

**Federal Information
Processing Standards Publication 197**

November 26, 2001

**Announcing the
ADVANCED ENCRYPTION STANDARD (AES)**

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1. **Name of Standard.** Advanced Encryption Standard (AES) (FIPS PUB 197).
2. **Category of Standard.** Computer Security Standard, Cryptography.
3. **Explanation.** The Advanced Encryption Standard (AES) specifies a FIPS-approved cryptographic algorithm that can be used to protect electronic data. The AES algorithm is a symmetric block cipher that can encrypt (encipher) and decrypt (decipher) information. Encryption converts data to an unintelligible form called ciphertext; decrypting the ciphertext converts the data back into its original form, called plaintext.

The AES algorithm is capable of using cryptographic keys of 128, 192, and 256 bits to encrypt and decrypt data in blocks of 128 bits.

4. **Approving Authority.** Secretary of Commerce.
5. **Maintenance Agency.** Department of Commerce, National Institute of Standards and Technology, Information Technology Laboratory (ITL).
6. **Applicability.** This standard may be used by Federal departments and agencies when an agency determines that sensitive (unclassified) information (as defined in P. L. 100-235) requires cryptographic protection.

Other FIPS-approved cryptographic algorithms may be used in addition to, or in lieu of, this standard. Federal agencies or departments that use cryptographic devices for protecting classified information can use those devices for protecting sensitive (unclassified) information in lieu of this standard.

In addition, this standard may be adopted and used by non-Federal Government organizations. Such use is encouraged when it provides the desired security for commercial and private organizations.

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13. ABSTRACT (Maximum 200 Words) This standard specifies the Rijndael algorithm ([3] and [4]), a symmetric block cipher that can process data blocks of 128 bits, using cipher keys with lengths of 128, 192, and 256 bits. Rijndael was designed to handle additional block sizes and key lengths, however they are not adopted in this standard. Throughout the remainder of this standard, the algorithm specified herein will be referred to as the AES algorithm. The algorithm may be used with the three different key lengths indicated above, and therefore these different flavors may be referred to as AES-128, AES-192, and AES-256.				
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7. Specifications. Federal Information Processing Standard (FIPS) 197, Advanced Encryption Standard (AES) (affixed).

8. Implementations. The algorithm specified in this standard may be implemented in software, firmware, hardware, or any combination thereof. The specific implementation may depend on several factors such as the application, the environment, the technology used, etc. The algorithm shall be used in conjunction with a FIPS approved or NIST recommended mode of operation. Object Identifiers (OIDs) and any associated parameters for AES used in these modes are available at the Computer Security Objects Register (CSOR), located at <http://csrc.nist.gov/csor/> [2].

Implementations of the algorithm that are tested by an accredited laboratory and validated will be considered as complying with this standard. Since cryptographic security depends on many factors besides the correct implementation of an encryption algorithm, Federal Government employees, and others, should also refer to NIST Special Publication 800-21, *Guideline for Implementing Cryptography in the Federal Government*, for additional information and guidance (NIST SP 800-21 is available at <http://csrc.nist.gov/publications/>).

9. Implementation Schedule. This standard becomes effective on May 26, 2002.

10. Patents. Implementations of the algorithm specified in this standard may be covered by U.S. and foreign patents.

11. Export Control. Certain cryptographic devices and technical data regarding them are subject to Federal export controls. Exports of cryptographic modules implementing this standard and technical data regarding them must comply with these Federal regulations and be licensed by the Bureau of Export Administration of the U.S. Department of Commerce. Applicable Federal government export controls are specified in Title 15, Code of Federal Regulations (CFR) Part 740.17; Title 15, CFR Part 742; and Title 15, CFR Part 774, Category 5, Part 2.

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1. Introduction

This standard specifies the **Rijndael** algorithm ([3] and [4]), a symmetric block cipher that can process **data blocks** of **128 bits**, using cipher **keys** with lengths of **128, 192, and 256 bits**. Rijndael was designed to handle additional block sizes and key lengths, however they are not adopted in this standard.

Throughout the remainder of this standard, the algorithm specified herein will be referred to as “the AES algorithm.” The algorithm may be used with the three different key lengths indicated above, and therefore these different “flavors” may be referred to as “AES-128”, “AES-192”, and “AES-256”.

This specification includes the following sections:

2. Definitions of terms, acronyms, and algorithm parameters, symbols, and functions;
3. Notation and conventions used in the algorithm specification, including the ordering and numbering of bits, bytes, and words;
4. Mathematical properties that are useful in understanding the algorithm;
5. Algorithm specification, covering the key expansion, encryption, and decryption routines;
6. Implementation issues, such as key length support, keying restrictions, and additional block/key/round sizes.

The standard concludes with several appendices that include step-by-step examples for Key Expansion and the Cipher, example vectors for the Cipher and Inverse Cipher, and a list of references.

2. Definitions

2.1 Glossary of Terms and Acronyms

The following definitions are used throughout this standard:

AES	Advanced Encryption Standard
Affine Transformation	A transformation consisting of multiplication by a matrix followed by the addition of a vector.
Array	An enumerated collection of identical entities (e.g., an array of bytes).
Bit	A binary digit having a value of 0 or 1.
Block	Sequence of binary bits that comprise the input, output, State, and Round Key. The length of a sequence is the number of bits it contains. Blocks are also interpreted as arrays of bytes.
Byte	A group of eight bits that is treated either as a single entity or as an array of 8 individual bits.

Cipher	Series of transformations that converts plaintext to ciphertext using the Cipher Key.
Cipher Key	Secret, cryptographic key that is used by the Key Expansion routine to generate a set of Round Keys; can be pictured as a rectangular array of bytes, having four rows and Nk columns.
Ciphertext	Data output from the Cipher or input to the Inverse Cipher.
Inverse Cipher	Series of transformations that converts ciphertext to plaintext using the Cipher Key.
Key Expansion	Routine used to generate a series of Round Keys from the Cipher Key.
Plaintext	Data input to the Cipher or output from the Inverse Cipher.
Rijndael	Cryptographic algorithm specified in this Advanced Encryption Standard (AES).
Round Key	Round keys are values derived from the Cipher Key using the Key Expansion routine; they are applied to the State in the Cipher and Inverse Cipher.
State	Intermediate Cipher result that can be pictured as a rectangular array of bytes, having four rows and Nb columns.
S-box	Non-linear substitution table used in several byte substitution transformations and in the Key Expansion routine to perform a one-for-one substitution of a byte value.
Word	A group of 32 bits that is treated either as a single entity or as an array of 4 bytes.

2.2 Algorithm Parameters, Symbols, and Functions

The following algorithm parameters, symbols, and functions are used throughout this standard:

AddRoundKey()	Transformation in the Cipher and Inverse Cipher in which a Round Key is added to the State using an XOR operation. The length of a Round Key equals the size of the State (i.e., for $Nb = 4$, the Round Key length equals 128 bits/16 bytes).
InvMixColumns()	Transformation in the Inverse Cipher that is the inverse of MixColumns() .
InvShiftRows()	Transformation in the Inverse Cipher that is the inverse of ShiftRows() .
InvSubBytes()	Transformation in the Inverse Cipher that is the inverse of SubBytes() .
K	Cipher Key.

MixColumns()	Transformation in the Cipher that takes all of the columns of the State and mixes their data (independently of one another) to produce new columns.
Nb	Number of columns (32-bit words) comprising the State. For this standard, Nb = 4. (Also see Sec. 6.3.)
Nk	Number of 32-bit words comprising the Cipher Key. For this standard, Nk = 4, 6, or 8. (Also see Sec. 6.3.)
Nr	Number of rounds, which is a function of Nk and Nb (which is fixed). For this standard, Nr = 10, 12, or 14. (Also see Sec. 6.3.)
Rcon[]	The round constant word array.
RotWord()	Function used in the Key Expansion routine that takes a four-byte word and performs a cyclic permutation.
ShiftRows()	Transformation in the Cipher that processes the State by cyclically shifting the last three rows of the State by different offsets.
SubBytes()	Transformation in the Cipher that processes the State using a non-linear byte substitution table (S-box) that operates on each of the State bytes independently.
SubWord()	Function used in the Key Expansion routine that takes a four-byte input word and applies an S-box to each of the four bytes to produce an output word.
XOR	Exclusive-OR operation.
$\oplus$	Exclusive-OR operation.
$\otimes$	Multiplication of two polynomials (each with degree < 4) modulo $x^4 + 1$.
•	Finite field multiplication.

3. Notation and Conventions

3.1 Inputs and Outputs

The **input** and **output** for the AES algorithm each consist of **sequences of 128 bits** (digits with values of 0 or 1). These sequences will sometimes be referred to as **blocks** and the number of bits they contain will be referred to as their length. The **Cipher Key** for the AES algorithm is a **sequence of 128, 192 or 256 bits**. Other input, output and Cipher Key lengths are not permitted by this standard.

The bits within such sequences will be numbered starting at zero and ending at one less than the sequence length (block length or key length). The number i attached to a bit is known as its index and will be in one of the ranges $0 \leq i < 128$, $0 \leq i < 192$ or $0 \leq i < 256$ depending on the block length and key length (specified above).

3.2 Bytes

The basic unit for processing in the AES algorithm is a **byte**, a sequence of eight bits treated as a single entity. The input, output and Cipher Key bit sequences described in Sec. 3.1 are processed as arrays of bytes that are formed by dividing these sequences into groups of eight contiguous bits to form arrays of bytes (see Sec. 3.3). For an input, output or Cipher Key denoted by a , the bytes in the resulting array will be referenced using one of the two forms, a_n or $a[n]$, where n will be in one of the following ranges:

Key length = 128 bits, $0 \leq n < 16$; Block length = 128 bits, $0 \leq n < 16$;

Key length = 192 bits, $0 \leq n < 24$;

Key length = 256 bits, $0 \leq n < 32$.

All byte values in the AES algorithm will be presented as the concatenation of its individual bit values (0 or 1) between braces in the order $\{b_7, b_6, b_5, b_4, b_3, b_2, b_1, b_0\}$. These bytes are interpreted as finite field elements using a polynomial representation:

$$b_7x^7 + b_6x^6 + b_5x^5 + b_4x^4 + b_3x^3 + b_2x^2 + b_1x + b_0 = \sum_{i=0}^7 b_i x^i. \quad (3.1)$$

For example, $\{01100011\}$ identifies the specific finite field element $x^6 + x^5 + x + 1$.

It is also convenient to denote byte values using hexadecimal notation with each of two groups of four bits being denoted by a single character as in Fig. 1.

Bit Pattern	Character	Bit Pattern	Character	Bit Pattern	Character	Bit Pattern	Character
0000	0	0100	4	1000	8	1100	c
0001	1	0101	5	1001	9	1101	d
0010	2	0110	6	1010	a	1110	e
0011	3	0111	7	1011	b	1111	f

Figure 1. Hexadecimal representation of bit patterns.

Hence the element $\{01100011\}$ can be represented as $\{63\}$, where the character denoting the four-bit group containing the higher numbered bits is again to the left.

Some finite field operations involve one additional bit (b_8) to the left of an 8-bit byte. Where this extra bit is present, it will appear as ‘ $\{01\}$ ’ immediately preceding the 8-bit byte; for example, a 9-bit sequence will be presented as $\{01\}\{1b\}$.

3.3 Arrays of Bytes

Arrays of bytes will be represented in the following form:

$$a_0 a_1 a_2 \dots a_{15}$$

The bytes and the bit ordering within bytes are derived from the 128-bit input sequence

$$input_0 input_1 input_2 \dots input_{126} input_{127}$$

as follows:

$$\begin{aligned}
a_0 &= \{input_0, input_1, \dots, input_7\}; \\
a_1 &= \{input_8, input_9, \dots, input_{15}\}; \\
&\vdots \\
a_{15} &= \{input_{120}, input_{121}, \dots, input_{127}\}.
\end{aligned}$$

The pattern can be extended to longer sequences (i.e., for 192- and 256-bit keys), so that, in general,

$$a_n = \{input_{8n}, input_{8n+1}, \dots, input_{8n+7}\}. \quad (3.2)$$

Taking Sections 3.2 and 3.3 together, Fig. 2 shows how bits within each byte are numbered.

Input bit sequence	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	...
Byte number	0								1								2								...
Bit numbers in byte	7	6	5	4	3	2	1	0	7	6	5	4	3	2	1	0	7	6	5	4	3	2	1	0	...

Figure 2. Indices for Bytes and Bits.

3.4 The State

Internally, the AES algorithm's operations are performed on a two-dimensional array of bytes called the **State**. The State consists of four rows of bytes, each containing Nb bytes, where Nb is the block length divided by 32. In the State array denoted by the symbol s , each individual byte has two indices, with its row number r in the range $0 \leq r < 4$ and its column number c in the range $0 \leq c < Nb$. This allows an individual byte of the State to be referred to as either $s_{r,c}$ or $s[r,c]$. For this standard, $Nb=4$, i.e., $0 \leq c < 4$ (also see Sec. 6.3).

At the start of the Cipher and Inverse Cipher described in Sec. 5, the input – the array of bytes $in_0, in_1, \dots, in_{15}$ – is copied into the State array as illustrated in Fig. 3. The Cipher or Inverse Cipher operations are then conducted on this State array, after which its final value is copied to the output – the array of bytes $out_0, out_1, \dots, out_{15}$.

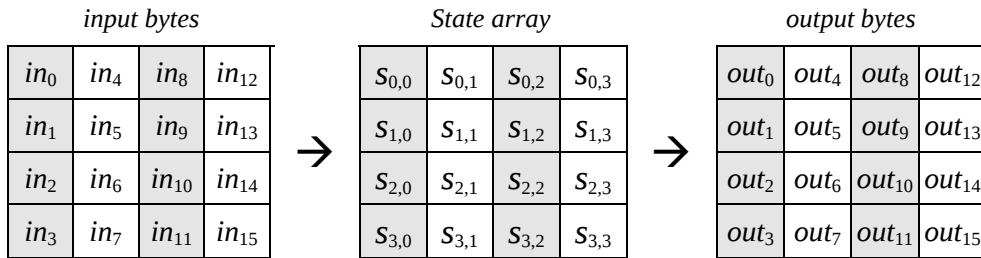


Figure 3. State array input and output.

Hence, at the beginning of the Cipher or Inverse Cipher, the input array, in , is copied to the State array according to the scheme:

$$s[r, c] = in[r + 4c] \quad \text{for } 0 \leq r < 4 \text{ and } 0 \leq c < Nb, \quad (3.3)$$

and at the end of the Cipher and Inverse Cipher, the State is copied to the output array *out* as follows:

$$out[r + 4c] = s[r, c] \quad \text{for } 0 \leq r < 4 \text{ and } 0 \leq c < Nb. \quad (3.4)$$

3.5 The State as an Array of Columns

The four bytes in each column of the State array form 32-bit **words**, where the row number *r* provides an index for the four bytes within each word. The state can hence be interpreted as a one-dimensional array of 32 bit words (columns), $w_0 \dots w_3$, where the column number *c* provides an index into this array. Hence, for the example in Fig. 3, the State can be considered as an array of four words, as follows:

$$\begin{aligned} w_0 &= s_{0,0} s_{1,0} s_{2,0} s_{3,0} & w_2 &= s_{0,2} s_{1,2} s_{2,2} s_{3,2} \\ w_1 &= s_{0,1} s_{1,1} s_{2,1} s_{3,1} & w_3 &= s_{0,3} s_{1,3} s_{2,3} s_{3,3} . \end{aligned} \quad (3.5)$$

4. Mathematical Preliminaries

All bytes in the AES algorithm are interpreted as finite field elements using the notation introduced in Sec. 3.2. Finite field elements can be added and multiplied, but these operations are different from those used for numbers. The following subsections introduce the basic mathematical concepts needed for Sec. 5.

4.1 Addition

The addition of two elements in a finite field is achieved by “adding” the coefficients for the corresponding powers in the polynomials for the two elements. The addition is performed with the XOR operation (denoted by $\oplus$) - i.e., modulo 2 - so that $1 \oplus 1 = 0$, $1 \oplus 0 = 1$, and $0 \oplus 0 = 0$. Consequently, subtraction of polynomials is identical to addition of polynomials.

Alternatively, addition of finite field elements can be described as the modulo 2 addition of corresponding bits in the byte. For two bytes $\{a_7 a_6 a_5 a_4 a_3 a_2 a_1 a_0\}$ and $\{b_7 b_6 b_5 b_4 b_3 b_2 b_1 b_0\}$, the sum is $\{c_7 c_6 c_5 c_4 c_3 c_2 c_1 c_0\}$, where each $c_i = a_i \oplus b_i$ (i.e., $c_7 = a_7 \oplus b_7$, $c_6 = a_6 \oplus b_6$, ... $c_0 = a_0 \oplus b_0$).

For example, the following expressions are equivalent to one another:

$$\begin{aligned} (x^6 + x^4 + x^2 + x + 1) + (x^7 + x + 1) &= x^7 + x^6 + x^4 + x^2 & \text{(polynomial notation);} \\ \{01010111\} \oplus \{10000011\} &= \{11010100\} & \text{(binary notation);} \\ \{57\} \oplus \{83\} &= \{d4\} & \text{(hexadecimal notation).} \end{aligned}$$

4.2 Multiplication

In the polynomial representation, multiplication in $GF(2^8)$ (denoted by $\bullet$) corresponds with the multiplication of polynomials modulo an **irreducible polynomial** of degree 8. A polynomial is irreducible if its only divisors are one and itself. **For the AES algorithm, this irreducible polynomial is**

$$m(x) = x^8 + x^4 + x^3 + x + 1, \quad (4.1)$$

or {01}{1b} in hexadecimal notation.

For example, {57} • {83} = {c1}, because

$$\begin{aligned}
 (x^6 + x^4 + x^2 + x + 1)(x^7 + x + 1) &= x^{13} + x^{11} + x^9 + x^8 + x^7 + \\
 &\quad x^7 + x^5 + x^3 + x^2 + x + \\
 &\quad x^6 + x^4 + x^2 + x + 1 \\
 &= x^{13} + x^{11} + x^9 + x^8 + x^6 + x^5 + x^4 + x^3 + 1
 \end{aligned}$$

and

$$\begin{aligned}
 x^{13} + x^{11} + x^9 + x^8 + x^6 + x^5 + x^4 + x^3 + 1 \text{ modulo } (x^8 + x^4 + x^3 + x + 1) \\
 = x^7 + x^6 + 1.
 \end{aligned}$$

The modular reduction by $m(x)$ ensures that the result will be a binary polynomial of degree less than 8, and thus can be represented by a byte. Unlike addition, there is no simple operation at the byte level that corresponds to this multiplication.

The multiplication defined above is associative, and the element {01} is the multiplicative identity. For any non-zero binary polynomial $b(x)$ of degree less than 8, the multiplicative inverse of $b(x)$, denoted $b^{-1}(x)$, can be found as follows: the extended Euclidean algorithm [7] is used to compute polynomials $a(x)$ and $c(x)$ such that

$$b(x)a(x) + m(x)c(x) = 1. \quad (4.2)$$

Hence, $a(x) \bullet b(x) \bmod m(x) = 1$, which means

$$b^{-1}(x) = a(x) \bmod m(x). \quad (4.3)$$

Moreover, for any $a(x)$, $b(x)$ and $c(x)$ in the field, it holds that

$$a(x) \bullet (b(x) + c(x)) = a(x) \bullet b(x) + a(x) \bullet c(x).$$

It follows that the set of 256 possible byte values, with XOR used as addition and the multiplication defined as above, has the structure of the finite field $GF(2^8)$.

4.2.1 Multiplication by x

Multiplying the binary polynomial defined in equation (3.1) with the polynomial x results in

$$b_7x^8 + b_6x^7 + b_5x^6 + b_4x^5 + b_3x^4 + b_2x^3 + b_1x^2 + b_0x. \quad (4.4)$$

The result $x \bullet b(x)$ is obtained by reducing the above result modulo $m(x)$, as defined in equation (4.1). If $b_7 = 0$, the result is already in reduced form. If $b_7 = 1$, the reduction is accomplished by subtracting (i.e., XORing) the polynomial $m(x)$. It follows that multiplication by x (i.e., {00000010} or {02}) can be implemented at the byte level as a left shift and a subsequent conditional bitwise XOR with {1b}. This operation on bytes is denoted by `xtime()`. Multiplication by higher powers of x can be implemented by repeated application of `xtime()`. By adding intermediate results, multiplication by any constant can be implemented.

For example, {57} • {13} = {fe} because

$$\begin{aligned}
\{57\} \bullet \{02\} &= \text{xtime}(\{57\}) = \{ae\} \\
\{57\} \bullet \{04\} &= \text{xtime}(\{ae\}) = \{47\} \\
\{57\} \bullet \{08\} &= \text{xtime}(\{47\}) = \{8e\} \\
\{57\} \bullet \{10\} &= \text{xtime}(\{8e\}) = \{07\},
\end{aligned}$$

thus,

$$\begin{aligned}
\{57\} \bullet \{13\} &= \{57\} \bullet (\{01\} \oplus \{02\} \oplus \{10\}) \\
&= \{57\} \oplus \{ae\} \oplus \{07\} \\
&= \{fe\}.
\end{aligned}$$

4.3 Polynomials with Coefficients in $GF(2^8)$

Four-term polynomials can be defined - with coefficients that are finite field elements - as:

$$a(x) = a_3x^3 + a_2x^2 + a_1x + a_0 \quad (4.5)$$

which will be denoted as a word in the form $[a_0, a_1, a_2, a_3]$. Note that the polynomials in this section behave somewhat differently than the polynomials used in the definition of finite field elements, even though both types of polynomials use the same indeterminate, x . The coefficients in this section are themselves finite field elements, i.e., bytes, instead of bits; also, the multiplication of four-term polynomials uses a different reduction polynomial, defined below. The distinction should always be clear from the context.

To illustrate the addition and multiplication operations, let

$$b(x) = b_3x^3 + b_2x^2 + b_1x + b_0 \quad (4.6)$$

define a second four-term polynomial. Addition is performed by adding the finite field coefficients of like powers of x . This addition corresponds to an XOR operation between the corresponding bytes in each of the words – in other words, the XOR of the complete word values.

Thus, using the equations of (4.5) and (4.6),

$$a(x) + b(x) = (a_3 \oplus b_3)x^3 + (a_2 \oplus b_2)x^2 + (a_1 \oplus b_1)x + (a_0 \oplus b_0) \quad (4.7)$$

Multiplication is achieved in two steps. In the first step, the polynomial product $c(x) = a(x) \bullet b(x)$ is algebraically expanded, and like powers are collected to give

$$c(x) = c_6x^6 + c_5x^5 + c_4x^4 + c_3x^3 + c_2x^2 + c_1x + c_0 \quad (4.8)$$

where

$$\begin{aligned}
c_0 &= a_0 \bullet b_0 & c_4 &= a_3 \bullet b_1 \oplus a_2 \bullet b_2 \oplus a_1 \bullet b_3 \\
c_1 &= a_1 \bullet b_0 \oplus a_0 \bullet b_1 & c_5 &= a_3 \bullet b_2 \oplus a_2 \bullet b_3 \\
c_2 &= a_2 \bullet b_0 \oplus a_1 \bullet b_1 \oplus a_0 \bullet b_2 & c_6 &= a_3 \bullet b_3
\end{aligned} \quad (4.9)$$

$$c_3 = a_3 \bullet b_0 \oplus a_2 \bullet b_1 \oplus a_1 \bullet b_2 \oplus a_0 \bullet b_3.$$

The result, $c(x)$, does not represent a four-byte word. Therefore, the second step of the multiplication is to reduce $c(x)$ modulo a polynomial of degree 4; the result can be reduced to a polynomial of degree less than 4. **For the AES algorithm, this is accomplished with the polynomial $x^4 + 1$, so that**

$$x^i \bmod (x^4 + 1) = x^{i \bmod 4}. \quad (4.10)$$

The modular product of $a(x)$ and $b(x)$, denoted by $a(x) \otimes b(x)$, is given by the four-term polynomial $d(x)$, defined as follows:

$$d(x) = d_3 x^3 + d_2 x^2 + d_1 x + d_0 \quad (4.11)$$

with

$$\begin{aligned} d_0 &= (a_0 \bullet b_0) \oplus (a_3 \bullet b_1) \oplus (a_2 \bullet b_2) \oplus (a_1 \bullet b_3) \\ d_1 &= (a_1 \bullet b_0) \oplus (a_0 \bullet b_1) \oplus (a_3 \bullet b_2) \oplus (a_2 \bullet b_3) \\ d_2 &= (a_2 \bullet b_0) \oplus (a_1 \bullet b_1) \oplus (a_0 \bullet b_2) \oplus (a_3 \bullet b_3) \\ d_3 &= (a_3 \bullet b_0) \oplus (a_2 \bullet b_1) \oplus (a_1 \bullet b_2) \oplus (a_0 \bullet b_3) \end{aligned} \quad (4.12)$$

When $a(x)$ is a fixed polynomial, the operation defined in equation (4.11) can be written in matrix form as:

$$\begin{bmatrix} d_0 \\ d_1 \\ d_2 \\ d_3 \end{bmatrix} = \begin{bmatrix} a_0 & a_3 & a_2 & a_1 \\ a_1 & a_0 & a_3 & a_2 \\ a_2 & a_1 & a_0 & a_3 \\ a_3 & a_2 & a_1 & a_0 \end{bmatrix} \begin{bmatrix} b_0 \\ b_1 \\ b_2 \\ b_3 \end{bmatrix} \quad (4.13)$$

Because $x^4 + 1$ is not an irreducible polynomial over $\text{GF}(2^8)$, multiplication by a fixed four-term polynomial is not necessarily invertible. However, the AES algorithm specifies a fixed four-term polynomial that *does* have an inverse (see Sec. 5.1.3 and Sec. 5.3.3):

$$a(x) = \{03\}x^3 + \{01\}x^2 + \{01\}x + \{02\} \quad (4.14)$$

$$a^{-1}(x) = \{0b\}x^3 + \{0d\}x^2 + \{09\}x + \{0e\}. \quad (4.15)$$

Another polynomial used in the AES algorithm (see the **RotWord()** function in Sec. 5.2) has $a_0 = a_1 = a_2 = \{00\}$ and $a_3 = \{01\}$, which is the polynomial x^3 . Inspection of equation (4.13) above will show that its effect is to form the output word by rotating bytes in the input word. This means that $[b_0, b_1, b_2, b_3]$ is transformed into $[b_1, b_2, b_3, b_0]$.

5. Algorithm Specification

For the AES algorithm, **the length of the input block, the output block and the State is 128 bits**. This is represented by $Nb = 4$, which reflects the number of 32-bit words (number of columns) in the State.

For the AES algorithm, **the length of the Cipher Key, K , is 128, 192, or 256 bits.** The key length is represented by $Nk = 4, 6$, or 8 , which reflects the number of 32-bit words (number of columns) in the Cipher Key.

For the AES algorithm, the number of rounds to be performed during the execution of the algorithm is dependent on the key size. The number of rounds is represented by Nr , where $Nr = 10$ when $Nk = 4$, $Nr = 12$ when $Nk = 6$, and $Nr = 14$ when $Nk = 8$.

The only Key-Block-Round combinations that conform to this standard are given in Fig. 4. For implementation issues relating to the key length, block size and number of rounds, see Sec. 6.3.

	Key Length (Nk words)	Block Size (Nb words)	Number of Rounds (Nr)
AES-128	4	4	10
AES-192	6	4	12
AES-256	8	4	14

Figure 4. Key-Block-Round Combinations.

For both its Cipher and Inverse Cipher, the AES algorithm uses a round function that is composed of four different byte-oriented transformations: 1) byte substitution using a substitution table (S-box), 2) shifting rows of the State array by different offsets, 3) mixing the data within each column of the State array, and 4) adding a Round Key to the State. These transformations (and their inverses) are described in Sec. 5.1.1-5.1.4 and 5.3.1-5.3.4.

The Cipher and Inverse Cipher are described in Sec. 5.1 and Sec. 5.3, respectively, while the Key Schedule is described in Sec. 5.2.

5.1 Cipher

At the start of the Cipher, the input is copied to the State array using the conventions described in Sec. 3.4. After an initial Round Key addition, the State array is transformed by implementing a round function 10, 12, or 14 times (depending on the key length), with the final round differing slightly from the first $Nr - 1$ rounds. The final State is then copied to the output as described in Sec. 3.4.

The round function is parameterized using a key schedule that consists of a one-dimensional array of four-byte words derived using the Key Expansion routine described in Sec. 5.2.

The Cipher is described in the pseudo code in Fig. 5. The individual transformations - **SubBytes()**, **ShiftRows()**, **MixColumns()**, and **AddRoundKey()** – process the State and are described in the following subsections. In Fig. 5, the array **w[]** contains the key schedule, which is described in Sec. 5.2.

As shown in Fig. 5, all Nr rounds are identical with the exception of the final round, which does not include the **MixColumns()** transformation.

Appendix B presents an example of the Cipher, showing values for the State array at the beginning of each round and after the application of each of the four transformations described in the following sections.

```

Cipher(byte in[4*Nb], byte out[4*Nb], word w[Nb*(Nr+1)])
begin
    byte state[4,Nb]

    state = in

    AddRoundKey(state, w[0, Nb-1])           // See Sec. 5.1.4

    for round = 1 step 1 to Nr-1
        SubBytes(state)                       // See Sec. 5.1.1
        ShiftRows(state)                     // See Sec. 5.1.2
        MixColumns(state)                    // See Sec. 5.1.3
        AddRoundKey(state, w[round*Nb, (round+1)*Nb-1])
    end for

    SubBytes(state)
    ShiftRows(state)
    AddRoundKey(state, w[Nr*Nb, (Nr+1)*Nb-1])

    out = state
end

```

Figure 5. Pseudo Code for the Cipher.¹

5.1.1 SubBytes() Transformation

The **SubBytes()** transformation is a non-linear byte substitution that operates independently on each byte of the State using a substitution table (S-box). This S-box (Fig. 7), which is invertible, is constructed by composing two transformations:

1. Take the multiplicative inverse in the finite field $GF(2^8)$, described in Sec. 4.2; the element $\{00\}$ is mapped to itself.
2. Apply the following affine transformation (over $GF(2)$):

$$b'_i = b_i \oplus b_{(i+4) \bmod 8} \oplus b_{(i+5) \bmod 8} \oplus b_{(i+6) \bmod 8} \oplus b_{(i+7) \bmod 8} \oplus c_i \quad (5.1)$$

for $0 \leq i < 8$, where b_i is the i^{th} bit of the byte, and c_i is the i^{th} bit of a byte c with the value $\{63\}$ or $\{01100011\}$. Here and elsewhere, a prime on a variable (e.g., b') indicates that the variable is to be updated with the value on the right.

In matrix form, the affine transformation element of the S-box can be expressed as:

¹ The various transformations (e.g., **SubBytes()**, **ShiftRows()**, etc.) act upon the State array that is addressed by the 'state' pointer. **AddRoundKey()** uses an additional pointer to address the Round Key.

$$\begin{bmatrix} b'_0 \\ b'_1 \\ b'_2 \\ b'_3 \\ b'_4 \\ b'_5 \\ b'_6 \\ b'_7 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \\ 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 \\ 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} b_0 \\ b_1 \\ b_2 \\ b_3 \\ b_4 \\ b_5 \\ b_6 \\ b_7 \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \\ 0 \\ 0 \\ 0 \\ 1 \\ 1 \\ 0 \end{bmatrix}. \quad (5.2)$$

Figure 6 illustrates the effect of the **SubBytes()** transformation on the State.

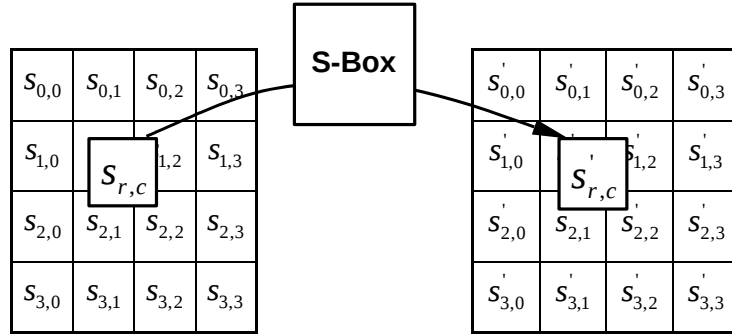


Figure 6. SubBytes () applies the S-box to each byte of the State.

The S-box used in the **SubBytes()** transformation is presented in hexadecimal form in Fig. 7.

For example, if $s_{1,1} = \{53\}$, then the substitution value would be determined by the intersection of the row with index '5' and the column with index '3' in Fig. 7. This would result in $s'_{1,1}$ having a value of $\{ed\}$.

		y															
		0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
x	0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
	1	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
	2	b7	fd	93	26	36	3f	f7	cc	34	a5	e5	f1	71	d8	31	15
	3	04	c7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
	4	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
	5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
	6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f	a8
	7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
	8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
	9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
	a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
	b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
	c	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
	d	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
	e	e1	f8	98	11	69	d9	8e	94	9b	1e	87	e9	ce	55	28	df
	f	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb	16

Figure 7. S-box: substitution values for the byte xy (in hexadecimal format).

5.1.2 ShiftRows() Transformation

In the **ShiftRows()** transformation, the bytes in the last three rows of the State are cyclically shifted over different numbers of bytes (offsets). The first row, $r = 0$, is not shifted.

Specifically, the **ShiftRows()** transformation proceeds as follows:

$$s'_{r,c} = s_{r,(c+shift(r,Nb)) \bmod Nb} \quad \text{for } 0 < r < 4 \quad \text{and} \quad 0 \leq c < Nb, \quad (5.3)$$

where the shift value $shift(r,Nb)$ depends on the row number, r , as follows (recall that $Nb = 4$):

$$shift(1,4) = 1; \quad shift(2,4) = 2; \quad shift(3,4) = 3. \quad (5.4)$$

This has the effect of moving bytes to “lower” positions in the row (i.e., lower values of c in a given row), while the “lowest” bytes wrap around into the “top” of the row (i.e., higher values of c in a given row).

Figure 8 illustrates the **ShiftRows()** transformation.

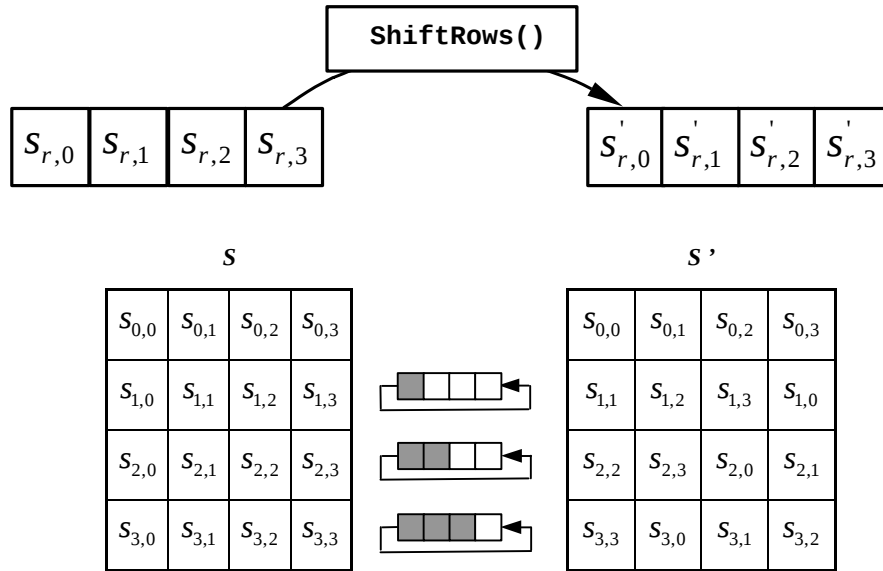


Figure 8. ShiftRows() cyclically shifts the last three rows in the State.

5.1.3 MixColumns() Transformation

The **MixColumns()** transformation operates on the State column-by-column, treating each column as a four-term polynomial as described in Sec. 4.3. The columns are considered as polynomials over $GF(2^8)$ and multiplied modulo $x^4 + 1$ with a fixed polynomial $a(x)$, given by

$$a(x) = \{03\}x^3 + \{01\}x^2 + \{01\}x + \{02\}. \quad (5.5)$$

As described in Sec. 4.3, this can be written as a matrix multiplication. Let

$$s'(x) = a(x) \otimes s(x):$$

$$\begin{bmatrix} s'_{0,c} \\ s'_{1,c} \\ s'_{2,c} \\ s'_{3,c} \end{bmatrix} = \begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix} \begin{bmatrix} s_{0,c} \\ s_{1,c} \\ s_{2,c} \\ s_{3,c} \end{bmatrix} \quad \text{for } 0 \leq c < Nb. \quad (5.6)$$

As a result of this multiplication, the four bytes in a column are replaced by the following:

$$\begin{aligned} s'_{0,c} &= (\{02\} \bullet s_{0,c}) \oplus (\{03\} \bullet s_{1,c}) \oplus s_{2,c} \oplus s_{3,c} \\ s'_{1,c} &= s_{0,c} \oplus (\{02\} \bullet s_{1,c}) \oplus (\{03\} \bullet s_{2,c}) \oplus s_{3,c} \\ s'_{2,c} &= s_{0,c} \oplus s_{1,c} \oplus (\{02\} \bullet s_{2,c}) \oplus (\{03\} \bullet s_{3,c}) \\ s'_{3,c} &= (\{03\} \bullet s_{0,c}) \oplus s_{1,c} \oplus s_{2,c} \oplus (\{02\} \bullet s_{3,c}). \end{aligned}$$

Figure 9 illustrates the **MixColumns()** transformation.

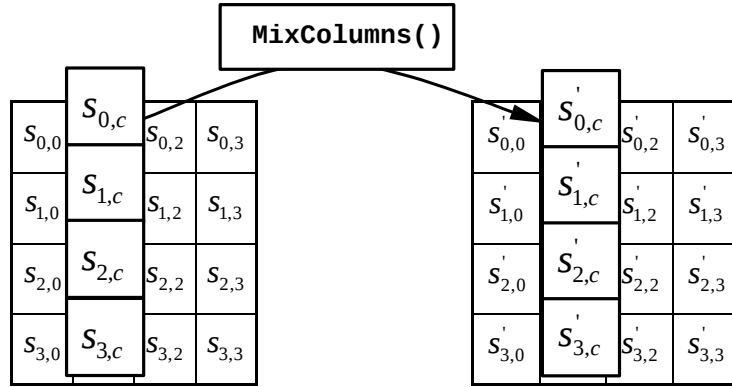


Figure 9. **MixColumns()** operates on the State column-by-column.

5.1.4 AddRoundKey() Transformation

In the **AddRoundKey()** transformation, a Round Key is added to the State by a simple bitwise XOR operation. Each Round Key consists of Nb words from the key schedule (described in Sec. 5.2). Those Nb words are each added into the columns of the State, such that

$$[s'_{0,c}, s'_{1,c}, s'_{2,c}, s'_{3,c}] = [s_{0,c}, s_{1,c}, s_{2,c}, s_{3,c}] \oplus [w_{round * Nb + c}] \quad \text{for } 0 \leq c < Nb, \quad (5.7)$$

where $[w_i]$ are the key schedule words described in Sec. 5.2, and $round$ is a value in the range $0 \leq round \leq Nr$. In the Cipher, the initial Round Key addition occurs when $round = 0$, prior to the first application of the round function (see Fig. 5). The application of the **AddRoundKey()** transformation to the Nr rounds of the Cipher occurs when $1 \leq round \leq Nr$.

The action of this transformation is illustrated in Fig. 10, where $l = round * Nb$. The byte address within words of the key schedule was described in Sec. 3.1.

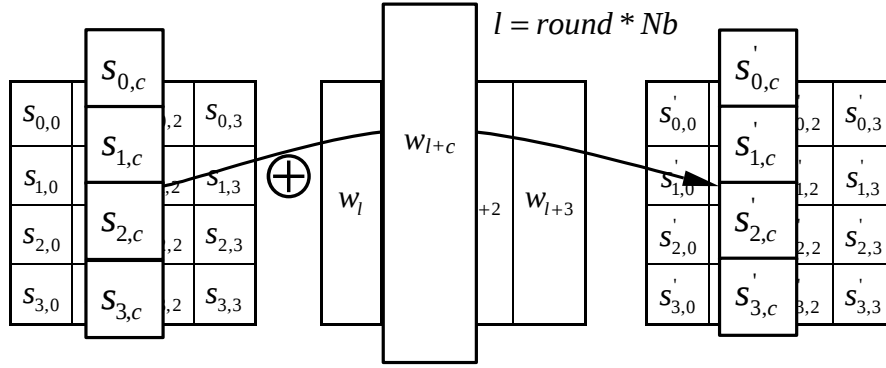


Figure 10. AddRoundKey () XORs each column of the State with a word from the key schedule.

5.2 Key Expansion

The AES algorithm takes the Cipher Key, K , and performs a Key Expansion routine to generate a key schedule. The Key Expansion generates a total of Nb ($Nr + 1$) words: the algorithm requires an initial set of Nb words, and each of the Nr rounds requires Nb words of key data. The resulting key schedule consists of a linear array of 4-byte words, denoted $[w_i]$, with i in the range $0 \leq i < Nb(Nr + 1)$.

The expansion of the input key into the key schedule proceeds according to the pseudo code in Fig. 11.

SubWord() is a function that takes a four-byte input word and applies the S-box (Sec. 5.1.1, Fig. 7) to each of the four bytes to produce an output word. The function **RotWord()** takes a word $[a_0, a_1, a_2, a_3]$ as input, performs a cyclic permutation, and returns the word $[a_1, a_2, a_3, a_0]$. The round constant word array, **Rcon[i]**, contains the values given by $[x^{i-1}, \{00\}, \{00\}, \{00\}]$, with x^{i-1} being powers of x (x is denoted as $\{02\}$) in the field $GF(2^8)$, as discussed in Sec. 4.2 (note that i starts at 1, not 0).

From Fig. 11, it can be seen that the first Nk words of the expanded key are filled with the Cipher Key. Every following word, $w[i]$, is equal to the XOR of the previous word, $w[i-1]$, and the word Nk positions earlier, $w[i-Nk]$. For words in positions that are a multiple of Nk , a transformation is applied to $w[i-1]$ prior to the XOR, followed by an XOR with a round constant, **Rcon[i]**. This transformation consists of a cyclic shift of the bytes in a word (**RotWord()**), followed by the application of a table lookup to all four bytes of the word (**SubWord()**).

It is important to note that the Key Expansion routine for 256-bit Cipher Keys ($Nk = 8$) is slightly different than for 128- and 192-bit Cipher Keys. If $Nk = 8$ and $i-4$ is a multiple of Nk , then **SubWord()** is applied to $w[i-1]$ prior to the XOR.

```

KeyExpansion(byte key[4*Nk], word w[Nb*(Nr+1)], Nk)
begin
    word temp

    i = 0

    while (i < Nk)
        w[i] = word(key[4*i], key[4*i+1], key[4*i+2], key[4*i+3])
        i = i+1
    end while

    i = Nk

    while (i < Nb * (Nr+1))
        temp = w[i-1]
        if (i mod Nk = 0)
            temp = SubWord(RotWord(temp)) xor Rcon[i/Nk]
        else if (Nk > 6 and i mod Nk = 4)
            temp = SubWord(temp)
        end if
        w[i] = w[i-Nk] xor temp
        i = i + 1
    end while
end

```

Note that $Nk=4$, 6, and 8 do not all have to be implemented; they are all included in the conditional statement above for conciseness. Specific implementation requirements for the Cipher Key are presented in Sec. 6.1.

Figure 11. Pseudo Code for Key Expansion.²

Appendix A presents examples of the Key Expansion.

5.3 Inverse Cipher

The Cipher transformations in Sec. 5.1 can be inverted and then implemented in reverse order to produce a straightforward Inverse Cipher for the AES algorithm. The individual transformations used in the Inverse Cipher - **InvShiftRows()**, **InvSubBytes()**, **InvMixColumns()**, and **AddRoundKey()** – process the State and are described in the following subsections.

The Inverse Cipher is described in the pseudo code in Fig. 12. In Fig. 12, the array **w[]** contains the key schedule, which was described previously in Sec. 5.2.

² The functions **SubWord()** and **RotWord()** return a result that is a transformation of the function input, whereas the transformations in the Cipher and Inverse Cipher (e.g., **ShiftRows()**, **SubBytes()**, etc.) transform the State array that is addressed by the ‘state’ pointer.

```

InvCipher(byte in[4*Nb], byte out[4*Nb], word w[Nb*(Nr+1)])
begin
    byte state[4,Nb]

    state = in

    AddRoundKey(state, w[Nr*Nb, (Nr+1)*Nb-1]) // See Sec. 5.1.4

    for round = Nr-1 step -1 downto 1
        InvShiftRows(state) // See Sec. 5.3.1
        InvSubBytes(state) // See Sec. 5.3.2
        AddRoundKey(state, w[round*Nb, (round+1)*Nb-1])
        InvMixColumns(state) // See Sec. 5.3.3
    end for

    InvShiftRows(state)
    InvSubBytes(state)
    AddRoundKey(state, w[0, Nb-1])

    out = state
end

```

Figure 12. Pseudo Code for the Inverse Cipher.³

5.3.1 **InvShiftRows()** Transformation

InvShiftRows() is the inverse of the **ShiftRows()** transformation. The bytes in the last three rows of the State are cyclically shifted over different numbers of bytes (offsets). The first row, $r = 0$, is not shifted. The bottom three rows are cyclically shifted by $Nb - \text{shift}(r, Nb)$ bytes, where the shift value $\text{shift}(r, Nb)$ depends on the row number, and is given in equation (5.4) (see Sec. 5.1.2).

Specifically, the **InvShiftRows()** transformation proceeds as follows:

$$s'_{r, (c + \text{shift}(r, Nb)) \bmod Nb} = s_{r, c} \quad \text{for } 0 < r < 4 \quad \text{and} \quad 0 \leq c < Nb \quad (5.8)$$

Figure 13 illustrates the **InvShiftRows()** transformation.

³ The various transformations (e.g., **InvSubBytes()**, **InvShiftRows()**, etc.) act upon the State array that is addressed by the 'state' pointer. **AddRoundKey()** uses an additional pointer to address the Round Key.

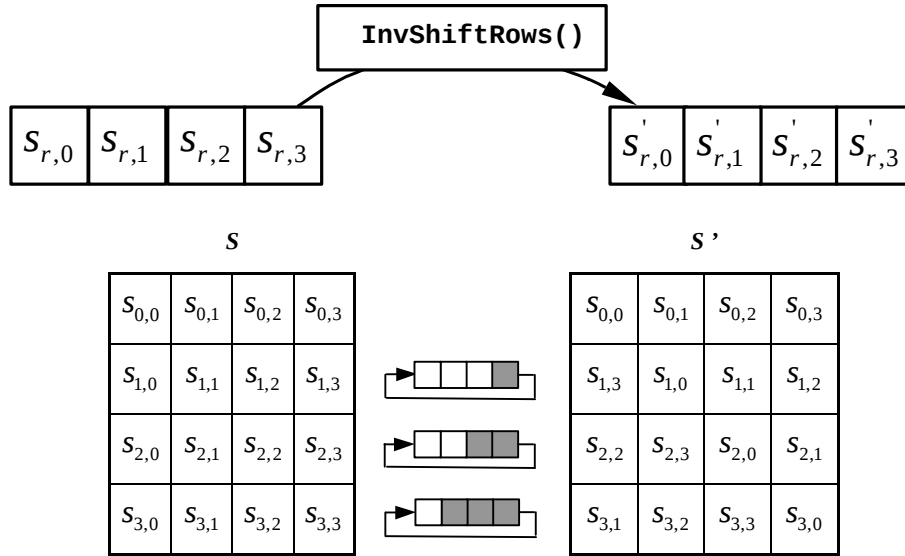


Figure 13. **InvShiftRows()** cyclically shifts the last three rows in the State.

5.3.2 InvSubBytes() Transformation

InvSubBytes() is the inverse of the byte substitution transformation, in which the inverse S-box is applied to each byte of the State. This is obtained by applying the inverse of the affine transformation (5.1) followed by taking the multiplicative inverse in $GF(2^8)$.

The inverse S-box used in the **InvSubBytes()** transformation is presented in Fig. 14:

		y															
		0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f
x	0	52	09	6a	d5	30	36	a5	38	bf	40	a3	9e	81	f3	d7	fb
	1	7c	e3	39	82	9b	2f	ff	87	34	8e	43	44	c4	de	e9	cb
	2	54	7b	94	32	a6	c2	23	3d	ee	4c	95	0b	42	fa	c3	4e
	3	08	2e	a1	66	28	d9	24	b2	76	5b	a2	49	6d	8b	d1	25
	4	72	f8	f6	64	86	68	98	16	d4	a4	5c	cc	5d	65	b6	92
	5	6c	70	48	50	fd	ed	b9	da	5e	15	46	57	a7	8d	9d	84
	6	90	d8	ab	00	8c	bc	d3	0a	f7	e4	58	05	b8	b3	45	06
	7	d0	2c	1e	8f	ca	3f	0f	02	c1	af	bd	03	01	13	8a	6b
	8	3a	91	11	41	4f	67	dc	ea	97	f2	cf	ce	f0	b4	e6	73
	9	96	ac	74	22	e7	ad	35	85	e2	f9	37	e8	1c	75	df	6e
	a	47	f1	1a	71	1d	29	c5	89	6f	b7	62	0e	aa	18	be	1b
	b	fc	56	3e	4b	c6	d2	79	20	9a	db	c0	fe	78	cd	5a	f4
	c	1f	dd	a8	33	88	07	c7	31	b1	12	10	59	27	80	ec	5f
	d	60	51	7f	a9	19	b5	4a	0d	2d	e5	7a	9f	93	c9	9c	ef
	e	a0	e0	3b	4d	ae	2a	f5	b0	c8	eb	bb	3c	83	53	99	61
	f	17	2b	04	7e	ba	77	d6	26	e1	69	14	63	55	21	0c	7d

Figure 14. Inverse S-box: substitution values for the byte xy (in hexadecimal format).

5.3.3 InvMixColumns() Transformation

InvMixColumns() is the inverse of the **MixColumns()** transformation. **InvMixColumns()** operates on the State column-by-column, treating each column as a four-term polynomial as described in Sec. 4.3. The columns are considered as polynomials over $GF(2^8)$ and multiplied modulo $x^4 + 1$ with a fixed polynomial $a^{-1}(x)$, given by

$$a^{-1}(x) = \{0b\}x^3 + \{0d\}x^2 + \{09\}x + \{0e\}. \quad (5.9)$$

As described in Sec. 4.3, this can be written as a matrix multiplication. Let

$$s'(x) = a^{-1}(x) \otimes s(x) :$$

$$\begin{bmatrix} s'_{0,c} \\ s'_{1,c} \\ s'_{2,c} \\ s'_{3,c} \end{bmatrix} = \begin{bmatrix} 0e & 0b & 0d & 09 \\ 09 & 0e & 0b & 0d \\ 0d & 09 & 0e & 0b \\ 0b & 0d & 09 & 0e \end{bmatrix} \begin{bmatrix} s_{0,c} \\ s_{1,c} \\ s_{2,c} \\ s_{3,c} \end{bmatrix} \quad \text{for } 0 \leq c < Nb. \quad (5.10)$$

As a result of this multiplication, the four bytes in a column are replaced by the following:

$$\begin{aligned} s'_{0,c} &= (\{0e\} \bullet s_{0,c}) \oplus (\{0b\} \bullet s_{1,c}) \oplus (\{0d\} \bullet s_{2,c}) \oplus (\{09\} \bullet s_{3,c}) \\ s'_{1,c} &= (\{09\} \bullet s_{0,c}) \oplus (\{0e\} \bullet s_{1,c}) \oplus (\{0b\} \bullet s_{2,c}) \oplus (\{0d\} \bullet s_{3,c}) \\ s'_{2,c} &= (\{0d\} \bullet s_{0,c}) \oplus (\{09\} \bullet s_{1,c}) \oplus (\{0e\} \bullet s_{2,c}) \oplus (\{0b\} \bullet s_{3,c}) \\ s'_{3,c} &= (\{0b\} \bullet s_{0,c}) \oplus (\{0d\} \bullet s_{1,c}) \oplus (\{09\} \bullet s_{2,c}) \oplus (\{0e\} \bullet s_{3,c}) \end{aligned}$$

5.3.4 Inverse of the AddRoundKey() Transformation

AddRoundKey(), which was described in Sec. 5.1.4, is its own inverse, since it only involves an application of the XOR operation.

5.3.5 Equivalent Inverse Cipher

In the straightforward Inverse Cipher presented in Sec. 5.3 and Fig. 12, the sequence of the transformations differs from that of the Cipher, while the form of the key schedules for encryption and decryption remains the same. However, several properties of the AES algorithm allow for an Equivalent Inverse Cipher that has the same sequence of transformations as the Cipher (with the transformations replaced by their inverses). This is accomplished with a change in the key schedule.

The two properties that allow for this Equivalent Inverse Cipher are as follows:

1. The **SubBytes()** and **ShiftRows()** transformations commute; that is, a **SubBytes()** transformation immediately followed by a **ShiftRows()** transformation is equivalent to a **ShiftRows()** transformation immediately followed by a **SubBytes()** transformation. The same is true for their inverses, **InvSubBytes()** and **InvShiftRows**.

2. The column mixing operations - **MixColumns()** and **InvMixColumns()** - are linear with respect to the column input, which means

$$\begin{aligned} \text{InvMixColumns}(\text{state XOR Round Key}) = \\ \text{InvMixColumns}(\text{state}) \text{ XOR } \text{InvMixColumns}(\text{Round Key}). \end{aligned}$$

These properties allow the order of **InvSubBytes()** and **InvShiftRows()** transformations to be reversed. The order of the **AddRoundKey()** and **InvMixColumns()** transformations can also be reversed, provided that the columns (words) of the decryption key schedule are modified using the **InvMixColumns()** transformation.

The equivalent inverse cipher is defined by reversing the order of the **InvSubBytes()** and **InvShiftRows()** transformations shown in Fig. 12, and by reversing the order of the **AddRoundKey()** and **InvMixColumns()** transformations used in the “round loop” after first modifying the decryption key schedule for *round* = 1 to *Nr*-1 using the **InvMixColumns()** transformation. The first and last *Nb* words of the decryption key schedule shall *not* be modified in this manner.

Given these changes, the resulting Equivalent Inverse Cipher offers a more efficient structure than the Inverse Cipher described in Sec. 5.3 and Fig. 12. Pseudo code for the Equivalent Inverse Cipher appears in Fig. 15. (The word array **dw[]** contains the modified decryption key schedule. The modification to the Key Expansion routine is also provided in Fig. 15.)

```

EqInvCipher(byte in[4*Nb], byte out[4*Nb], word dw[Nb*(Nr+1)])
begin
    byte state[4,Nb]

    state = in

    AddRoundKey(state, dw[Nr*Nb, (Nr+1)*Nb-1])

    for round = Nr-1 step -1 downto 1
        InvSubBytes(state)
        InvShiftRows(state)
        InvMixColumns(state)
        AddRoundKey(state, dw[round*Nb, (round+1)*Nb-1])
    end for

    InvSubBytes(state)
    InvShiftRows(state)
    AddRoundKey(state, dw[0, Nb-1])

    out = state
end

```

For the Equivalent Inverse Cipher, the following pseudo code is added at the end of the Key Expansion routine (Sec. 5.2):

```

    for i = 0 step 1 to (Nr+1)*Nb-1
        dw[i] = w[i]
    end for

    for round = 1 step 1 to Nr-1
        InvMixColumns(dw[round*Nb, (round+1)*Nb-1])    // note change of
type
    end for

```

Note that, since InvMixColumns operates on a two-dimensional array of bytes while the Round Keys are held in an array of words, the call to InvMixColumns in this code sequence involves a change of type (i.e. the input to InvMixColumns() is normally the State array, which is considered to be a two-dimensional array of bytes, whereas the input here is a Round Key computed as a one-dimensional array of words).

Figure 15. Pseudo Code for the Equivalent Inverse Cipher.

6. Implementation Issues

6.1 Key Length Requirements

An implementation of the AES algorithm shall support *at least one* of the three key lengths specified in Sec. 5: 128, 192, or 256 bits (i.e., $Nk = 4, 6$, or 8 , respectively). Implementations

may optionally support two or three key lengths, which may promote the interoperability of algorithm implementations.

6.2 Keying Restrictions

No weak or semi-weak keys have been identified for the AES algorithm, and there is no restriction on key selection.

6.3 Parameterization of Key Length, Block Size, and Round Number

This standard explicitly defines the allowed values for the key length (Nk), block size (Nb), and number of rounds (Nr) – see Fig. 4. However, future reaffirmations of this standard could include changes or additions to the allowed values for those parameters. Therefore, implementers may choose to design their AES implementations with future flexibility in mind.

6.4 Implementation Suggestions Regarding Various Platforms

Implementation variations are possible that may, in many cases, offer performance or other advantages. Given the same input key and data (plaintext or ciphertext), any implementation that produces the same output (ciphertext or plaintext) as the algorithm specified in this standard is an acceptable implementation of the AES.

Reference [3] and other papers located at Ref. [1] include suggestions on how to efficiently implement the AES algorithm on a variety of platforms.

Appendix A - Key Expansion Examples

This appendix shows the development of the key schedule for various key sizes. Note that multi-byte values are presented using the notation described in Sec. 3. The intermediate values produced during the development of the key schedule (see Sec. 5.2) are given in the following table (all values are in hexadecimal format, with the exception of the index column (i)).

A.1 Expansion of a 128-bit Cipher Key

This section contains the key expansion of the following cipher key:

Cipher Key = 2b 7e 15 16 28 ae d2 a6 ab f7 15 88 09 cf 4f 3c

for $Nk = 4$, which results in

$w_0 = 2b7e1516$ $w_1 = 28aed2a6$ $w_2 = abf71588$ $w_3 = 09cf4f3c$

i (dec)	temp	After RotWord()	After SubWord()	Rcon[i/Nk]	After XOR with Rcon	w[i-Nk]	w[i]= temp XOR w[i-Nk]
4	09cf4f3c	cf4f3c09	8a84eb01	01000000	8b84eb01	2b7e1516	a0fafe17
5	a0fafe17					28aed2a6	88542cb1
6	88542cb1					abf71588	23a33939
7	23a33939					09cf4f3c	2a6c7605
8	2a6c7605	6c76052a	50386be5	02000000	52386be5	a0fafe17	f2c295f2
9	f2c295f2					88542cb1	7a96b943
10	7a96b943					23a33939	5935807a
11	5935807a					2a6c7605	7359f67f
12	7359f67f	59f67f73	cb42d28f	04000000	cf42d28f	f2c295f2	3d80477d
13	3d80477d					7a96b943	4716fe3e
14	4716fe3e					5935807a	1e237e44
15	1e237e44					7359f67f	6d7a883b
16	6d7a883b	7a883b6d	dac4e23c	08000000	d2c4e23c	3d80477d	ef44a541
17	ef44a541					4716fe3e	a8525b7f
18	a8525b7f					1e237e44	b671253b
19	b671253b					6d7a883b	db0bad00
20	db0bad00	0bad00db	2b9563b9	10000000	3b9563b9	ef44a541	d4d1c6f8
21	d4d1c6f8					a8525b7f	7c839d87
22	7c839d87					b671253b	caf2b8bc
23	caf2b8bc					db0bad00	11f915bc

24	11f915bc	f915bc11	99596582	20000000	b9596582	d4d1c6f8	6d88a37a
25	6d88a37a					7c839d87	110b3efd
26	110b3efd					caf2b8bc	dbf98641
27	dbf98641					11f915bc	ca0093fd
28	ca0093fd	0093fdca	63dc5474	40000000	23dc5474	6d88a37a	4e54f70e
29	4e54f70e					110b3efd	5f5fc9f3
30	5f5fc9f3					dbf98641	84a64fb2
31	84a64fb2					ca0093fd	4ea6dc4f
32	4ea6dc4f	a6dc4f4e	2486842f	80000000	a486842f	4e54f70e	ead27321
33	ead27321					5f5fc9f3	b58dbad2
34	b58dbad2					84a64fb2	312bf560
35	312bf560					4ea6dc4f	7f8d292f
36	7f8d292f	8d292f7f	5da515d2	1b000000	46a515d2	ead27321	ac7766f3
37	ac7766f3					b58dbad2	19fadc21
38	19fadc21					312bf560	28d12941
39	28d12941					7f8d292f	575c006e
40	575c006e	5c006e57	4a639f5b	36000000	7c639f5b	ac7766f3	d014f9a8
41	d014f9a8					19fadc21	c9ee2589
42	c9ee2589					28d12941	e13f0cc8
43	e13f0cc8					575c006e	b6630ca6

A.2 Expansion of a 192-bit Cipher Key

This section contains the key expansion of the following cipher key:

Cipher Key = **8e 73 b0 f7 da 0e 64 52 c8 10 f3 2b**
 80 90 79 e5 62 f8 ea d2 52 2c 6b 7b

for $Nk = 6$, which results in

$w_0 = \mathbf{8e73b0f7}$ $w_1 = \mathbf{da0e6452}$ $w_2 = \mathbf{c810f32b}$ $w_3 = \mathbf{809079e5}$
 $w_4 = \mathbf{62f8ead2}$ $w_5 = \mathbf{522c6b7b}$

i (dec)	temp	After RotWord()	After SubWord()	Rcon[i/Nk]	After XOR with Rcon	w[i-Nk]	w[i]= temp XOR w[i-Nk]
6	522c6b7b	2c6b7b52	717f2100	01000000	707f2100	8e73b0f7	fe0c91f7
7	fe0c91f7					da0e6452	2402f5a5
8	2402f5a5					c810f32b	ec12068e

9	ec12068e					809079e5	6c827f6b
10	6c827f6b					62f8ead2	0e7a95b9
11	0e7a95b9					522c6b7b	5c56fec2
12	5c56fec2	56fec25c	b1bb254a	02000000	b3bb254a	fe0c91f7	4db7b4bd
13	4db7b4bd					2402f5a5	69b54118
14	69b54118					ec12068e	85a74796
15	85a74796					6c827f6b	e92538fd
16	e92538fd					0e7a95b9	e75fad44
17	e75fad44					5c56fec2	bb095386
18	bb095386	095386bb	01ed44ea	04000000	05ed44ea	4db7b4bd	485af057
19	485af057					69b54118	21efb14f
20	21efb14f					85a74796	a448f6d9
21	a448f6d9					e92538fd	4d6dce24
22	4d6dce24					e75fad44	aa326360
23	aa326360					bb095386	113b30e6
24	113b30e6	3b30e611	e2048e82	08000000	ea048e82	485af057	a25e7ed5
25	a25e7ed5					21efb14f	83b1cf9a
26	83b1cf9a					a448f6d9	27f93943
27	27f93943					4d6dce24	6a94f767
28	6a94f767					aa326360	c0a69407
29	c0a69407					113b30e6	d19da4e1
30	d19da4e1	9da4e1d1	5e49f83e	10000000	4e49f83e	a25e7ed5	ec1786eb
31	ec1786eb					83b1cf9a	6fa64971
32	6fa64971					27f93943	485f7032
33	485f7032					6a94f767	22cb8755
34	22cb8755					c0a69407	e26d1352
35	e26d1352					d19da4e1	33f0b7b3
36	33f0b7b3	f0b7b333	8ca96dc3	20000000	aca96dc3	ec1786eb	40beeb28
37	40beeb28					6fa64971	2f18a259
38	2f18a259					485f7032	6747d26b
39	6747d26b					22cb8755	458c553e
40	458c553e					e26d1352	a7e1466c
41	a7e1466c					33f0b7b3	9411f1df
42	9411f1df	11f1df94	82a19e22	40000000	c2a19e22	40beeb28	821f750a
43	821f750a					2f18a259	ad07d753

44	ad07d753					6747d26b	ca400538
45	ca400538					458c553e	8fcc5006
46	8fcc5006					a7e1466c	282d166a
47	282d166a					9411f1df	bc3ce7b5
48	bc3ce7b5	3ce7b5bc	eb94d565	80000000	6b94d565	821f750a	e98ba06f
49	e98ba06f					ad07d753	448c773c
50	448c773c					ca400538	8ecc7204
51	8ecc7204					8fcc5006	01002202

A.3 Expansion of a 256-bit Cipher Key

This section contains the key expansion of the following cipher key:

Cipher Key = **60 3d eb 10 15 ca 71 be 2b 73 ae f0 85 7d 77 81**
1f 35 2c 07 3b 61 08 d7 2d 98 10 a3 09 14 df f4

for $Nk = 8$, which results in

$w_0 = \mathbf{603deb10}$ $w_1 = \mathbf{15ca71be}$ $w_2 = \mathbf{2b73aef0}$ $w_3 = \mathbf{857d7781}$
 $w_4 = \mathbf{1f352c07}$ $w_5 = \mathbf{3b6108d7}$ $w_6 = \mathbf{2d9810a3}$ $w_7 = \mathbf{0914dff4}$

i (dec)	temp	After RotWord()	After SubWord()	Rcon[i/Nk]	After XOR with Rcon	w[i-Nk]	w[i]= temp XOR w[i-Nk]
8	0914dff4	14dff409	fa9ebf01	01000000	fb9ebf01	603deb10	9ba35411
9	9ba35411					15ca71be	8e6925af
10	8e6925af					2b73aef0	a51a8b5f
11	a51a8b5f					857d7781	2067fcde
12	2067fcde		b785b01d			1f352c07	a8b09c1a
13	a8b09c1a					3b6108d7	93d194cd
14	93d194cd					2d9810a3	be49846e
15	be49846e					0914dff4	b75d5b9a
16	b75d5b9a	5d5b9ab7	4c39b8a9	02000000	4e39b8a9	9ba35411	d59aecb8
17	d59aecb8					8e6925af	5bf3c917
18	5bf3c917					a51a8b5f	fee94248
19	fee94248					2067fcde	de8ebe96
20	de8ebe96		1d19ae90			a8b09c1a	b5a9328a
21	b5a9328a					93d194cd	2678a647
22	2678a647					be49846e	98312229

23	98312229					b75d5b9a	2f6c79b3
24	2f6c79b3	6c79b32f	50b66d15	04000000	54b66d15	d59aecb8	812c81ad
25	812c81ad					5bf3c917	dadf48ba
26	dadf48ba					fee94248	24360af2
27	24360af2					de8ebe96	fab8b464
28	fab8b464		2d6c8d43			b5a9328a	98c5bfc9
29	98c5bfc9					2678a647	bebd198e
30	bebd198e					98312229	268c3ba7
31	268c3ba7					2f6c79b3	09e04214
32	09e04214	e0421409	e12cfa01	08000000	e92cfa01	812c81ad	68007bac
33	68007bac					dadf48ba	b2df3316
34	b2df3316					24360af2	96e939e4
35	96e939e4					fab8b464	6c518d80
36	6c518d80		50d15dcd			98c5bfc9	c814e204
37	c814e204					bebd198e	76a9fb8a
38	76a9fb8a					268c3ba7	5025c02d
39	5025c02d					09e04214	59c58239
40	59c58239	c5823959	a61312cb	10000000	b61312cb	68007bac	de136967
41	de136967					b2df3316	6ccc5a71
42	6ccc5a71					96e939e4	fa256395
43	fa256395					6c518d80	9674ee15
44	9674ee15		90922859			c814e204	5886ca5d
45	5886ca5d					76a9fb8a	2e2f31d7
46	2e2f31d7					5025c02d	7e0af1fa
47	7e0af1fa					59c58239	27cf73c3
48	27cf73c3	cf73c327	8a8f2ecc	20000000	aa8f2ecc	de136967	749c47ab
49	749c47ab					6ccc5a71	18501dda
50	18501dda					fa256395	e2757e4f
51	e2757e4f					9674ee15	7401905a
52	7401905a		927c60be			5886ca5d	cafaaae3
53	cafaaae3					2e2f31d7	e4d59b34
54	e4d59b34					7e0af1fa	9adf6ace
55	9adf6ace					27cf73c3	bd10190d
56	bd10190d	10190dbd	cad4d77a	40000000	8ad4d77a	749c47ab	fe4890d1
57	fe4890d1					18501dda	e6188d0b

58	e6188d0b					e2757e4f	046df344
59	046df344					7401905a	706c631e

Appendix B – Cipher Example

The following diagram shows the values in the State array as the Cipher progresses for a block length and a Cipher Key length of 16 bytes each (i.e., $Nb = 4$ and $Nk = 4$).

Input = 32 43 f6 a8 88 5a 30 8d 31 31 98 a2 e0 37 07 34

Cipher Key = 2b 7e 15 16 28 ae d2 a6 ab f7 15 88 09 cf 4f 3c

The Round Key values are taken from the Key Expansion example in Appendix A.

Round Number	Start of Round	After SubBytes	After ShiftRows	After MixColumns	Round Key Value																																																																																	
input	<table><tr><td>32</td><td>88</td><td>31</td><td>e0</td></tr><tr><td>43</td><td>5a</td><td>31</td><td>37</td></tr><tr><td>f6</td><td>30</td><td>98</td><td>07</td></tr><tr><td>a8</td><td>8d</td><td>a2</td><td>34</td></tr></table>	32	88	31	e0	43	5a	31	37	f6	30	98	07	a8	8d	a2	34	<table><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr></table>																	<table><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr></table>																	<table><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr></table>																	<table><tr><td>2b</td><td>28</td><td>ab</td><td>09</td></tr><tr><td>7e</td><td>ae</td><td>f7</td><td>cf</td></tr><tr><td>15</td><td>d2</td><td>15</td><td>4f</td></tr><tr><td>16</td><td>a6</td><td>88</td><td>3c</td></tr></table> $\oplus$	2b	28	ab	09	7e	ae	f7	cf	15	d2	15	4f	16	a6	88	3c	=
	32	88	31	e0																																																																																		
	43	5a	31	37																																																																																		
	f6	30	98	07																																																																																		
a8	8d	a2	34																																																																																			
2b	28	ab	09																																																																																			
7e	ae	f7	cf																																																																																			
15	d2	15	4f																																																																																			
16	a6	88	3c																																																																																			
1	<table><tr><td>19</td><td>a0</td><td>9a</td><td>e9</td></tr><tr><td>3d</td><td>f4</td><td>c6</td><td>f8</td></tr><tr><td>e3</td><td>e2</td><td>8d</td><td>48</td></tr><tr><td>be</td><td>2b</td><td>2a</td><td>08</td></tr></table>	19	a0	9a	e9	3d	f4	c6	f8	e3	e2	8d	48	be	2b	2a	08	<table><tr><td>d4</td><td>e0</td><td>b8</td><td>1e</td></tr><tr><td>27</td><td>bf</td><td>b4</td><td>41</td></tr><tr><td>11</td><td>98</td><td>5d</td><td>52</td></tr><tr><td>ae</td><td>f1</td><td>e5</td><td>30</td></tr></table>	d4	e0	b8	1e	27	bf	b4	41	11	98	5d	52	ae	f1	e5	30	<table><tr><td>d4</td><td>e0</td><td>b8</td><td>1e</td></tr><tr><td>bf</td><td>b4</td><td>41</td><td>27</td></tr><tr><td>5d</td><td>52</td><td>11</td><td>98</td></tr><tr><td>30</td><td>ae</td><td>f1</td><td>e5</td></tr></table>	d4	e0	b8	1e	bf	b4	41	27	5d	52	11	98	30	ae	f1	e5	<table><tr><td>04</td><td>e0</td><td>48</td><td>28</td></tr><tr><td>66</td><td>cb</td><td>f8</td><td>06</td></tr><tr><td>81</td><td>19</td><td>d3</td><td>26</td></tr><tr><td>e5</td><td>9a</td><td>7a</td><td>4c</td></tr></table> $\oplus$	04	e0	48	28	66	cb	f8	06	81	19	d3	26	e5	9a	7a	4c	= <table><tr><td>a0</td><td>88</td><td>23</td><td>2a</td></tr><tr><td>fa</td><td>54</td><td>a3</td><td>6c</td></tr><tr><td>fe</td><td>2c</td><td>39</td><td>76</td></tr><tr><td>17</td><td>b1</td><td>39</td><td>05</td></tr></table>	a0	88	23	2a	fa	54	a3	6c	fe	2c	39	76	17	b1	39	05	
	19	a0	9a	e9																																																																																		
	3d	f4	c6	f8																																																																																		
	e3	e2	8d	48																																																																																		
be	2b	2a	08																																																																																			
d4	e0	b8	1e																																																																																			
27	bf	b4	41																																																																																			
11	98	5d	52																																																																																			
ae	f1	e5	30																																																																																			
d4	e0	b8	1e																																																																																			
bf	b4	41	27																																																																																			
5d	52	11	98																																																																																			
30	ae	f1	e5																																																																																			
04	e0	48	28																																																																																			
66	cb	f8	06																																																																																			
81	19	d3	26																																																																																			
e5	9a	7a	4c																																																																																			
a0	88	23	2a																																																																																			
fa	54	a3	6c																																																																																			
fe	2c	39	76																																																																																			
17	b1	39	05																																																																																			
2	<table><tr><td>a4</td><td>68</td><td>6b</td><td>02</td></tr><tr><td>9c</td><td>9f</td><td>5b</td><td>6a</td></tr><tr><td>7f</td><td>35</td><td>ea</td><td>50</td></tr><tr><td>f2</td><td>2b</td><td>43</td><td>49</td></tr></table>	a4	68	6b	02	9c	9f	5b	6a	7f	35	ea	50	f2	2b	43	49	<table><tr><td>49</td><td>45</td><td>7f</td><td>77</td></tr><tr><td>de</td><td>db</td><td>39</td><td>02</td></tr><tr><td>d2</td><td>96</td><td>87</td><td>53</td></tr><tr><td>89</td><td>f1</td><td>1a</td><td>3b</td></tr></table>	49	45	7f	77	de	db	39	02	d2	96	87	53	89	f1	1a	3b	<table><tr><td>49</td><td>45</td><td>7f</td><td>77</td></tr><tr><td>db</td><td>39</td><td>02</td><td>de</td></tr><tr><td>87</td><td>53</td><td>d2</td><td>96</td></tr><tr><td>3b</td><td>89</td><td>f1</td><td>1a</td></tr></table>	49	45	7f	77	db	39	02	de	87	53	d2	96	3b	89	f1	1a	<table><tr><td>58</td><td>1b</td><td>db</td><td>1b</td></tr><tr><td>4d</td><td>4b</td><td>e7</td><td>6b</td></tr><tr><td>ca</td><td>5a</td><td>ca</td><td>b0</td></tr><tr><td>f1</td><td>ac</td><td>a8</td><td>e5</td></tr></table> $\oplus$	58	1b	db	1b	4d	4b	e7	6b	ca	5a	ca	b0	f1	ac	a8	e5	= <table><tr><td>f2</td><td>7a</td><td>59</td><td>73</td></tr><tr><td>c2</td><td>96</td><td>35</td><td>59</td></tr><tr><td>95</td><td>b9</td><td>80</td><td>f6</td></tr><tr><td>f2</td><td>43</td><td>7a</td><td>7f</td></tr></table>	f2	7a	59	73	c2	96	35	59	95	b9	80	f6	f2	43	7a	7f	
	a4	68	6b	02																																																																																		
	9c	9f	5b	6a																																																																																		
	7f	35	ea	50																																																																																		
f2	2b	43	49																																																																																			
49	45	7f	77																																																																																			
de	db	39	02																																																																																			
d2	96	87	53																																																																																			
89	f1	1a	3b																																																																																			
49	45	7f	77																																																																																			
db	39	02	de																																																																																			
87	53	d2	96																																																																																			
3b	89	f1	1a																																																																																			
58	1b	db	1b																																																																																			
4d	4b	e7	6b																																																																																			
ca	5a	ca	b0																																																																																			
f1	ac	a8	e5																																																																																			
f2	7a	59	73																																																																																			
c2	96	35	59																																																																																			
95	b9	80	f6																																																																																			
f2	43	7a	7f																																																																																			
3	<table><tr><td>aa</td><td>61</td><td>82</td><td>68</td></tr><tr><td>8f</td><td>dd</td><td>d2</td><td>32</td></tr><tr><td>5f</td><td>e3</td><td>4a</td><td>46</td></tr><tr><td>03</td><td>ef</td><td>d2</td><td>9a</td></tr></table>	aa	61	82	68	8f	dd	d2	32	5f	e3	4a	46	03	ef	d2	9a	<table><tr><td>ac</td><td>ef</td><td>13</td><td>45</td></tr><tr><td>73</td><td>c1</td><td>b5</td><td>23</td></tr><tr><td>cf</td><td>11</td><td>d6</td><td>5a</td></tr><tr><td>7b</td><td>df</td><td>b5</td><td>b8</td></tr></table>	ac	ef	13	45	73	c1	b5	23	cf	11	d6	5a	7b	df	b5	b8	<table><tr><td>ac</td><td>ef</td><td>13</td><td>45</td></tr><tr><td>c1</td><td>b5</td><td>23</td><td>73</td></tr><tr><td>d6</td><td>5a</td><td>cf</td><td>11</td></tr><tr><td>b8</td><td>7b</td><td>df</td><td>b5</td></tr></table>	ac	ef	13	45	c1	b5	23	73	d6	5a	cf	11	b8	7b	df	b5	<table><tr><td>75</td><td>20</td><td>53</td><td>bb</td></tr><tr><td>ec</td><td>0b</td><td>c0</td><td>25</td></tr><tr><td>09</td><td>63</td><td>cf</td><td>d0</td></tr><tr><td>93</td><td>33</td><td>7c</td><td>dc</td></tr></table> $\oplus$	75	20	53	bb	ec	0b	c0	25	09	63	cf	d0	93	33	7c	dc	= <table><tr><td>3d</td><td>47</td><td>1e</td><td>6d</td></tr><tr><td>80</td><td>16</td><td>23</td><td>7a</td></tr><tr><td>47</td><td>fe</td><td>7e</td><td>88</td></tr><tr><td>7d</td><td>3e</td><td>44</td><td>3b</td></tr></table>	3d	47	1e	6d	80	16	23	7a	47	fe	7e	88	7d	3e	44	3b	
	aa	61	82	68																																																																																		
	8f	dd	d2	32																																																																																		
	5f	e3	4a	46																																																																																		
03	ef	d2	9a																																																																																			
ac	ef	13	45																																																																																			
73	c1	b5	23																																																																																			
cf	11	d6	5a																																																																																			
7b	df	b5	b8																																																																																			
ac	ef	13	45																																																																																			
c1	b5	23	73																																																																																			
d6	5a	cf	11																																																																																			
b8	7b	df	b5																																																																																			
75	20	53	bb																																																																																			
ec	0b	c0	25																																																																																			
09	63	cf	d0																																																																																			
93	33	7c	dc																																																																																			
3d	47	1e	6d																																																																																			
80	16	23	7a																																																																																			
47	fe	7e	88																																																																																			
7d	3e	44	3b																																																																																			
4	<table><tr><td>48</td><td>67</td><td>4d</td><td>d6</td></tr><tr><td>6c</td><td>1d</td><td>e3</td><td>5f</td></tr><tr><td>4e</td><td>9d</td><td>b1</td><td>58</td></tr><tr><td>ee</td><td>0d</td><td>38</td><td>e7</td></tr></table>	48	67	4d	d6	6c	1d	e3	5f	4e	9d	b1	58	ee	0d	38	e7	<table><tr><td>52</td><td>85</td><td>e3</td><td>f6</td></tr><tr><td>50</td><td>a4</td><td>11</td><td>cf</td></tr><tr><td>2f</td><td>5e</td><td>c8</td><td>6a</td></tr><tr><td>28</td><td>d7</td><td>07</td><td>94</td></tr></table>	52	85	e3	f6	50	a4	11	cf	2f	5e	c8	6a	28	d7	07	94	<table><tr><td>52</td><td>85</td><td>e3</td><td>f6</td></tr><tr><td>a4</td><td>11</td><td>cf</td><td>50</td></tr><tr><td>c8</td><td>6a</td><td>2f</td><td>5e</td></tr><tr><td>94</td><td>28</td><td>d7</td><td>07</td></tr></table>	52	85	e3	f6	a4	11	cf	50	c8	6a	2f	5e	94	28	d7	07	<table><tr><td>0f</td><td>60</td><td>6f</td><td>5e</td></tr><tr><td>d6</td><td>31</td><td>c0</td><td>b3</td></tr><tr><td>da</td><td>38</td><td>10</td><td>13</td></tr><tr><td>a9</td><td>bf</td><td>6b</td><td>01</td></tr></table> $\oplus$	0f	60	6f	5e	d6	31	c0	b3	da	38	10	13	a9	bf	6b	01	= <table><tr><td>ef</td><td>a8</td><td>b6</td><td>db</td></tr><tr><td>44</td><td>52</td><td>71</td><td>0b</td></tr><tr><td>a5</td><td>5b</td><td>25</td><td>ad</td></tr><tr><td>41</td><td>7f</td><td>3b</td><td>00</td></tr></table>	ef	a8	b6	db	44	52	71	0b	a5	5b	25	ad	41	7f	3b	00	
	48	67	4d	d6																																																																																		
	6c	1d	e3	5f																																																																																		
	4e	9d	b1	58																																																																																		
ee	0d	38	e7																																																																																			
52	85	e3	f6																																																																																			
50	a4	11	cf																																																																																			
2f	5e	c8	6a																																																																																			
28	d7	07	94																																																																																			
52	85	e3	f6																																																																																			
a4	11	cf	50																																																																																			
c8	6a	2f	5e																																																																																			
94	28	d7	07																																																																																			
0f	60	6f	5e																																																																																			
d6	31	c0	b3																																																																																			
da	38	10	13																																																																																			
a9	bf	6b	01																																																																																			
ef	a8	b6	db																																																																																			
44	52	71	0b																																																																																			
a5	5b	25	ad																																																																																			
41	7f	3b	00																																																																																			
5	<table><tr><td>e0</td><td>c8</td><td>d9</td><td>85</td></tr><tr><td>92</td><td>63</td><td>b1</td><td>b8</td></tr><tr><td>7f</td><td>63</td><td>35</td><td>be</td></tr><tr><td>e8</td><td>c0</td><td>50</td><td>01</td></tr></table>	e0	c8	d9	85	92	63	b1	b8	7f	63	35	be	e8	c0	50	01	<table><tr><td>e1</td><td>e8</td><td>35</td><td>97</td></tr><tr><td>4f</td><td>fb</td><td>c8</td><td>6c</td></tr><tr><td>d2</td><td>fb</td><td>96</td><td>ae</td></tr><tr><td>9b</td><td>ba</td><td>53</td><td>7c</td></tr></table>	e1	e8	35	97	4f	fb	c8	6c	d2	fb	96	ae	9b	ba	53	7c	<table><tr><td>e1</td><td>e8</td><td>35</td><td>97</td></tr><tr><td>fb</td><td>c8</td><td>6c</td><td>4f</td></tr><tr><td>96</td><td>ae</td><td>d2</td><td>fb</td></tr><tr><td>7c</td><td>9b</td><td>ba</td><td>53</td></tr></table>	e1	e8	35	97	fb	c8	6c	4f	96	ae	d2	fb	7c	9b	ba	53	<table><tr><td>25</td><td>bd</td><td>b6</td><td>4c</td></tr><tr><td>d1</td><td>11</td><td>3a</td><td>4c</td></tr><tr><td>a9</td><td>d1</td><td>33</td><td>c0</td></tr><tr><td>ad</td><td>68</td><td>8e</td><td>b0</td></tr></table> $\oplus$	25	bd	b6	4c	d1	11	3a	4c	a9	d1	33	c0	ad	68	8e	b0	= <table><tr><td>d4</td><td>7c</td><td>ca</td><td>11</td></tr><tr><td>d1</td><td>83</td><td>f2</td><td>f9</td></tr><tr><td>c6</td><td>9d</td><td>b8</td><td>15</td></tr><tr><td>f8</td><td>87</td><td>bc</td><td>bc</td></tr></table>	d4	7c	ca	11	d1	83	f2	f9	c6	9d	b8	15	f8	87	bc	bc	
	e0	c8	d9	85																																																																																		
	92	63	b1	b8																																																																																		
	7f	63	35	be																																																																																		
e8	c0	50	01																																																																																			
e1	e8	35	97																																																																																			
4f	fb	c8	6c																																																																																			
d2	fb	96	ae																																																																																			
9b	ba	53	7c																																																																																			
e1	e8	35	97																																																																																			
fb	c8	6c	4f																																																																																			
96	ae	d2	fb																																																																																			
7c	9b	ba	53																																																																																			
25	bd	b6	4c																																																																																			
d1	11	3a	4c																																																																																			
a9	d1	33	c0																																																																																			
ad	68	8e	b0																																																																																			
d4	7c	ca	11																																																																																			
d1	83	f2	f9																																																																																			
c6	9d	b8	15																																																																																			
f8	87	bc	bc																																																																																			

6

f1	c1	7c	5d
00	92	c8	b5
6f	4c	8b	d5
55	ef	32	0c

a1	78	10	4c
63	4f	e8	d5
a8	29	3d	03
fc	df	23	fe

a1	78	10	4c
4f	e8	d5	63
3d	03	a8	29
fe	fc	df	23

4b	2c	33	37
86	4a	9d	d2
8d	89	f4	18
6d	80	e8	d8

 $\oplus$

6d	11	db	ca
88	0b	f9	00
a3	3e	86	93
7a	fd	41	fd

=

7

26	3d	e8	fd
0e	41	64	d2
2e	b7	72	8b
17	7d	a9	25

f7	27	9b	54
ab	83	43	b5
31	a9	40	3d
f0	ff	d3	3f

f7	27	9b	54
83	43	b5	ab
40	3d	31	a9
3f	f0	ff	d3

14	46	27	34
15	16	46	2a
b5	15	56	d8
bf	ec	d7	43

 $\oplus$

4e	5f	84	4e
54	5f	a6	a6
f7	c9	4f	dc
0e	f3	b2	4f

=

8

5a	19	a3	7a
41	49	e0	8c
42	dc	19	04
b1	1f	65	0c

be	d4	0a	da
83	3b	e1	64
2c	86	d4	f2
c8	c0	4d	fe

be	d4	0a	da
3b	e1	64	83
d4	f2	2c	86
fe	c8	c0	4d

00	b1	54	fa
51	c8	76	1b
2f	89	6d	99
d1	ff	cd	ea

 $\oplus$

ea	b5	31	7f
d2	8d	2b	8d
73	ba	f5	29
21	d2	60	2f

=

9

ea	04	65	85
83	45	5d	96
5c	33	98	b0
f0	2d	ad	c5

87	f2	4d	97
ec	6e	4c	90
4a	c3	46	e7
8c	d8	95	a6

87	f2	4d	97
6e	4c	90	ec
46	e7	4a	c3
a6	8c	d8	95

47	40	a3	4c
37	d4	70	9f
94	e4	3a	42
ed	a5	a6	bc

 $\oplus$

ac	19	28	57
77	fa	d1	5c
66	dc	29	00
f3	21	41	6e

=

10

eb	59	8b	1b
40	2e	a1	c3
f2	38	13	42
1e	84	e7	d2

e9	cb	3d	af
09	31	32	2e
89	07	7d	2c
72	5f	94	b5

e9	cb	3d	af
31	32	2e	09
7d	2c	89	07
b5	72	5f	94

 $\oplus$

d0	c9	e1	b6
14	ee	3f	63
f9	25	0c	0c
a8	89	c8	a6

=

output

39	02	dc	19
25	dc	11	6a
84	09	85	0b
1d	fb	97	32

Appendix C – Example Vectors

This appendix contains example vectors, including intermediate values – for all three AES key lengths ($Nk = 4, 6$, and 8), for the Cipher, Inverse Cipher, and Equivalent Inverse Cipher that are described in Sec. 5.1, 5.3, and 5.3.5, respectively. Additional examples may be found at [1] and [5].

All vectors are in hexadecimal notation, with each pair of characters giving a byte value in which the left character of each pair provides the bit pattern for the 4 bit group containing the higher numbered bits using the notation explained in Sec. 3.2, while the right character provides the bit pattern for the lower-numbered bits. The array index for all bytes (groups of two hexadecimal digits) within these test vectors starts at zero and increases from left to right.

Legend for CIPHER (ENCRYPT) (round number $r = 0$ to $10, 12$ or 14):

input: cipher input
start: state at start of round[r]
s_box: state after SubBytes()
s_row: state after ShiftRows()
m_col: state after MixColumns()
k_sch: key schedule value for round[r]
output: cipher output

Legend for INVERSE CIPHER (DECRYPT) (round number $r = 0$ to $10, 12$ or 14):

iinput: inverse cipher input
istart: state at start of round[r]
is_box: state after InvSubBytes()
is_row: state after InvShiftRows()
ik_sch: key schedule value for round[r]
ik_add: state after AddRoundKey()
ioutput: inverse cipher output

Legend for EQUIVALENT INVERSE CIPHER (DECRYPT) (round number $r = 0$ to $10, 12$ or 14):

iinput: inverse cipher input
istart: state at start of round[r]
is_box: state after InvSubBytes()
is_row: state after InvShiftRows()
im_col: state after InvMixColumns()
ik_sch: key schedule value for round[r]
ioutput: inverse cipher output

C.1 AES-128 ($Nk=4, Nr=10$)

PLAINTEXT: 00112233445566778899aabbccddeeff
KEY: 000102030405060708090a0b0c0d0e0f

CIPHER (ENCRYPT):

```

round[ 0].input      00112233445566778899aabbccddeeff
round[ 0].k_sch      000102030405060708090a0b0c0d0e0f
round[ 1].start      00102030405060708090a0b0c0d0e0f0
round[ 1].s_box      63cab7040953d051cd60e0e7ba70e18c
round[ 1].s_row      6353e08c0960e104cd70b751bacad0e7
round[ 1].m_col      5f72641557f5bc92f7be3b291db9f91a
round[ 1].k_sch      d6aa74fdd2af72fadaa678f1d6ab76fe
round[ 2].start      89d810e8855ace682d1843d8cb128fe4
round[ 2].s_box      a761ca9b97be8b45d8ad1a611fc97369
round[ 2].s_row      7fbe1a6997ad739bd8c9ca451f618b61
round[ 2].m_col      ff87968431d86a51645151fa773ad009
round[ 2].k_sch      b692cf0b643dbdf1be9bc5006830b3fe
round[ 3].start      4915598f55e5d7a0daca94fa1f0a63f7
round[ 3].s_box      3b59cb73fcd90ee05774222dc067fb68
round[ 3].s_row      3bd92268fc74fb735767cbe0c0590e2d
round[ 3].m_col      4c9c1e66f771f0762c3f868e534df256
round[ 3].k_sch      b6ff744ed2c2c9bf6c590cbf0469bf41
round[ 4].start      fa636a2825b339c940668a3157244d17
round[ 4].s_box      2dfb02343f6d12dd09337ec75b36e3f0
round[ 4].s_row      2d6d7ef03f33e334093602dd5bfb12c7
round[ 4].m_col      6385b79ffc538df997be478e7547d691
round[ 4].k_sch      47f7f7bc95353e03f96c32bcfd058dfd
round[ 5].start      247240236966b3fa6ed2753288425b6c
round[ 5].s_box      36400926f9336d2d9fb59d23c42c3950
round[ 5].s_row      36339d50f9b539269f2c092dc4406d23
round[ 5].m_col      f4bcd45432e554d075f1d6c51dd03b3c
round[ 5].k_sch      3caaa3e8a99f9deb50f3af57adf622aa
round[ 6].start      c81677bc9b7ac93b25027992b0261996
round[ 6].s_box      e847f56514dadde23f77b64fe7f7d490
round[ 6].s_row      e8dab6901477d4653fff7f5e2e747dd4f
round[ 6].m_col      9816ee7400f87f556b2c049c8e5ad036
round[ 6].k_sch      5e390f7df7a69296a7553dc10aa31f6b
round[ 7].start      c62fe109f75eedc3cc79395d84f9cf5d
round[ 7].s_box      b415f8016858552e4bb6124c5f998a4c
round[ 7].s_row      b458124c68b68a014b99f82e5f15554c
round[ 7].m_col      c57e1c159a9bd286f05f4be098c63439
round[ 7].k_sch      14f9701ae35fe28c440adf4d4ea9c026
round[ 8].start      d1876c0f79c4300ab45594add66ff41f
round[ 8].s_box      3e175076b61c04678dfc2295f6a8bfc0
round[ 8].s_row      3e1c22c0b6fcbf768da85067f6170495
round[ 8].m_col      baa03de7a1f9b56ed5512cba5f414d23
round[ 8].k_sch      47438735a41c65b9e016baf4aebf7ad2
round[ 9].start      fde3bad205e5d0d73547964ef1fe37f1
round[ 9].s_box      5411f4b56bd9700e96a0902fa1bb9aa1
round[ 9].s_row      54d990a16ba09ab596bbf40ea111702f
round[ 9].m_col      e9f74eec023020f61bf2ccf2353c21c7
round[ 9].k_sch      549932d1f08557681093ed9cbe2c974e
round[10].start      bd6e7c3df2b5779e0b61216e8b10b689
round[10].s_box      7a9f102789d5f50b2beffd9f3dca4ea7
round[10].s_row      7ad5fda789ef4e272bca100b3d9ff59f
round[10].k_sch      13111d7fe3944a17f307a78b4d2b30c5
round[10].output     69c4e0d86a7b0430d8cdb78070b4c55a

```

INVERSE CIPHER (DECRYPT):

```

round[ 0].iinput      69c4e0d86a7b0430d8cdb78070b4c55a
round[ 0].ik_sch      13111d7fe3944a17f307a78b4d2b30c5
round[ 1].istart      7ad5fda789ef4e272bca100b3d9ff59f

```

```

round[ 1].is_row 7a9f102789d5f50b2beffd9f3dca4ea7
round[ 1].is_box bd6e7c3df2b5779e0b61216e8b10b689
round[ 1].ik_sch 549932d1f08557681093ed9cbe2c974e
round[ 1].ik_add e9f74eec023020f61bf2ccf2353c21c7
round[ 2].istart 54d990a16ba09ab596bbf40ea111702f
round[ 2].is_row 5411f4b56bd9700e96a0902fa1bb9aa1
round[ 2].is_box fde3bad205e5d0d73547964ef1fe37f1
round[ 2].ik_sch 47438735a41c65b9e016baf4aebf7ad2
round[ 2].ik_add baa03de7a1f9b56ed5512cba5f414d23
round[ 3].istart 3e1c22c0b6fcbf768da85067f6170495
round[ 3].is_row 3e175076b61c04678dfc2295f6a8bfc0
round[ 3].is_box d1876c0f79c4300ab45594add66ff41f
round[ 3].ik_sch 14f9701ae35fe28c440adf4d4ea9c026
round[ 3].ik_add c57e1c159a9bd286f05f4be098c63439
round[ 4].istart b458124c68b68a014b99f82e5f15554c
round[ 4].is_row b415f8016858552e4bb6124c5f998a4c
round[ 4].is_box c62fe109f75eedc3cc79395d84f9cf5d
round[ 4].ik_sch 5e390f7df7a69296a7553dc10aa31f6b
round[ 4].ik_add 9816ee7400f87f556b2c049c8e5ad036
round[ 5].istart e8dab6901477d4653ff7f5e2e747dd4f
round[ 5].is_row e847f56514dadde23f77b64fe7f7d490
round[ 5].is_box c81677bc9b7ac93b25027992b0261996
round[ 5].ik_sch 3caaa3e8a99f9deb50f3af57adf622aa
round[ 5].ik_add f4bcd45432e554d075f1d6c51dd03b3c
round[ 6].istart 36339d50f9b539269f2c092dc4406d23
round[ 6].is_row 36400926f9336d2d9fb59d23c42c3950
round[ 6].is_box 247240236966b3fa6ed2753288425b6c
round[ 6].ik_sch 47f7f7bc95353e03f96c32bcfd058dfd
round[ 6].ik_add 6385b79ffc538df997be478e7547d691
round[ 7].istart 2d6d7ef03f33e334093602dd5bfb12c7
round[ 7].is_row 2dfb02343f6d12dd09337ec75b36e3f0
round[ 7].is_box fa636a2825b339c940668a3157244d17
round[ 7].ik_sch b6ff744ed2c2c9bf6c590cbf0469bf41
round[ 7].ik_add 4c9c1e66f771f0762c3f868e534df256
round[ 8].istart 3bd92268fc74fb735767cbe0c0590e2d
round[ 8].is_row 3b59cb73fcd90ee05774222dc067fb68
round[ 8].is_box 4915598f55e5d7a0daca94fa1f0a63f7
round[ 8].ik_sch b692cf0b643dbdf1be9bc5006830b3fe
round[ 8].ik_add ff87968431d86a51645151fa773ad009
round[ 9].istart a7be1a6997ad739bd8c9ca451f618b61
round[ 9].is_row a761ca9b97be8b45d8ad1a611fc97369
round[ 9].is_box 89d810e8855ace682d1843d8cb128fe4
round[ 9].ik_sch d6aa74fdd2af72fadaa678f1d6ab76fe
round[ 9].ik_add 5f72641557f5bc92f7be3b291db9f91a
round[10].istart 6353e08c0960e104cd70b751bacad0e7
round[10].is_row 63cab7040953d051cd60e0e7ba70e18c
round[10].is_box 00102030405060708090a0b0c0d0e0f0
round[10].ik_sch 000102030405060708090a0b0c0d0e0f
round[10].ioutput 00112233445566778899aabbccddeeff

```

EQUIVALENT INVERSE CIPHER (DECRYPT):

```

round[ 0].iinput 69c4e0d86a7b0430d8cdb78070b4c55a
round[ 0].ik_sch 13111d7fe3944a17f307a78b4d2b30c5
round[ 1].istart 7ad5fda789ef4e272bca100b3d9ff59f
round[ 1].is_box bdb52189f261b63d0b107c9e8b6e776e
round[ 1].is_row bd6e7c3df2b5779e0b61216e8b10b689
round[ 1].im_col 4773b91ff72f354361cb018ea1e6cf2c

```

```

round[ 1].ik_sch 13aa29be9c8faff6f770f58000f7bf03
round[ 2].istart 54d990a16ba09ab596bbf40ea111702f
round[ 2].is_box fde596f1054737d235febad7f1e3d04e
round[ 2].is_row fde3bad205e5d0d73547964ef1fe37f1
round[ 2].im_col 2d7e86a339d9393ee6570a1101904e16
round[ 2].ik_sch 1362a4638f2586486bff5a76f7874a83
round[ 3].istart 3e1c22c0b6fcbf768da85067f6170495
round[ 3].is_box d1c4941f7955f40fb46f6c0ad68730ad
round[ 3].is_row d1876c0f79c4300ab45594add66ff41f
round[ 3].im_col 39daee38f4f1a82aaf432410c36d45b9
round[ 3].ik_sch 8d82fc749c47222be4dad3e9c7810f5
round[ 4].istart b458124c68b68a014b99f82e5f15554c
round[ 4].is_box c65e395df779cf09ccf9e1c3842fed5d
round[ 4].is_row c62fe109f75eedc3cc79395d84f9cf5d
round[ 4].im_col 9a39bf1d05b20a3a476a0bf79fe51184
round[ 4].ik_sch 72e3098d11c5de5f789dfe1578a2cccb
round[ 5].istart e8dab6901477d4653ff7f5e2e747dd4f
round[ 5].is_box c87a79969b0219bc2526773bb016c992
round[ 5].is_row c81677bc9b7ac93b25027992b0261996
round[ 5].im_col 18f78d779a93eef4f6742967c47f5ffd
round[ 5].ik_sch 2ec410276326d7d26958204a003f32de
round[ 6].istart 36339d50f9b539269f2c092dc4406d23
round[ 6].is_box 2466756c69d25b236e4240fa8872b332
round[ 6].is_row 247240236966b3fa6ed2753288425b6c
round[ 6].im_col 85cf8bf472d124c10348f545329c0053
round[ 6].ik_sch a8a2f5044de2c7f50a7ef79869671294
round[ 7].istart 2d6d7ef03f33e334093602dd5bfb12c7
round[ 7].is_box fab38a1725664d2840246ac957633931
round[ 7].is_row fa636a2825b339c940668a3157244d17
round[ 7].im_col fc1fc1f91934c98210fbfb8da340eb21
round[ 7].ik_sch c7c6e391e54032f1479c306d6319e50c
round[ 8].istart 3bd92268fc74fb735767cbe0c0590e2d
round[ 8].is_box 49e594f755ca638fda0a59a01f15d7fa
round[ 8].is_row 4915598f55e5d7a0daca94fa1f0a63f7
round[ 8].im_col 076518f0b52ba2fb7a15c8d93be45e00
round[ 8].ik_sch a0db02992286d160a2dc029c2485d561
round[ 9].istart a7be1a6997ad739bd8c9ca451f618b61
round[ 9].is_box 895a43e485188fe82d121068cbd8ced8
round[ 9].is_row 89d810e8855ace682d1843d8ch128fe4
round[ 9].im_col ef053f7c8b3d32fd4d2a64ad3c93071a
round[ 9].ik_sch 8c56dff0825dd3f9805ad3fc8659d7fd
round[10].istart 6353e08c0960e104cd70b751bacad0e7
round[10].is_box 0050a0f04090e03080d02070c01060b0
round[10].is_row 00102030405060708090a0b0c0d0e0f0
round[10].ik_sch 000102030405060708090a0b0c0d0e0f
round[10].ioutput 00112233445566778899aabbccddeeff

```

C.2 AES-192 ($N_k=6$, $N_r=12$)

PLAINTEXT: 00112233445566778899aabbccddeeff
 KEY: 000102030405060708090a0b0c0d0e0f1011121314151617

CIPHER (ENCRYPT):
 round[0].input 00112233445566778899aabbccddeeff
 round[0].k_sch 000102030405060708090a0b0c0d0e0f
 round[1].start 00102030405060708090a0b0c0d0e0f0

round[1].s_box	63cab7040953d051cd60e0e7ba70e18c
round[1].s_row	6353e08c0960e104cd70b751bacad0e7
round[1].m_col	5f72641557f5bc92f7be3b291db9f91a
round[1].k_sch	10111213141516175846f2f95c43f4fe
round[2].start	4f63760643e0aa85aff8c9d041fa0de4
round[2].s_box	84fb386f1ae1ac977941dd70832dd769
round[2].s_row	84e1dd691a41d76f792d389783fbac70
round[2].m_col	9f487f794f955f662afc86abd7f1ab29
round[2].k_sch	544afef55847f0fa4856e2e95c43f4fe
round[3].start	cb02818c17d2af9c62aa64428bb25fd7
round[3].s_box	1f770c64f0b579deaaac432c3d37cf0e
round[3].s_row	1fb5430ef0accf64aa370cde3d77792c
round[3].m_col	b7a53ecbbf9d75a0c40efc79b674cc11
round[3].k_sch	40f949b31cbabd4d48f043b810b7b342
round[4].start	f75c7778a327c8ed8cfefbc1a6c37f53
round[4].s_box	684af5bc0acce85564bb0878242ed2ed
round[4].s_row	68cc08ed0abbd2bc642ef555244ae878
round[4].m_col	7a1e98bdacb6d1141a6944dd06eb2d3e
round[4].k_sch	58e151ab04a2a5557effb5416245080c
round[5].start	22ffc916a81474416496f19c64ae2532
round[5].s_box	9316dd47c2fa92834390a1de43e43f23
round[5].s_row	93faa123c2903f4743e4dd83431692de
round[5].m_col	aaa755b34cffe57cef6f98e1f01c13e6
round[5].k_sch	2ab54bb43a02f8f662e3a95d66410c08
round[6].start	80121e0776fd1d8a8d8c31bc965d1fee
round[6].s_box	cdc972c53854a47e5d64c765904cc028
round[6].s_row	cd54c7283864c0c55d4c727e90c9a465
round[6].m_col	921f748fd96e937d622d7725ba8ba50c
round[6].k_sch	f501857297448d7ebdf1c6ca87f33e3c
round[7].start	671ef1fd4e2a1e03dfdcb1ef3d789b30
round[7].s_box	8572a1542fe5727b9e86c8df27bc1404
round[7].s_row	85e5c8042f8614549ebca17b277272df
round[7].m_col	e913e7b18f507d4b227ef652758acbcc
round[7].k_sch	e510976183519b6934157c9ea351f1e0
round[8].start	0c0370d00c01e622166b8accd6db3a2c
round[8].s_box	fe7b5170fe7c8e93477f7e4bf6b98071
round[8].s_row	fe7c7e71fe7f807047b95193f67b8e4b
round[8].m_col	6cf5edf996eb0a069c4ef21cbfc25762
round[8].k_sch	1ea0372a995309167c439e77ff12051e
round[9].start	7255dad30fb80310e00d6c6b40d0527c
round[9].s_box	40fc5766766c7bcae1d7507f09700010
round[9].s_row	406c501076d70066e17057ca09fc7b7f
round[9].m_col	7478bcdce8a50b81d4327a9009188262
round[9].k_sch	dd7e0e887e2fff68608fc842f9dcc154
round[10].start	a906b254968af4e9b4bdb2d2f0c44336
round[10].s_box	d36f3720907ebf1e8d7a37b58c1c1a05
round[10].s_row	d37e3705907a1a208d1c371e8c6fbfb5
round[10].m_col	0d73cc2d8f6abe8b0cf2dd9bb83d422e
round[10].k_sch	859f5f237a8d5a3dc0c02952beefd63a
round[11].start	88ec930ef5e7e4b6cc32f4c906d29414
round[11].s_box	c4cedcabe694694e4b23bfdd6fb522fa
round[11].s_row	c494bffaef62322ab4bb5dc4e6fce69dd
round[11].m_col	71d720933b6d677dc00b8f28238e0fb7
round[11].k_sch	de601e7827bcdff2ca223800fd8aeda32
round[12].start	afb73eeb1cd1b85162280f27fb20d585
round[12].s_box	79a9b2e99c3e6cd1aa3476cc0fb70397
round[12].s_row	793e76979c3403e9aab7b2d10fa96ccc

```
round[12].k_sch      a4970a331a78dc09c418c271e3a41d5d
round[12].output     dda97ca4864cdfe06eaf70a0ec0d7191
```

INVERSE CIPHER (DECRYPT):

```
round[ 0].iinput      dda97ca4864cdfe06eaf70a0ec0d7191
round[ 0].ik_sch      a4970a331a78dc09c418c271e3a41d5d
round[ 1].istart      793e76979c3403e9aab7b2d10fa96ccc
round[ 1].is_row      79a9b2e99c3e6cd1aa3476cc0fb70397
round[ 1].is_box      afb73eeb1cd1b85162280f27fb20d585
round[ 1].ik_sch      de601e7827bcdff2ca223800fd8aeda32
round[ 1].ik_add      71d720933b6d677dc00b8f28238e0fb7
round[ 2].istart      c494bffae62322ab4bb5dc4e6fce69dd
round[ 2].is_row      c4cedcabe694694e4b23bfd6fb522fa
round[ 2].is_box      88ec930ef5e7e4b6cc32f4c906d29414
round[ 2].ik_sch      859f5f237a8d5a3dc0c02952beefd63a
round[ 2].ik_add      0d73cc2d8f6abe8b0cf2dd9bb83d422e
round[ 3].istart      d37e3705907a1a208d1c371e8c6fbfb5
round[ 3].is_row      d36f3720907ebf1e8d7a37b58c1c1a05
round[ 3].is_box      a906b254968af4e9b4bdb2d2f0c44336
round[ 3].ik_sch      dd7e0e887e2fff68608fc842f9dcc154
round[ 3].ik_add      7478bcdce8a50b81d4327a9009188262
round[ 4].istart      406c501076d70066e17057ca09fc7b7f
round[ 4].is_row      40fc5766766c7bcae1d7507f09700010
round[ 4].is_box      7255dad30fb80310e00d6c6b40d0527c
round[ 4].ik_sch      1ea0372a995309167c439e77ff12051e
round[ 4].ik_add      6cf5edf996eb0a069c4ef21cbfc25762
round[ 5].istart      fe7c7e71fe7f807047b95193f67b8e4b
round[ 5].is_row      fe7b5170fe7c8e93477f7e4bf6b98071
round[ 5].is_box      0c0370d00c01e622166b8accd6db3a2c
round[ 5].ik_sch      e510976183519b6934157c9ea351f1e0
round[ 5].ik_add      e913e7b18f507d4b227ef652758achcc
round[ 6].istart      85e5c8042f8614549ebca17b277272df
round[ 6].is_row      8572a1542fe5727b9e86c8df27bc1404
round[ 6].is_box      671ef1fd4e2a1e03dfdcdb1ef3d789b30
round[ 6].ik_sch      f501857297448d7ebdf1c6ca87f33e3c
round[ 6].ik_add      921f748fd96e937d622d7725ba8ba50c
round[ 7].istart      cd54c7283864c0c55d4c727e90c9a465
round[ 7].is_row      cdc972c53854a47e5d64c765904cc028
round[ 7].is_box      80121e0776fd1d8a8d8c31bc965d1fee
round[ 7].ik_sch      2ab54bb43a02f8f662e3a95d66410c08
round[ 7].ik_add      aaa755b34cffe57cef6f98e1f01c13e6
round[ 8].istart      93faa123c2903f4743e4dd83431692de
round[ 8].is_row      9316dd47c2fa92834390a1de43e43f23
round[ 8].is_box      22ffc916a81474416496f19c64ae2532
round[ 8].ik_sch      58e151ab04a2a5557effb5416245080c
round[ 8].ik_add      7a1e98bdacb6d1141a6944dd06eb2d3e
round[ 9].istart      68cc08ed0abbd2bc642ef555244ae878
round[ 9].is_row      684af5bc0acce85564bb0878242ed2ed
round[ 9].is_box      f75c7778a327c8ed8cfefbc1a6c37f53
round[ 9].ik_sch      40f949b31cbabd4d48f043b810b7b342
round[ 9].ik_add      b7a53ecbbf9d75a0c40efc79b674cc11
round[10].istart      1fb5430ef0accf64aa370cde3d77792c
round[10].is_row      1f770c64f0b579deaaac432c3d37cf0e
round[10].is_box      cb02818c17d2af9c62aa64428bb25fd7
round[10].ik_sch      544afef55847f0fa4856e2e95c43f4fe
round[10].ik_add      9f487f794f955f662afc86abd7f1ab29
round[11].istart      84e1dd691a41d76f792d389783fbac70
```

```

round[11].is_row 84fb386f1ae1ac977941dd70832dd769
round[11].is_box 4f63760643e0aa85aff8c9d041fa0de4
round[11].ik_sch 10111213141516175846f2f95c43f4fe
round[11].ik_add 5f72641557f5bc92f7be3b291db9f91a
round[12].istart 6353e08c0960e104cd70b751bacad0e7
round[12].is_row 63cab7040953d051cd60e0e7ba70e18c
round[12].is_box 00102030405060708090a0b0c0d0e0f0
round[12].ik_sch 000102030405060708090a0b0c0d0e0f
round[12].ioutput 00112233445566778899aabbccddeeff

```

EQUIVALENT INVERSE CIPHER (DECRYPT):

```

round[ 0].iinput dda97ca4864cdfef06eaf70a0ec0d7191
round[ 0].ik_sch a4970a331a78dc09c418c271e3a41d5d
round[ 1].istart 793e76979c3403e9aab7b2d10fa96ccc
round[ 1].is_box afd10f851c28d5eb62203e51fbb7b827
round[ 1].is_row afb73eeb1cd1b85162280f27fb20d585
round[ 1].im_col 122a02f7242ac8e20605afce51cc7264
round[ 1].ik_sch d6bebd0dc209ea494db073803e021bb9
round[ 2].istart c494bffae62322ab4bb5dc4e6fce69dd
round[ 2].is_box 88e7f414f532940eccd293b606ece4c9
round[ 2].is_row 88ec930ef5e7e4b6cc32f4c906d29414
round[ 2].im_col 5cc7aebbe3c872194ae5ef8309a933c7
round[ 2].ik_sch 8fb999c973b26839c7f9d89d85c68c72
round[ 3].istart d37e3705907a1a208d1c371e8c6fbfb5
round[ 3].is_box a98ab23696bd4354b4c4b2e9f006f4d2
round[ 3].is_row a906b254968af4e9b4bdb2d2f0c44336
round[ 3].im_col b7113ed134e85489b20866b51d4b2c3b
round[ 3].ik_sch f77d6ec1423f54ef5378317f14b75744
round[ 4].istart 406c501076d70066e17057ca09fc7b7f
round[ 4].is_box 72b86c7c0f0d52d3e0d0da104055036b
round[ 4].is_row 7255dad30fb80310e00d6c6b40d0527c
round[ 4].im_col ef3b1be1b9b0e64bdcb79f1e0a707fbb
round[ 4].ik_sch 1147659047cf663b9b0ece8dfc0bf1f0
round[ 5].istart fe7c7e71fe7f807047b95193f67b8e4b
round[ 5].is_box 0c018a2c0c6b3ad016db7022d603e6cc
round[ 5].is_row 0c0370d00c01e622166b8accd6db3a2c
round[ 5].im_col 592460b248832b2952e0b831923048f1
round[ 5].ik_sch dcc1a8b667053f7dcc5c194ab5423a2e
round[ 6].istart 85e5c8042f8614549ebca17b277272df
round[ 6].is_box 672ab1304edc9bfddf78f1033d1e1eef
round[ 6].is_row 671ef1fd4e2a1e03dfdcdb1ef3d789b30
round[ 6].im_col 0b8a7783417ae3a1f9492dc0c641a7ce
round[ 6].ik_sch c6deb0ab791e2364a4055f5be568803ab
round[ 7].istart cd54c7283864c0c55d4c727e90c9a465
round[ 7].is_box 80fd31ee768c1f078d5d1e8a96121dbc
round[ 7].is_row 80121e0776fd1d8a8d8c31bc965d1fee
round[ 7].im_col 4ee1ddf9301d6352c9ad769ef8d20515
round[ 7].ik_sch dd1b7cdaf28d5c158a49ab1dbbc497cb
round[ 8].istart 93faa123c2903f4743e4dd83431692de
round[ 8].is_box 2214f132a896251664aec94164ff749c
round[ 8].is_row 22ffc916a81474416496f19c64ae2532
round[ 8].im_col 1008ffe53b36ee6af27b42549b8a7bb7
round[ 8].ik_sch 78c4f708318d3cd69655b701bfc093cf
round[ 9].istart 68cc08ed0abbd2bc642ef555244ae878
round[ 9].is_box f727bf53a3fe7f788cc377eda65cc8c1
round[ 9].is_row f75c7778a327c8ed8cfefbc1a6c37f53
round[ 9].im_col 7f69ac1ed939ebaac8ece3cb12e159e3

```

```

round[ 9].ik_sch 60dcef10299524ce62dbef152f9620cf
round[10].istart 1fb5430ef0accf64aa370cde3d77792c
round[10].is_box cbd264d717aa5f8c62b2819c8b02af42
round[10].is_row cb02818c17d2af9c62aa64428bb25fd7
round[10].im_col cfaf16b2570c18b52e7fef50cab267ae
round[10].ik_sch 4b4ecbdb4d4dcfda5752d7c74949cbde
round[11].istart 84e1dd691a41d76f792d389783fbac70
round[11].is_box 4fe0c9e443f80d06affa76854163aad0
round[11].is_row 4f63760643e0aa85aff8c9d041fa0de4
round[11].im_col 794cf891177bfd1d8a327086f3831b39
round[11].ik_sch 1a1f181d1e1b1c194742c7d74949cbde
round[12].istart 6353e08c0960e104cd70b751bacad0e7
round[12].is_box 0050a0f04090e03080d02070c01060b0
round[12].is_row 00102030405060708090a0b0c0d0e0f0
round[12].ik_sch 000102030405060708090a0b0c0d0e0f
round[12].ioutput 00112233445566778899aabbccddeeff

```

C.3 AES-256 ($Nk=8$, $Nr=14$)

PLAINTEXT: 00112233445566778899aabbccddeeff

KEY: 000102030405060708090a0b0c0d0e0f101112131415161718191a1b1c1d1e1f

CIPHER (ENCRYPT):

```

round[ 0].input 00112233445566778899aabbccddeeff
round[ 0].k_sch 000102030405060708090a0b0c0d0e0f
round[ 1].start 00102030405060708090a0b0c0d0e0f0
round[ 1].s_box 63cab7040953d051cd60e0e7ba70e18c
round[ 1].s_row 6353e08c0960e104cd70b751bacad0e7
round[ 1].m_col 5f72641557f5bc92f7be3b291db9f91a
round[ 1].k_sch 101112131415161718191a1b1c1d1e1f
round[ 2].start 4f63760643e0aa85efa7213201a4e705
round[ 2].s_box 84fb386f1ae1ac97df5cfd237c49946b
round[ 2].s_row 84e1fd6b1a5c946fdf4938977cfbac23
round[ 2].m_col bd2a395d2b6ac438d192443e615da195
round[ 2].k_sch a573c29fa176c498a97fce93a572c09c
round[ 3].start 1859fbc28a1c00a078ed8aadca2f6109
round[ 3].s_box adcb0f257e9c63e0bc557e951c15ef01
round[ 3].s_row ad9c7e017e55ef25bc150fe01ccb6395
round[ 3].m_col 810dce0cc9db8172b3678c1e88a1b5bd
round[ 3].k_sch 1651a8cd0244beda1a5da4c10640bade
round[ 4].start 975c66c1cb9f3fa8a93a28df8ee10f63
round[ 4].s_box 884a33781fdb75c2d380349e19f876fb
round[ 4].s_row 88db34fb1f807678d3f833c2194a759e
round[ 4].m_col b2822d81abe6fb275faf103a078c0033
round[ 4].k_sch ae87dff00ff11b68a68ed5fb03fc1567
round[ 5].start 1c05f271a417e04ff921c5c104701554
round[ 5].s_box 9c6b89a349f0e18499fda678f2515920
round[ 5].s_row 9cf0a62049fd59a399518984f26be178
round[ 5].m_col aeb65ba974e0f822d73f567bdb64c877
round[ 5].k_sch 6de1f1486fa54f9275f8eb5373b8518d
round[ 6].start c357aae11b45b7b0a2c7bd28a8dc99fa
round[ 6].s_box 2e5bacf8af6ea9e73ac67a34c286ee2d
round[ 6].s_row 2e6e7a2dafc6eef83a86ace7c25ba934
round[ 6].m_col b951c33c02e9bd29ae25cdb1efa08cc7
round[ 6].k_sch c656827fc9a799176f294cec6cd5598b
round[ 7].start 7f074143cb4e243ec10c815d8375d54c
round[ 7].s_box d2c5831a1f2f36b278fe0c4cec9d0329

```

round[7].s_row	d22f0c291ffe031a789d83b2ecc5364c
round[7].m_col	ebb19e1c3ee7c9e87d7535e9ed6b9144
round[7].k_sch	3de23a75524775e727bf9eb45407cf39
round[8].start	d653a4696ca0bc0f5acaab5db96c5e7d
round[8].s_box	f6ed49f950e06576be74624c565058ff
round[8].s_row	f6e062ff507458f9be50497656ed654c
round[8].m_col	5174c8669da98435a8b3e62ca974a5ea
round[8].k_sch	0bdc905fc27b0948ad5245a4c1871c2f
round[9].start	5aa858395fd28d7d05e1a38868f3b9c5
round[9].s_box	bec26a12cfb55dff6bf80ac4450d56a6
round[9].s_row	beb50aa6cff856126b0d6aff45c25dc4
round[9].m_col	0f77ee31d2ccadc05430a83f4ef96ac3
round[9].k_sch	45f5a66017b2d387300d4d33640a820a
round[10].start	4a824851c57e7e47643de50c2af3e8c9
round[10].s_box	d61352d1a6f3f3a04327d9fee50d9bdd
round[10].s_row	d6f3d9dda6279bd1430d52a0e513f3fe
round[10].m_col	bd86f0ea748fc4f4630f11c1e9331233
round[10].k_sch	7ccff71cbeb4fe5413e6bbf0d261a7df
round[11].start	c14907f6ca3b3aa070e9aa313b52b5ec
round[11].s_box	783bc54274e280e0511eacc7e200d5ce
round[11].s_row	78e2acce741ed5425100c5e0e23b80c7
round[11].m_col	af8690415d6e1dd387e5fbedd5c89013
round[11].k_sch	f01afafee7a82979d7a5644ab3afe640
round[12].start	5f9c6abfbac634aa50409fa766677653
round[12].s_box	cfde0208f4b418ac5309db5c338538ed
round[12].s_row	cfb4dbedf4093808538502ac33de185c
round[12].m_col	7427fae4d8a695269ce83d315be0392b
round[12].k_sch	2541fe719bf500258813bbd55a721c0a
round[13].start	516604954353950314fb86e401922521
round[13].s_box	d133f22a1aed2a7bfa0f44697c4f3ffd
round[13].s_row	d1ed44fd1a0f3f2afa4ff27b7c332a69
round[13].m_col	2c21a820306f154ab712c75eee0da04f
round[13].k_sch	4e5a6699a9f24fe07e572baacdf8cdea
round[14].start	627bceb9999d5aaac945ecf423f56da5
round[14].s_box	aa218b56ee5ebeacdd6ecef26e63c06
round[14].s_row	aa5ece06ee6e3c56dde68bac2621bebf
round[14].k_sch	24fc79ccb0979e9371ac23c6d68de36
round[14].output	8ea2b7ca516745bfeafc49904b496089

INVERSE CIPHER (DECRYPT):

round[0].iinput	8ea2b7ca516745bfeafc49904b496089
round[0].ik_sch	24fc79ccb0979e9371ac23c6d68de36
round[1].istart	aa5ece06ee6e3c56dde68bac2621bebf
round[1].is_row	aa218b56ee5ebeacdd6ecef26e63c06
round[1].is_box	627bceb9999d5aaac945ecf423f56da5
round[1].ik_sch	4e5a6699a9f24fe07e572baacdf8cdea
round[1].ik_add	2c21a820306f154ab712c75eee0da04f
round[2].istart	d1ed44fd1a0f3f2afa4ff27b7c332a69
round[2].is_row	d133f22a1aed2a7bfa0f44697c4f3ffd
round[2].is_box	516604954353950314fb86e401922521
round[2].ik_sch	2541fe719bf500258813bbd55a721c0a
round[2].ik_add	7427fae4d8a695269ce83d315be0392b
round[3].istart	cfb4dbedf4093808538502ac33de185c
round[3].is_row	cfde0208f4b418ac5309db5c338538ed
round[3].is_box	5f9c6abfbac634aa50409fa766677653
round[3].ik_sch	f01afafee7a82979d7a5644ab3afe640
round[3].ik_add	af8690415d6e1dd387e5fbedd5c89013

```

round[ 4].istart 78e2acce741ed5425100c5e0e23b80c7
round[ 4].is_row 783bc54274e280e0511eacc7e200d5ce
round[ 4].is_box c14907f6ca3b3aa070e9aa313b52b5ec
round[ 4].ik_sch 7ccff71cbeb4fe5413e6bbf0d261a7df
round[ 4].ik_add bd86f0ea748fc4f4630f11c1e9331233
round[ 5].istart d6f3d9dda6279bd1430d52a0e513f3fe
round[ 5].is_row d61352d1a6f3f3a04327d9fee50d9bdd
round[ 5].is_box 4a824851c57e7e47643de50c2af3e8c9
round[ 5].ik_sch 45f5a66017b2d387300d4d33640a820a
round[ 5].ik_add 0f77ee31d2ccadc05430a83f4ef96ac3
round[ 6].istart beb50aa6cfff856126b0d6aff45c25dc4
round[ 6].is_row bec26a12cfb55dff6bf80ac4450d56a6
round[ 6].is_box 5aa858395fd28d7d05e1a38868f3b9c5
round[ 6].ik_sch 0bdc905fc27b0948ad5245a4c1871c2f
round[ 6].ik_add 5174c8669da98435a8b3e62ca974a5ea
round[ 7].istart f6e062ff507458f9be50497656ed654c
round[ 7].is_row f6ed49f950e06576be74624c565058ff
round[ 7].is_box d653a4696ca0bc0f5acaab5db96c5e7d
round[ 7].ik_sch 3de23a75524775e727bf9eb45407cf39
round[ 7].ik_add ebb19e1c3ee7c9e87d7535e9ed6b9144
round[ 8].istart d22f0c291ffe031a789d83b2ecc5364c
round[ 8].is_row d2c5831a1f2f36b278fe0c4cec9d0329
round[ 8].is_box 7f074143cb4e243ec10c815d8375d54c
round[ 8].ik_sch c656827fc9a799176f294cec6cd5598b
round[ 8].ik_add b951c33c02e9bd29ae25cdb1efa08cc7
round[ 9].istart 2e6e7a2dafc6eef83a86ace7c25ba934
round[ 9].is_row 2e5bacf8af6ea9e73ac67a34c286ee2d
round[ 9].is_box c357aae11b45b7b0a2c7bd28a8dc99fa
round[ 9].ik_sch 6de1f1486fa54f9275f8eb5373b8518d
round[ 9].ik_add aeb65ba974e0f822d73f567bdb64c877
round[10].istart 9cf0a62049fd59a399518984f26be178
round[10].is_row 9c6b89a349f0e18499fda678f2515920
round[10].is_box 1c05f271a417e04ff921c5c104701554
round[10].ik_sch ae87dff00ff11b68a68ed5fb03fc1567
round[10].ik_add b2822d81abe6fb275faf103a078c0033
round[11].istart 88db34fb1f807678d3f833c2194a759e
round[11].is_row 884a33781fdb75c2d380349e19f876fb
round[11].is_box 975c66c1cb9f3fa8a93a28df8ee10f63
round[11].ik_sch 1651a8cd0244beda1a5da4c10640bade
round[11].ik_add 810dce0cc9db8172b3678c1e88a1b5bd
round[12].istart ad9c7e017e55ef25bc150fe01ccb6395
round[12].is_row adcb0f257e9c63e0bc557e951c15ef01
round[12].is_box 1859fbc28a1c00a078ed8aad42f6109
round[12].ik_sch a573c29fa176c498a97f9ce93a572c09c
round[12].ik_add bd2a395d2b6ac438d192443e615da195
round[13].istart 84e1fd6b1a5c946fdf4938977cfbac23
round[13].is_row 84fb386f1ae1ac97df5cfd237c49946b
round[13].is_box 4f63760643e0aa85efa7213201a4e705
round[13].ik_sch 101112131415161718191a1b1c1d1e1f
round[13].ik_add 5f72641557f5bc92f7be3b291db9f91a
round[14].istart 6353e08c0960e104cd70b751bacad0e7
round[14].is_row 63cab7040953d051cd60e0e7ba70e18c
round[14].is_box 00102030405060708090a0b0c0d0e0f0
round[14].ik_sch 000102030405060708090a0b0c0d0e0f
round[14].ioutput 00112233445566778899aabbccddeeff

```

EQUIVALENT INVERSE CIPHER (DECRYPT):

round[0].iinput	8ea2b7ca516745bfeafc49904b496089
round[0].ik_sch	24fc79ccbf0979e9371ac23c6d68de36
round[1].istart	aa5ece06ee6e3c56dde68bac2621bebfb
round[1].is_box	629deca599456db9c9f5ceaa237b5af4
round[1].is_row	627bceb9999d5aaac945ecf423f56da5
round[1].im_col	e51c9502a5c1950506a61024596b2b07
round[1].ik_sch	34f1d1ffbfceaa2ffce9e25f2558016e
round[2].istart	d1ed44fd1a0f3f2afa4ff27b7c332a69
round[2].is_box	5153862143fb259514920403016695e4
round[2].is_row	516604954353950314fb86e401922521
round[2].im_col	91a29306cc450d0226f4b5eaf5efed8
round[2].ik_sch	5e1648eb384c350a7571b746dc80e684
round[3].istart	cfb4dbedf4093808538502ac33de185c
round[3].is_box	5fc69f53ba4076bf50676aaa669c34a7
round[3].is_row	5f9c6abfbac634aa50409fa766677653
round[3].im_col	b041a94eff21ae9212278d903b8a63f6
round[3].ik_sch	c8a305808b3f7bd043274870d9b1e331
round[4].istart	78e2acce741ed5425100c5e0e23b80c7
round[4].is_box	c13baaeccae9b5f6705207a03b493a31
round[4].is_row	c14907f6ca3b3aa070e9aa313b52b5ec
round[4].im_col	638357cec07de6300e30d0ec4ce2a23c
round[4].ik_sch	b5708e13665a7de14d3d824ca9f151c2
round[5].istart	d6f3d9dda6279bd1430d52a0e513f3fe
round[5].is_box	4a7ee5c9c53de85164f348472a827e0c
round[5].is_row	4a824851c57e7e47643de50c2af3e8c9
round[5].im_col	ca6f71058c642842a315595fdf54f685
round[5].ik_sch	74da7ba3439c7e50c81833a09a96ab41
round[6].istart	beb50aa6cff856126b0d6aff45c25dc4
round[6].is_box	5ad2a3c55fe1b93905f3587d68a88d88
round[6].is_row	5aa858395fd28d7d05e1a38868f3b9c5
round[6].im_col	ca46f5ea835eab0b9537b6dbb221b6c2
round[6].ik_sch	3ca69715d32af3f22b67ffade4ccd38e
round[7].istart	f6e062ff507458f9be50497656ed654c
round[7].is_box	d6a0ab7d6cca5e695a6ca40fb953bc5d
round[7].is_row	d653a4696ca0bc0f5acaab5db96c5e7d
round[7].im_col	2a70c8da28b806e9f319ce42be4baead
round[7].ik_sch	f85fc4f3374605f38b844df0528e98e1
round[8].istart	d22f0c291ffe031a789d83b2ecc5364c
round[8].is_box	7f4e814ccb0cd543c175413e8307245d
round[8].is_row	7f074143cb4e243ec10c815d8375d54c
round[8].im_col	f0073ab7404a8a1fc2cba0b80df08517
round[8].ik_sch	de69409aef8c64e7f84d0c5fcfab2c23
round[9].istart	2e6e7a2dafc6eef83a86ace7c25ba934
round[9].is_box	c345bdfa1bc799e1a2dcaab0a857b728
round[9].is_row	c357aae11b45b7b0a2c7bd28a8dc99fa
round[9].im_col	3225fe3686e498a32593c1872b613469
round[9].ik_sch	aed55816cf19c100bcc24803d90ad511
round[10].istart	9cf0a62049fd59a399518984f26be178
round[10].is_box	1c17c554a4211571f970f24f0405e0c1
round[10].is_row	1c05f271a417e04ff921c5c104701554
round[10].im_col	9d1d5c462e655205c4395b7a2eac55e2
round[10].ik_sch	15c668bd31e5247d17c168b837e6207c
round[11].istart	88db34fb1f807678d3f833c2194a759e
round[11].is_box	979f2863cb3a0fc1a9e166a88e5c3fdf
round[11].is_row	975c66c1cb9f3fa8a93a28df8ee10f63
round[11].im_col	d24bfb0e1f997633cfce86e37903fe87
round[11].ik_sch	7fd7850f61cc991673db890365c89d12

round[12].istart	ad9c7e017e55ef25bc150fe01ccb6395
round[12].is_box	181c8a098aed61c2782ffba0c45900ad
round[12].is_row	1859fbc28a1c00a078ed8aadca2f6109
round[12].im_col	aec9bda23e7fd8aff96d74525cdce4e7
round[12].ik_sch	2a2840c924234cc026244cc5202748c4
round[13].istart	84e1fd6b1a5c946fdf4938977cfbac23
round[13].is_box	4fe0210543a7e706efa476850163aa32
round[13].is_row	4f63760643e0aa85efa7213201a4e705
round[13].im_col	794cf891177bfd1ddf67a744acd9c4f6
round[13].ik_sch	1a1f181d1e1b1c191217101516131411
round[14].istart	6353e08c0960e104cd70b751bacad0e7
round[14].is_box	0050a0f04090e03080d02070c01060b0
round[14].is_row	00102030405060708090a0b0c0d0e0f0
round[14].ik_sch	000102030405060708090a0b0c0d0e0f
round[14].ioutput	00112233445566778899aabbccddeeff

Appendix D - References

- [1] AES page available via <http://www.nist.gov/CryptoToolkit>.⁴
- [2] Computer Security Objects Register (CSOR): <http://csrc.nist.gov/csor/>.
- [3] J. Daemen and V. Rijmen, *AES Proposal: Rijndael*, AES Algorithm Submission, September 3, 1999, available at [1].
- [4] J. Daemen and V. Rijmen, *The block cipher Rijndael*, Smart Card research and Applications, LNCS 1820, Springer-Verlag, pp. 288-296.
- [5] B. Gladman's AES related home page
http://fp.gladman.plus.com/cryptography_technology/.
- [6] A. Lee, NIST Special Publication 800-21, *Guideline for Implementing Cryptography in the Federal Government*, National Institute of Standards and Technology, November 1999.
- [7] A. Menezes, P. van Oorschot, and S. Vanstone, *Handbook of Applied Cryptography*, CRC Press, New York, 1997, p. 81-83.
- [8] J. Nechvatal, et. al., *Report on the Development of the Advanced Encryption Standard (AES)*, National Institute of Standards and Technology, October 2, 2000, available at [1].

⁴ A complete set of documentation from the AES development effort – including announcements, public comments, analysis papers, conference proceedings, etc. – is available from this site.