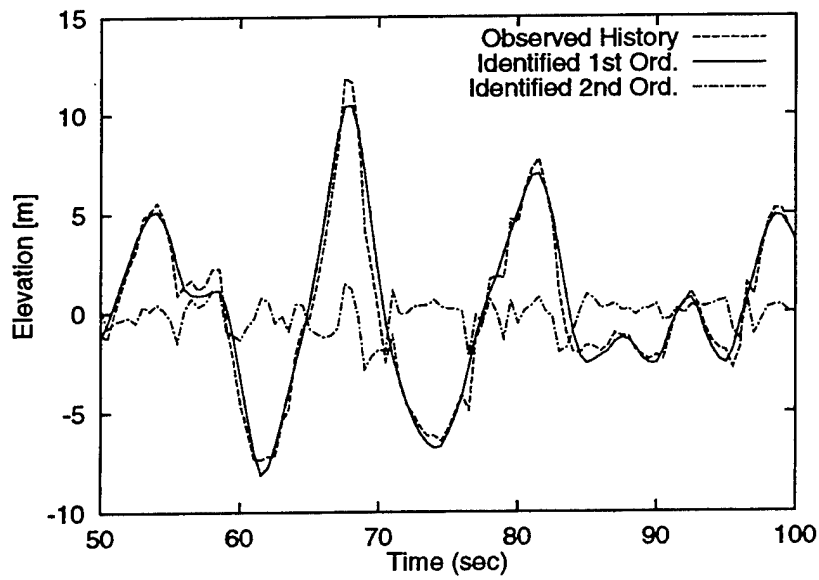


Figure 3.3: Wave history: observed vs. identified first- and second-order

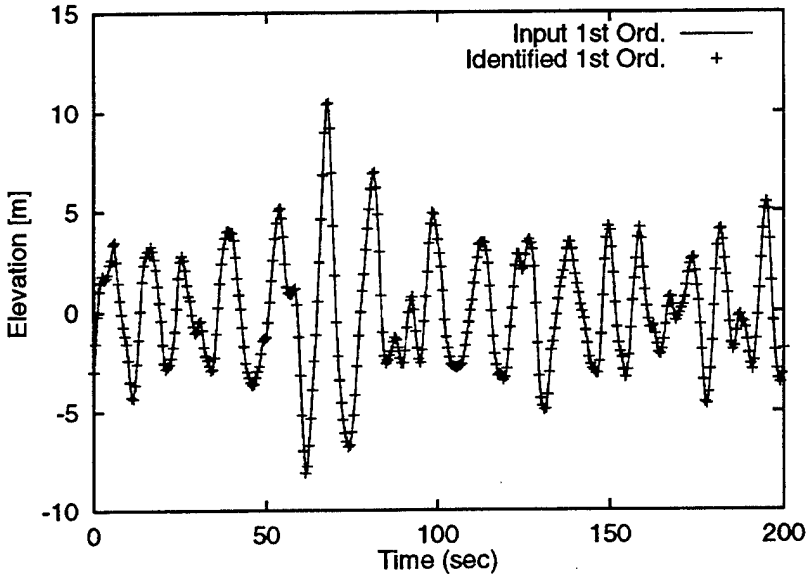
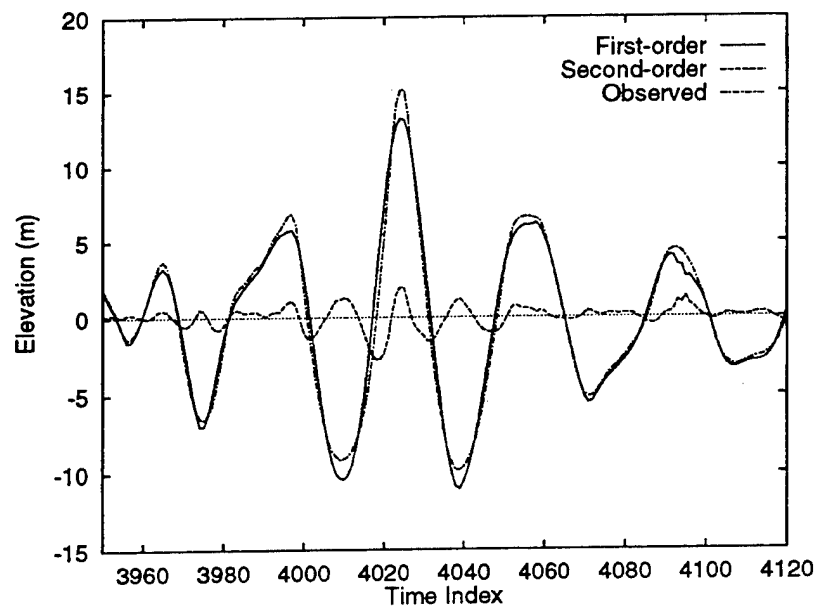
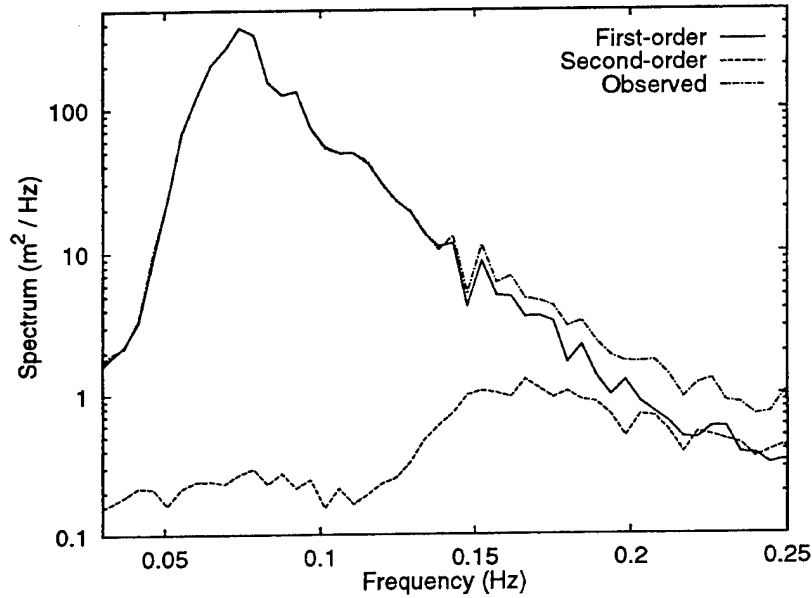


Figure 3.4: Identified first-order vs. actual first-order wave history



**Figure 3.5:** Wave history in wave tank: observed vs. identified first- and second-order



**Figure 3.6:** Wave spectrum in wave tank: observed vs. identified first- and second-order

## Chapter 4

# Distribution

The WAVEMAKER routine and example files have been distributed on a DOS formatted 3.5 inch floppy diskette. The diskette contains the source code files (of the form \*.f), example input (\*.inp), and output files (\*.sta, \*.his, and \*.ide). The diskette also contains this manual in postscript format in manual.ps.

### 4.1 Copying the Diskette

Copy the contents of the diskette on to your host computer (computer on which you will run WAVEMAKER). After the copying is done, your host computer should have:

- Example input files wavmkr.inp, wavide.inp, and hist.dat.
- Example output files gauss.his, ngauss.his, gauss.sta, ngauss.sta, gauss.ide, and ngauss.ide.
- manual.ps containing this manual in postscript format
- all the source files \*.f and Makefile

Table 4.1 shows the input and output files that are specific to the simulation and to the identification examples.

**Table 4.1:** Distributed Files for Simulation and Identification Examples

<b>Simulation Example</b>		
<b>File Type</b>	<b>File Name</b>	<b>Description</b>
Input File	wavmkr.inp	Input to WAVEMAKER
Output Files	gauss.his	Simulated first-order wave histories at each specified location
	ngauss.his	Simulated combined first- and second-order wave histories at each specified location
	gauss.sta	Statistics of the simulated first-order histories at each specified location
	ngauss.sta	Statistics of the simulated combined histories at each specified location
<b>Identification Example</b>		
<b>File Type</b>	<b>File Name</b>	<b>Description</b>
Input Files	wavide.inp	Input to WAVEMAKER
	hist.dat	Observed wave history for which underlying first-order history is to be identified
Output Files	gauss.ide	Identified first-order wave history
	ngauss.ide	Identified second-order, combined first- and second-order, and observed wave histories

## 4.2 Compiling the Source

On a Unix workstation, the Makefile can be used to build the WAVEMAKER executable. To compile on your host Computer:

- change directory to the subdirectory containing the source code files
- type "make wavmkr" (without the double quotes) at the Unix prompt and press return

The above will compile all the files listed in Makefile and link them to make the executable wavmkr. Note that the executable wavmkr is still in the current directory, and may be moved to the directory which contains the input file, or you can specify the path to the executable file in order to run it from other directories.

On other operating systems and architectures, follow whatever is the standard procedure for compiling and linking FORTRAN source code distributed over multiple files.

WAVEMAKER has been developed on a Sun Sparcstation2, using version 1.4 of the Sun FORTRAN compiler. Every attempt has been made to adhere to the ANSI FORTRAN 77 standard, ensuring portability of the code.

### 4.3 Executing the Routine

At the Unix prompt type "wavmkr < wavmkr.inp" (without the double quotes) in order to execute WAVEMAKER and perform the simulation example analysis. The program reads input from the standard logical input unit. The logical units for standard input, standard output, and standard error are all used in WAVEMAKER. On the Sun compiler, 0 is used for standard error, 5 is standard input and 6 is standard output. If the appropriate unit numbers are different, they can be set using the IOER, IOIN, and IOOU variables in the WAVEMAKER driver program, and the package can be recompiled.

Run the example problem using the compiled code to check if you get the same output as provided in the example output files. Note that wavmkr will overwrite any existing file if you specify its name as the target output file using the write command in the input file.

Similarly, at the Unix prompt type "wavmkr < wavide.inp" (without the double quotes) in order to execute WAVEMAKER and perform the identification example analysis. The resulting output histories can be compared to the corresponding example output histories to verify successful compilation of WAVEMAKER.



## List of References

- Bitner-Gregerson, E., and Haver, S. 1991. Joint environmental model for reliability calculations. *Pages 472-478 of: Proceedings of the 1st international offshore and polar engineering conference (ISOPE)*.
- Borgman, L. E. 1969. Ocean wave simulation for engineering design. *Journal of waterways, harbors division*, **95**(4), 556-583. ASCE.
- Jha, A. K., and Winterstein, S. R. 1995. *Second-order random waves: Simulation in time and space*. Tech. rept. RMS-17. Reliability of Marine Structures Program, Stanford University, Dept. of Civil Engineering.
- Langley, R. S. 1987. A statistical analysis of non-linear random waves. *Ocean engineering (pergamon)*, **14**(5), 389-407.
- Longuet-Higgins, M. S. 1963. The effect of non-linearities on statistical distributions in the theory of sea waves. *Journal of fluid mechanics*, **17**(3), 459-480.
- Marthinsen, T., and Winterstein, S. R. 1992. On the skewness of random surface waves. *Pages 472-478 of: Proceedings of the 2nd international offshore and polar engineering conference, san francisco*. ISOPE.
- Molin, B, and Chen, X. B. 1990. *Calculation of second-order sum-frequency loads on tlp hulls*. Tech. rept. Institute Français du Petrole Report.
- SWIM, 2.1. 1995. *SWIM: Slow wave-induced motions- user's manual*. Dept. of Ocean Engineering, M.I.T.
- Ude, T. C. 1994. *Second-order load and response models for floating structures: Probabilistics analysis and system identification*. Tech. rept. RMS-16. Reliability of Marine Structures, Dept. of Civil Engr., Stanford University.
- Ude, T. C., and Winterstein, S. R. 1996. Calibration of models for slow drift motions using statistical moments of observed data. *In: 6th international offshore and polar engineering conference ISOPE*. to appear.

Vinje, T., and Haver, S. 1994. On the non-Gaussian structure of ocean waves. *Pages 453-480 of: Proceedings of the 7th international conference on the behaviour of offshore structures (BOSS)*, vol. 2.

WAMIT, 4.0. 1995. *WAMIT: A radiation-diffraction panel program for wave-body interactions-user's manual*. Dept. of Ocean Engineering, M.I.T.

Winterstein, S. R., and Jha, A. K. 1995. Random models of second-order waves and local wave statistics. *Pages 1171-1174 of: Proceedings of the 10th engineering mechanics speciality conference*. ASCE.

## Appendix A

# Output Files for Simulation Example

## Output File: gauss.his

# Underlying First-Order Wave Process		
#	Wave Elevation at Spatial Location	
# Time(sec.)	0.00	60.00
0.000000	-3.189	-4.754
0.500000	-1.754	-5.466
1.000000	-0.239	-5.410
1.500000	0.906	-4.667
2.000000	1.436	-3.660
2.500000	1.681	-2.714
3.000000	1.623	-1.676
3.500000	1.595	-0.875
4.000000	1.862	-0.137
4.500000	2.282	0.582
5.000000	2.802	1.211
5.500000	3.230	1.379
6.000000	3.263	1.263
6.500000	2.448	1.252
7.000000	1.403	1.572
7.500000	0.553	2.166
8.000000	-0.121	2.447
8.500000	-0.773	3.076
9.000000	-1.216	3.472
9.500000	-1.588	3.272
10.000000	-2.433	2.507
10.500000	-3.543	1.492
11.000000	-4.310	0.022
11.500000	-4.343	-1.441
:	:	:
:	:	:
:	:	:
2046.500000	-3.871	0.056
2047.000000	-4.266	-1.729
2047.500000	-4.040	-3.447

Note that ":" indicates more numbers. Since the files are long, we present truncated versions of the output files.

Output File: ngauss.his

# Total Second-Order Wave Process			
#	Wave Elevation at Spatial Location		
#	Time(sec.)	0.00	60.00
	0.000000	-3.487	-4.814
	0.500000	-2.747	-5.039
	1.000000	-0.970	-4.773
	1.500000	0.975	-4.589
	2.000000	1.927	-3.459
	2.500000	1.920	-2.768
	3.000000	2.210	-1.844
	3.500000	1.738	-0.534
	4.000000	2.034	-0.256
	4.500000	2.353	0.534
	5.000000	2.974	1.072
	5.500000	3.595	2.033
	6.000000	3.481	1.523
	6.500000	1.913	1.684
	7.000000	1.236	1.334
	7.500000	0.644	2.374
	8.000000	0.019	2.724
	8.500000	-0.826	3.160
	9.000000	-0.572	3.945
	9.500000	-1.304	3.330
	10.000000	-2.734	2.573
	10.500000	-3.700	1.296
	11.000000	-3.854	-1.195
	11.500000	-4.087	-1.811
	12.000000	-3.686	-2.346
	12.500000	-2.784	-2.356
	13.000000	-1.532	-2.498
	13.500000	-1.026	-2.256
	:	:	:
	:	:	:
	:	:	:
	2046.500000	-3.594	-1.165
	2047.000000	-3.918	-3.159
	2047.500000	-3.660	-4.297

Output File: gauss.sta

# Underlying First-Order Wave Process						
# Location	Mean	Sigma	Skewness	Kurtosis	Minimum	Maximum
0.00	0.9966E-09	2.975	0.3566E-01	2.917	-8.928	10.41
60.00	0.1000E-08	2.975	0.2010E-01	2.919	-9.241	9.784

---

Output File: ngauss.sta

# Total Second-Order Wave Process						
# Location	Mean	Sigma	Skewness	Kurtosis	Minimum	Maximum
0.00	-.3673E-09	3.027	0.1949	2.975	-8.235	11.85
60.00	-.1193E-08	3.037	0.1778	2.988	-8.576	11.18

## **Appendix B**

### **Input/Output Files for Identification Example**

Input File: **hist.dat**

```
-3.487  
-2.747  
-0.970  
0.975  
1.927  
1.920  
2.210  
1.738  
2.034  
2.353  
2.974  
3.595  
3.480  
1.914  
1.236  
0.644  
0.019  
-0.826  
-0.572  
-1.304  
-2.734  
-3.700  
:  
:  
:  
-1.458  
-2.043  
-2.767  
-3.241  
-3.594  
-3.918  
-3.660
```

Note that ":" indicates more numbers. Since the files are long, we present truncated versions of the output files.

## Output File: gauss.ide

```
# Identified First-Order Wave History
# Window: number iterations restarts
# Window      1      6      0
-2.9780
-1.5528
-0.1932
 1.0374
 1.4503
  :
-0.4398
 0.9539
-1.0007
# Window      2      8      0
 0.6255
 0.8085
 0.5614
 0.5256
 1.0275
 0.9476
 1.1145
  :
  :
# Window      8      5      0
-2.2065
-1.4332
-1.1666
-1.0438
-0.8492
  :
-3.2288
-3.7402
-4.1472
-3.4963
```

Output File: ngauss.ide

# Identified 2nd-Order Wave, Identified Total Wave, Input Wave History			
# Window:	number	iterations	restarts
# Window	1	6	0
	-0.5090	-3.4870	-3.4870
	-1.1942	-2.7470	-2.7470
	-0.7768	-0.9700	-0.9700
	-0.0624	0.9750	0.9750
	0.4767	1.9270	1.9270
	:	:	:
	-0.0489	-1.7070	-1.7070
	-0.8702	-1.3100	-1.3100
	-0.3039	0.6500	0.6500
	2.0597	1.0590	1.0590
# Window	2	8	0
	0.1029	0.7284	0.7320
	0.4542	1.2627	1.2660
	0.3126	0.8740	0.8710
	0.0864	0.6120	0.6120
	0.1123	1.1399	1.1390
	0.4375	1.3851	1.3860
	0.0240	1.1385	1.1380
	:	:	:
	:	:	:
# Window	8	5	0
	-0.3825	-2.5890	-2.5890
	0.3802	-1.0530	-1.0530
	0.3296	-0.8370	-0.8370
	0.2628	-0.7810	-0.7810
	0.1202	-0.7290	-0.7290
	:	:	:
	-0.0122	-3.2410	-3.2410
	0.1462	-3.5940	-3.5940
	0.2292	-3.9180	-3.9180
	-0.1637	-3.6600	-3.6600

## Appendix C

# Random Models of Second-Order Waves and Local Wave Statistics

The following paper demonstrates the application of these nonlinear wave models and simulation techniques. It also shows how wave moments can be estimated analytically, and resulting estimates of extreme waves formed. Finally, various local wave characteristics found from the simulation are compared with field and wave tank data.

It has appeared in the Proceedings of the 10th Engineering Mechanics Specialty Conference, ASCE, held in Boulder, May 1995.

## RANDOM MODELS OF SECOND-ORDER WAVES AND LOCAL WAVE STATISTICS

Steven R. Winterstein and Alok K. Jha  
Civil Eng. Dept., Stanford University

### Abstract

We consider second-order random models of ocean waves at arbitrary water depths. We derive convenient new analytical results for wave moments, and show results for crests and other local wave statistics. Theoretical predictions are compared with observed wave tank results in extreme seas.

### Introduction

Nonlinear hydrodynamic effects are of growing interest for ocean structures and vessels. This has spurred development of efficient methods to estimate statistics of second-order hydrodynamic models (e.g., Winterstein et al, 1994). Here we apply these to one of the most fundamental nonlinearities in ocean engineering: the wave elevation  $\eta(t)$  at a fixed spatial location.

Linear wave theory results in a Gaussian model of  $\eta(t)$ . This ignores the marked asymmetry of  $\eta(t)$ : wave crests that systematically exceed subsequent troughs. This has several practical implications: (1) asymmetric waves are more likely to strike decks of offshore platforms, particularly older Gulf-of-Mexico structures with fairly low decks; and (2) unusually large dynamic response has been found in high, steep waves that may not follow linear theory.

Second-order random wave models are not new; indeed, they have been a research topic for more than 30 years (e.g., Longuet-Higgins, 1963) and remain so today (e.g., Marthinsen and Winterstein, 1992; Hu and Zhao, 1993; Vinje and Haver, 1994). However, they have not yet entered common offshore engineering practice, which applies either (1) random linear (Gaussian) waves or (2) regular Stokes waves that fail to preserve  $S_\eta(\omega)$ , the wave power spectrum. Several drawbacks to second-order random waves may be suggested: (1) they omit potentially important higher-order effects; and (2) convenient statistical analysis methods for second-order models are often lacking. We seek to address both concerns here—the first through systematic comparison of theory with observed wave tank results in extreme seas. The second issue is met by fitting new analytical results for wave moments, and using these to construct simple Hermite models of extreme crests.

### Statistics of Second-Order Models

Our “input” is the first-order, Gaussian wave process  $\eta_1(t)$  from linear theory. The standard Fourier sum for  $\eta_1(t)$  is then  $\text{Re} \sum C_k \exp(i\omega_k t)$ , in which  $C_k = A_k \exp(i\phi_k)$  in

terms of Rayleigh distributed amplitudes,  $A_k$ , and uniformly distributed phases  $\phi_k$ . The resulting "output" is  $x(t) = x_1(t) + x_2(t)$ , in which

$$x_1 = \text{Re} \sum_k C_k H_k e^{i\omega_k t}; \quad x_2 = \text{Re} \sum_k \sum_l C_k C_l [H_{kl}^+ e^{i(\omega_k + \omega_l)t} + H_{kl}^- e^{i(\omega_k - \omega_l)t}] \quad (1)$$

Here the transfer function  $H_k$  describes first-order effects, while  $H_{kl}^+$  and  $H_{kl}^-$  reflect second-order effects at sums and differences of all wave frequencies ( $\omega_k \pm \omega_l$ ). In our case  $x(t)$  is the second-order wave itself, for which  $H_{kl}^+$  and  $H_{kl}^-$  are given analytically (e.g., Marthinsen and Winterstein, 1992), and  $H_k = 1$ . The same analysis applies more generally to the diffracted wave, applied force and response of large-volume structures, with numerical  $H_k$  and  $H_{kl}$  estimates from second-order diffraction (Winterstein et al, 1994).

Because  $x(t)$  is non-Gaussian, interest focuses on its skewness  $\alpha_3$  and kurtosis  $\alpha_4$ . In terms of the significant wave height  $H_S = 4\sigma_{\eta_1}$  and peak spectral period  $T_P$ , these are

$$\alpha_3 \sigma_x^3 = m_{31}(T_P) H_S^4 + m_{33}(T_P) H_S^6 \quad (2)$$

$$(\alpha_4 - 3) \sigma_x^4 = m_{42}(T_P) H_S^6 + m_{44}(T_P) H_S^8 \quad (3)$$

The  $m_{ij}(T_P)$  are "response moment influence coefficients," the contribution to response moment (cumulant)  $i$  due to terms of order  $O(x_2^j)$ . In general these are conveniently calculated from Kac-Siegert analysis (Eqs. 12-15, Winterstein et al, 1994). We assume here the spectrum of  $\eta_1(t)$  is of the form  $H_S^2 T_P f(\omega T_P)$ , so that  $\eta_1(t)$  scales in amplitude with  $H_S$  and in time with  $T_P$ .

It is useful to define the unitless wave steepness  $s_P = H_S/L_P$ , in which the characteristic wave length  $L_P = gT_P^2/2\pi$  uses the linear dispersion relation. For deep-water waves the coefficients  $m_{ij}(T_P)$  are proportional to  $L_P^{-j}$ . Retaining leading terms in  $s_P$  from Eqs. 2-3:

$$\alpha_3 = k_3 s_P; \quad \alpha_4 - 3 = k_4 \alpha_3^2 \quad (4)$$

In particular, for a JONSWAP wave spectrum with peakedness factor  $\gamma$ , we have fit the following  $k_3$  and  $k_4$  expressions to results for a wide range of depths:

$$k_3 = \frac{\alpha_3}{s_P} = 5.45\gamma^{-.084} + .135\left(\frac{d}{L_P}\right)^{-1.22}; \quad k_4 = \frac{\alpha_4 - 3}{\alpha_3^2} = 1.41\gamma^{-.020} \quad (5)$$

The second term in this result for  $\alpha_3$  reflects the effect of a finite water depth  $d$ : in shallower water  $\alpha_3$  grows, as the waves begin to "feel" the bottom.

Note also that while the skewness varies linearly with steepness, the kurtosis varies quadratically. This suggests that nonlinear effects will be most strongly displayed by the skewness, and hence by the wave crests rather than the total peak-to-trough wave height. This second-order model may less accurately predict kurtosis, however, as higher-order omitted effects may be of the same order of magnitude.

## Numerical Results

Figure 1 compares skewness predictions with results from wave tank tests. The tests include 18 large seastates (target  $H_S = 14.5\text{m} - 15.5\text{m}$ ), each over 3 hours in length, at water depths exceeding 300m. Figure 1 shows the resulting skewness and steepness in each hour of each test. While there is considerable scatter, regression on these data

gives the estimated slope  $k_3=5.50$ , remarkably close to Eq. 5 with  $\gamma=1$ . The scatter in Figure 1 is also consistent: the observed  $\sigma_{\alpha_3}$  is found well-predicted by simulated hourly segments of second-order seastates. Figure 2 shows kurtosis estimates to deviate, however. The data yield the estimate  $k_4=4.2$ , roughly 3 times the value in Eq. 5 regardless of  $\gamma$ . This again supports theory, which suggests that unlike the skewness, the kurtosis may be notably affected by unmodelled, higher-order effects.

*Wave Crests.* Figure 3 shows the observed distribution of crest heights. These results combine six seastates with the same target spectrum, and hence give roughly 20 hours of similar wave conditions. As expected the Rayleigh model, based on linear theory, is significantly unconservative. An alternative empirical model (Haring et al, 1976) offers an improvement, but only mildly changes the Rayleigh for these deep-water conditions. Better agreement is found from a Non-Gaussian (Hermite) model, which uses a cubic distortion of the normal process (and hence its Rayleigh peaks) to match  $\alpha_3$  and  $\alpha_4$  (Winterstein et al, 1994). Here estimates of  $\alpha_3$  and  $\alpha_4$  use Eq. 5, tripling its  $k_4$  value to reflect unmodelled effects. These give excellent agreement with observed moments, though still somewhat unconservative crest predictions at higher levels.

*Local Wave Characteristics.* Figure 4 shows the conditional mean and standard deviation of crest height, given the peak-to-trough wave height. Again the data use 20 hours of wave tank studies, all with the same target wave spectrum. Also shown are corresponding estimates from simulation of Gaussian and Non-Gaussian (second-order) models. Due to the symmetry of the Gaussian model, its crests are on average 50% of the total wave height. The data shows systematically larger crests. The second-order model is found to predict this vertical asymmetry quite accurately.

We may also consider horizontal wave asymmetry: do crest front periods—during which  $\eta$  increases from its mean level to a crest—differ statistically from subsequent crest back periods? This temporal asymmetry is not predicted by either the Gaussian or second-order model. It is difficult, however, to find this asymmetry in the data: Figure 5 shows observed crest fronts to be quite close to 50% of the total crest period. Finally, Figure 6 shows the variation of wave period with crest height. All results show the same trend of increasing periods over small-to-moderate heights, and roughly constant period at large heights. The Non-Gaussian model appears to somewhat better predict results at larger crest height levels.

## References

- Haring, R.E., A.R. Osborne, and L.-P. Spencer (1976). Extreme wave parameters based on continental shelf storm wave records. *Proc., 15th Coastal Eng. Conf., ASCE*, 151–170.
- Hu, S.J. and D. Zhao (1993). Non-Gaussian properties of second-order random waves. *J. Engrg. Mech., ASCE*, 119(2), 344–364.
- Longuet-Higgins, M.S. (1963). The effect of non-linearities on statistical distributions in the theory of sea waves. *J. Fluid Mech.*, 17(3), 459–480.
- Marthinsen, T.M. and S.R. Winterstein (1992). On the skewness of random surface waves. *Proc., 2nd Intl. Offshore Polar Eng. Conf., ISOPE*, 472–478.
- Vinje, T. and S. Haver (1994). On the non-Gaussian structure of ocean waves. *Proc., BOSS-94*, 2, 453–480.
- Winterstein, S.R., T.C. Ude and T. Marthinsen (1994). Volterra models of ocean structures: extreme and fatigue reliability. *J. Engrg. Mech., ASCE*, 120(6), 1369–1385.

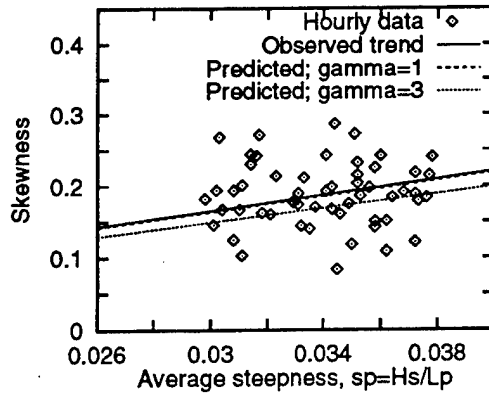


Figure 1: Skewness: Theory vs Data

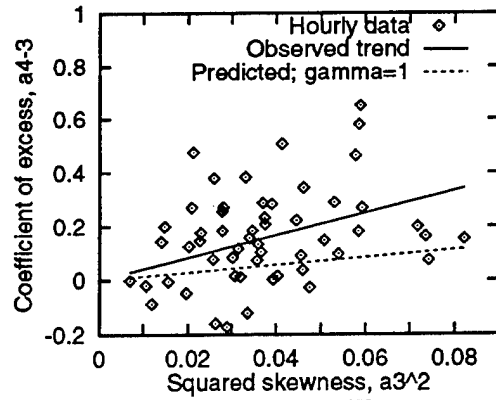


Figure 2: Kurtosis: Theory vs Data

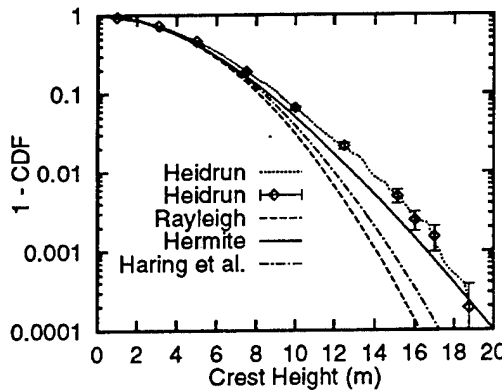


Figure 3: Crest Heights: Theory vs Data

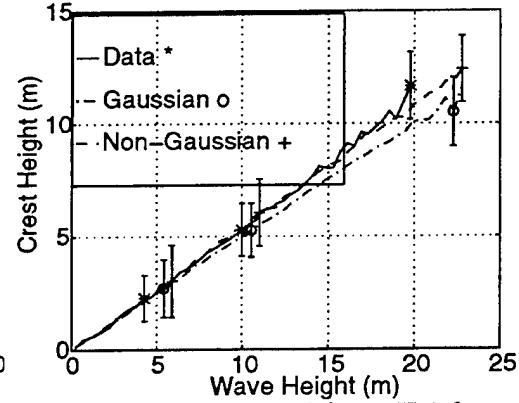


Figure 4: Variation of Crest Height with Wave Height

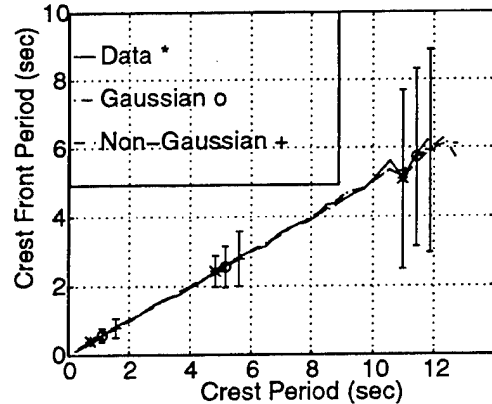


Figure 5: Variation of Crest Front Period with Total Crest Period

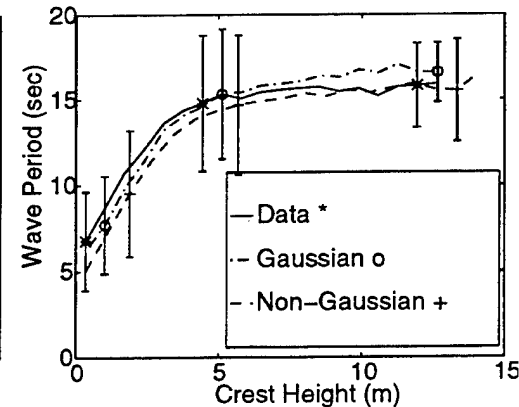


Figure 6: Variation of Crest Height with Wave Period

# REPORT DOCUMENTATION PAGE

Form Approved  
OMB No. 0704-0188

Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden to Washington Headquarters Service, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188) Washington, DC 20503.

PLEASE DO NOT RETURN YOUR FORM TO THE ABOVE ADDRESS.

1. REPORT DATE (DD-MM-YYYY) 00-06-1996		2. REPORT DATE June, 1996		3. DATES COVERED (From - To)	
4. TITLE AND SUBTITLE Wavemaker 2D: SIMULATION AND IDENTIFICATION OF SECOND-ORDER RANDOM WAVES.				5a. CONTRACT NUMBER	
				5b. GRANT NUMBER N00014-96-1-0641	
				5c. PROGRAM ELEMENT NUMBER	
6. AUTHOR(S) Alok K. Jha Steven R. Winterstein				5d. PROJECT NUMBER	
				5e. TASK NUMBER	
				5f. WORK UNIT NUMBER	
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) RMS GROUP S.R. Winterstein, C.A. Cornell Blume Center Stanford University, CA 94305				8. PERFORMING ORGANIZATION REPORT NUMBER RMS-22	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES) OFFICE OF NAVAL RESEARCH 800 NORTH QUINLY ST ARLINGTON, VA 22217-4620 ATTN: ROSHDY BARSOUM				10. SPONSOR/MONITOR'S ACRONYM(S)	
				11. SPONSORING/MONITORING AGENCY REPORT NUMBER	
12. DISTRIBUTION AVAILABILITY STATEMENT APPROVED FOR PUBLIC RELEASE					
13. SUPPLEMENTARY NOTES					
14. ABSTRACT This report documents the theory and use of the routine <u>WAVEMAKER</u> . The routine simulates a first-order wave process with an arbitrary power spectrum, and applies nonlinear corrections based on second-order hydrodynamics. The routine also includes the ability to identify the underlying first-order Gaussian history from a given observed time history. The identification is an inverse feature to simulation, and is based on a Newton-Raphson scheme to solve N simultaneous non-linear equations, where N is the number of specified points in the input time-history.					
15. SUBJECT TERMS					
16. SECURITY CLASSIFICATION OF:			17. LIMITATION OF ABSTRACT	18. NUMBER OF PAGES	19a. NAME OF RESPONSIBLE PERSON
a. REPORT	b. ABSTRACT	c. THIS PAGE			19b. TELEPHONE NUMBER (Include area code)