

# HIGH RESOLUTION CONVECTIVE HEAT TRANSFER MEASUREMENTS

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Aerodynamics

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# Acknowledgements

- Internal cooling
  - David Gillespie, Calvin Tsang, Changmin Son
- Stepped solution and fin research
  - Andrew Neely
- Recuperator research underway
  - Marty Cerza and Juan Adams
- Transition work
  - Richard Anthony

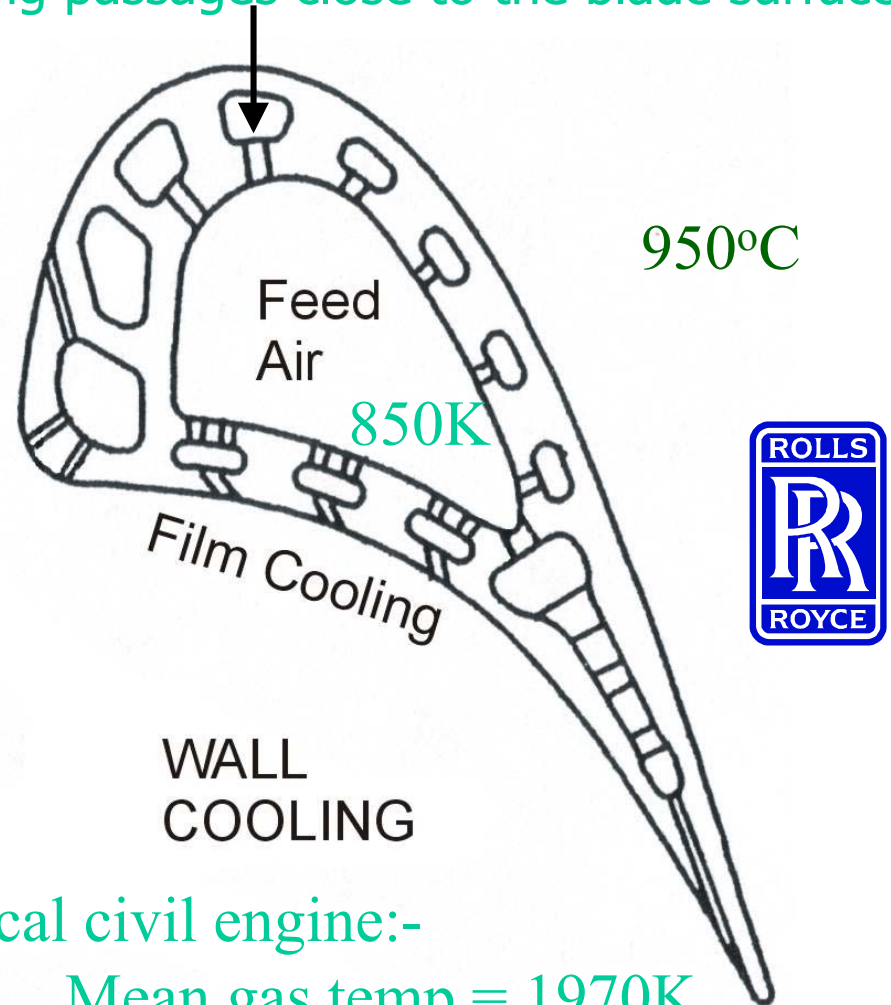
# Content

- High resolution htc measurements using temperature sensitive liquid crystals
  - Need for high resolution htc data
  - Scaling strategy
  - Liquid crystal instrument features
  - Application and test details
  - Example applications new developments
- Thin film gauges
  - Instrument details and recent developments
  - Applications
  - High density platinum gauges
- Conclusions

# Need for high resolution htc data in turbomachinery

- Detailed thermal model of the engine component required for component life predictions
- Aerospace turbine blades are small and cooling systems are usually compact.

Cooling passages close to the blade surface



Typical civil engine:-

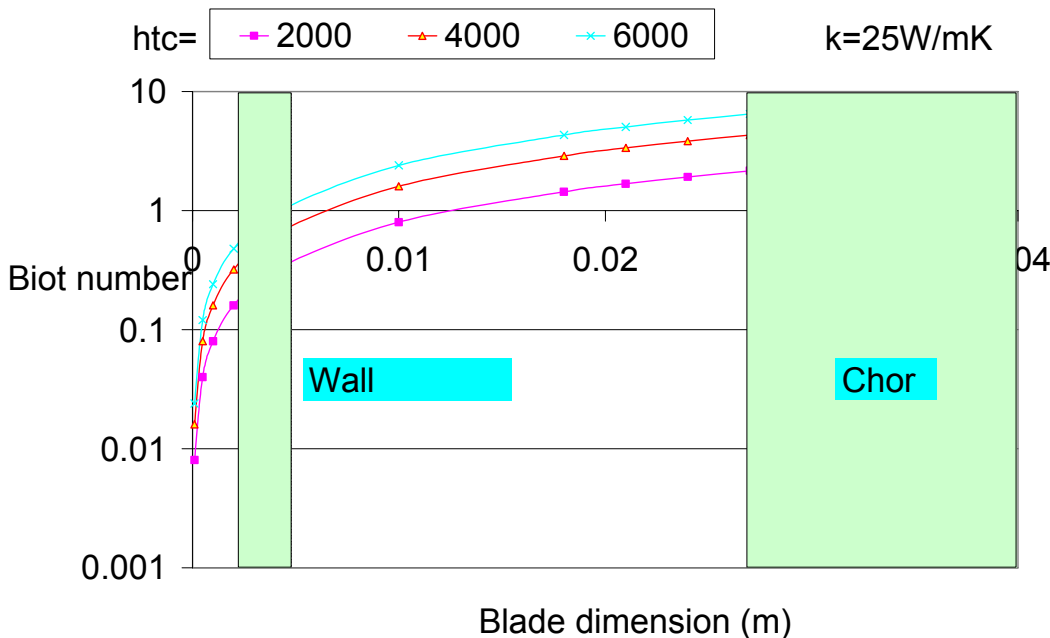
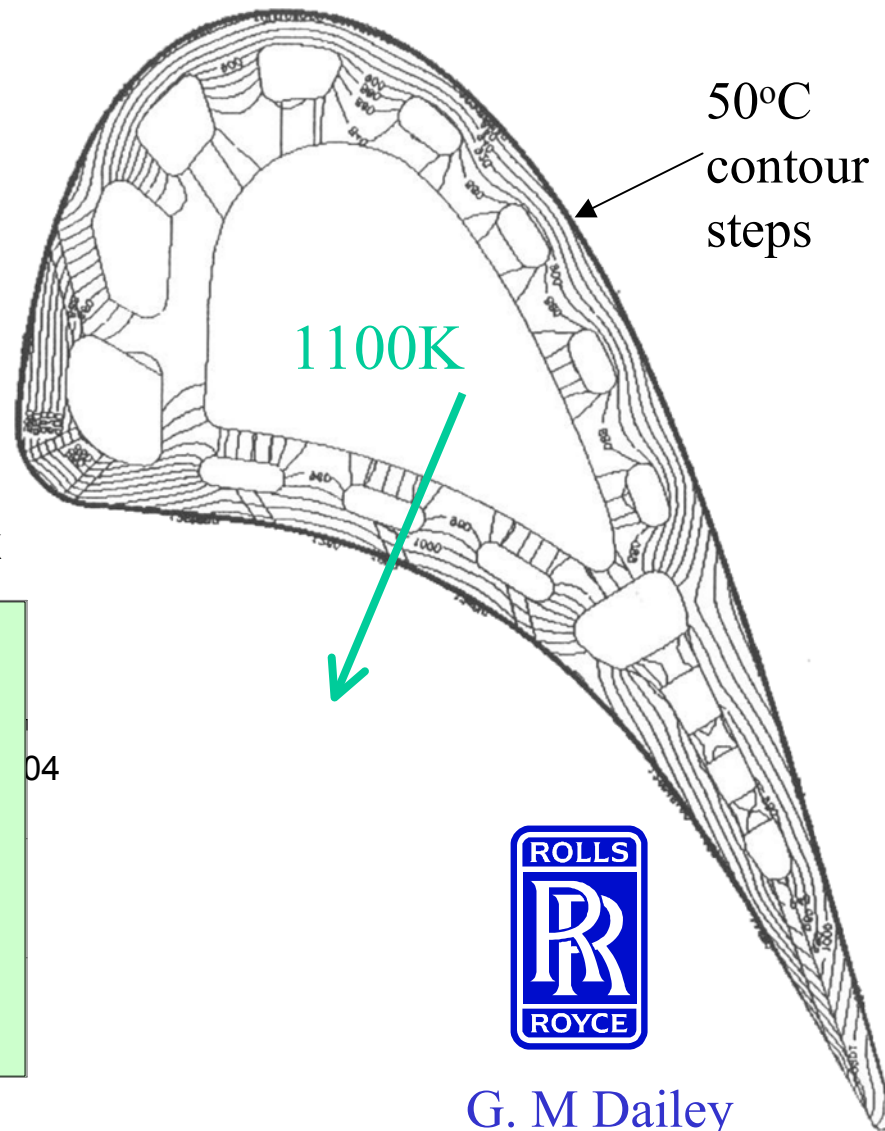
Mean gas temp = 1970K

Max relative = 2375K

# Example blade cooling temp distribution

- Blade far from isothermal
- Biot number not small enough

$$Biot = \frac{hL}{k}$$



G. M Dailey

# Scaling issues

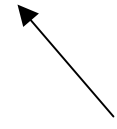
- Large scale model improves effective resolution.
- Switch off sideways (lateral) conduction to achieve local htc measurement with 1-d processing.
- No need for engine temperatures.
- Fluid dynamics correct through use of Reynolds number, Mach number and Prandtl number.

$$\text{Nu} = f(\text{Re}, \text{Pr}, \text{Mach})$$

Dimensionless  
heat transfer coefficient



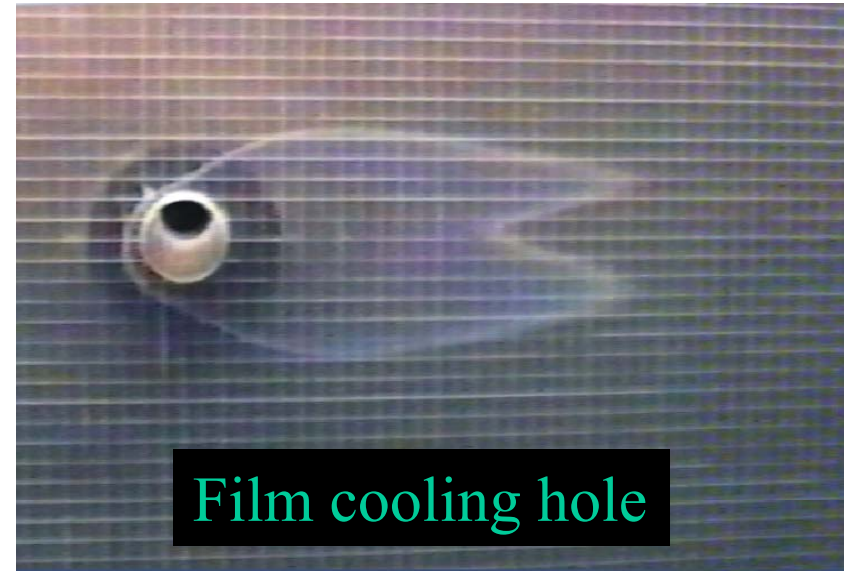
Dimensionless  
flow speed



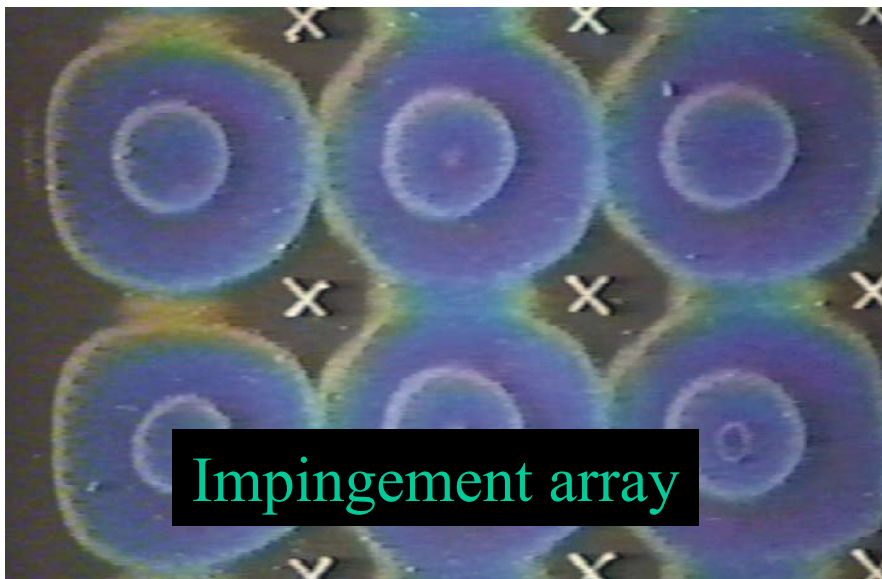
# Transient method with liquid crystals for internal cooling



Inclined ribs



Film cooling hole

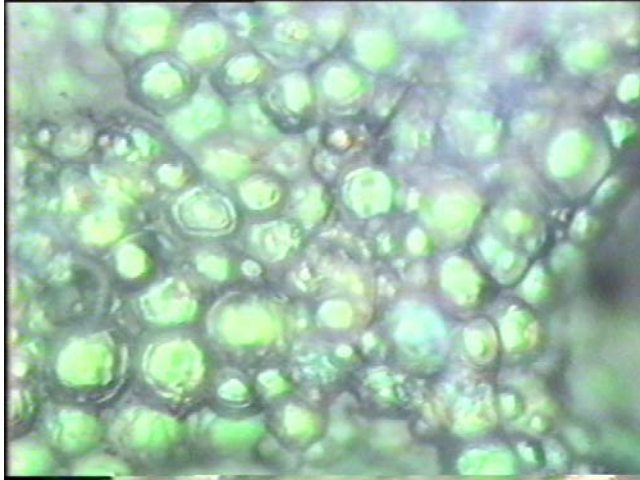


Impingement array



Pedestal bank

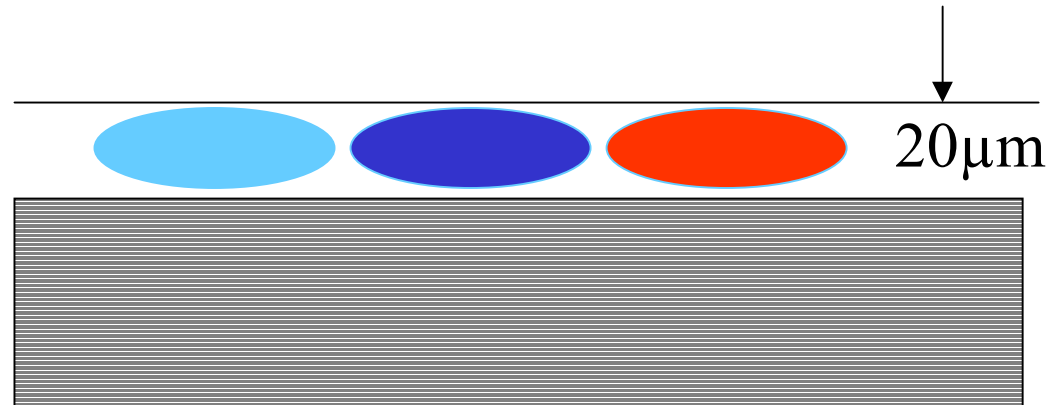
# Temperature measurement



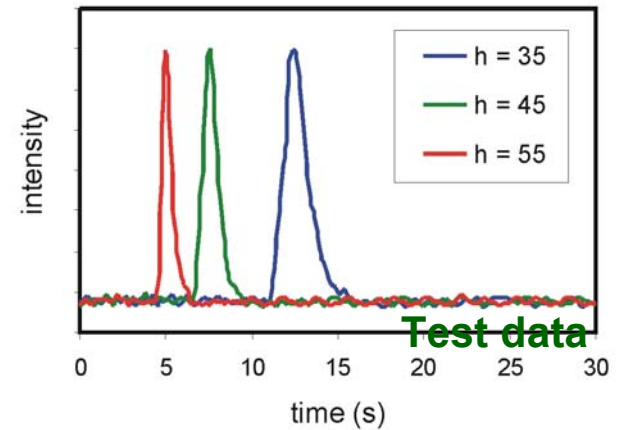
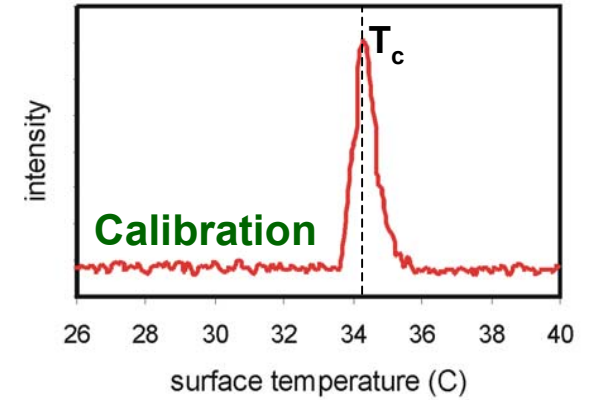
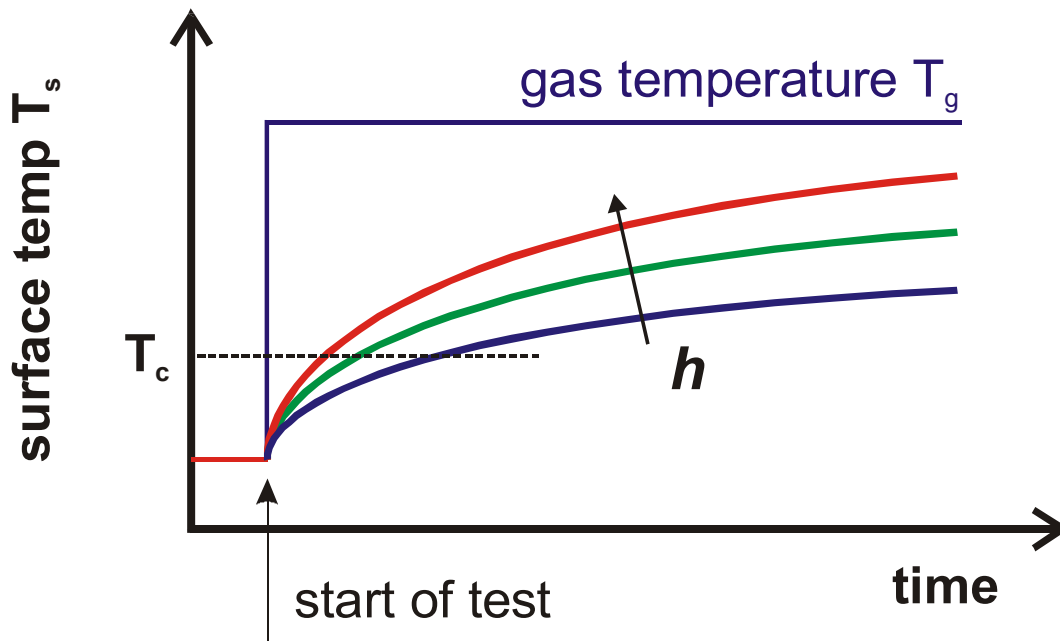
**R** **G** **B** signals from video  
→ **I**ntensity or **H**ue processing

$$I = R + G + B$$

$$\cos(H) = \frac{2R - G - B}{\sqrt{6((R - I)^2 + (G - I)^2 + (B - I)^2)}}$$

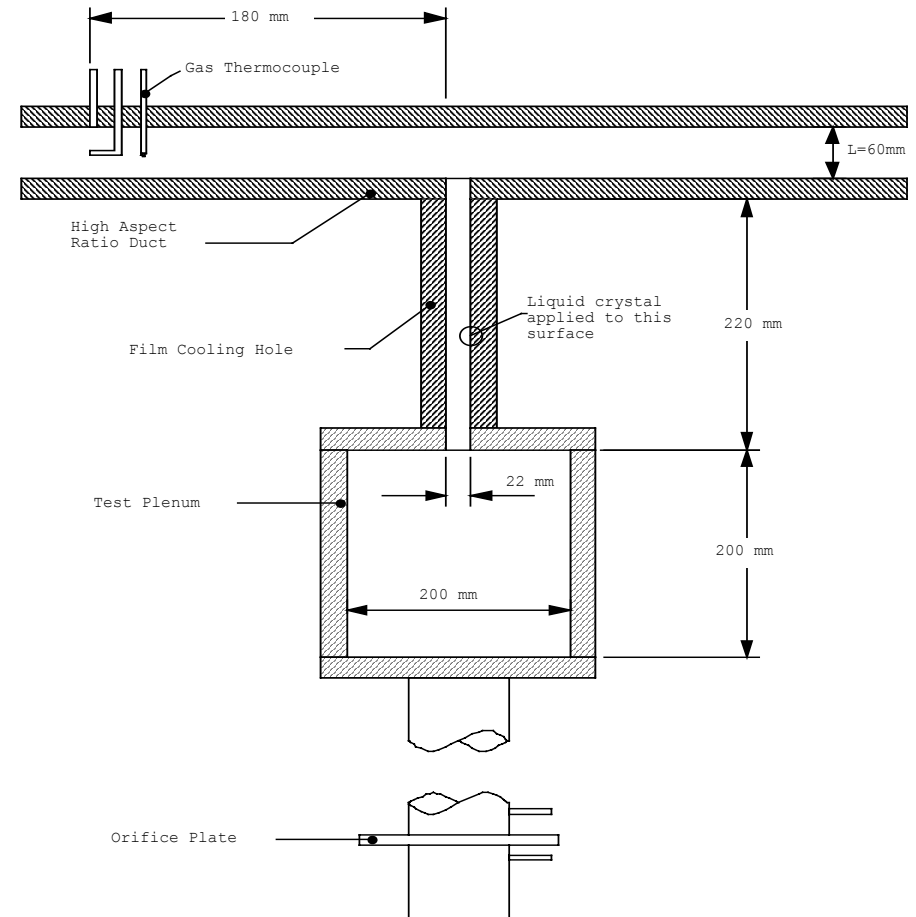
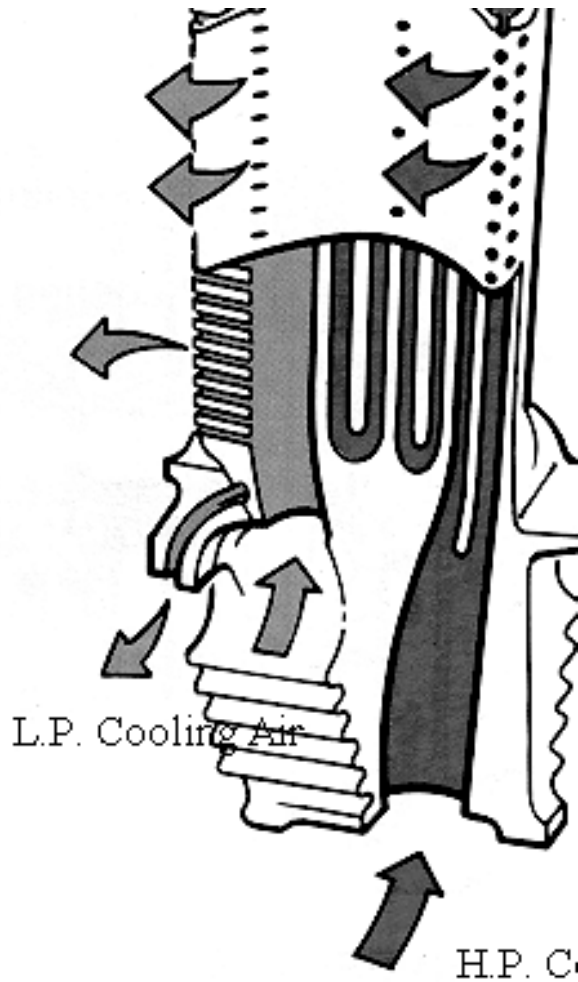


# Time of crystal colour change depends on local $h$



# Heat transfer inside a film-cooling hole fed in cross-flow

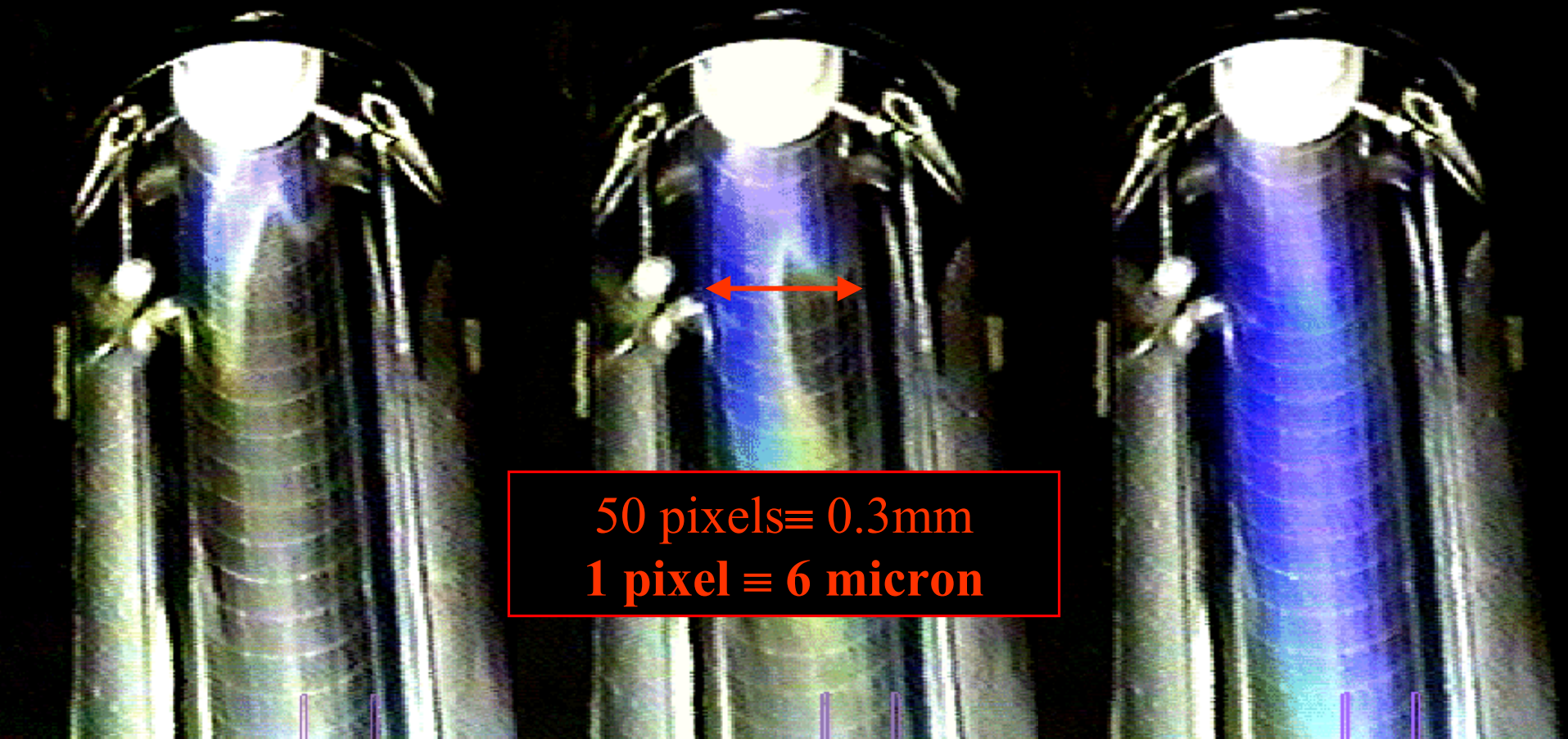
Hole diameter = 0.3mm



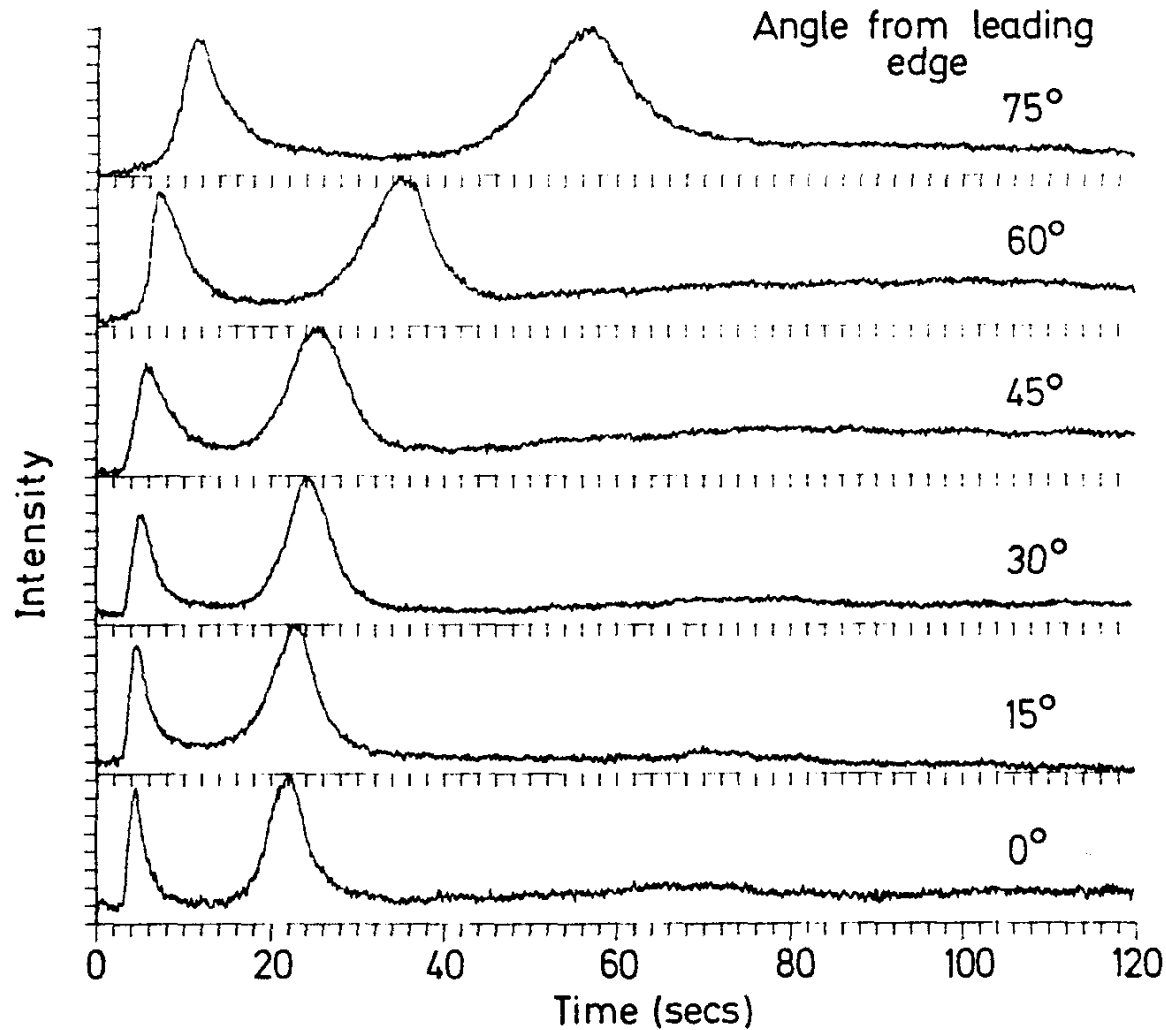
Hole diameter = 22mm

00:11:69 00:16:19 00:22:19

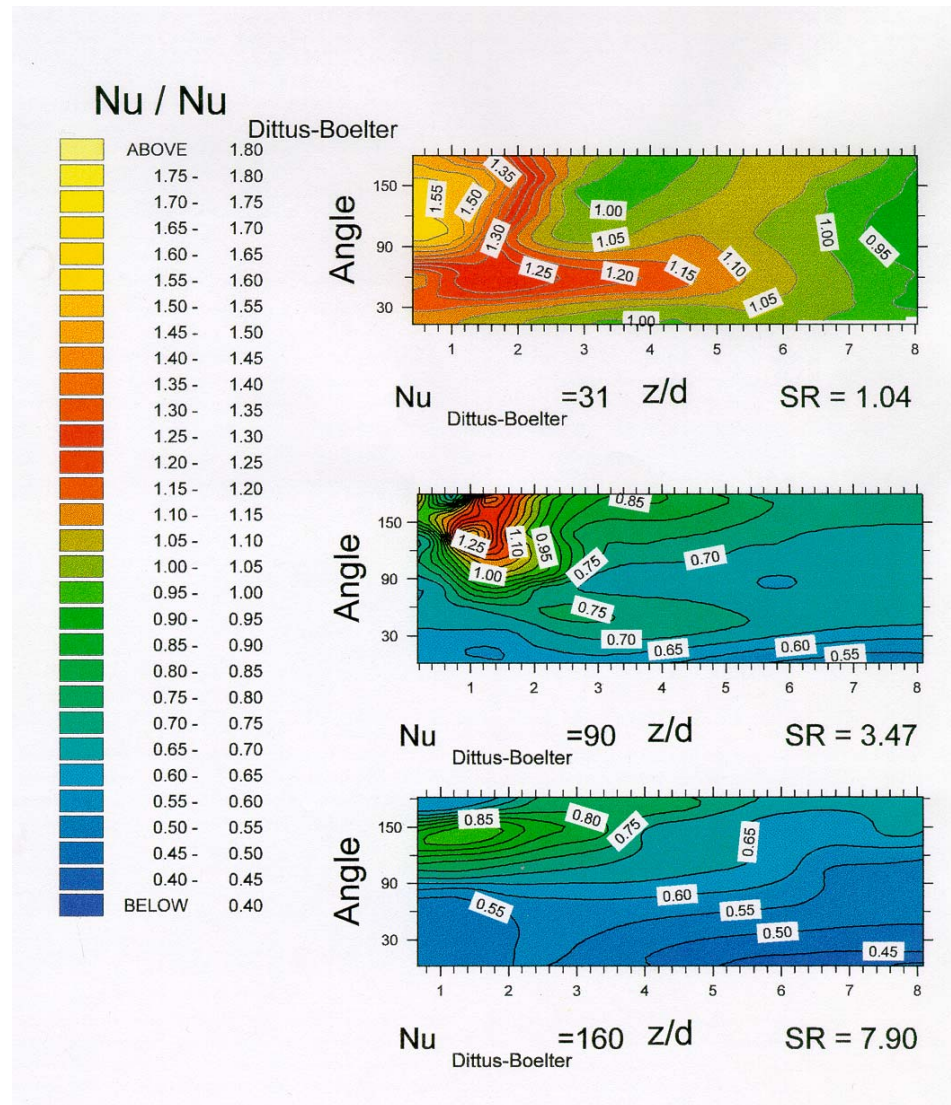
## Recorded Colour Play within the Hole



# Typical Intensity Histories at 6 Positions on the Film Cooling Hole Surface. Monochromatic processing.

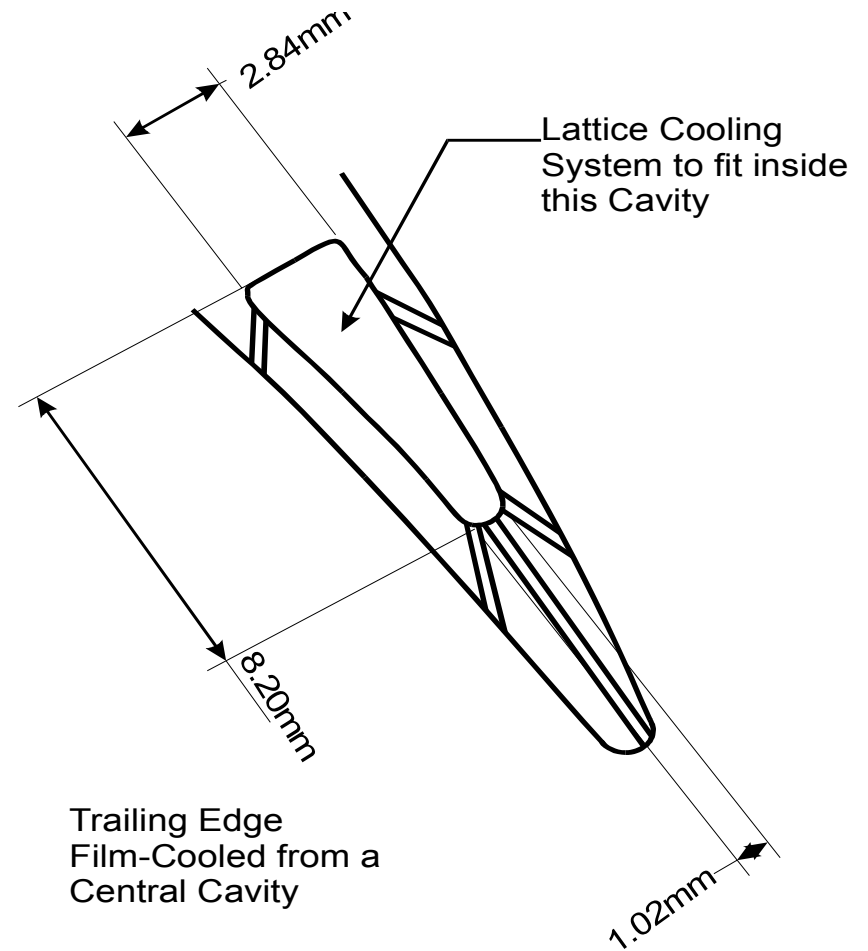


# Local Nusselt Number Distribution, 90° Hole

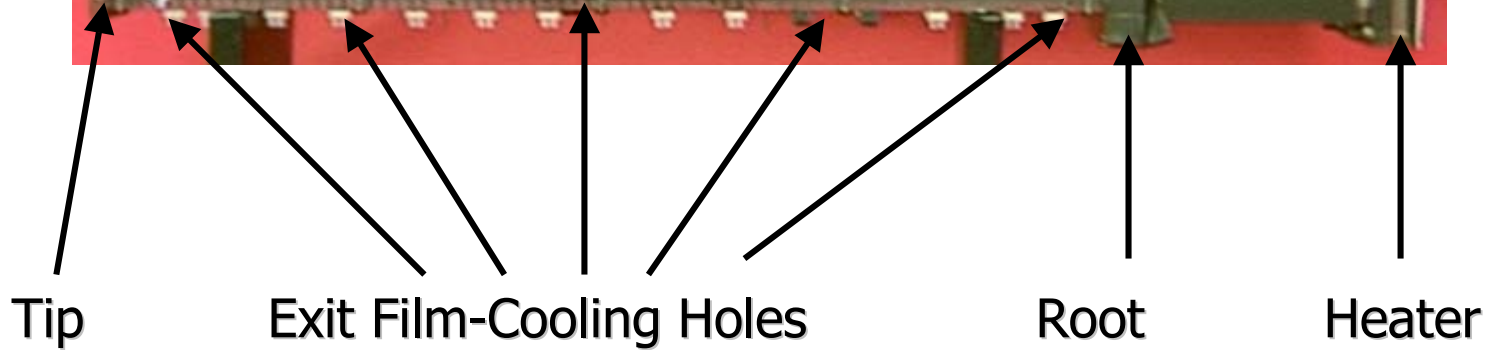
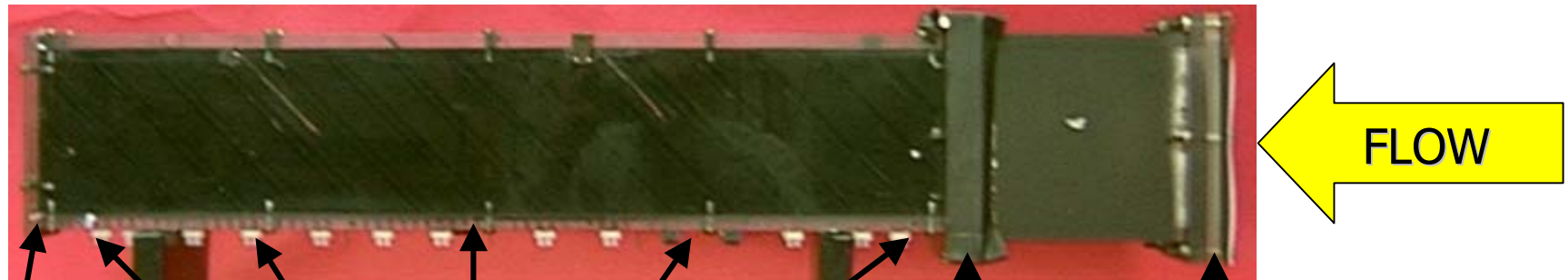


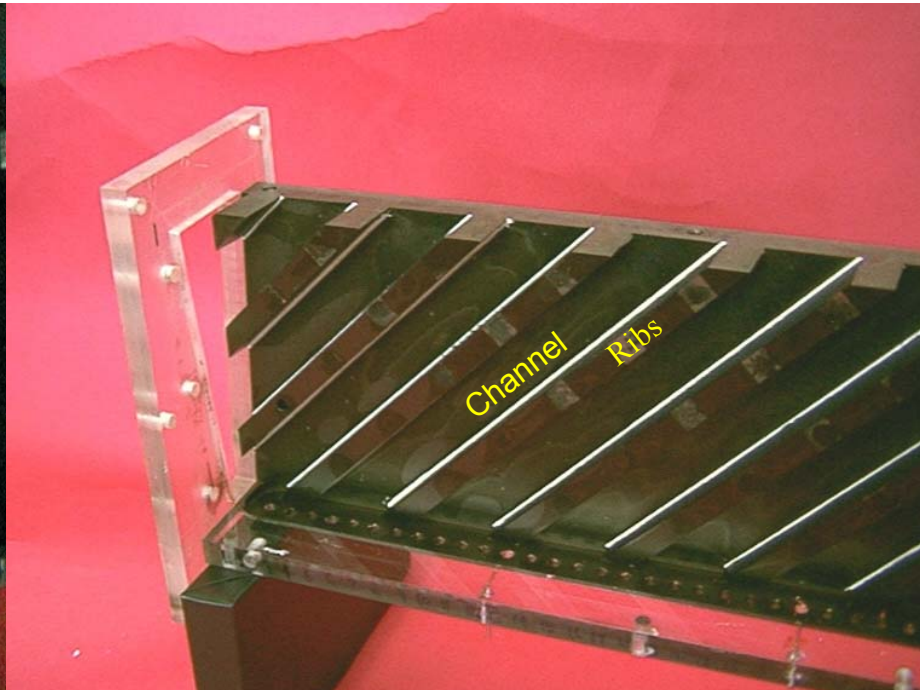
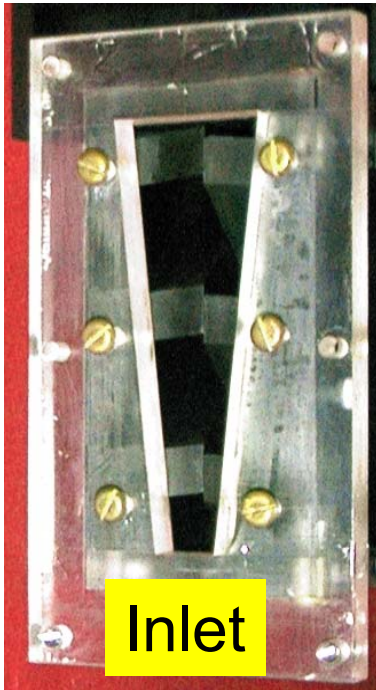
# Lattice cooling system for trailing edge

Geometric scaling essential  
for resolution

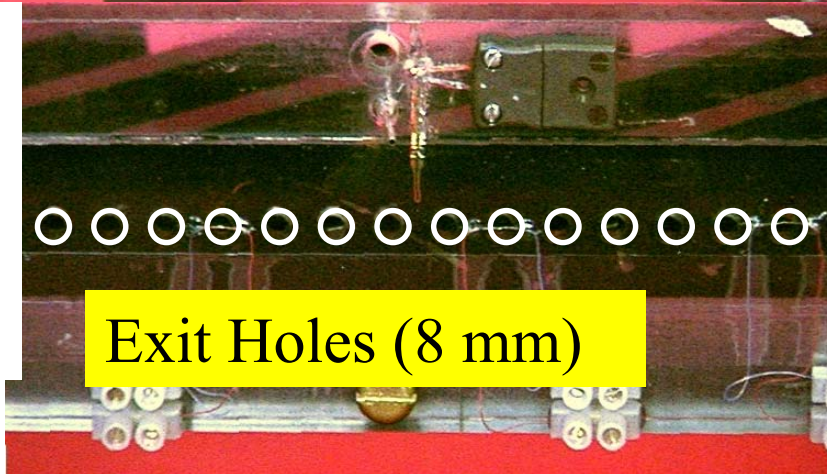


# The Assembled Lattice Model

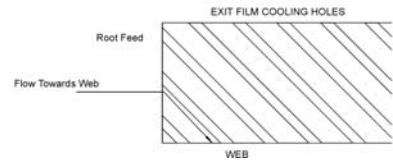
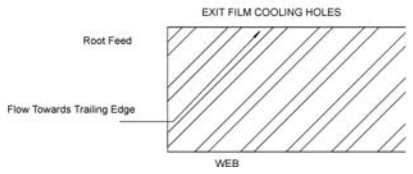
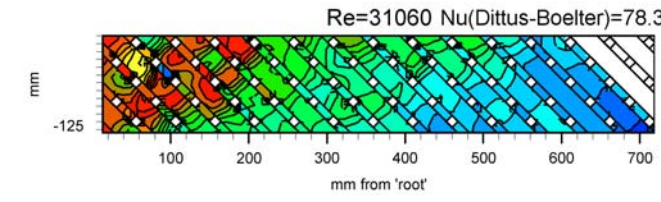
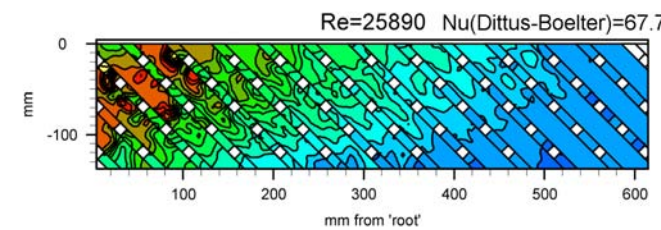
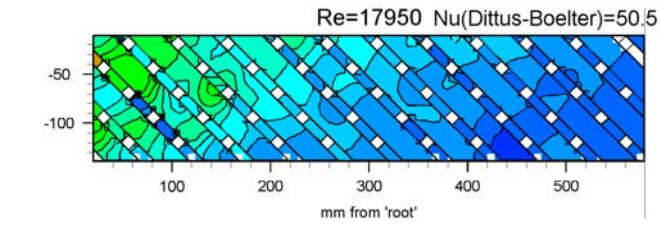
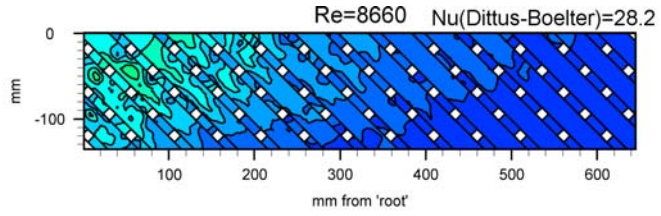
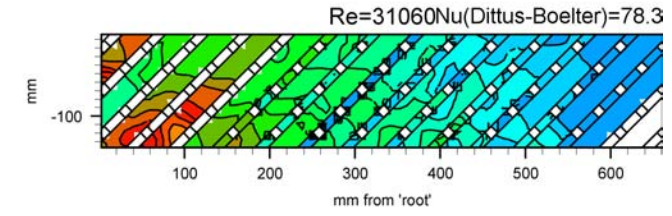
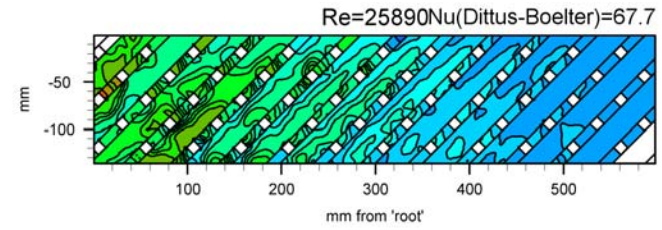
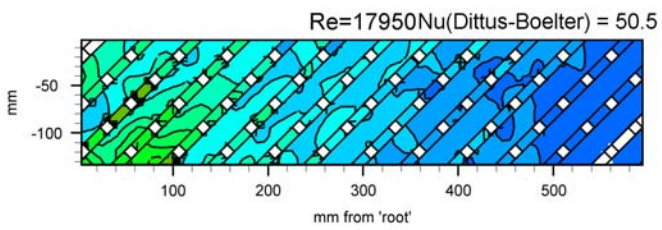
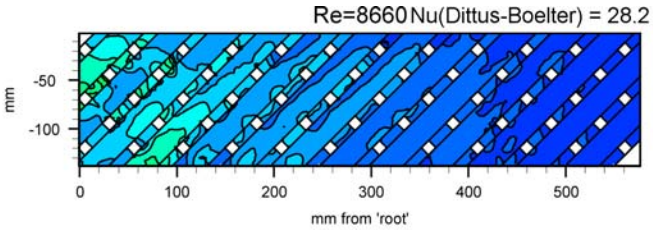
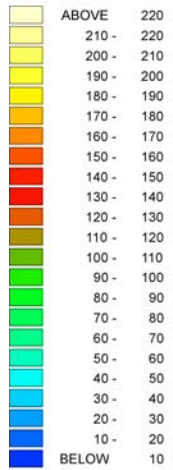




Photographs of the Working Section

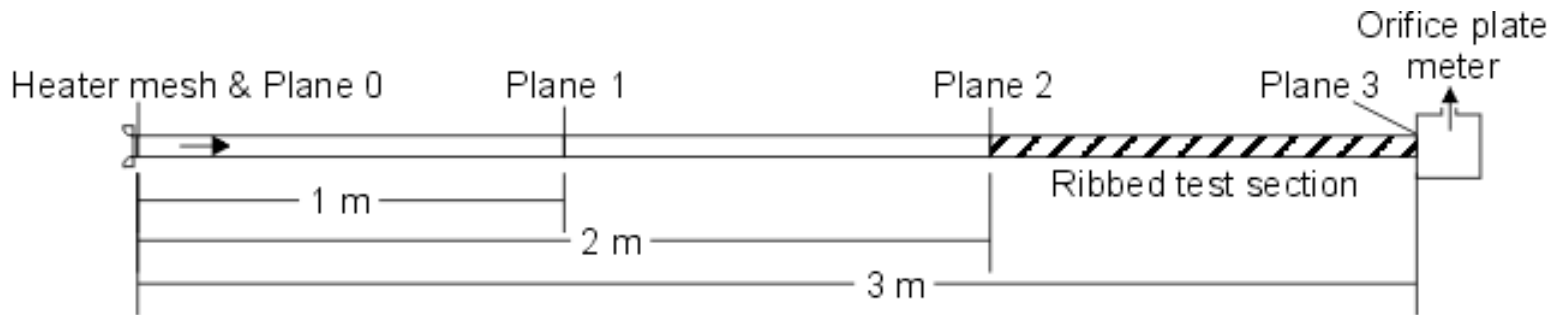


# Nusselt number distribution at several Reynolds numbers



# Rib roughened passage

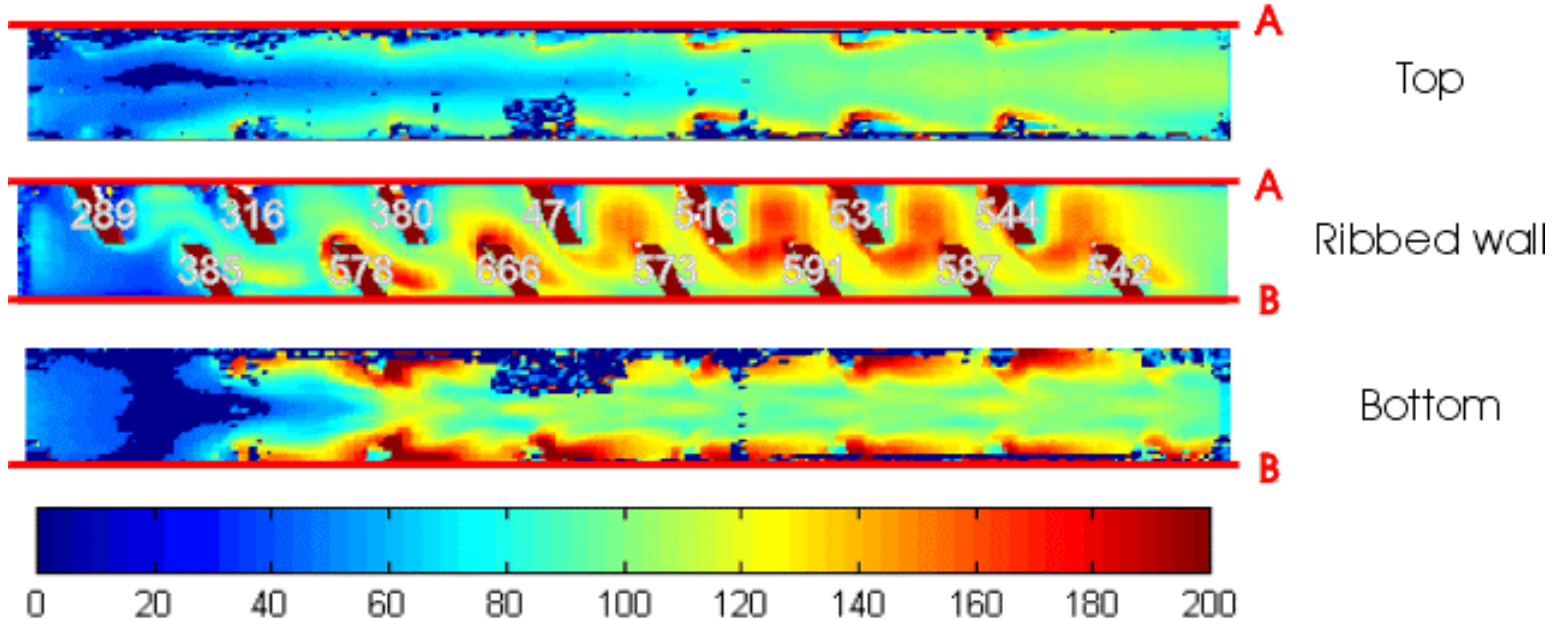
- 3 metres (60d) long, square cross section cooling passage
- Perspex walls with temperature sensitive liquid crystal coated on the inner surface.
- Reynolds number from 20,000 to 60,000
- Air is heated at the inlet using heater mesh
- Test section situated from 40d to 60d
- Fully developed flow established ahead of the test section
- Rotation not simulated in the experiment



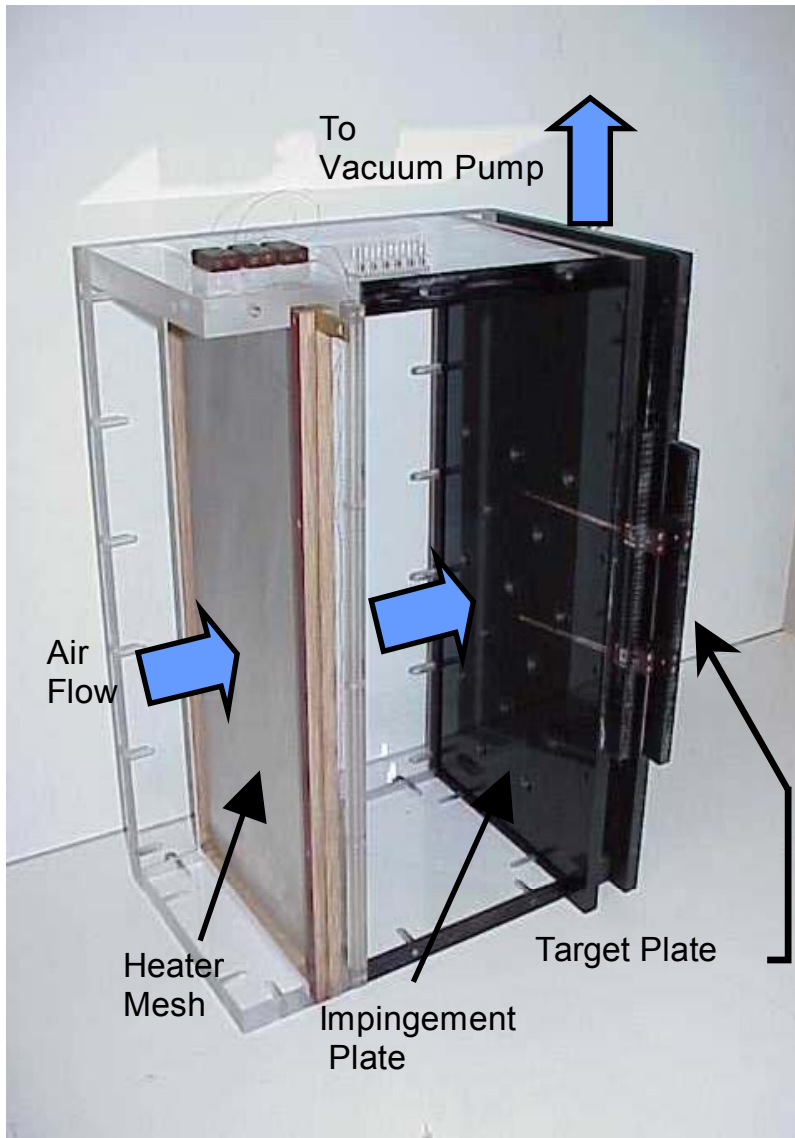
# Heat transfer distribution

## 60° interrupted inline ribs

Flow Direction

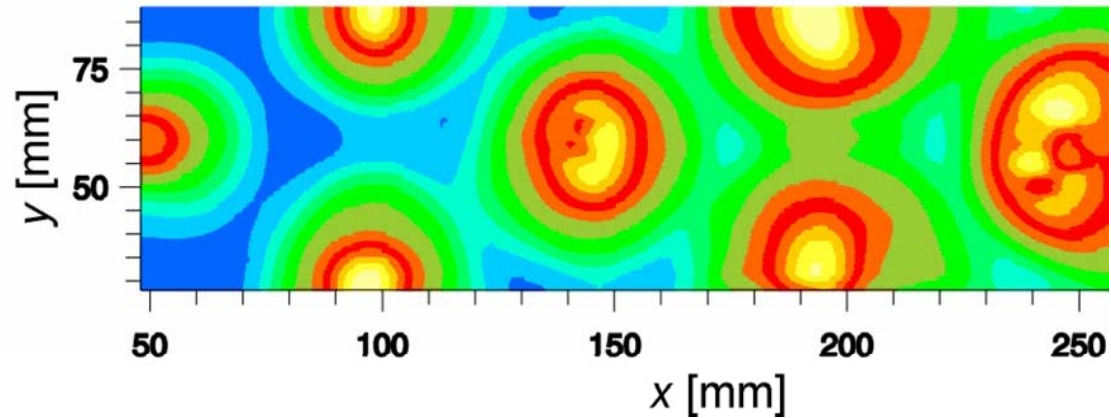
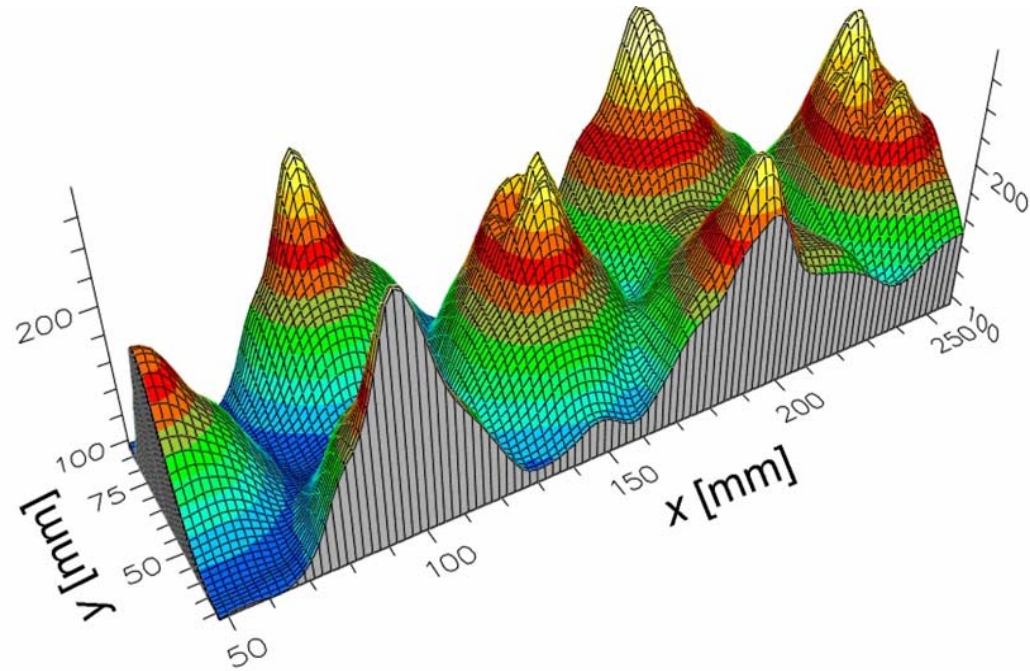
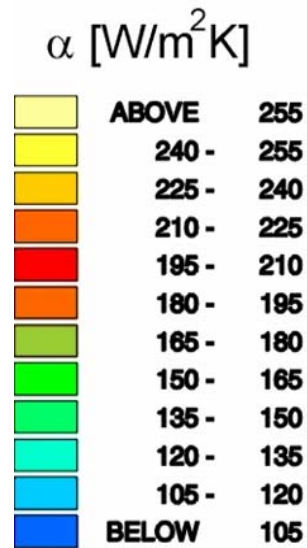


# Impingement heat transfer rig



The perspex test rig is instrumented with liquid crystal coated impingement and target plates, and fast response gas thermocouples at the entrance and exit of the working section

# Impinging jet heat transfer

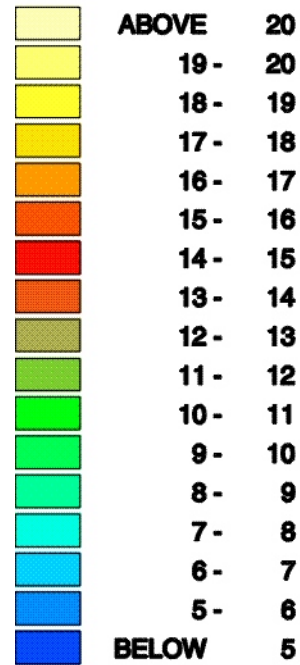
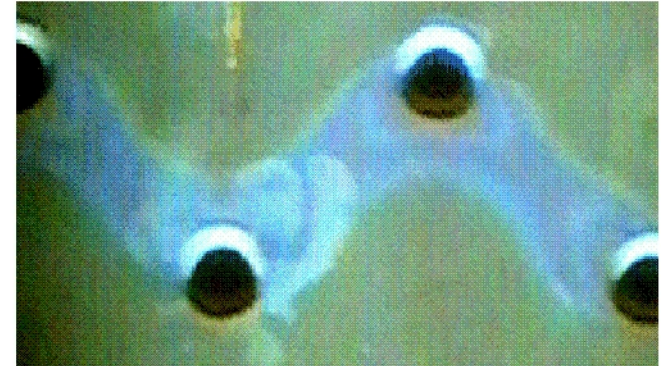
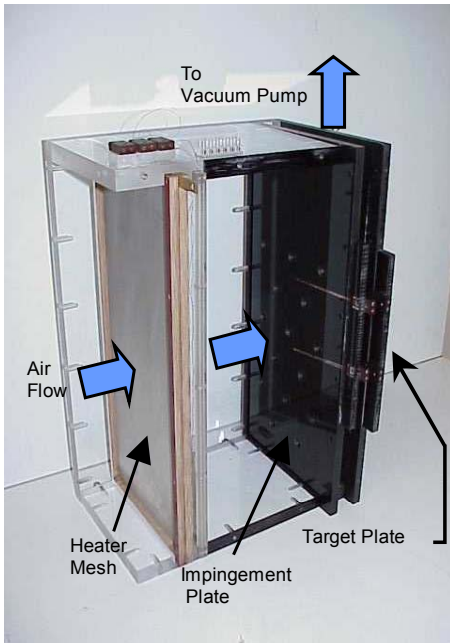


$$Re_{javg} = 26710$$

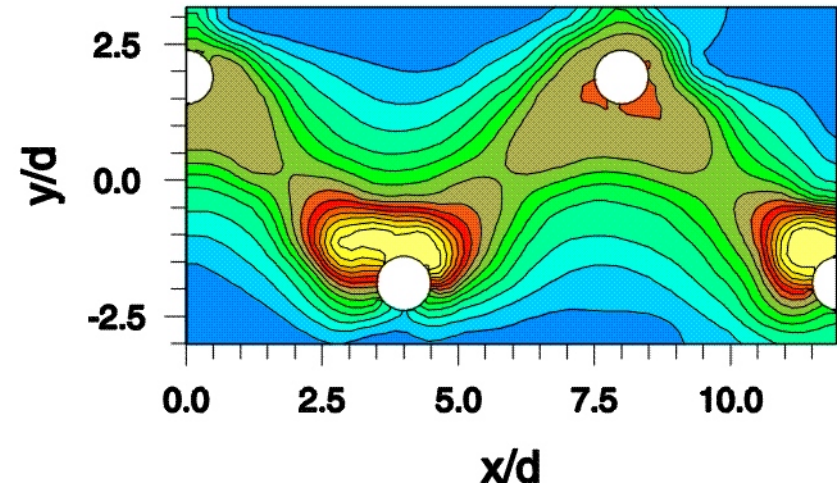
# Data through the mesh heater

Reynolds Number = 38000

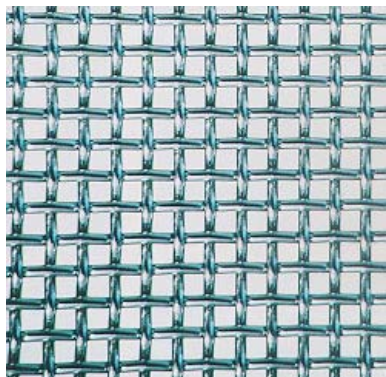
Image at time = 60 seconds



Nusselt Number



60 $\mu$ m square apertures



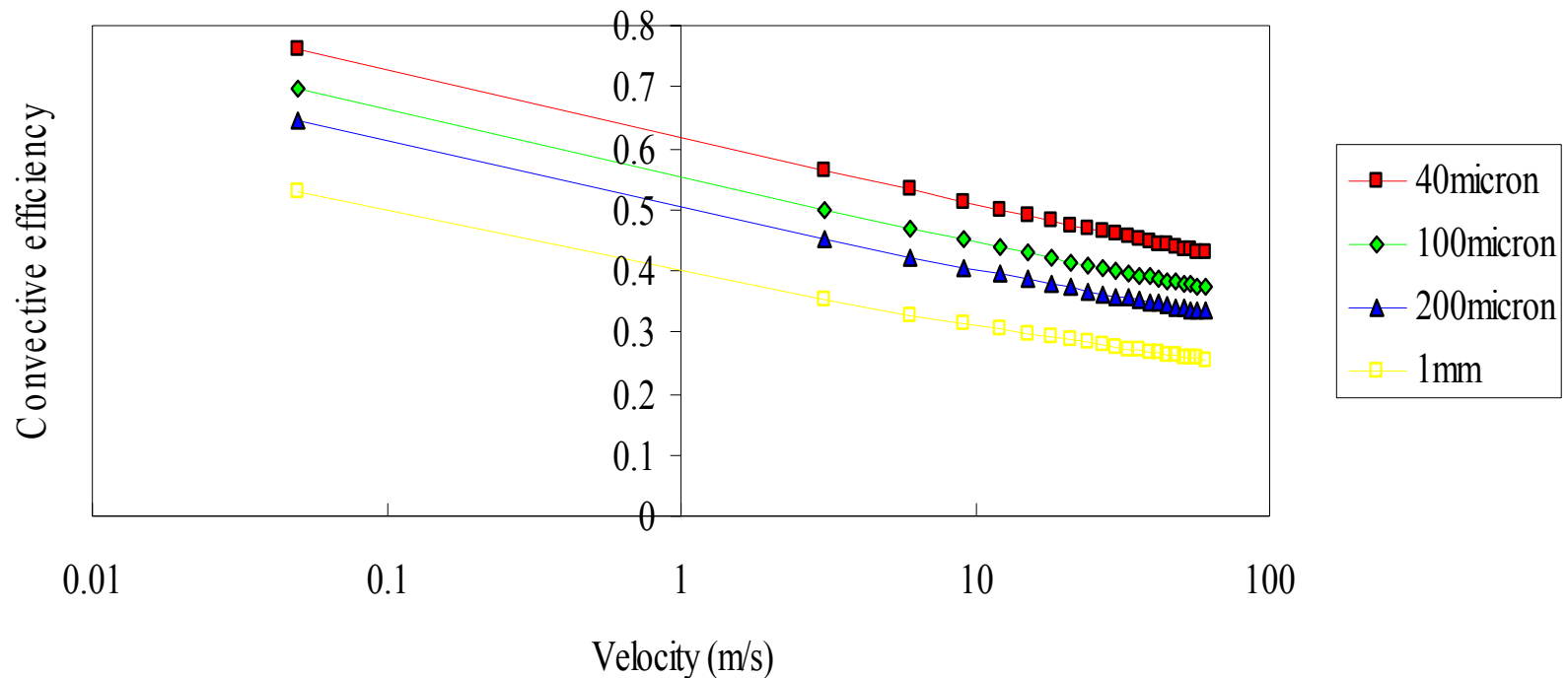
# Heater convective efficiency

- High convective efficiency ( ~50%) so:

- wires run cool
- radiation insignificant
- support easy to engineer

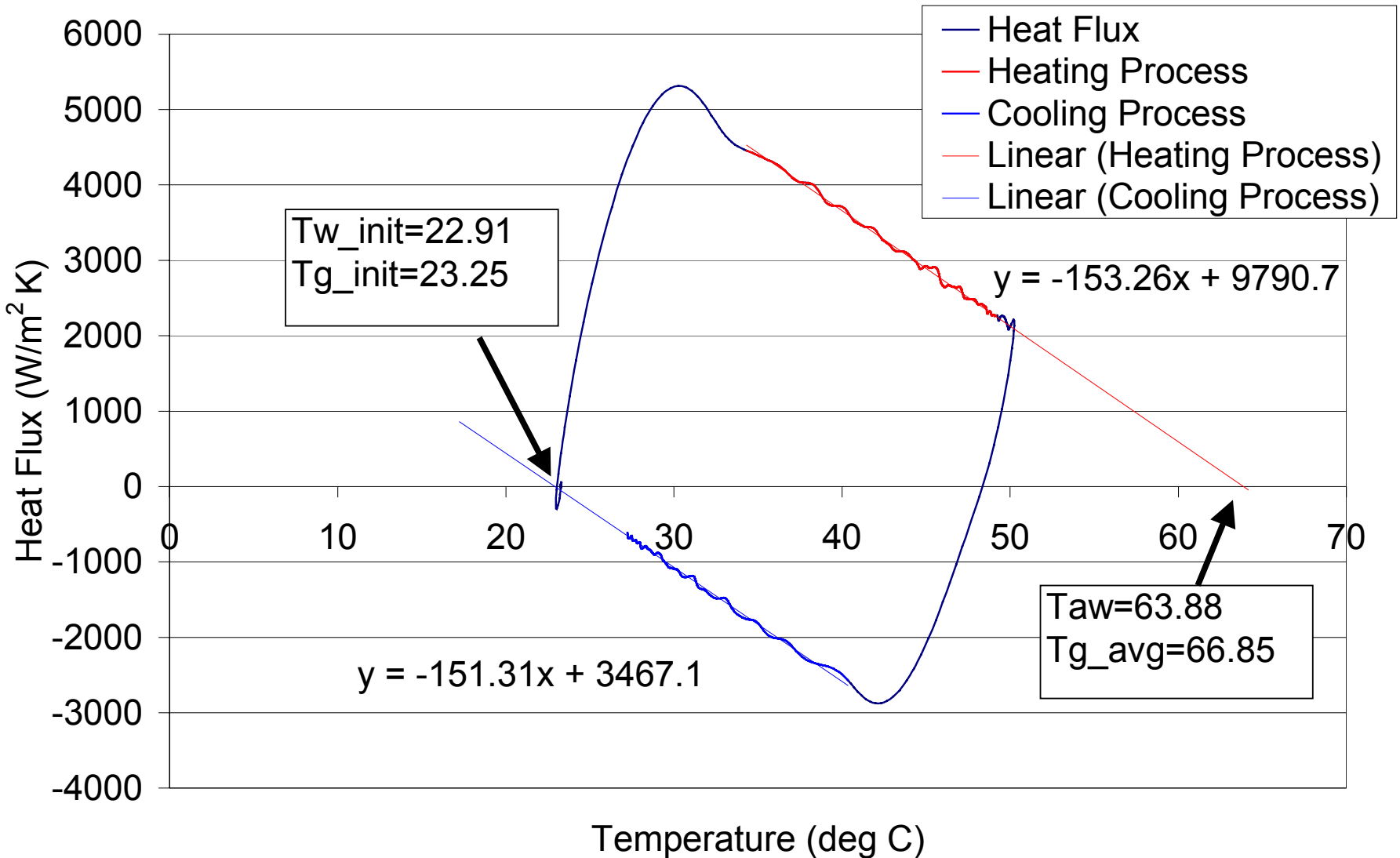
$$\eta_{CONVECTIVE} = \frac{T_{wire} - T_{downstream}}{T_{wire} - T_{upstream}}$$

- Suitable for switching temperature of low speed flows



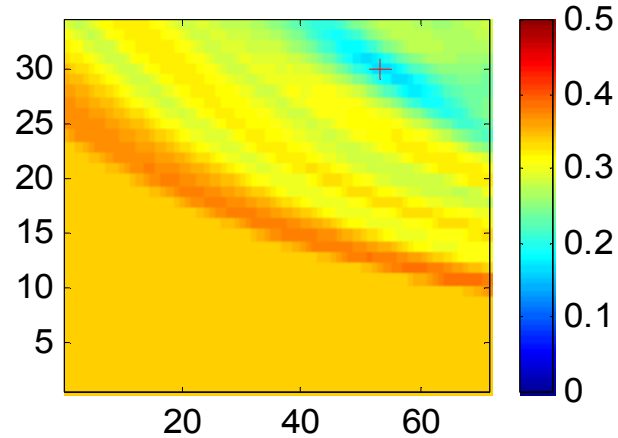
Fluid temperature	Surface temperature
Step change to $T_g$	$T_s = T_0 + (T_g - T_0) \left( 1 - \exp\left(\frac{h^2 t}{\rho c k}\right) \times \operatorname{erfc}\left(\frac{h\sqrt{t}}{\sqrt{\rho c k}}\right) \right)$
Series of steps	$T_s = T_0 + \sum_{i=1}^n (T_{g_i} - T_{g_{i-1}}) \left( 1 - \exp\left(\frac{h^2 (t - \tau_i)}{\rho c k}\right) \operatorname{erfc}\left(\frac{h\sqrt{t - \tau_i}}{\sqrt{\rho c k}}\right) \right)$
Exponential with asymptote $T_g$	$\frac{T_s - T_0}{T_g - T_0} = 1 - \frac{\frac{\rho c k}{h^2 \tau}}{\left(1 + \frac{\rho c k}{h^2 \tau}\right)} e^{-\frac{h^2 t}{\rho c k}}$ $\operatorname{erfc}\left(\frac{h\sqrt{t}}{\sqrt{\rho c k}}\right) - e^{-\frac{t}{\tau}} \frac{1}{\left(1 + \frac{\rho c k}{h^2 \tau}\right)}$ $\left( 1 + \frac{\sqrt{\rho c k}}{h \sqrt{\tau}} \left( \frac{1}{\pi} \sqrt{\frac{t}{\tau}} + \frac{2}{\pi} \sum_1^\infty \frac{1}{n} e^{-\frac{n^2}{4}} \right) \right)$ $\left( \sinh \quad n \sqrt{\frac{t}{\tau}} \right)$
Ramp function with slope $m$	$T_s = T_0 + mt \left\{ 1 - \frac{2}{\beta} + \frac{1 - \exp(\beta^2) \operatorname{erfd}(\beta)}{\beta^2} \right\}$

# Works heating or cooling

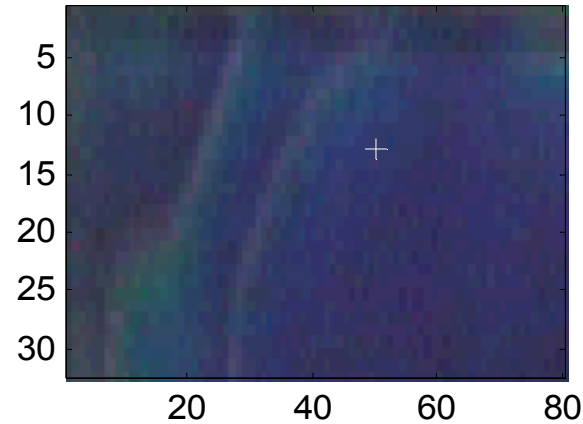


# Use of stepped flow temperature

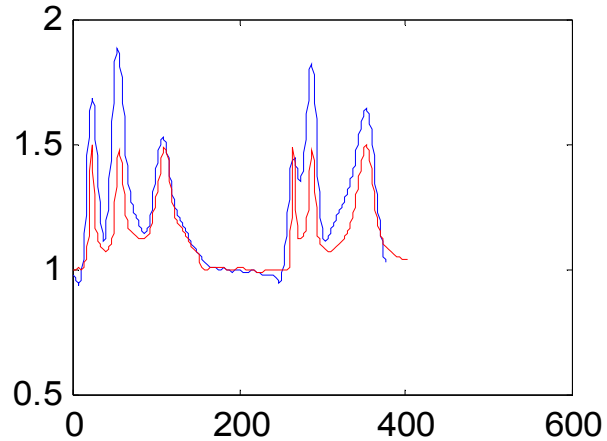
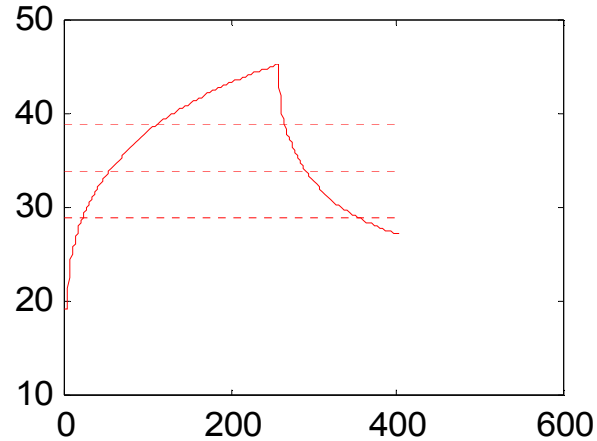
RMS error in intensity fit (htc x Tbar)



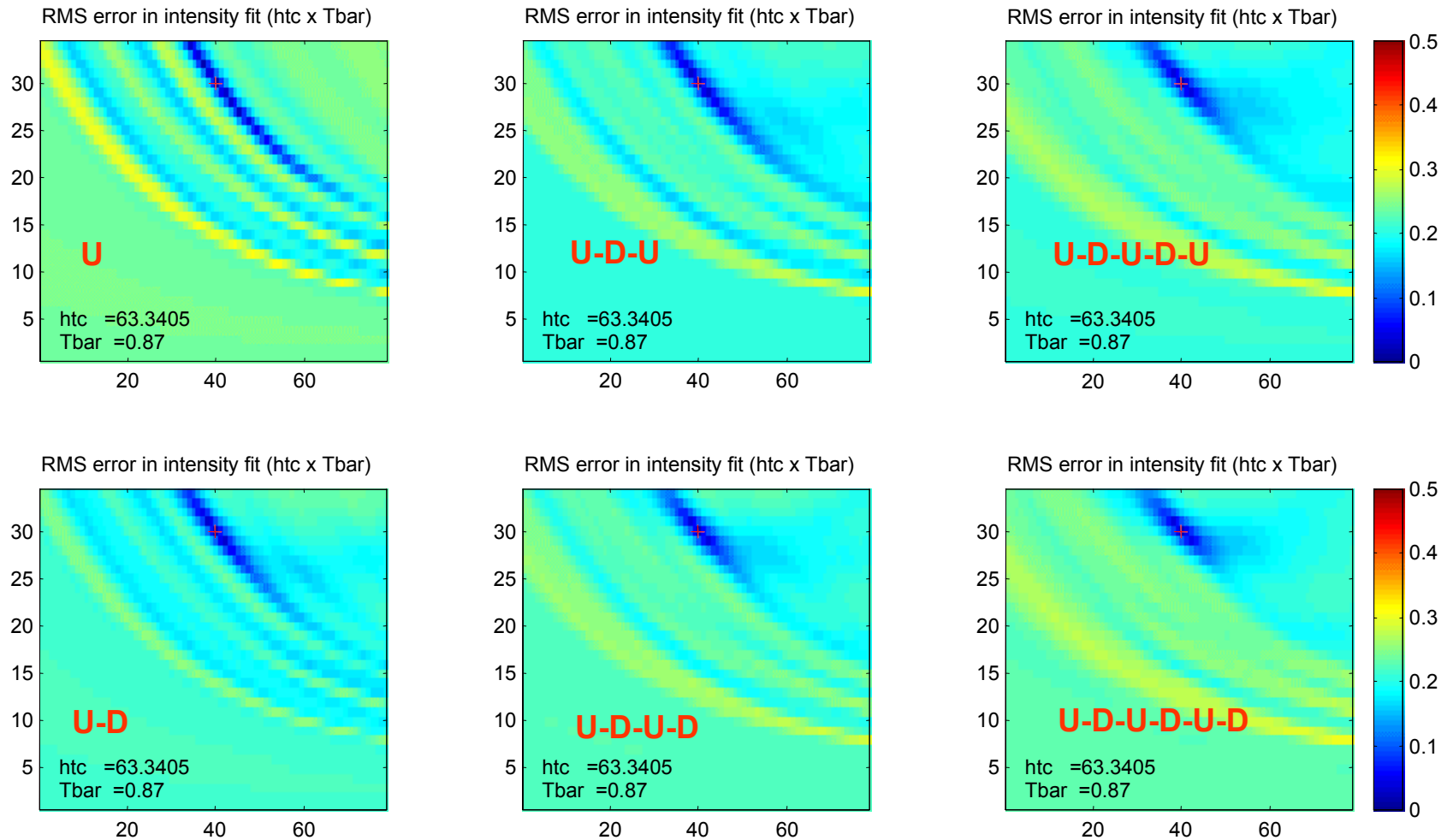
pixel position



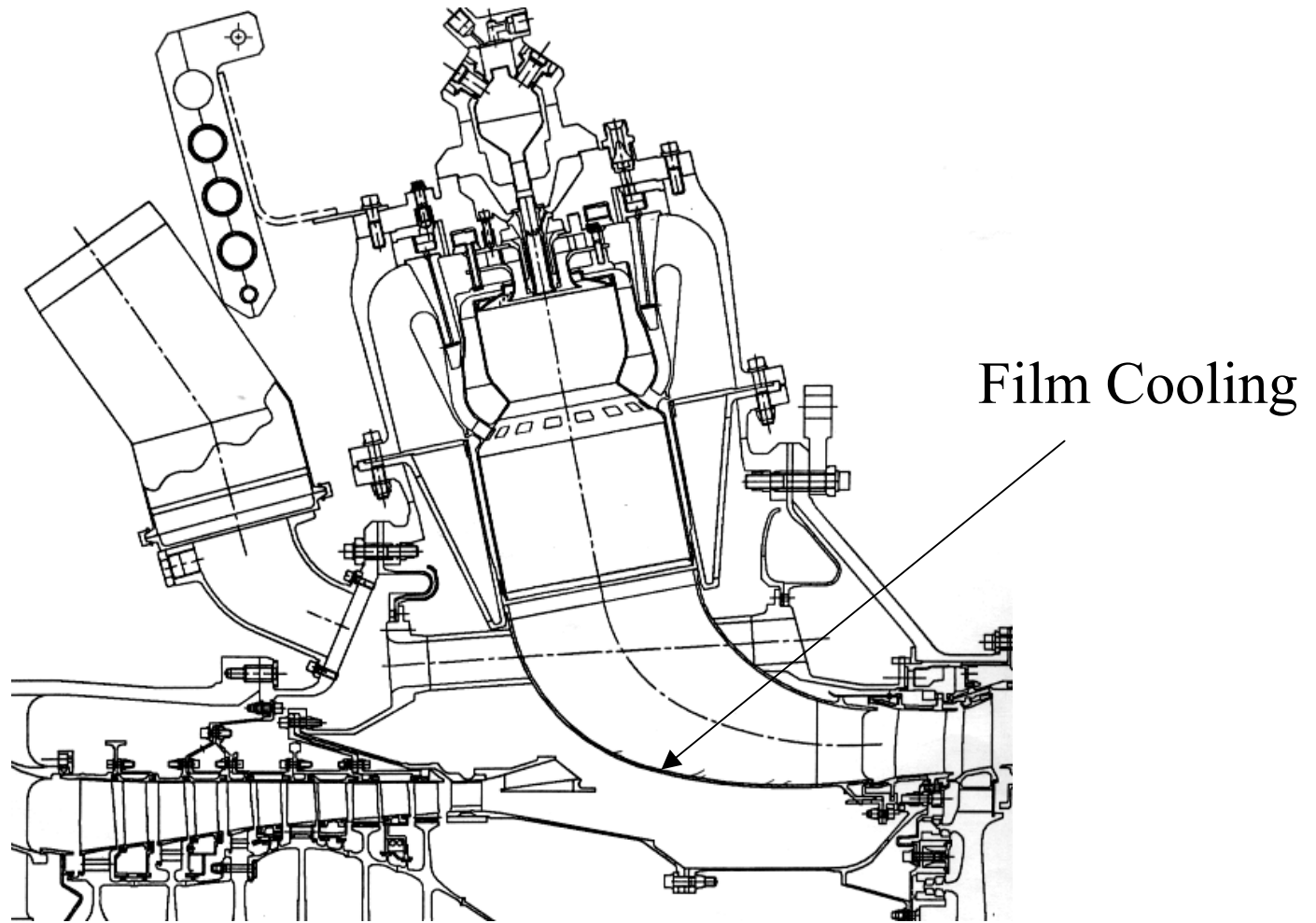
surface temperature history (red = best fit) intensity history (blue = exp, red = best fit)



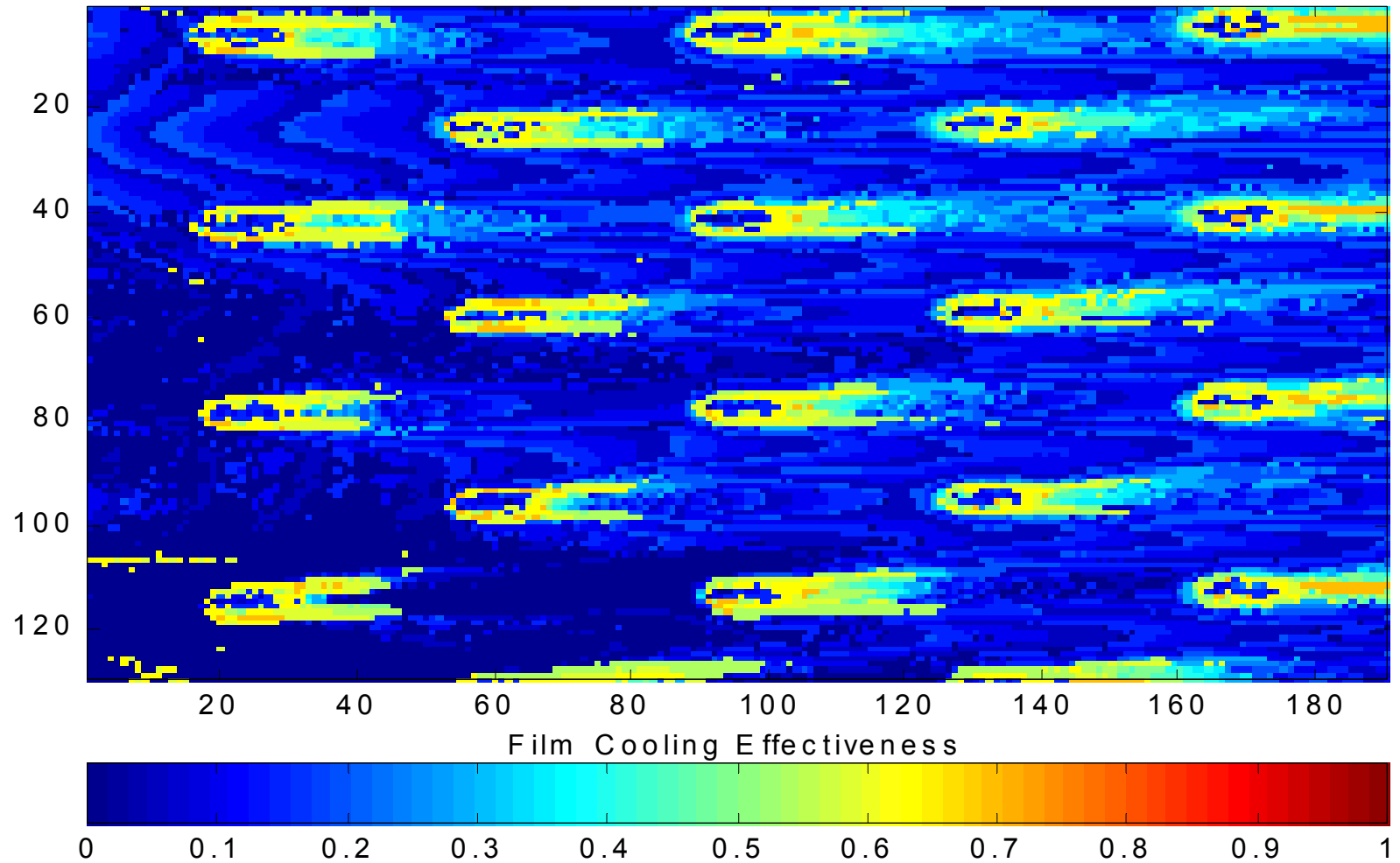
# Increasing the number of steps



# Work on Dry Low Emission Combustor



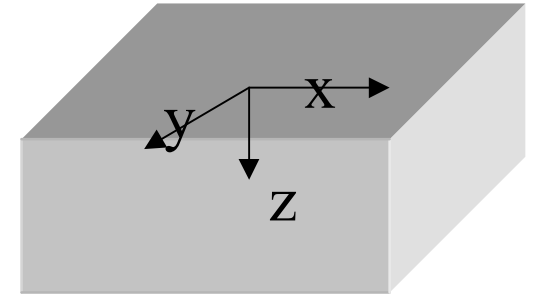
# Film Cooling Effectiveness



# Lateral Conduction Correction

## Step Two: Alternating Direction Methods (after Jim Douglas)

$$\frac{\partial T}{\partial t} = \alpha \left( \frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} \right)$$



$$\mathbf{a)} \quad \left( \Delta_x^2 - \frac{2}{\Delta t} \right) T_{n+1}^* = - \left( \Delta_x^2 + 2 \Delta_y^2 + 2 \Delta_z^2 + \frac{2}{\Delta t} \right) T_n$$

$$\mathbf{b)} \quad \left( \Delta_y^2 - \frac{2}{\Delta t} \right) T_{n+1}^{**} = \Delta_y^2 T_n - \frac{2}{\Delta t} T_{n+1}^*$$

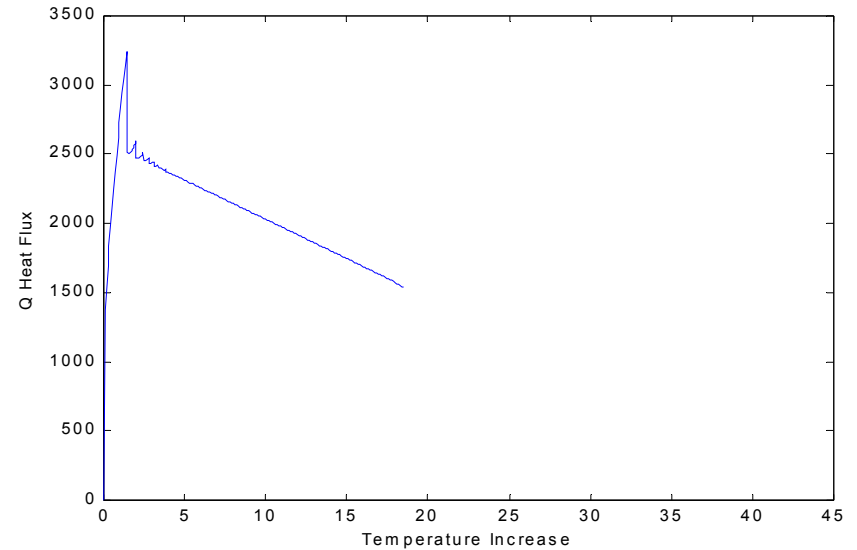
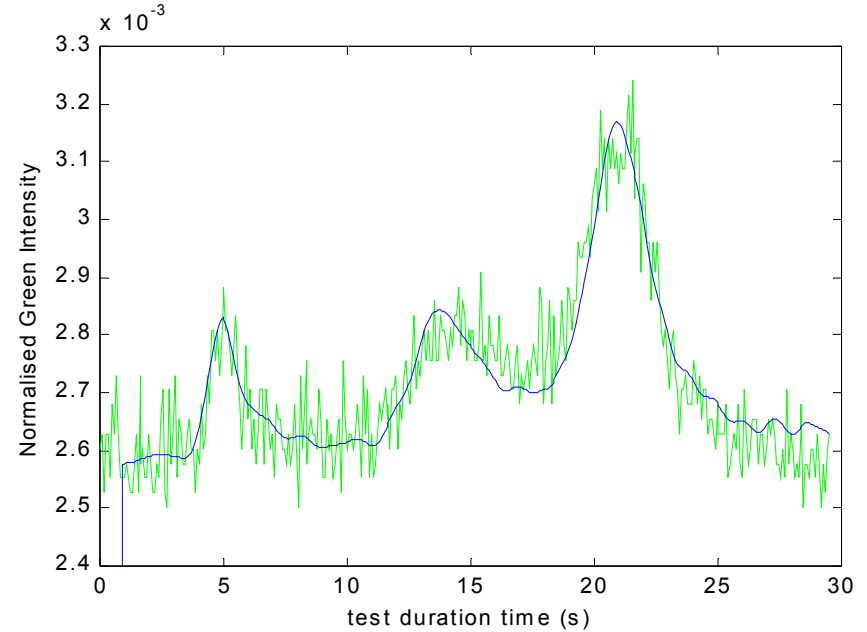
$$\mathbf{c)} \quad \left( \Delta_z^2 - \frac{2}{\Delta t} \right) T_{n+1} = \Delta_z^2 T_n - \frac{2}{\Delta t} T_{n+1}^{**}$$

where  $\Delta_x^2 T_{i,j,k,n} = (T_{i+1,j,k,n} - 2T_{i,j,k,n} + T_{i-1,j,k,n}) / (\Delta x)^2$

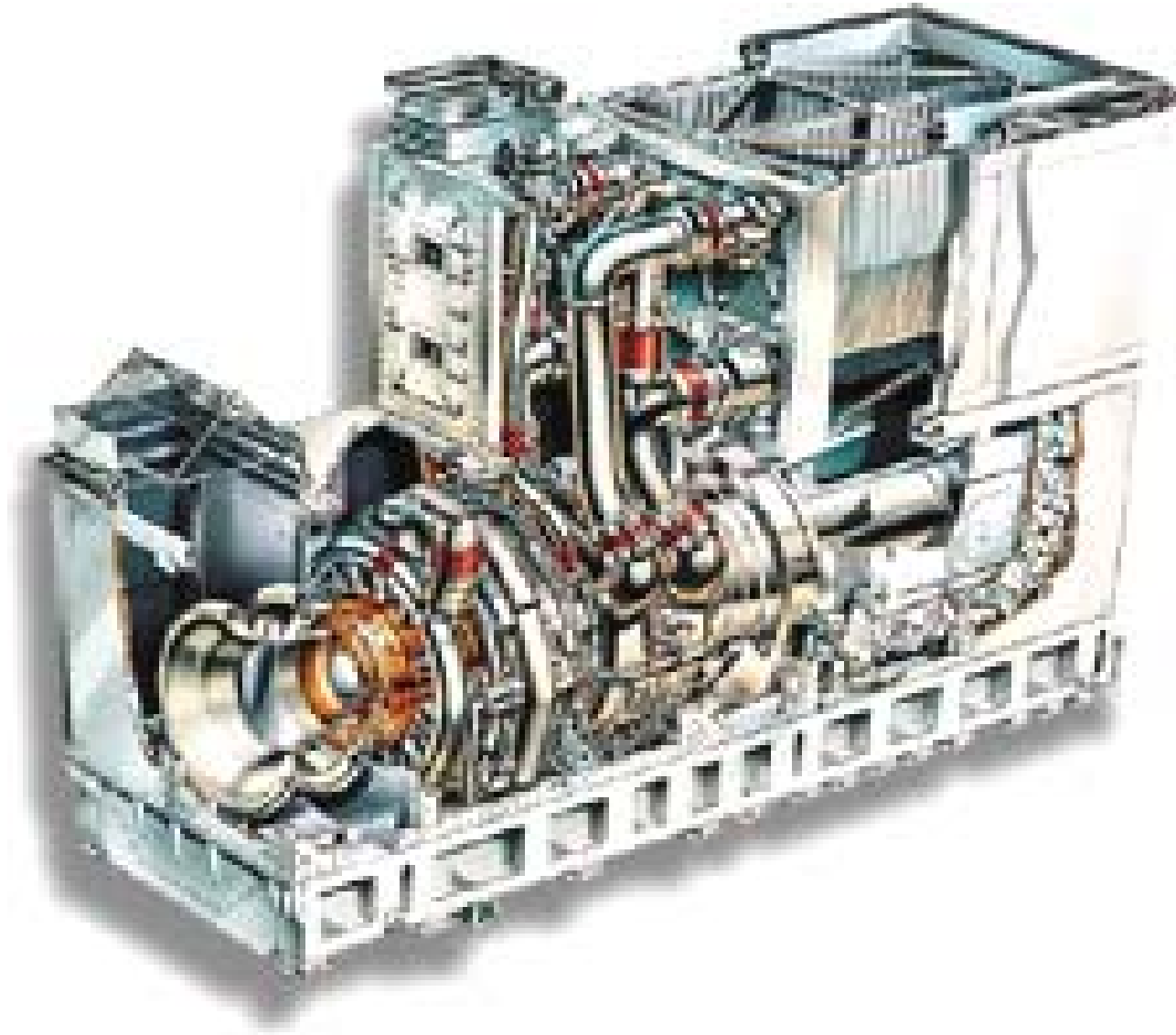
# Lateral Conduction

Heat Flux at each pixel can be then be calculated. The Film Cooling Effectiveness and Heat Transfer Coefficient can be determined by the interception of the

Temperature axis and the gradient of the heat flux graph shown above.



# Current marine application



- 832 channels in the specimen.
- Length of each channel: 197 mm.

# RR spiral recuperator

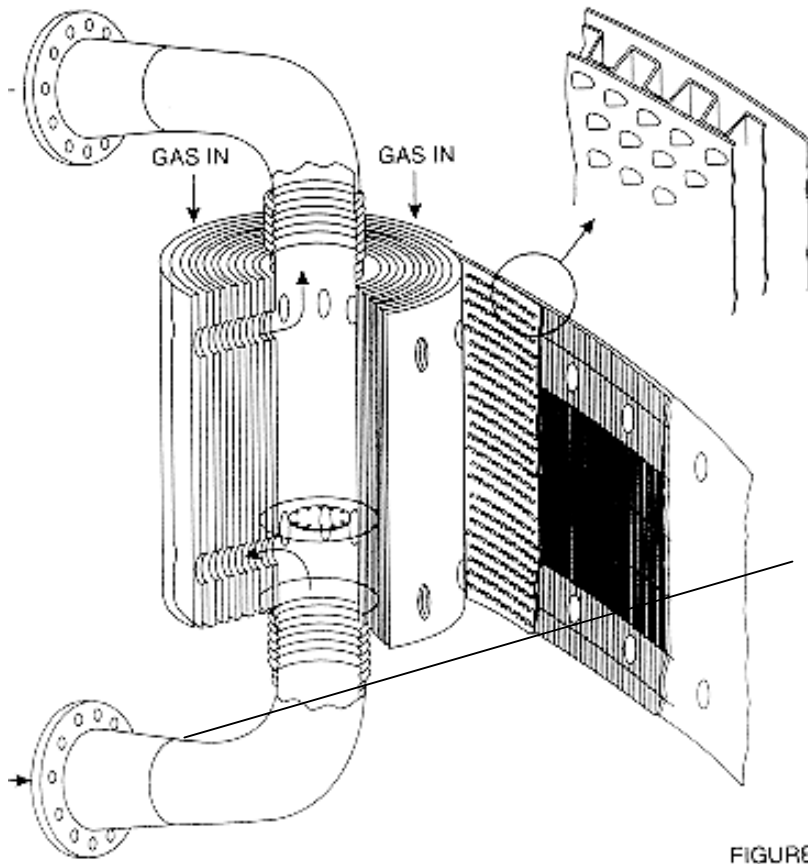


FIGURE 2

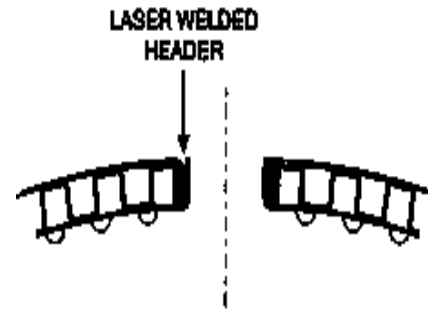


FIGURE 5

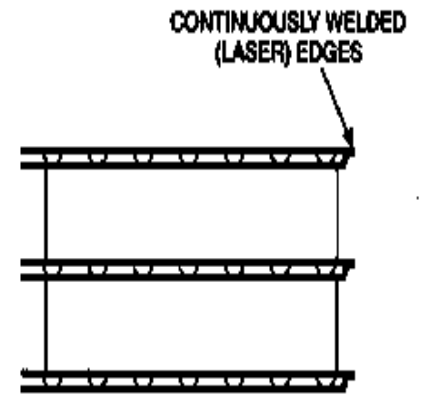
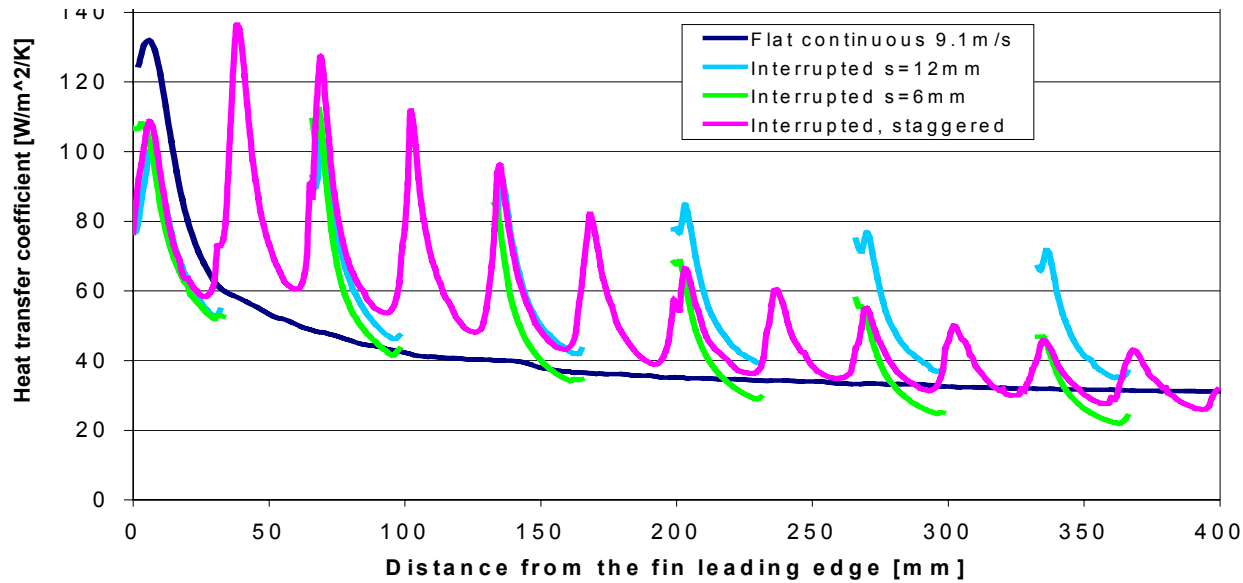
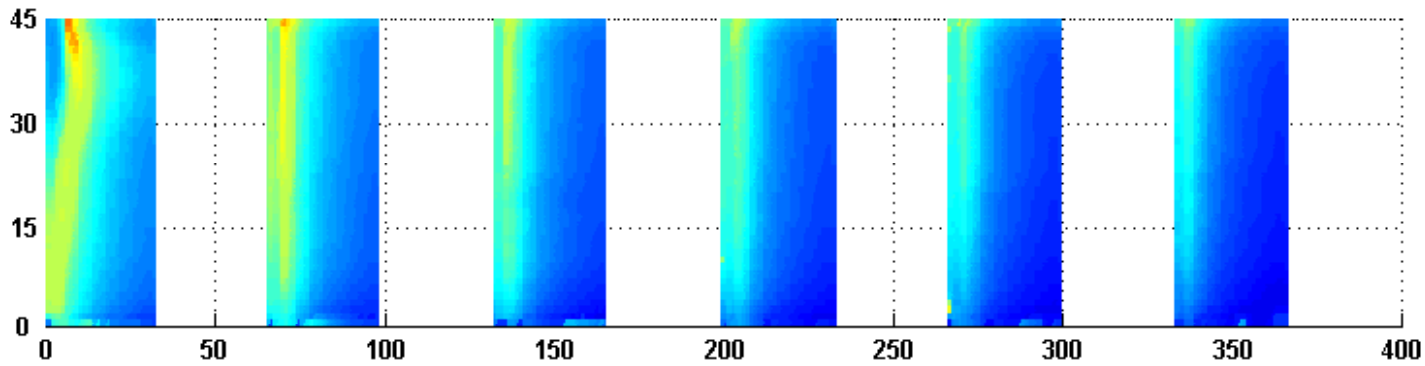
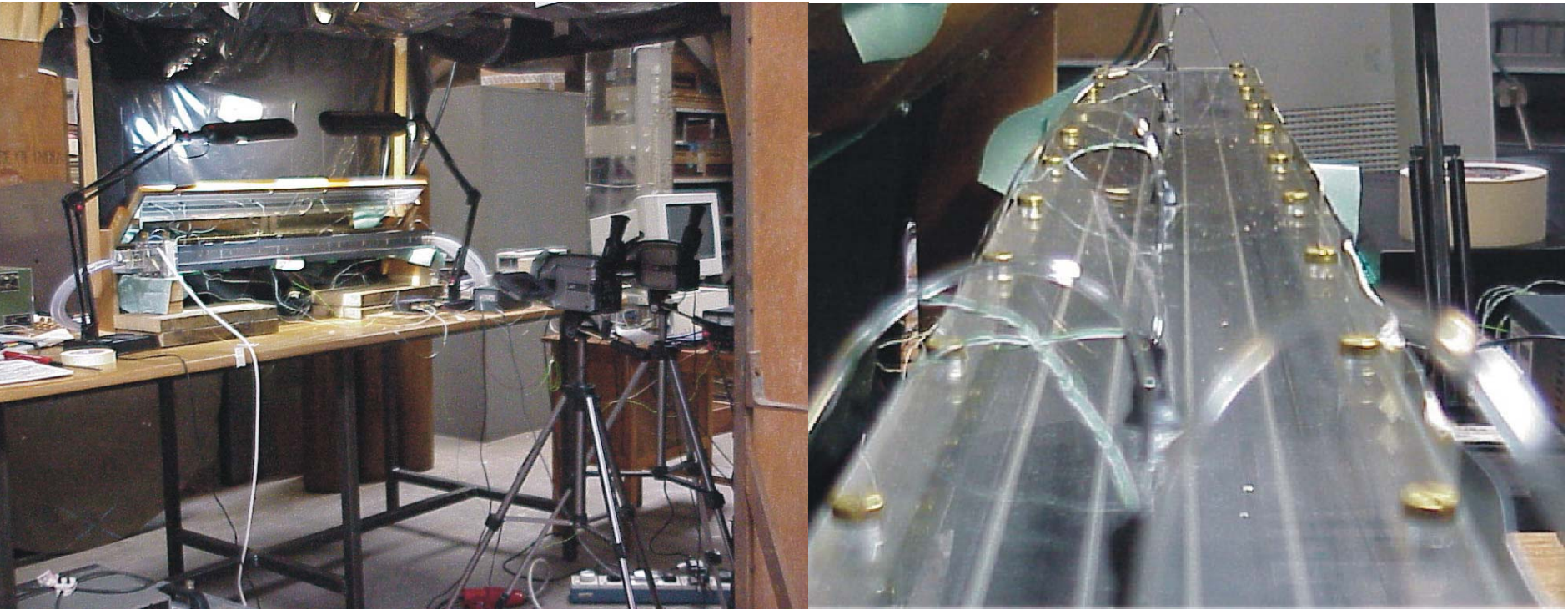


FIGURE 6

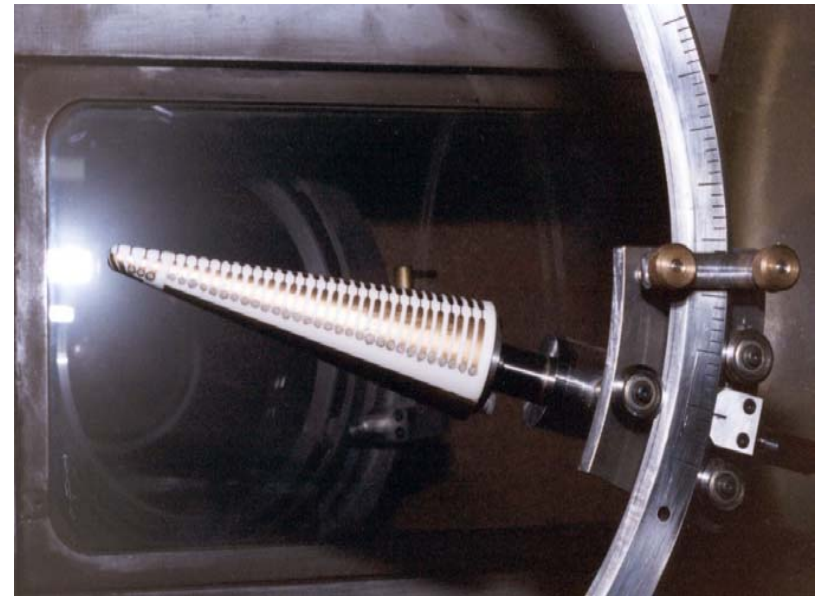
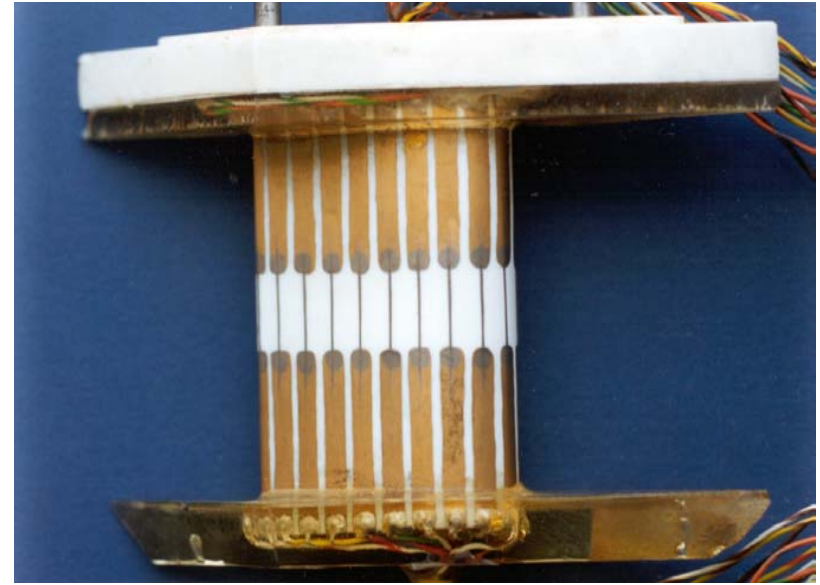
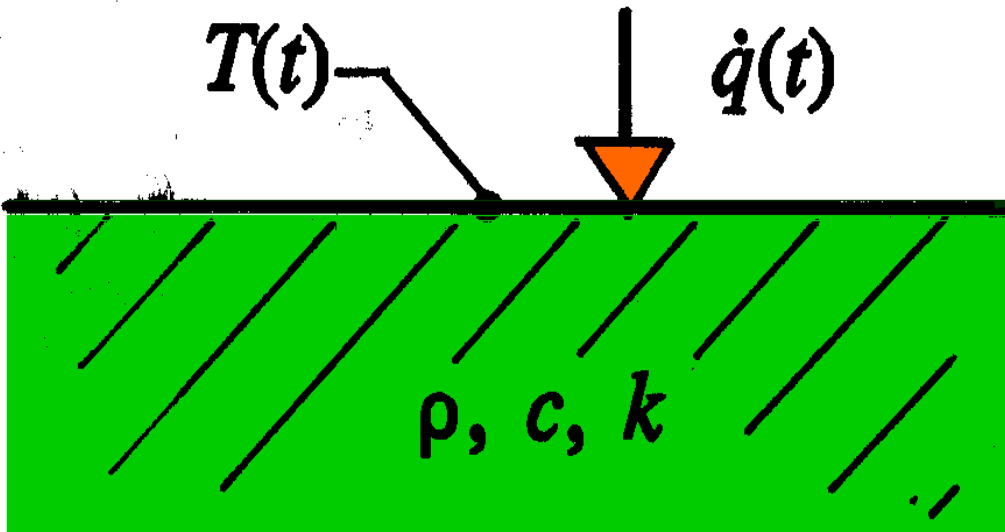
# Earlier interrupted fin htc



# Recuperator heat transfer research underway



# Early thin film gauges



DIFFUSION  
EQUATION

$$\frac{\partial^2 T}{\partial x^2} = \frac{\rho c}{k} \frac{\partial T}{\partial t}$$

LAPLACE  
TRANSFORM

$$\dot{q} = \sqrt{\rho c k} \sqrt{s T}$$

FREQUENCY

$$\dot{q}(\omega) = \sqrt{\rho c k} \sqrt{j \omega T(\omega)}$$

# Analysis

$$T \rightarrow \dot{q}$$

$$\bar{q} = \sqrt{\rho c k} \sqrt{s \bar{T}}$$

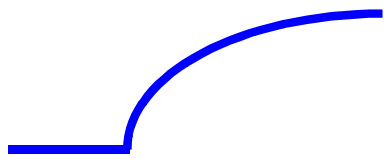
STEP  $\dot{q}(t)$



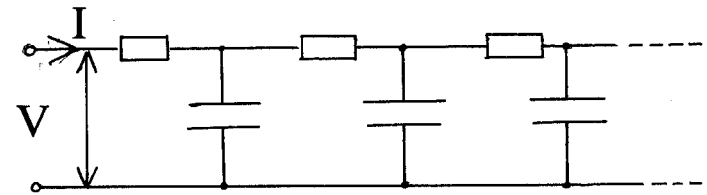
$$\bar{q} \sim \frac{1}{s}$$

$$\bar{T} \sim \frac{1}{s^{3/2}}$$

$$T(t) \sim t^{1/2}$$



## ANALOGUE

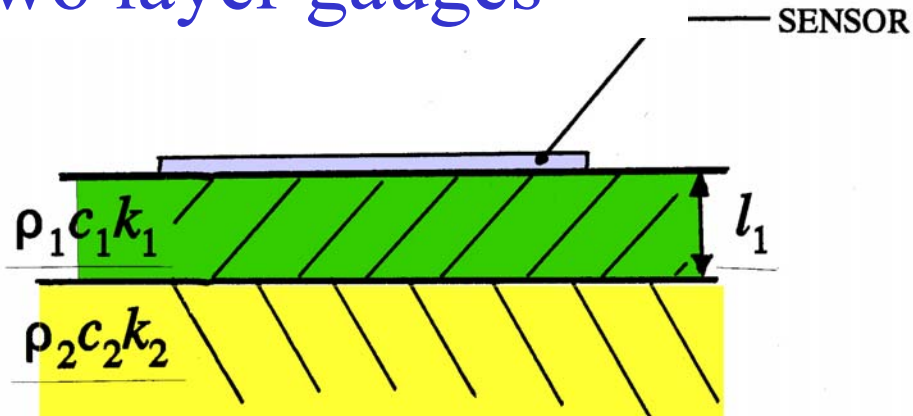


$$\frac{\partial^2 v}{\partial x^2} = \frac{r}{c} \frac{\partial v}{\partial t}$$

$$V \equiv T$$

$$I \equiv \dot{q}$$

# Two layer gauges

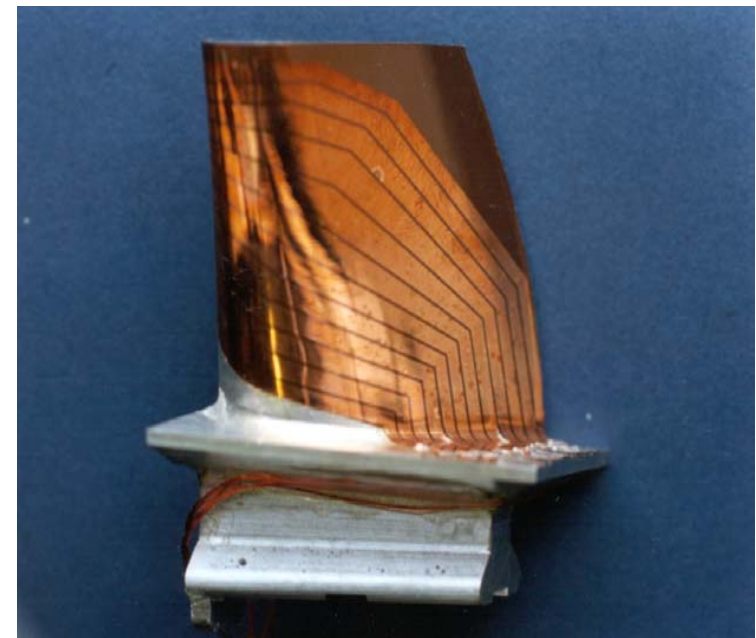
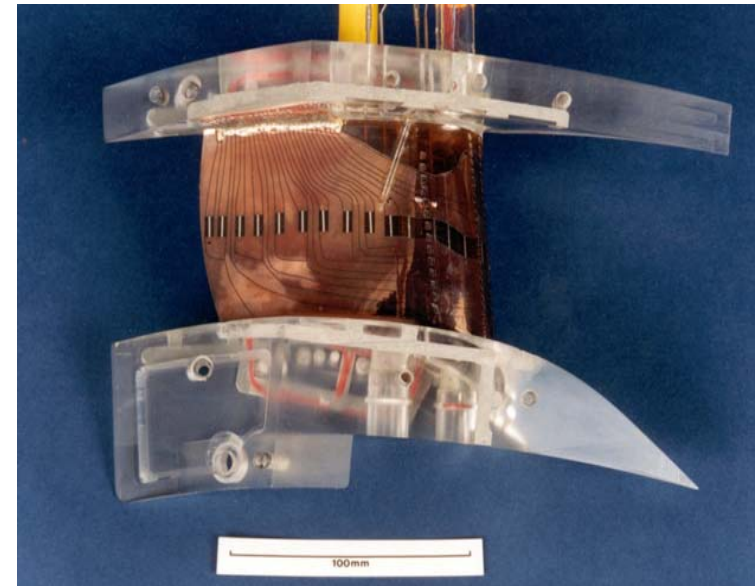


$$\bar{q} = \sqrt{\rho_1 c_1 k_1} \sqrt{sT}$$

$$\times \left[ \frac{1 - A \exp\left(-2l_1 \left(\frac{s}{\alpha_1}\right)^{1/2}\right)}{1 + A \exp\left(-2l_1 \left(\frac{s}{\alpha_1}\right)^{1/2}\right)} \right]$$

$$A = \frac{1 - \sigma}{1 + \sigma}$$

$$\sigma^2 = \frac{\rho_2 c_2 k_2}{\rho_1 c_1 k_1}$$

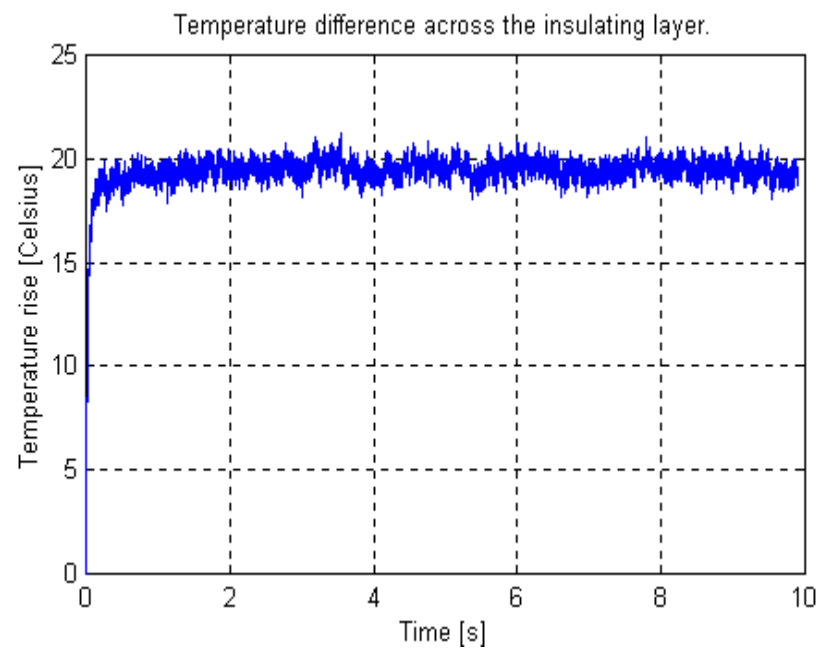
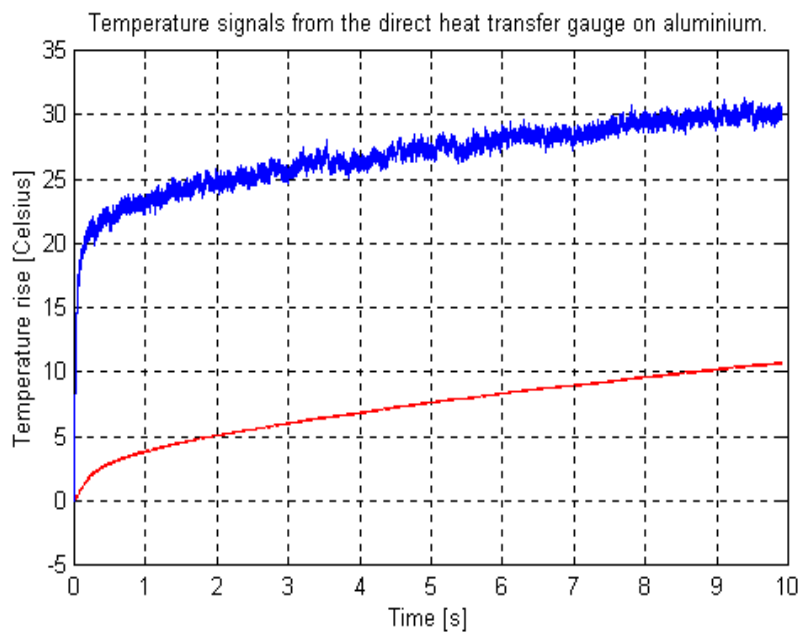
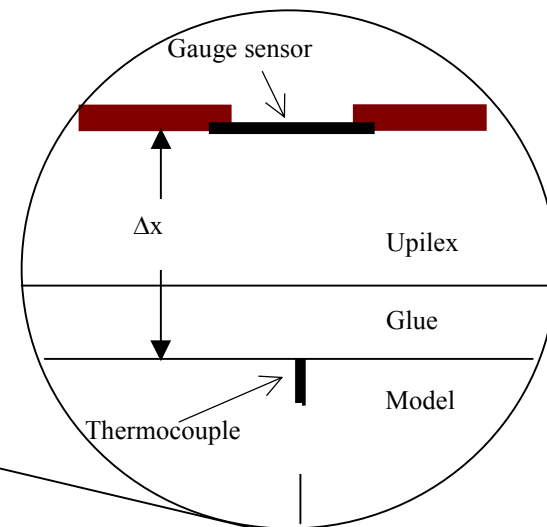
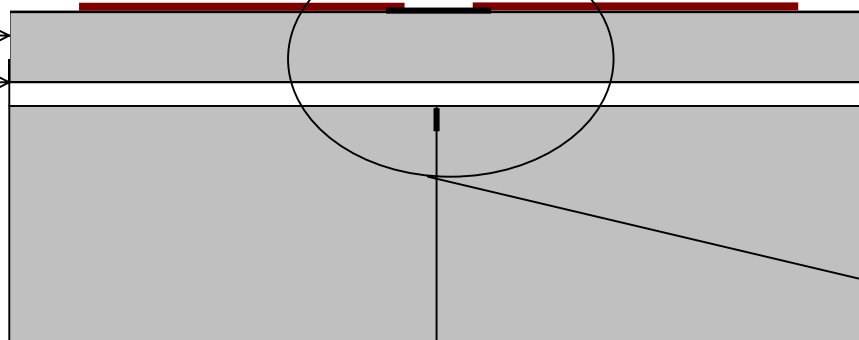


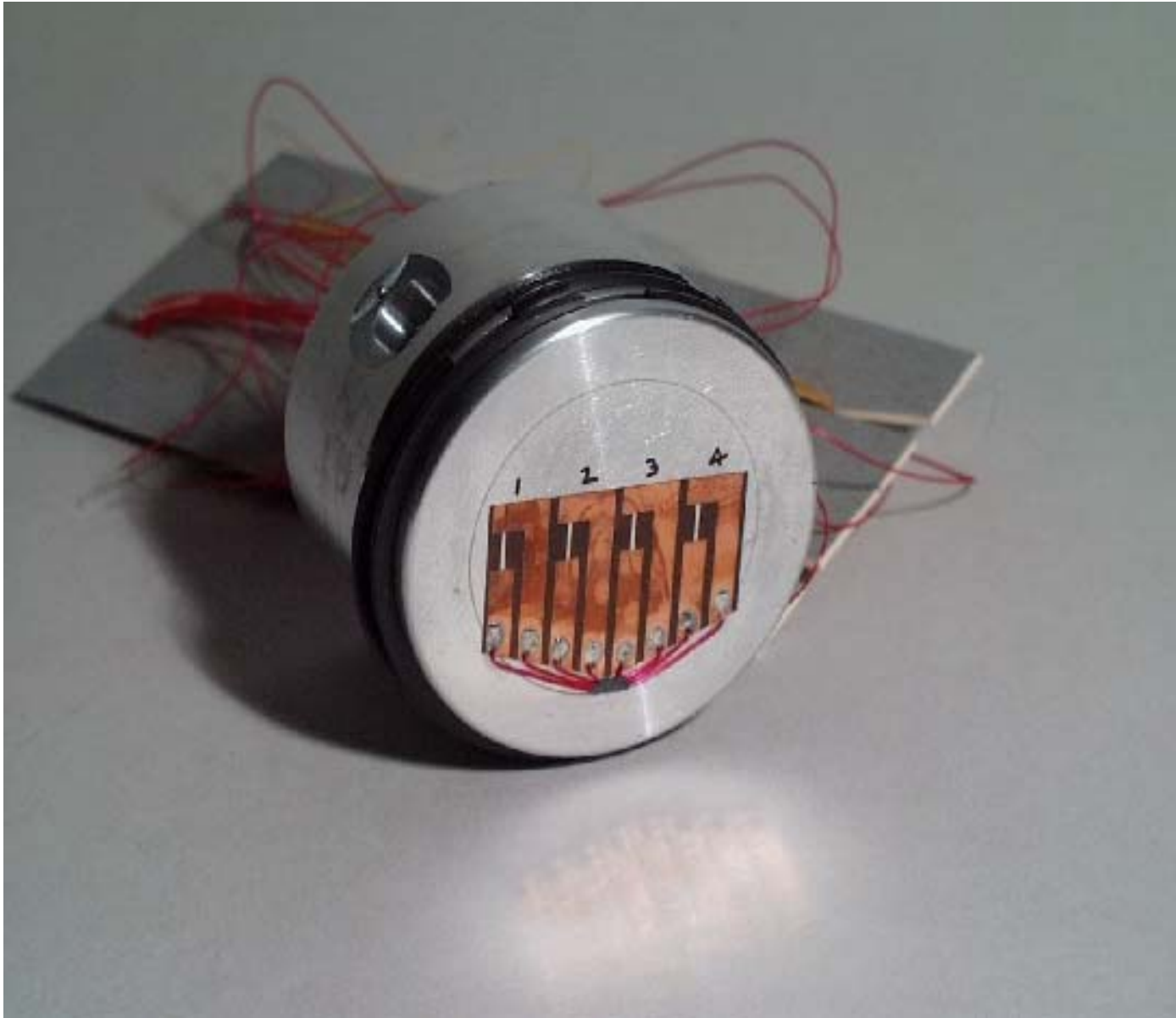
Gauge sensor (Platinum)

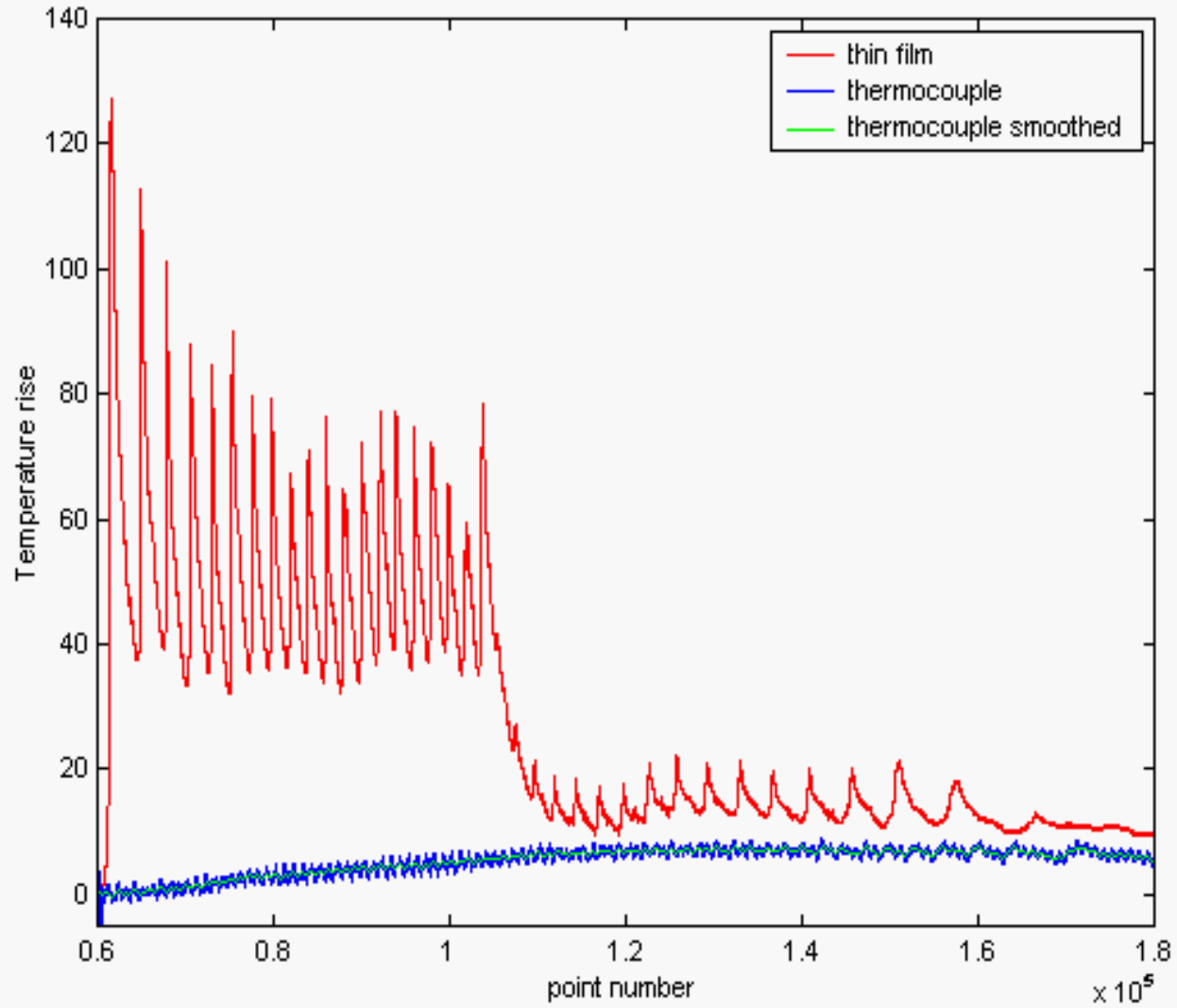
Copper leads C

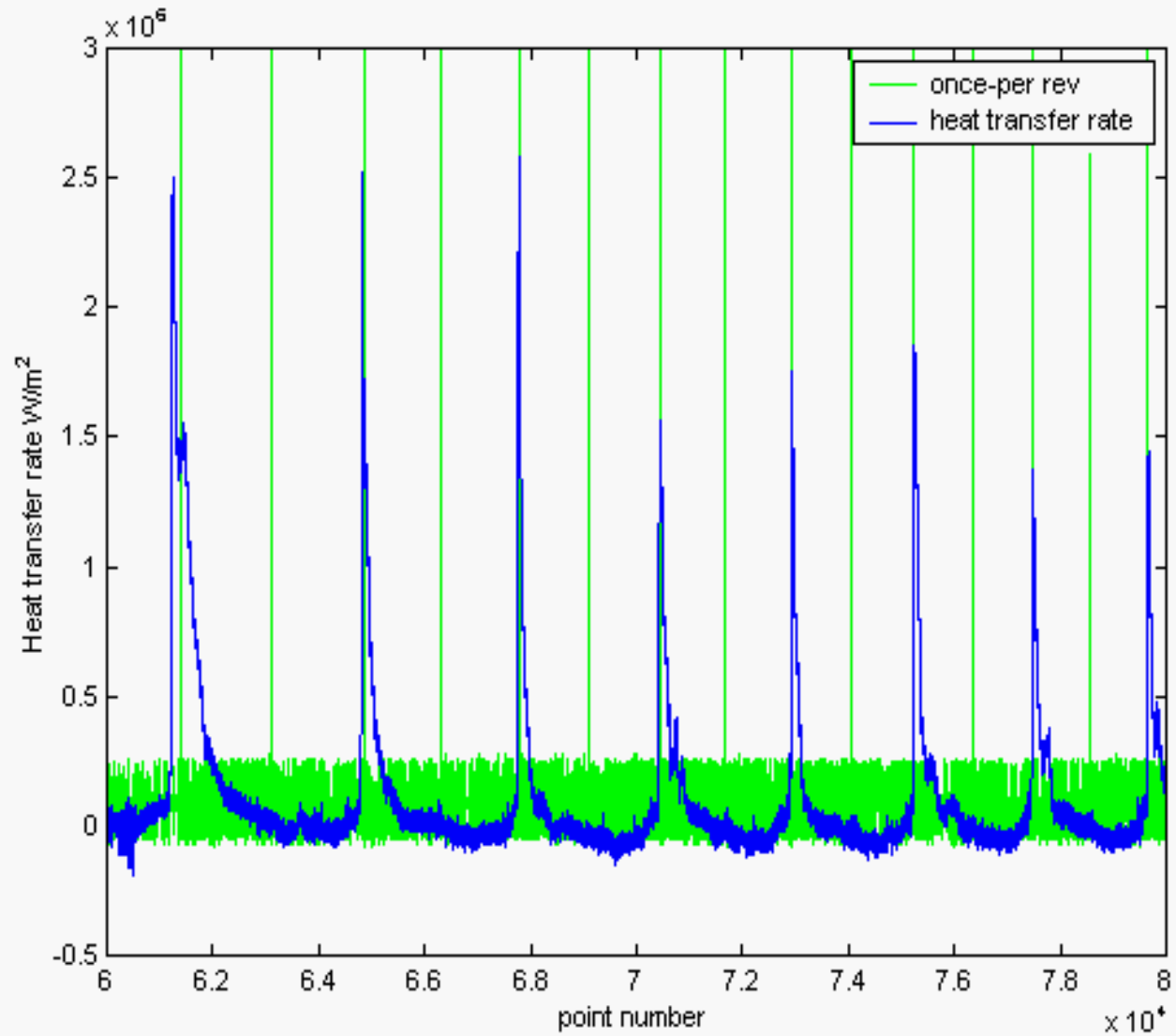
Upilex

Glue

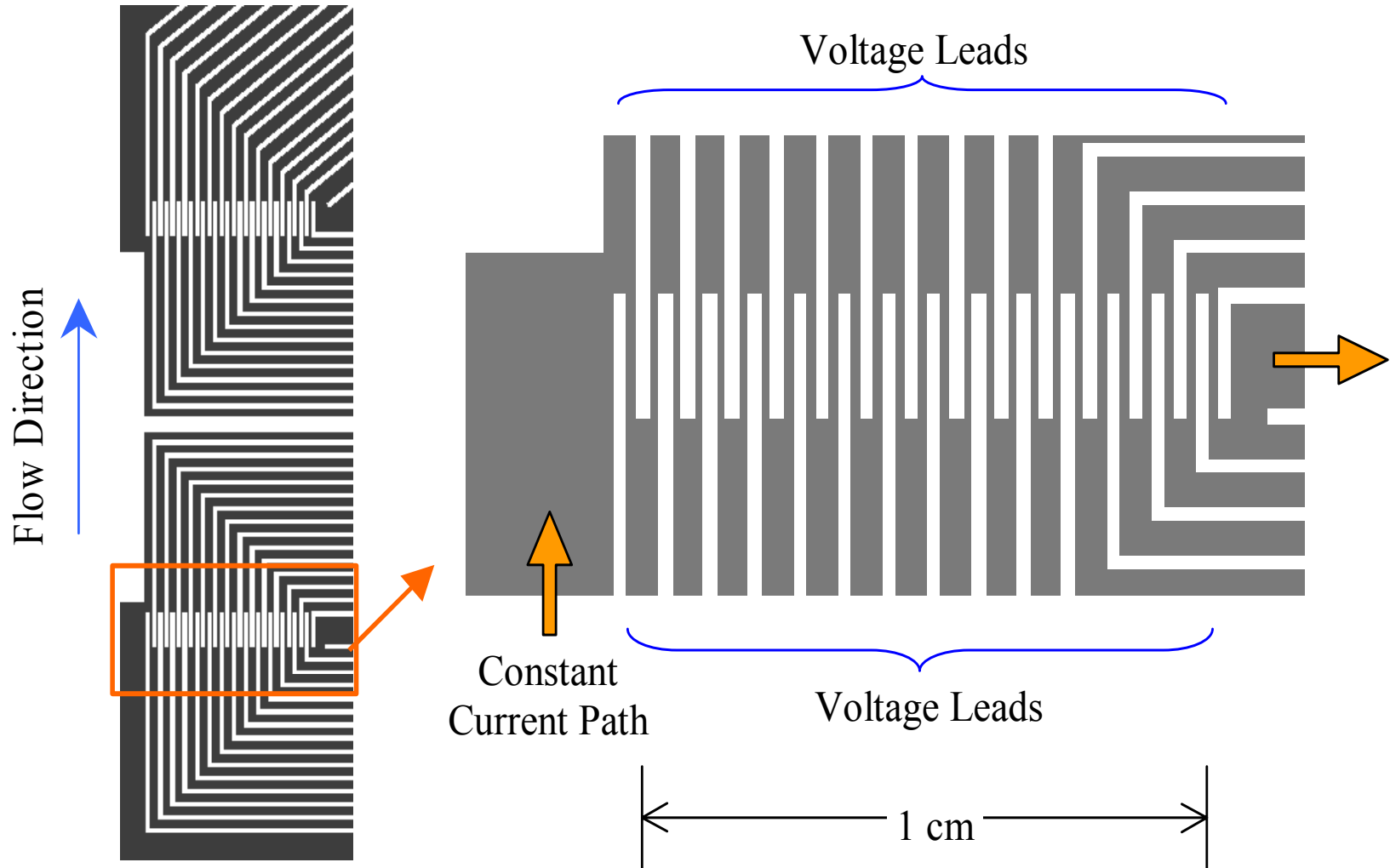




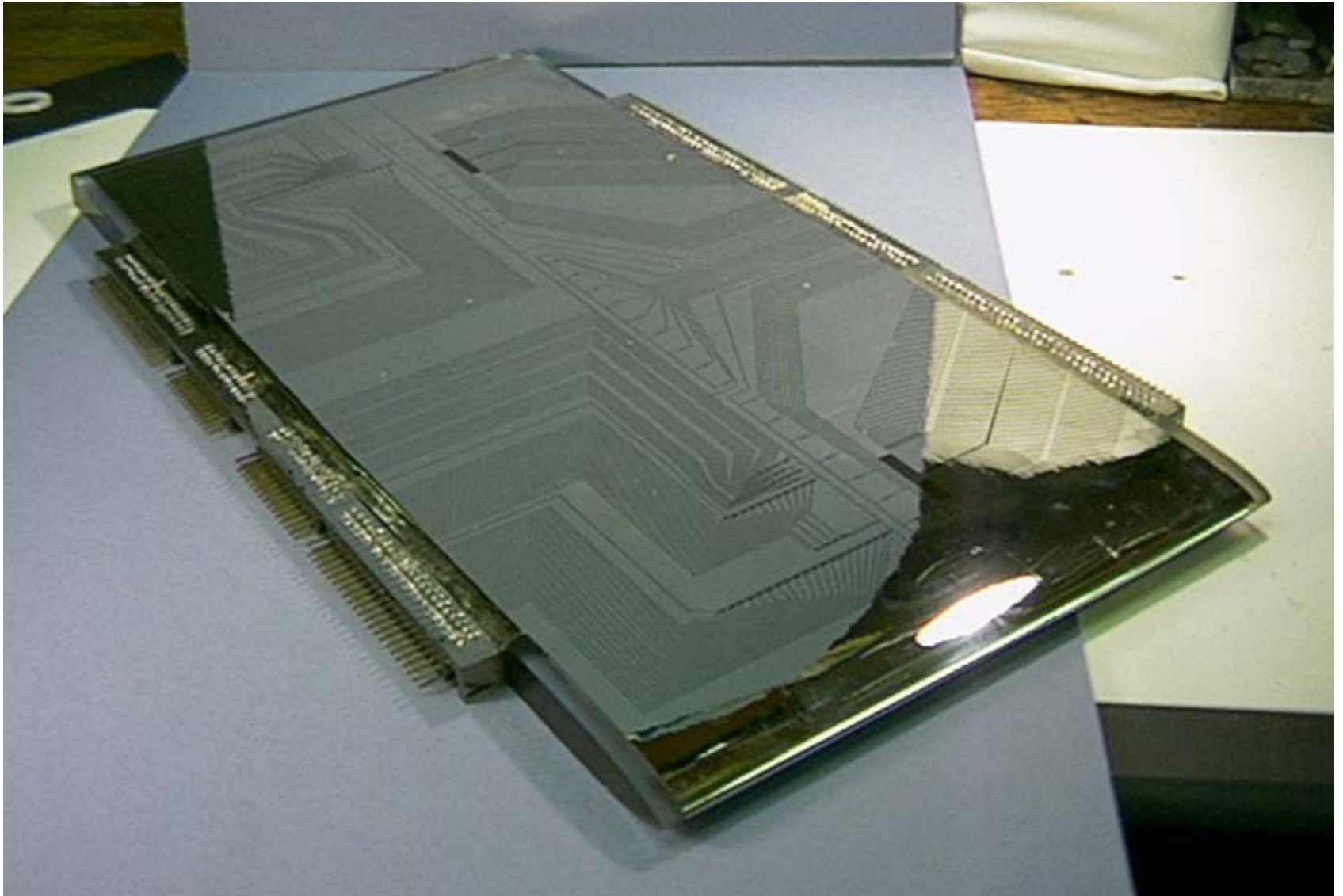




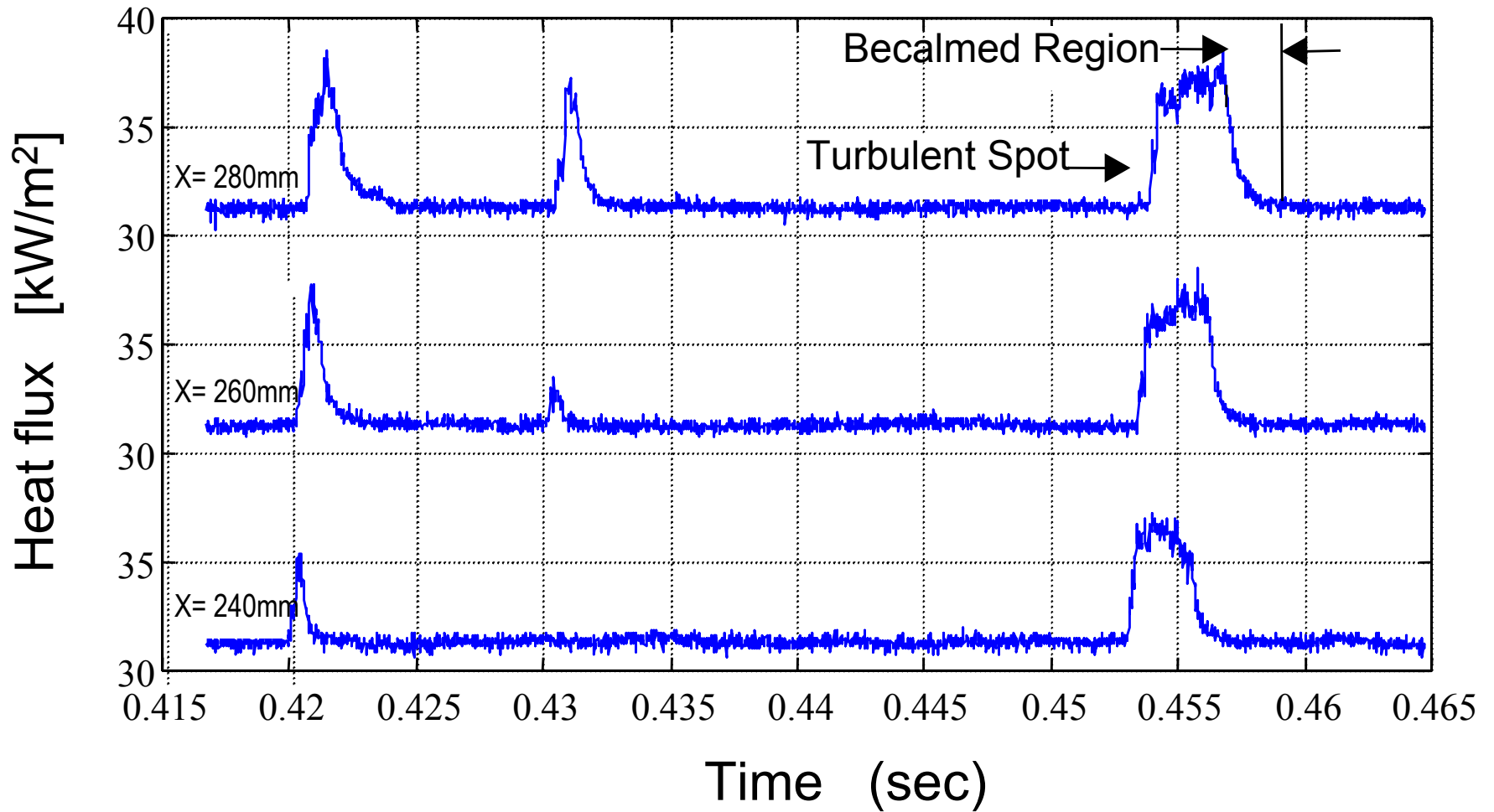
# High Density Layout using Gauge Arrays



# Model covered with sheet of TFG arrays



# Turbulent Spot Detection with Surface TFG's



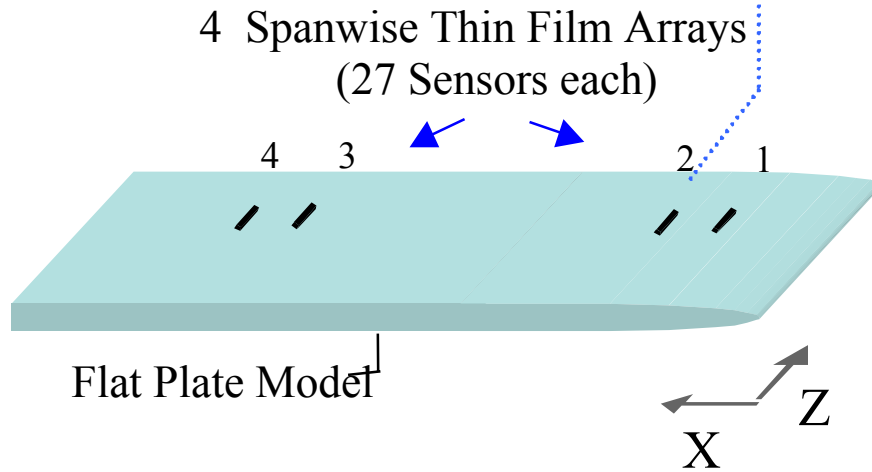
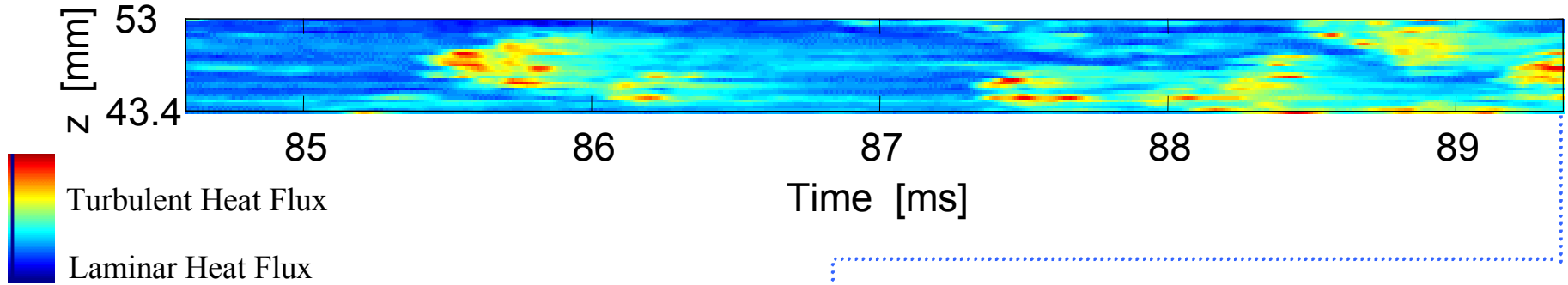
# Visualizing Transitional Heat Flux

run302

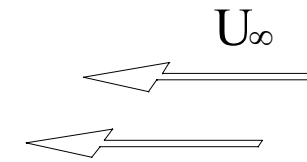
$Re_x = 1.3e+005$

$U = 48.0$  m/s

$Tu = 2.4\%$



Freestream Turbulence  
Bar Grid



Flow Direction

# Conclusions

- Presentation of existing techniques for miniature measurements.
- Scaling can be useful for determination of convective loads at high resolution.
- Miniature thin film gauges being continuously developed.