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**TEMPERATURE VARIATION OF  
ACTUATION VOLTAGE IN  
CAPACITIVE MEMS SWITCHES**



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# Temperature Variation of Actuation Voltage in Capacitive MEMS Switches

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**Abstract**—A simple theoretical model for temperature variation of actuation voltage for fixed-fixed beam switches is developed and applied to model capacitive RF MEMS switches. Measured data from these switches fits very well with the model over a 120°C operating temperature range, while demonstrating a 3x reduction in variation compared to previous publications. The proposed model provides valuable insight into the factors impacting variability of actuation voltage over broad temperature ranges.

**Index Terms** – Microelectromechanical systems, RF MEMS, capacitive switch, electrostatic, actuation, temperature

## I. INTRODUCTION

Robust operation over temperature is a critical criterion for any electronics technology. The ability to maintain consistent device performance irrespective of temperature is a necessary ingredient for useful application of electronic devices. Fixed-fixed beam capacitive MEMS switches commonly possess an actuation voltage that varies significantly over temperature. This is due to their inherent mechanical design which allows the substrate to induce changes in the stress state of the mechanical membrane over temperature. The sparse data that has been published on this topic demonstrates variations in the range of 0.3-0.5 V/°C [1], [2]. Over a broad temperature range, this can lead to excessively large supply voltage variations. Additionally, operation at high voltages (necessary for low temperatures) can also adversely impact device longevity [3]. Clearly, it is important to understand and control the mechanisms which determine the actuation voltage for a fixed-fixed beam MEMS switch. This article develops a simple analytical description of the mechanisms inducing change in pulldown voltage over temperature and compares them with experimental results. The result is an excellent fit between theory and experiment, and better insight into the factors affecting robust operation over temperature.

## II. THEORY

Fixed-fixed beam micromechanical structures have been utilized to make RF MEMS capacitive switches [4] for more than a decade. A thin, flexible metal membrane is suspended across two support posts, and is electrostatically actuated via a lower electrode beneath the membrane. The pulldown voltage for this switch is a function of geometrical dimensions and material characteristics of the mechanical material. A simple, first-order model for the elastic deformation of the membrane gives an expression for the pulldown voltage of the membrane as [5]

$$V_p = \sqrt{\frac{8kg_o^3}{27\epsilon_o A}} \quad (1)$$

where  $k$  is the linear spring constant of the membrane,  $g_o$  is the undeflected gap between the membrane and lower electrode,  $\epsilon_o$  is the permittivity of free space, and  $A$  is the overlap area of the membrane and electrode. The spring constant of a membrane switch in the stress-dominated regime is given by [5] as

$$k \sim \frac{8\sigma(1-\nu)tw}{L} \cdot \gamma_g \quad (2)$$

which is generally within 20% of a more detailed finite element simulation. Other geometrical factors may impact this model, including the finite width of the lower electrode beneath the membrane and the impact of a flared membrane shape rather than a rectangular shape. These are taken into account by the geometrical constant  $\gamma_g$  in the above equation.

The cause of pulldown voltage changes over temperature is due to strain caused by the difference in expansion coefficients between the mechanical membrane and the substrate. Often, the metal membrane and the insulating substrate possess a significant difference in expansion coefficients, on the order of 20ppm/°C. This results in a situation where the substrate will force substantial changes in the membrane stress. At a deposition temperature,  $T_d$ , the membrane is deposited with a residual stress,  $\sigma_d$ , set by the deposition conditions. As the temperature decreases from the deposition temperature, the tensile stress linearly increases due to the strain induced by substrate expansion. This can be characterized by the simple relationship

$$\sigma(T) = \Delta\alpha E [T_{zs} - T]$$

where  $T_{zs}$  is the effective temperature of zero stress within the membrane and is determined by

$$T_{zs} = T_d - \frac{\sigma_d}{\Delta\alpha E} \quad (3)$$

This formulation makes obvious that a single variable,  $T_{zs}$ , accounts for the as-deposited stress and deposition temperature of the membrane.

Combining (1), (2), and (3) yields an expression for the actuation voltage as a function of temperature caused by strain induced temperature variations-

$$V_p(T) = \sqrt{\frac{64\gamma_g(1-\nu)tg_o^3}{27L^2\epsilon_o} (\Delta\alpha E (T_{zs} - T))} \quad (4)$$

This equation expresses the fundamental nonlinear square-root relationship of the switch actuation voltage over temperature. This variation is approximately linear at colder temperatures

or over small temperature ranges. In general, previous publications have broadly characterized their variation in terms of a linear change in actuation voltage over temperature. Equation (5) clearly defines the variation over temperature and the central parameters affecting that variation.

### III. EXPERIMENT

Experimental verification of the proposed model was obtained using capacitive MEMS switches. These switches were fabricated on Pyrex glass substrates (Corning 7740) with copper posts, gold electrodes, and aluminum alloy membranes. A photograph of the top view of the switch is shown in Fig. 1. The CPW transmission lines have a 150  $\mu\text{m}$  center linewidth and 35  $\mu\text{m}$  spacing. These conductors are approximately 2.5  $\mu\text{m}$  tall with a 300  $\mu\text{m}$  ground-ground spacing. The lower electrode is constructed from gold, being approximately 0.3  $\mu\text{m}$  tall and 80  $\mu\text{m}$  wide. The center conductor is covered by 0.25  $\mu\text{m}$  of silicon dioxide as the switch dielectric.

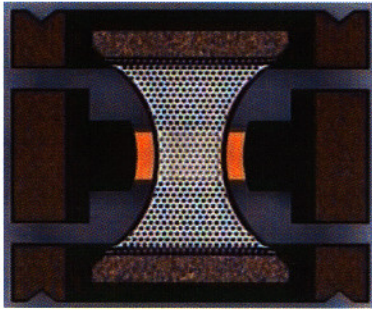


Fig. 1 - Top view of a shunt MEMS capacitive switch

These RF MEMS switches were tested on a Cascade Microtech Attoguard test station outfitted with a Tempronic temperature controller capable of setting and controlling the chuck temperature over the  $-50^{\circ}\text{C}$  to  $+100^{\circ}\text{C}$  temperature range. The switches were actuated using an Agilent Model 33220A arbitrary waveform generator driving a Tabor Electronics Model 9100 high voltage amplifier. The waveform was programmed to be a dual-pulse waveform similar to that described in [3] to minimize dielectric charging. The amplitude of the actuation pulse was variable over a 20-50 volt actuation range. The duration of this peak holding voltage was approximately 500  $\mu\text{s}$ . The holding voltage in the waveform was set to approximately 38% of the peak actuation voltage (i.e. a 15 volt holding voltage for a 40 volt actuation voltage). The repetition rate of the waveform was 10 Hz so that actuation was visible through the test station microscope. Voltage drive was initially set low and increased until the onset of switch actuation. The minimum actuation voltage was then recorded for each switch over the temperature range of  $-50^{\circ}\text{C}$  to  $+100^{\circ}\text{C}$ . Six MEMS switches were measured across the face of two different wafers and all results tabulated.

### IV. RESULTS

Prior to the above described actuation voltage measurements, a measurement of switch off-capacitance was taken over

temperature. This data was taken to investigate whether the height of the membrane changed appreciably over temperature. A graph of gap capacitance vs. temperature is shown for one of the MEMS switches in Fig. 2. As can be seen from this figure, the off-capacitance is maintained constant until the "critical buckling stress" is reached at approximately  $90^{\circ}\text{C}$ . This implies that the gap between the membrane and electrode remains constant until the onset of buckling. This data is counter to the simulations run by Espinosa [6] which show the membrane changing height over temperature. However, this data supports the validity of the model of (4), which would be incorrect if the membrane gap changed significantly over temperature. In order to avoid buckling of the membrane at the high temperatures, a maximum temperature of  $70^{\circ}\text{C}$  was used for model fitting.

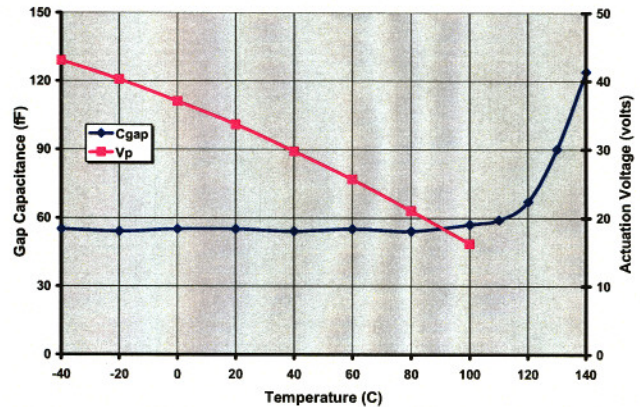


Fig. 2 - Measurement of gap capacitance and actuation voltage over temperature.

Graphs of actuation voltage for the six devices from each of two wafers are represented by individual datapoints in Fig. 3. The data from the first wafer, Wafer A, demonstrates an average actuation voltage at  $25^{\circ}\text{C}$  of 32 volts. Total variation over a  $115^{\circ}\text{C}$  temperature range, from  $-45^{\circ}\text{C}$  to  $+70^{\circ}\text{C}$ , is approximately 14.5 volts. This represents an average variation of  $0.127 \text{ V}/^{\circ}\text{C}$ . Similarly for Wafer B, the average room temperature actuation voltage is approximately 24 volts with a 16 volt variation over a full  $120^{\circ}\text{C}$  temperature range. This represents an average variation of  $0.132 \text{ V}/^{\circ}\text{C}$  over the temperature range. This data represents a roughly 3x reduction in total variation of actuation voltage over temperature compared to previous publications.

Next, the measured data was fitted to the model represented by (4). The data from six switches was fitted with individual values for the gap,  $g_0$ , and a common value of  $T_{zs}$  from each wafer. For the aluminum membrane, a Young's modulus of 70 GPa and Poisson ratio of 0.35 were used (those of bulk aluminum). The average thickness of the aluminum membranes are taken to be 2800  $\text{\AA}$ . The difference in expansion coefficient between the aluminum membrane and glass substrate was taken as 20 ppm. For the particular switch portrayed in Fig. 1, the geometrical constant  $\gamma_g$  in (3) is 1.1. This encompasses contributions from the finite width of the electrode beneath the membrane (approximately 0.53) and the

flared shape of the membrane relative to a rectangular shape (approximately 2.1, as measured experimentally).

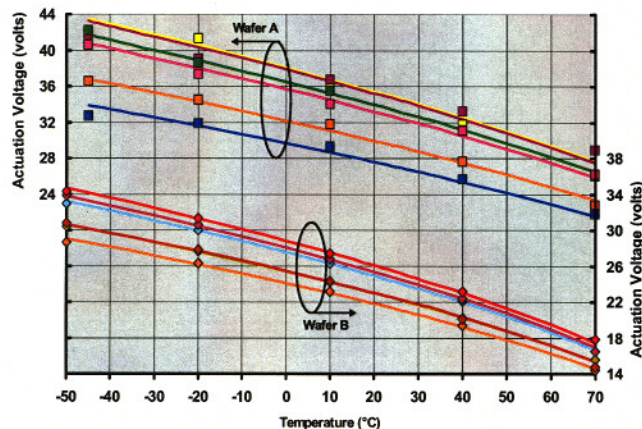


Fig. 3 - Measured and modeled actuation voltage over temperature for Wafers A and B.

Fig. 3 displays the fitted models (solid lines) for Wafer A and B against the measured datapoints. As can be seen from the figure, the measured data and fitted models correlate very well. The resulting parameters from the model fit, the individual values of  $g_0$  and  $T_{zs}$  for each of the two wafers, is shown in Table 1. Maximum deviation between fitted and measured data over temperature is less than 8%, or about 2.5 volts maximum. In the specific case of Wafer B, the fit is better than 4% and 0.5 volts over the temperature range. The gap values given in Table 1 are consistent with the measurements of switch dimensions and off-capacitances. Similarly, the derived values for  $T_{zs}$  are consistent with the general deposition conditions of the membranes. The data in Table 1 suggests that the roughly 8 volt difference in actuation voltage at room temperature is mostly due to differences in residual stress of the membranes rather than the gaps between the membrane and lower electrode. The excellent fit between model and experimental results over temperature enables interesting insights into techniques which might lessen the actuation variation over temperature.

Table 1 - Fitting results of  $T_{zs}$  and switch gap to achieve model fit given in Fig. 3.

Wafer A	$T_{zs}$ 148.01 Deg C					
Device	1	2	3	4	5	6
Gap ( $\mu\text{m}$ )	1.92	2.27	2.26	2.21	2.03	2.18

Wafer B	$T_{zs}$ 110.41 Deg C					
Device	1	2	3	4	5	6
Gap ( $\mu\text{m}$ )	2.02	2.04	2.08	1.91	1.85	1.92

Despite the excellent fit between measured and modeled data, it should be noted that the actual mechanical structure of the fixed-fixed beam switch is far more complicated than the simple first-order model presented here. The actual as-deposited residual stress of the mechanical membranes is commonly monitored as part of the process flow and tends to be quite high. In the case of aluminum membranes, this stress is a function of the temperature history of the membrane as it undergoes inelastic deformation at elevated temperatures

during sacrificial layer removal [7]. However, the presence of release holes in the membrane tends to allow stress relaxation of the residual stress [8] making the released stress significantly lower. In addition, developers of MEMS devices commonly incorporate three dimensional features into the membrane [9] to reduce the final stress of the membrane. The impact of both of these features is to lower the effective residual stress on the membrane in order to maintain reasonable control voltages. With the theoretical basis for the variation in actuation voltage over temperature established, it is now possible to understand the impact of these features on actuation voltage variation over temperature.

## V. CONCLUSION

A simple model for variation in actuation voltage over temperature has been put forth and experimentally verified for one particular design of fixed-fixed beam capacitive switches. This model provides insight into the parameters impacting this temperature variation, and allows simple design changes to minimize this undesired variation over temperature. The measured switch data conforms to the shape of the theoretical curve of actuation voltage over temperature, and demonstrates reduced variation compared to previous publications. Measurements of switches from other wafers produce similar results. It is believed that this model will accurately represent the variation in actuation voltage over temperature for a variety of RF MEMS capacitive switches being designed and produced today.

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