

# DFT MODELING OF SWCNT GROWTH ON IRON CATALYST

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## ABSTRACT

We performed simulations of initial stages of a carbon nanotube growth catalyzed by iron particles using all-electron density functional theory with generalized gradient approximation for the exchange-correlation functional. The systems studied are  $\text{Fe}_4 + \text{C}_n$  for  $n=7-25$ ,  $\text{Fe}_{10} + \text{C}_{15}$ , and  $\text{Fe}_{10}\text{C}_{15} + 10\text{C}$ . In addition, we performed a detailed study of development of different isomers in the  $\text{C}_n$  series,  $n=7-25$ .

## 1. INTRODUCTION

Single-walled carbon nanotubes (SWCNT) are expected to have an enormous impact on various technological areas related to fabrication of composite materials, sensors, hydrogen storages, protective coatings, and computer memories. The SWCNTs are produced typically from hydrocarbons [1], alcohol [2], and graphite [3]. The method of catalytic chemical vapor deposition (CCVD) [1] makes use of high temperatures to produce carbon and a supported catalyst to initiate the carbon nanotube growth. The catalyst needs restoration after each cycle. Carbon nanotubes grown using this method are often multi-walled, while single-walled nanotubes are of more interest from a technological point of view. On the contrary, the high-pressure high-temperature HiPco [4] method is continuous and its floating or gas-phase catalyst is formed *in situ* from iron pentacarbonyl  $\text{Fe}(\text{CO})_5$ . Using carbon monoxide as feedstock is rather intriguing, because CO is one of the most stable diatomics with the measured bond strength of 11.09 eV. Carbon nanotubes produced in this process are always single-walled and are believed to nucleate and grow via the Boudouard disproportionation reaction  $\text{CO} + \text{CO} \rightarrow \text{C}_{\text{SWCNT}} + \text{CO}_2$ . However, the mechanism of carbon nanotube growth is not well understood.

In order to gain insight into carbon nucleation in the HiPco process, we have performed all-electron density functional theory calculations with a generalized gradient approximation (DFT-GGA) on  $\text{Fe}_n\text{C}$  [5],  $\text{Fe}_n\text{CO}$  ( $n \leq 6$ ) [6], and  $\text{Fe}_4\text{C}_n(\text{CO})_m$  ( $n+m \leq 3$ , both C and CO are attached to  $\text{Fe}_4$ ) [7] clusters, and estimated the energies of Boudouard CO disproportionation reactions  $\text{Fe}_4\text{C}_n(\text{CO})_m + \text{CO} \rightarrow \text{Fe}_4\text{C}_{n+1}(\text{CO})_{m+1} + \text{CO}_2$ . The energies found are relatively small and are in the range from -0.26 eV to +0.74 eV. Next, we explored [8] the thermodynamics of CO attachment to a carbon atom that had already

precipitated on an iron cluster due to a preceding Boudouard reaction and evaluated the energetics of CO disproportionation reactions  $\text{Fe}_4\text{C}_n(\text{CO})_m + \text{CO} \rightarrow \text{Fe}_4\text{C}_{n+1}(\text{CO})_{m+1} + \text{CO}_2$  for higher coverage ( $n+m \leq 5$ ). We choose  $\text{Fe}_4^-$ ,  $\text{Fe}_4$ , and  $\text{Fe}_4^+$  clusters since the  $\text{Fe}_4^+$  cluster is known to catalyze the growth of benzene from ethylene and cyclopropane in a low-pressure gas-phase process. The number of iron atoms in the clusters formed in the HiPco process ranges from  $\sim 10$  to  $\sim 300$  and it is not clear if smaller iron clusters  $\text{Fe}_3$  to  $\text{Fe}_{10}$  can technologically be effective for the SWCNT growth because of different restrictions such as coalescence of small clusters. However, one can anticipate that our computations using computationally less demanding  $\text{Fe}_4$  clusters are capable of reproducing the essentials in initiating the SWCNT growth. According to the results of our previous computations, dimerization of carbon atoms is preferable in  $\text{Fe}_4\text{C}_4$ ,  $\text{Fe}_4\text{C}_5$  and its ions, while  $\text{C}_3$  trimers form in the ground states of  $\text{Fe}_4\text{C}_6$  and its ions. Since attachment of COs followed by subsequent Boudouard reaction leads to precipitation of carbon atoms, we considered next the trends in rearrangement of carbon atoms in the lowest energy isomers of clusters  $\text{Fe}_4\text{C}_n$ ,  $n=7-20$  [9]. This work discusses some results from Ref. [9] and presents the results of our simulations using  $\text{Fe}_{10}$  and  $\text{Fe}_4\text{C}_{15}$  clusters.

## 2. COMPUTATIONAL DETAILS

The Gaussian 98 and 03 programs [10,11] were used. We have used the 6-311+G\* basis set (15s11p6d1f)/[10s7p4d1f] [12] and (12s6p1d)/[5s4p1d] [13] for Fe and C, respectively. In some computations involving  $\text{Fe}_{10}$  and  $\text{Fe}_4\text{C}_{15}$ , we used a smaller 6-31G basis for carbon atoms. Our previous study [14-16] of bare iron clusters and 3d-metal dimers showed that results obtained using many of the DFT-GGA methods included in Gaussian 98 and 03 programs are rather similar; however, the BPW91 vibrational frequencies appear to be less sensitive to the quality of the grid used in the numerical integration than some of the other functionals. On this ground, we choose the BPW91 method, where the exchange-correlation functional is comprised of the Becke's exchange [17] and Perdew-Wang's correlation [18].

The geometry of each cluster was optimized without imposing any symmetry constraints. Iron clusters possess high spin multiplicities and our optimizations of the clusters interacting with carbon species were performed in the range of spin multiplicities enclosing the

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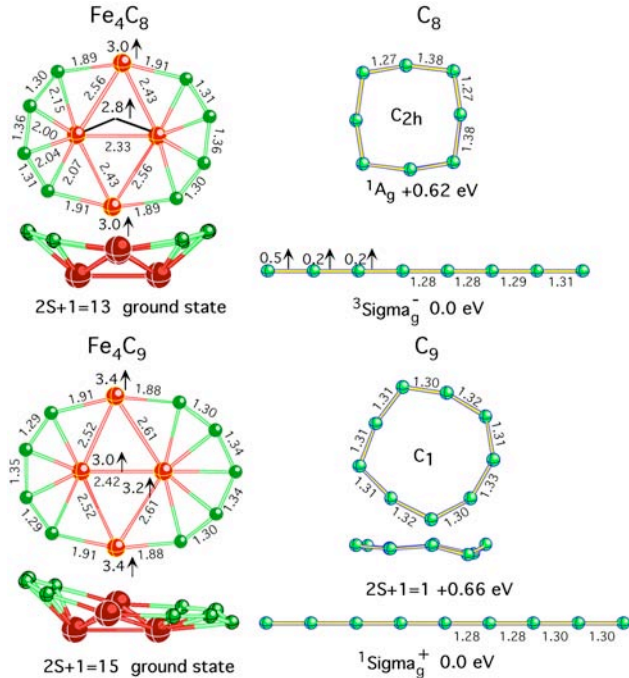
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ground-state spin multiplicity of the corresponding bare iron cluster. Each geometry optimization was followed by the calculation of the harmonic vibrational frequencies using analytical second derivatives, in order to confirm that the optimized geometry corresponds to a minimum. We computed atomic spin densities using Mulliken [19] approach.

### 3. GEOMETRICAL STRUCTURES OF $\text{Fe}_4\text{C}_n$

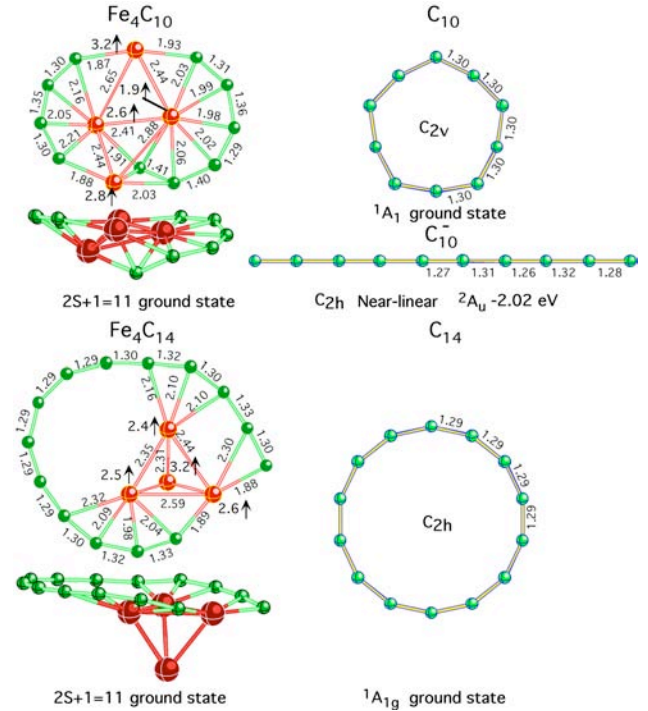
Our optimizations revealed a large number of isomers for each  $\text{Fe}_4\text{C}_n$  with a general trend of the carbon ring formation. The rings may contain also iron atoms in  $\text{Fe}_4\text{C}_6$ – $\text{Fe}_4\text{C}_{15}$ . The electronic states of  $\text{C}_n$  possessing ring-type geometries in the gas phase have the lowest total energies [20] beginning with  $\text{C}_{10}$ . We found that the formation of pure carbon rings in the lowest total energy of the  $\text{Fe}_4\text{C}_n$  clusters begins with  $n=15$ –16. Figure 1 presents the results of our computations for clusters  $\text{Fe}_4\text{C}_8$  and  $\text{Fe}_4\text{C}_9$  and shows free carbon clusters  $\text{C}_8$  and  $\text{C}_9$  optimized at the same level of theory.



**Fig. 1.** Top and side views of the ground-state  $\text{Fe}_4$  clusters with attached carbon  $\text{C}_8$  and  $\text{C}_9$  species. The ground and first excited ring states of the latter are shown in the right-hand side. Bond lengths are in Å, excess electronic densities at iron sites are in electrons.

As is seen, carbon atoms form ring structures containing two iron atoms in  $\text{Fe}_4\text{C}_8$  and in  $\text{Fe}_4\text{C}_9$ , while the ground states of  $\text{C}_8$  and  $\text{C}_9$  are linear. The ring structures of  $\text{C}_8$  and  $\text{C}_9$  are above the ground states by about 0.6 eV. The ground-state of the  $\text{C}_8^-$  and  $\text{C}_9^-$  anions are also linear. As for the  $\text{C}_n^-$  anions, there are near-linear

states that were a subject of experimental [21] and theoretical [22] studies. According to Ref. [22] and our computations performed with a larger basis set than that used in Ref. [22], the anion ring structure is more stable than a nearly linear one up to  $n = 14$ . (Note that optimizations of  $\text{C}_n^-$  anions imposing  $D_{\infty h}$  constraints produce transition states beginning with  $n=10$ .) It appears that this number is critical for formation of carbon ring structures on the top of an iron catalyst since there is a charge transfer from iron particles to a more electronegative carbon chain. Figure 2 shows that  $\text{Fe}_4\text{C}_{10}$  contains a ring with two inserted iron atoms while  $\text{Fe}_4\text{C}_{14}$  forms a ring with one inserted iron atom.

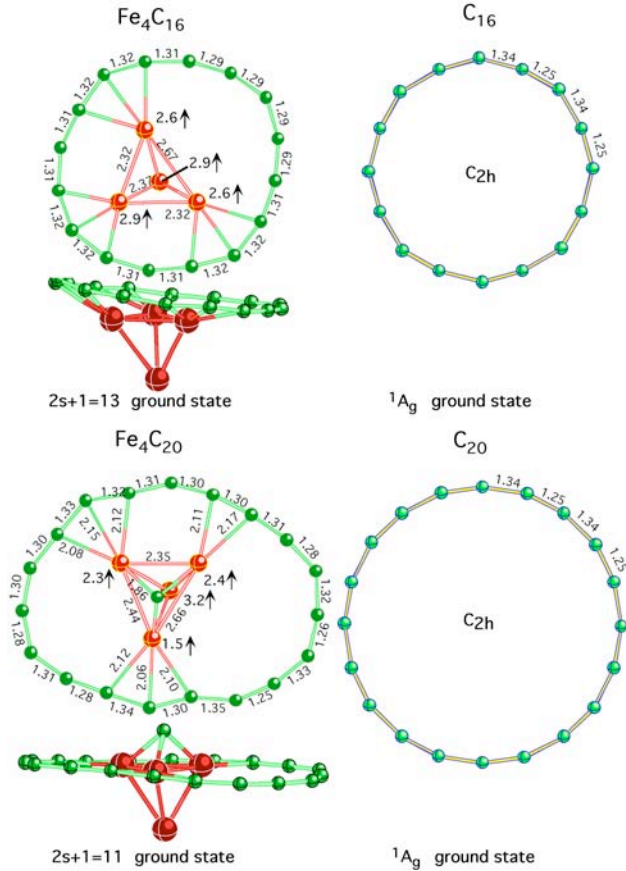


**Fig. 2.** Top and side views of the ground-state  $\text{Fe}_4\text{C}_{10}$  and  $\text{Fe}_4\text{C}_{14}$  clusters together with the ground states of  $\text{C}_{10}$ ,  $\text{C}_{10}^-$ , and  $\text{C}_{14}$ .

In  $\text{Fe}_4\text{C}_{15}$ , there is a competition between configurations containing a pure  $\text{C}_{15}$  ring and a  $\text{C}_{15}$  ring with an iron atom inserted inside the ring. The pure carbon ring structure on the top of  $\text{Fe}_4$  becomes favorable in  $\text{Fe}_4 + \text{C}_{16}$ . The lowest energy state of  $\text{Fe}_4 + \text{C}_{20}$  correspond to a  $\text{C}_{19}$  ring around the cluster and one carbon atom attached to a face of the iron cluster.

In order to gain insight which geometrical structure corresponds to the lowest energy state in  $\text{C}_n$  we performed optimizations [9] of  $\text{C}_n$  up to  $n=25$ . The first fullerene-type structure with 12 carbon pentagons appears at  $n=20$ , but the ring structure is the lowest energy one, followed by a bowl (flake-type) structure, and a fullerene (or cage) structure. Increasing the  $n$  number to  $n=25$ , we found the ring structures to correspond to the lowest energy states for  $n = 21, 22, 23$ , and 25, while the lowest

energy state corresponds to a flake composed of seven hexagons for  $n=24$ . At this size, there appears the smallest fullerene possessing two hexagons in addition to 12 pentagons. The results of our optimizations for  $n=24$  are presented in Fig. 4. There are a large number of different shape isomers; some of them are shown in the figure. The triplet states are higher for each flake, ring, or fullerene structures.



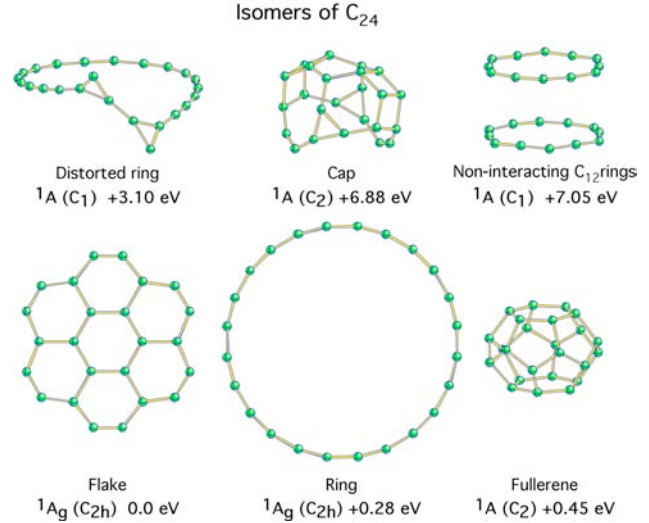
**Fig. 3.** Top and side views of the ground-state  $\text{Fe}_4$  clusters interacting with  $\text{C}_{16}$  and  $\text{C}_{20}$ .

#### 4. ISOMERS OF $\text{Fe}_{10}$ AND $\text{Fe}_{10}\text{C}_{15}$

To explore the influence of an iron cluster size, we have optimized several isomers of  $\text{Fe}_{10}$ . Next, we added a  $\text{C}_{15}$  ring to one of the isomers in different positions: on the top of long and short sides and wrapped around the center part of the cluster. The results of our optimizations are presented in Fig. 5.

We found that the carbon ring placed along the larger side has acquired one inserted iron atom. This configuration corresponds to the lowest energy state. The ring placed over a shorter side of the iron cluster slightly changes the perfect ring shape and attaches perpendicular to the iron cluster. The  $\text{C}_{15}$  ring placed around the center shifts during lengthy optimization cycles to the cluster tip while the initial bi-octahedral  $\text{Fe}_{10}$  configuration

transforms to another isomer configuration. The carbon ring placed above the tip is tilted to be nearly parallel to a  $\text{Fe}_3$  edge. The latter two  $\text{Fe}_{10}\text{C}_{15}$  isomers are nearly degenerate in total energy and are above the ground state by about 3 eV. The binding energy gain in the ground state apparently comes from breaking a C–C bond and the formation of two Fe–C bonds. This is apparently related with the shape of the surface and does not happen when  $\text{C}_{15}$  is attached to a shorter side



**Fig. 4.** Different isomers of  $\text{C}_{24}$ .

One could speculate that the upward growth on the tilted ring might produce a carbon nanotube with a certain chirality. That is, the part of the cluster surface, which initiates the carbon ring, is related to the chirality of a SWNT grown from the corresponding carbon ring.

#### 5. SIMULATED $\text{Fe}_{10}\text{C}_{15} + 10\text{C}$ GROWTH

In order to gain an insight how carbon atoms attach to a ring formed on an iron particle, we chose a  $\text{Fe}_4\text{C}_{15}$  isomer with a ring  $\text{C}_{15}$  pattern and added 10 carbon atoms randomly placed at the distance of 5 Å above the ring. Initial and final configurations together with several intermediate configurations obtained at different optimization steps are presented in Fig. 6.

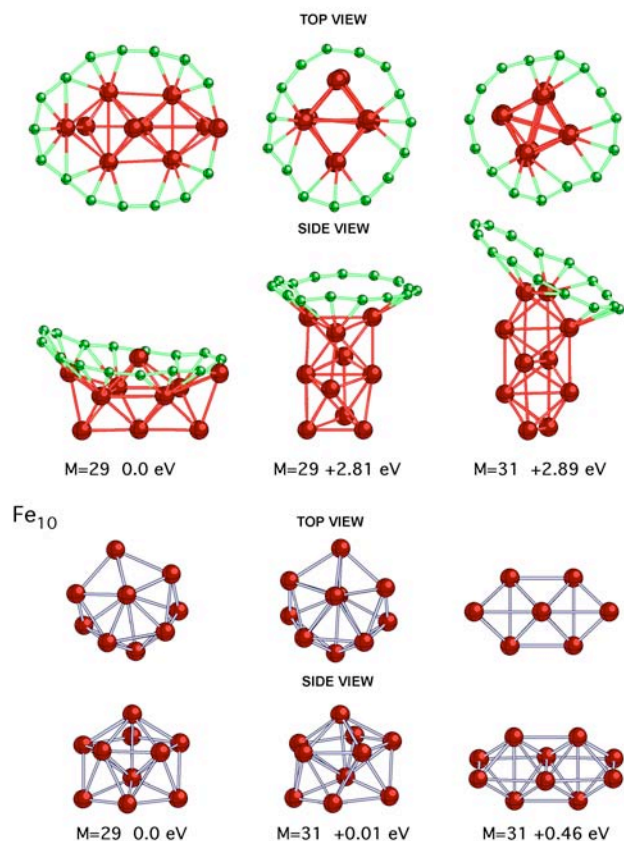
It is found that carbon atoms may form first dimers and trimers in correspondence with experimental observations of such a formation in arc discharges. Next, chains are formed, while the final configuration correspond to a cage with an open 15-carbon ring.

#### CONCLUSION

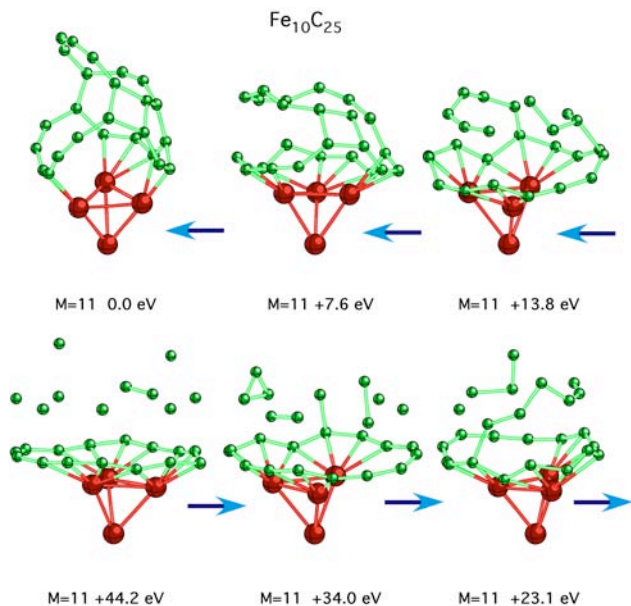
Our simulations at a rather reliable DFT-GGA level show that the prime role of a catalyst is to assemble carbon atoms in the optimal gas-phase configuration of  $\text{C}_n$  that

corresponds to a ring configuration for a rather large  $n$ . The surface topology of a catalyst particle is most likely

$\text{Fe}_{10}\text{C}_{15}$



**Fig. 5.** Different lowest energy isomers of  $\text{Fe}_{10}$   $\text{Fe}_{10}\text{C}_{15}$



**Fig. 6.** Configurations obtained in optimizations of  $\text{Fe}_{10}\text{C}_{15} + 10\text{C}$ .

responsible for the chirality of a carbon nanotube grown from a seed ring.

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