

Further examination of the thermodynamic modification of the inflow layer of tropical cyclones by vertical wind shear

M. Riemer¹, M. T. Montgomery^{2,3}, and M. E. Nicholls⁴

¹Institut für Physik der Atmosphäre, Johannes Gutenberg-Universität, Mainz, Germany

²Department of Meteorology, Naval Postgraduate School, Monterey, California, USA

³NOAA's Hurricane Research Division, Miami, Florida, USA

⁴University of Colorado, Cooperative Institute for Research in Environmental Sciences, Boulder, CO, USA

Correspondence to: Michael Riemer
(mriemer@uni-mainz.de)

Abstract. Recent work has developed a new framework for the impact of vertical wind shear on the intensity evolution of tropical cyclones. A focus of this framework is on the frustration of the tropical cyclone's power machine by shear-induced, persistent downdrafts that flush relatively cool and dry (lower equivalent potential temperature, θ_e) air into the storm's inflow layer. These previous results have been based on idealised numerical experiments for which we have deliberately chosen a simple set of physical parameterisations. Before efforts are undertaken to test the proposed framework with real atmospheric data, we here survey and diagnose five additional numerical experiments with some modifications of the experimental setup to assess the robustness of our previous results. The modifications comprise the values of the exchange coefficients of surface heat and momentum fluxes, the inclusion of experiments with ice microphysics, and the consideration of weaker, but still mature tropical cyclones.

In all experiments, the depression of the inflow layer θ_e values is significant and all tropical cyclones exhibit the same general structural changes when interacting with the imposed vertical wind shear. Tropical cyclones with a higher downdraft activity exhibit a more pronounced depression of inflow layer θ_e *outside* of the eyewall in our experiments. The magnitude of the θ_e depression *underneath* the eyewall early after shear is imposed in our experiments correlates well with the magnitude of the ensuing weakening of the respective tropical cyclone. Based on the evidence presented, it is concluded that the newly proposed framework is a robust description of intensity modification in our suite of experiments.

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20 1 Introduction

1.1 A new framework for intensity modification of tropical cyclones in vertical wind shear

The intensity evolution of tropical cyclones (TCs) embedded in an environmental flow with vertical wind shear poses an important forecast problem. To date, the physical processes that govern this intensity evolution are not well understood. In a recent publication (Riemer et al., 2010, referred to
25 as RMN10 hereafter) a new framework for the intensity modification of TCs in vertical wind shear was proposed. While previous hypotheses have focused almost exclusively on processes above the boundary layer, RMN10 showed that vertical wind shear has a significant impact on the thermodynamic properties of the TC's inflow layer¹. Strong and persistent, shear-induced downdrafts flush
30 the inflow layer with low moist-entropy (or equivalent potential temperature, θ_e) air - "anti-fuel" for the TC power machine. The replenishment of this air by surface heat fluxes is not complete while the air spirals towards the storm centre leading to a reduction of θ_e values within the inner-core updrafts in the *azimuthal mean*. When viewed from the simplified perspective of an idealised Carnot-cycle a decrease in the potential intensity of the TC can be expected (Tang and Emanuel, 2010).

The downdrafts that flush the inflow layer with low- θ_e air are associated with a quasi-stationary,
35 azimuthal wave-number 1, convective asymmetry *outside* of the eyewall. This convective asymmetry is reminiscent of the 'stationary band complex' (Willoughby et al., 1984) and for this reason will be referred to as the SBC hereafter. The SBC and the associated downdraft pattern extends outwards to approximately 150 km – 180 km. On account of the swirling winds, the updrafts within the SBC rise along a helical path. A simple kinematic model (Riemer and Montgomery, 2011) suggests
40 that, at low levels above the inflow layer, environmental low- θ_e air approaches the storm closely underneath the helical updrafts in the downshear and downshear-left quadrants. Evaporative cooling of precipitation falling out of the SBC, and into this unsaturated air, most likely drives the strong and persistent, vortex-scale downdrafts that cool and dry the TC's inflow layer.

In RMN10, evidence was presented that the formation of the SBC is connected to the tilt² of the
45 TC vortex. When subject to vertical wind shear, the tilt evolution of the TC vortex was shown to be governed to zero order by asymmetric-balance dynamics. Vortex tilt can thus be described in terms of a standing vortex-Rossby-wave (VRW) pattern with azimuthal and vertical wave-number 1 structure. Even though the tilt of the inner core is only 10 km–20 km, the VRW pattern associated with the tilt of the outer vortex extends outwards to radii of 150 km–200 km (Fig. 15a in RMN10)³. After vertical

¹In the current study, the term 'inflow layer' will refer to the layer of strong inflow associated with surface friction in the lowest 1 km - 1.5 km where the departure from gradient wind balance in the radial direction is generally a maximum (e.g., Bui et al. (2009), their Figs. 5 and 6 and accompanying discussion).

²In RMN10, the tilt is defined as the vector difference between the location of the vorticity centroids at 10 km and 1 km height.

³A considerable tilt of the outer parts of TC-like vortices with small tilt of the inner core has been noted previously by other authors also (see e.g. Fig. 6a in Jones (1995), Fig. 10 in Reasor et al. (2004)).

wind shear is suddenly imposed, the TC settles quickly (approx. within 3 h) into a quasi-equilibrium tilt direction that is to the downshear-left. Thus, the positive vorticity anomaly associated with the standing wave-number 1 VRW pattern is found downshear-left at upper levels and downshear-right at low levels. Frictional convergence associated with this positive low-level vorticity anomaly then provides forcing for the asymmetric convection within the SBC. The foregoing results suggest an important connection between the asymmetric-balance dynamics governing the tilt evolution of the vortex subject to vertical shear and the thermodynamic impact on the inflow layer.

The findings of RMN10 were derived from idealised numerical experiments following the setup of Bender (1997) and Frank and Ritchie (2001). In this experimental setup, a uni-directional vertical wind shear profile is imposed suddenly on a mature model TC. In an attempt to minimise complexity and to understand the fundamental processes, RMN10 deliberately chose a simple set of model parameterisations. As is the nature of results derived from such an idealised approach, uncertainties exist whether the newly proposed pathway operates in the real atmosphere. Although some preliminary observational support was offered in RMN10 a more comprehensive test of the new hypothesis with atmospheric data awaits future studies. Before undertaking such efforts we here survey and diagnose five additional numerical experiments with some modifications of the experimental setup to assess the robustness of RMN10's results.

1.2 Summary of numerical experiments

The numerical experiments in RMN10 employed a microphysics scheme that considers “warm cloud” processes associated with the collision-coalescence process only (hereafter termed “warm rain”). The current study considers experiments with ice microphysics also. Adding ice processes introduces the latent heat of fusion/ sublimation, new classes of hydrometeors with various fall speeds, and additional pathways to form precipitation. Details of the employed ice microphysic scheme are given in section 2.2. Arguably, the most significant of the above processes is the additional conversion of latent heat associated with the freezing and melting of ice. Ice microphysics produce stronger updrafts than a warm-rain scheme due to the additional latent heat release associated with freezing. In addition, the inclusion of precipitation in the form of ice may significantly enhance the formation and intensity of downdrafts (Srivastava, 1987).

Previous studies have shown that the inclusion of ice microphysics in numerical models may alter the radial profile of the swirling winds of TCs as compared to a warm-rain experiment (e.g. Fovell et al., 2009). In general, it is not well understood how these differences arise. Fovell et al. have proposed a mechanism that is based on the sedimentation of ice particles from the outflow anvil, the subsequent sublimation of these ice particles, and radiative feedback. In our suite of experiments, however, radiative processes are neglected. Nevertheless, potentially significant differences in the TC-vortex structure between the warm-rain and the ice microphysic experiments do arise, indicating that the mechanism suggested by Fovell et al. is not of primary importance. The

potentially important differences in the TC-vortex structure and their implication for the interaction with vertical wind shear will be discussed in some detail in section 3.1.

Recent studies have highlighted the importance of the representation of the planetary boundary layer in numerical models for vortex intensification and structure changes of simulated storms (Braun and Tao, 2000; Smith and Thomsen, 2010; Montgomery et al., 2010; Smith et al., 2011). The exchange coefficients for enthalpy, C_K , and momentum, C_D , play a most prominent role. They govern the energy extraction from the ocean surface and the dissipation of kinetic energy in the frictional boundary layer, respectively. In the framework of RMN10, the values of C_K and C_D can be expected to play an important role in the replenishment of the depressed boundary layer θ_e air while spiralling towards the inner-core updrafts. The replenishment rate is proportional to C_K^4 . The strength of the inflow within the frictional boundary layer is determined in part by C_D . Smaller values of C_D may lead to less radial inflow and thus to an *increase* of the replenishment time. Assuming that C_K is not changed, the replenishment of depressed inflow layer θ_e values is then *more complete* than for larger values of C_D . Based on these considerations, one would expect that the shear-induced flushing of the inflow layer with low- θ_e air has a more pronounced impact on TC intensity for smaller values of C_K and larger values of C_D . The interpretation of the importance of C_K and C_D in an axisymmetric theory for a TC in vertical wind shear by Tang and Emanuel (2010) is consistent with the foregoing considerations.

Considerable uncertainties exist about the values of C_K and C_D at the high wind speeds occurring in TCs. Deacon's formula for C_D was employed in RMN10 and the ratio of C_K/C_D was set to unity. Recent results derived from observational data (Black et al., 2007; Zhang et al., 2008) strongly indicate that Deacon's formula overestimates C_D at high wind speeds and that C_K/C_D is considerably less than unity. The observational data exhibit considerable scatter and are limited to wind speeds of marginal hurricane strength⁵. To address the likely overestimation of C_K and C_K/C_D in RMN10, we employ in this study values of C_K and C_K/C_D that are consistent with, but rather on the lower end of the range of values observed by Black et al. and Zhang et al.. Further details are provided in section 2.3.

The TCs considered in RMN10 were intense and rapidly intensifying at the time when the vertical wind shear profile was imposed. In the current study we will consider, inter alia, weaker, but still mature TCs. Finally, our additional experiments now exhibit various rates of intensification just before vertical wind shear is imposed. We did not, however, find a sensitivity of the subsequent TC evolution in vertical shear on this preceding intensification rate in our experiments. Thus, the various rates of intensification just before vertical wind shear is imposed will not be considered hereafter.

The next section provides an overview of the numerical model employed and the additional experiments performed, an expanded description of the ice microphysics scheme, and the values for

⁴The replenishment rate is proportional to the air-sea thermodynamic disequilibrium also.

⁵Some significant strides towards determining these coefficients at major hurricane wind conditions have been made recently by Bell (2010) as part of his Ph.D. dissertation.

the surface exchange coefficients. In section 3 we compare the evolution of the quintessential ingredients of RMN10’s newly proposed framework in the different numerical experiments. One experiment with ice microphysics is examined in further detail in section 4, including an estimate of the spindown time-scale of the simulated TC-vortex based on simple axisymmetric theory. Section 5 contains our conclusions.

2 Model setup and additional experiments

2.1 A brief model description

For the numerical experiments we employ the Regional Atmospheric Modeling System (RAMS), developed at Colorado State University (Pielke and Coauthors, 1992; Cotton and Coauthors, 2003).

The RAMS is a three-dimensional, non-hydrostatic numerical modeling system comprising time-dependent equations for velocity, non-dimensional pressure perturbation, ice-liquid water potential temperature (Tripoli and Cotton, 1981), and mixing ratios of total water and hydrometeors.

A standard first-order turbulence scheme developed by Smagorinsky (1963) is used for sub-grid-scale mixing, with modifications by Lilly (1962) and Hill (1974) that enhance diffusion in unstable conditions and reduce diffusion in stable conditions. For simplicity, radiative processes are neglected. The bulk aerodynamic formulas are used to calculate momentum and sensible and latent heat fluxes from the sea surface. The values of the exchange coefficients are given in subsection 2.3. We either employ a warm-rain microphysics scheme based on the scheme of Kessler (1969) or the RAMS standard ice microphysics scheme (subsection 2.2). A comprehensive description of RAMS, the surface interaction parameterisation, and the warm-rain scheme is given in RMN10.

2.2 Ice microphysics in RAMS

The RAMS ice microphysics scheme has eight water categories: vapour, cloud droplets, rain, pristine ice, snow, aggregates, graupel and hail (Walko et al., 1995; Meyers et al., 1997). The liquid phase categories, cloud droplets and rain, may be supercooled. Pristine ice, snow and aggregates are assumed to be completely frozen, whereas graupel and hail are mixed phase categories, capable of consisting of ice only, or a mixture of ice and liquid. All hydrometeor categories except cloud droplets are assumed large enough to fall. Cloud droplets and pristine ice are the only categories to nucleate from vapour. All other categories form from existing hydrometeors, but once formed may also grow by vapour deposition. Pristine ice crystals form from heterogeneous nucleation, homogeneous nucleation, and secondary production that involves splintering of riming crystals. The snow category is defined in RAMS as relatively large ice crystals, which have grown from the pristine ice category due to vapour deposition and may continue to grow by riming. Aggregates are defined as ice particles that have formed by collision and coalescence of pristine ice, snow and/or aggregates. Snow and aggregates retain their identity with moderate amounts of riming, but convert to graupel

155 if the amount of riming is large. In addition to forming by heavy riming graupel can also form by partial melting of snow or aggregates. Graupel is allowed to carry up to half its mass in liquid. If the percentage becomes larger, by either melting, riming or collection by rain, a graupel particle is re-categorised as hail. Hail is formed by freezing of rain drops or by riming or partial melting of graupel. Hail is allowed to be a large fraction liquid and converts to rain when completely liquid.

160 The hydrometeor size distribution in RAMS is represented by a generalised Gamma function. A user specified shape parameter controls the width of the distribution. Also, a scaling diameter is often specified for a one-moment scheme that is related to the mean diameter of the distribution, with the particular relation depending on the chosen spectral parameters. For this study a one-moment scheme is employed for all categories except cloud droplets and pristine ice. A scaling
165 diameter is specified and the number concentration is diagnosed using the predicted mixing ratio of the hydrometeor scheme.

A heat budget equation is formulated for rain, graupel, and hail hydrometeors. This allows the temperature of a hydrometeor to differ from that of the surrounding ambient air temperature due to latent heat release or absorption in the hydrometeor, and sensible heating by collisions with other
170 hydrometeors. The temperature of a hydrometeor often differs substantially from that of the air, which can significantly influence the rates of heat and vapour diffusion, as well as the amount of sensible heat transfer that occurs in coalescence of hydrometeors. Collision and coalescence of hydrometeors is governed by the stochastic equation derived by Verlinde et al. (1990).

Gravitational settling of hydrometeors causes them to fall relative to air. Terminal velocities in-
175 crease as a power of the droplet diameter, and are based on empirical data. Pristine ice has very small fall speeds. Snow crystals fall faster than pristine ice, but still relatively slowly. Aggregates are large crystals that have moderate fall speeds. Graupel and hail have high fall speeds. Sedimentation in RAMS uses a Lagrangian scheme to transport the mixing ratio from any given grid cell to a lower height in the vertical column, so that a proportion is transferred to the lower adjacent grid cell.

180 2.3 Modification of surface exchange coefficients

Deacon's formula for the dependence of the drag exchange coefficient C_D on wind speed is given by

$$C_D = 1.1 \times 10^{-3} + 4 \times 10^{-5} |V|^1, \quad (1)$$

with $|V|^1$ being the wind speed in ms^{-1} at the lowest model level (here: 49 m). In RMN10 we used
185 Deacon's formula and $C_K = C_D$. For reference, this formula furnishes values of the exchange coefficients of 1.5×10^{-3} , 2.1×10^{-3} , and 3.1×10^{-3} for 10 ms^{-1} , 25 ms^{-1} , and 50 ms^{-1} , respectively.

Zhang et al. (2008) found that 'The exchange coefficient of enthalpy flux shows no significant dependence on wind speed up to hurricane force with a value of 1.16×10^{-3} .' and that 'The average

ratio of the C_K/C_D values is 0.63, ...'. We therefore use these values and set

$$190 \quad C_K = 1.16 \times 10^{-3} = \text{constant} \quad (2)$$

and

$$C_K/C_D = 0.63. \quad (3)$$

Experiments that employ these values are referred to as CBLAST below. Note that Deacon's formula and $C_K/C_D = 1$ furnishes values of C_K and C_D that, for $|V|^1 = 50 \text{ ms}^{-1}$, are approx. 2.7 and 4.2

195 times higher, respectively, than the corresponding CBLAST values.

2.4 Summary of experiments

A summary of the experiments examined in this study is given in table 1. We refer to experiments that employ warm rain and Deacon's formula for the exchange coefficients (with $C_K/C_D = 1$) as RMN. The CBLAST experiments employ warm rain also. Experiments that include ice microphysics are

200 referred to as ICE. ICE experiments use Deacon's formula with $C_K/C_D = 1$.

The shear profile employed in this study has a cosine structure in the vertical with zero winds at the surface and maximum easterly winds at 12 km and above. We will follow the convention of the TC community to define vertical wind shear as the vector difference between the winds at upper and lower levels. Here, we use the vector difference between 12 km and the surface. The shear

205 magnitude is thus given in ms^{-1} . Unless otherwise noted, we will consider TCs in vertical wind shear with a magnitude of 15 ms^{-1} . The shear profile is imposed at a high intensity⁶ of 68 ms^{-1} , after the TCs have spun up in quiescent environment. These experiments are referred to as RMN₆₈, CBLAST₆₈, and ICE₆₈, respectively. The intensity at the time when shear is imposed will be referred to as "initial intensity" below. Experiment RMN₆₈ is the 15mps case of RMN10 and constitutes our

210 reference experiment.

We have performed experiments with a weaker initial intensity of 54 ms^{-1} also, referred to as RMN₅₄ and CBLAST₅₄. Furthermore, an ICE experiment has been performed with 10 ms^{-1} vertical shear (₁₀ICE₆₈) which will be compared briefly to the 10mps case of RMN10 (here: ₁₀RMN₆₈).

3 Assessing the robustness of the new framework

215 We shall focus on the key features of RMN10's new framework for intensity modification in vertical wind shear: the vortex tilt, the occurrence and location of the SBC, the flushing of the inflow layer with low- θ_e air, the ensuing depression of inflow layer θ_e , and the associated weakening of the TC. The general characteristics of these key feature will be found to be consistent in all experiments.

⁶The storm intensity metric in this study, as well as in RMN10, is the maximum azimuthally averaged tangential wind speed at 1 km height.

As can be expected, differences arise in the specific characteristics of these key features. For some
 220 of these differences it is very difficult to establish the causal link to the changes in the experimental
 setup. Most prominently, differences between the evolution of the TCs in RMN₆₈ and ICE₆₈ are
 partly due to the enhancement of downdrafts by ice microphysics (Sec. 3.7) but very likely also
 due to changes in the radial profile of the swirling winds at the time when vertical wind shear is
 imposed. Disentangling the individual contributions requires a more complete understanding of the
 225 processes at work, and extended numerical experimentation and diagnostic analyses, preferably in an
 ensemble-based framework. A more comprehensive examination of such differences is thus deferred
 to future research.

3.1 Importance of the radial profile of the swirling winds

3.1.1 Impact on the resiliency of TC-like vortices

230 It is generally believed that the presence of vertical wind shear increases the interaction of a TC with
 dry environmental air (Riemer and Montgomery, 2011, and references therein). Based on a simple
 kinematic model, Riemer and Montgomery (2011) argue that a TC with a broad radial profile of the
 swirling winds should have a stronger ability to isolate itself from the detrimental interaction with
 dry environmental air than a smaller-scale TC. Furthermore, the radial profile of the swirling winds
 235 has a profound impact on the *dynamic* resiliency of TC-like vortices, i.e. the ability to maintain
 vertical coherence in the presence of differential advection by the vertical shear flow (e.g. Jones,
 1995; Reasor et al., 2004). These studies investigated the resiliency of initially barotropic, dry
 vortices and are reviewed briefly below.

Jones (1995) examined vortex evolution in terms of the formation and subsequent interaction of
 240 potential vorticity (PV) anomalies. PV anomalies were defined as deviations from the azimuthal
 mean. Due to the differential advection by the vertical shear flow, PV anomalies representing the
 tilt of the vortex form at lower and upper levels. These anomalies mutually interact through the
 vertical penetration of their “induced” quasi-horizontal circulations, causing the vortex to precess.
 This precession helps the vortex to counteract the differential advection by the vertical wind shear.
 245 In general, the vertical interaction of PV anomalies depends on the Rossby penetration depth. The
 penetration depth increases with the strength of the background rotation and with the horizontal scale
 of the interacting anomalies. Jones noted that it is not entirely clear how to quantify the penetration
 depth for a tilted TC-like vortex but concluded that intense and broad vortices are more resilient than
 their weaker, smaller-scale counterparts.

250 Reasor et al. (2004) re-visited the problem of vortex resiliency and re-alignment using VRWs con-
 cepts and models. Their results are in qualitative agreements with Jones’s finding that vortex (and
 environment) parameters that increase the penetration depth improve the resistance of a vortex to
 tilting by an imposed vertical shear flow. In addition, Reasor et al. demonstrated that vortex preces-

sion is not the only element in the resiliency of TC-like vortices. An inviscid damping mechanism of the vortex-tilt mode exists, associated with PV mixing at the critical radius of the near-discrete VRW that represents the vortex tilt. The critical radius is typically located in the “skirt” region of the vortex, i.e. in the region of small PV values outside of the high-PV values in the inner core (approx. outside 50 km - 70 km in Fig. 1(a)). The inviscid damping mechanism depends on the radial gradient of the skirt PV at the critical radius (Schecter and Montgomery, 2003). Inviscid damping, and thus re-alignment of the vortex, occurs when the radial PV gradient in this region is negative. The damping rate increases with the magnitude of the gradient. For a positive skirt-PV gradient a tilt instability may occur. Reasor et al. ’s results clearly demonstrate that vortex resiliency may crucially depend on the radial profile of the swirling winds.

The radial profile of the swirling winds has been confirmed to play a role in the intensity evolution of vertically sheared TCs in idealised, moist numerical experiments (Wong and Chan, 2004). In these experiments the weakening of smaller-scale TCs is found to be more pronounced than that of their broader-scale counterparts. Wong and Chan based their interpretation of this difference in the intensity evolution on the results of Jones (1995) derived from dry TC-like vortices. To us, however, it is not clear what the underlying processes are that govern the intensity evolution in Wong and Chan’s experiments. In particular, the role of *moist* processes and/or the associated secondary circulation remain unclear.

In the real atmosphere, an indication of a higher susceptibility of smaller-scale TCs to vertical shear has been found by DeMaria (1996) based on a regression analysis.

3.1.2 Diagnosed radial vortex structure in our experiments

Because the radial profile of the swirling winds may play a prominent role in the evolution of TCs in vertical wind shear, we begin the examination of our experiments with the comparison of the vortex structure at the time when vertical wind shear is imposed. The radial, azimuthal mean profiles of the swirling winds at this time are illustrated in Fig. 1. In CBLAST₆₈, the radius of maximum winds (RMW) is found at 40 km (Fig. 1(a)). The vorticity maximum is $35 \times 10^{-4} \text{ s}^{-1}$ at a radius of 20 km. This vortex structure is very similar as in RMN₆₈ (shown in Fig. 4 in RMN10)⁷. For the weaker TC in CBLAST₅₄, the vorticity structure outside a radius of 35 km is almost identical to CBLAST₆₈. Inside this radius, vorticity is virtually constant with a value of approx. $20 \times 10^{-4} \text{ s}^{-1}$. The corresponding RMW is found at 48 km. The initial radial structure of the TC in RMN₅₄ is very similar (not shown).

The vorticity structure of the TC in ICE₆₈ exhibits some notable differences as compared to the warm-rain experiments CBLAST₆₈ and RMN₆₈. The vorticity maximum is found inside a radius of 10 km with values of $55 \times 10^{-4} \text{ s}^{-1}$, i.e. approx. 60 % higher than in CBLAST₆₈. Radially outside

⁷A potential impact of barotropic instability associated with the reversal of the radial vorticity gradient in the inner core on the intensity evolution of the sheared TCs in our experiments is arguably negligible (see Sec. 3.1 in RMN10).

of this maximum, the high vorticity values decrease rapidly. Corresponding to the smaller radius of maximum vorticity, the RMW is smaller (located at 30 km) than in CBLAST₆₈ and RMN₆₈ also.

As discussed above, the resiliency of the TC vortex may crucially depend on the gradient of (potential) vorticity at the critical radius of the (near-discrete) VRW mode that represents the vortex tilt. The critical radius is found where the azimuthal propagation of this VRW, i.e. the vortex precession, equals the speed of the swirling winds. The precession rate, and thus the critical radius, in our experiments is difficult to determine. After the vortices have re-aligned, a short precession period of 2 h - 3 h is indicated in all experiments (see Fig. 4 below⁸). Using the values of the axisymmetric swirling winds at 1 km, as depicted in Fig. 1(a), our rough estimate of the critical radius is then 50 km - 90 km.

In ICE, the vorticity gradient is near-zero between 50 km and 65 km while in CBLAST₆₈ and RMN₅₄ the gradient is negative and of large magnitude (Fig. 1(b)). Between 65 km and 100 km the radial vorticity profiles are broadly similar. At larger radii (not shown) the average vorticity gradient is *positive* in RMN₅₄ (between 120 km and 200 km) and ICE (between 150 km - 200 km). In CBLAST, in contrast, vorticity decreases monotonically out to 200 km radius. It is questionable, however, whether these differences at a radius considerably larger than our estimate for the critical radius play a role for the TC-vortex evolution in our experiments.

From the discussion in this subsection it is clear that differences in the evolution of the TCs when interacting with the vertical shear flow in the various experiments potentially arise due to differences in the radial vorticity profiles *before* shear is imposed. The weaker vortices in RMN₅₄ and CBLAST₅₄, as well as the smaller-scale vortex in ICE₆₈, can be expected to be more susceptible to tilting than their stronger, respectively broader-scale counterparts in RMN₆₈ and CBLAST₆₈. In ICE₆₈, the susceptibility to tilting is potentially enhanced by the near-zero gradient of the skirt vorticity inside of 65 km. In Sec. 3.3 it will be shown that the tilt evolution is broadly consistent with these expectations. Furthermore, based on the results of Wong and Chan (2004), one can expect a more pronounced intensity decrease in ICE₆₈ based on the radial scale of the vortex alone. The latter point needs to be borne in mind when attempting to attribute differences between ICE₆₈ and RMN₆₈ to their different representation of cloud microphysical processes.

3.2 Intensity evolution

An overview of the intensity evolution in our experiments is presented in Fig. 2. First, a brief account of the intensity evolution in a quiescent environment is given. The intensity evolution in RMN is described in some detail in RMN10. In CBLAST (Fig. 2(a)), the incipient TC slowly intensifies to 25 ms⁻¹ in the first 20 h. A period of rapid intensification ensues during which the TC reaches an intensity of 53 ms⁻¹ at 33 h. In the subsequent 20 h the TC consolidates and slightly intensifies

⁸Note that the temporal resolution of the data in Fig. 4 is 1 h. It is thus most likely that the vortex precession is undersampled.

to 56 ms^{-1} . Then, the TC continues to intensify at a moderate rate until it reaches a quasi-steady intensity of 80 ms^{-1} - 85 ms^{-1} at 80 h. In ICE (Fig. 2(b)), the TC intensifies to approx. 40 ms^{-1} at 30 h after a short gestation period. Very rapid intensification ensues and the intensity reaches
 325 90 ms^{-1} at 50 h. The maximum, quasi-steady intensity of 95 ms^{-1} - 100 ms^{-1} is reached around 72 h.

In all experiments, intensity decreases after vertical wind shear is imposed. As in RMN10, all TCs are resilient to the detrimental impact of vertical wind shear. After a period of weakening the TCs re-intensify; particularly rapidly in RMN₅₄⁹. The re-intensification process in this experimental
 330 configuration is discussed in some detail in RMN10 (their Sec. 6).

To facilitate the intercomparison of the intensity evolution in the various experiments, the intensity difference to the respective no-shear experiment is presented in Figs. 2(c) and 2(d). Time 0 h in these figures denotes the time when vertical wind shear is imposed in the respective experiment. In all warm-rain experiments (Fig. 2(c)), the characteristics of this *relative* weakening are similar in
 335 the first 20 h. The only exception being that the weakening in CBLAST₅₄ is delayed by 4 h. This detail will be examined in section 3.6.2. After 20 h, the experiments with weaker TCs (RMN₅₄ and CBLAST₅₄) continue to weaken. In contrast, CBLAST₆₈ maintains its intensity difference for the next 20 h and RMN₆₈ re-intensifies. Based on these plots alone it might therefore be concluded that the weaker storms are more susceptible to shear. However, this is not necessarily the case here.
 340 Note that 20 h after shear is imposed in RMN₅₄ and CBLAST₅₄ the respective reference TCs in quiescent environment are still rapidly intensifying. In contrast, the reference TCs in RMN₆₈ and CBLAST₆₈ intensify only slowly 20 h after vertical wind shear is imposed. Thus, the differences in the *relative* intensity evolution partly arise due to the differences in the contemporaneous evolution of the reference TC. This brief discussion illustrates one of the inevitable challenges to interpreting
 345 different TC simulations in vertical wind shear.

The comparison of the RMN and ICE shear experiments is less complicated because the intensity evolution of the reference runs in quiescent environment is similar (Figs. 2(b) and 2(d)). A comparison of the intensity evolution in ₁₀ICE₆₈ and ICE₆₈, respectively, clearly shows that the TCs in the ICE experiments are more susceptible to shear than their counterparts in the warm-rain experiments.
 350 The differences between the relative weakening in ₁₀ICE₆₈ and ₁₀RMN₆₈, i.e. the experiments with imposed vertical shear of 10 ms^{-1} , is on average approx. 10 ms^{-1} before 16 h, and on average approx. 5 ms^{-1} between 16 h and 36 h (Figs. 2(d)). After this time, it is no longer evident that the weakening in ₁₀ICE₆₈ is more pronounced than in ₁₀RMN₆₈.

For 15 ms^{-1} shear, the difference in the intensity evolution between the ice and warm-rain experiments is striking. The maximum relative weakening in ICE₆₈ is -60 ms^{-1} (Figs. 2(d)). The TC reaches a minimum intensity of 35 ms^{-1} (Figs. 2(b)). For RMN₆₈, the respective values are -

⁹Because the focus of this study is on the structural changes of the TCs during the weakening phase, this experiment was discontinued at 84 h.

25 ms⁻¹ and 63 ms⁻¹. Notwithstanding this distinct intensity evolution, it will be shown below that the structural changes in ICE₆₈ and RMN₆₈ are very similar. In particular, the pronounced weakening in ICE₆₈ is associated with by far the most significant depression of inflow layer θ_e (sections 3.6 and 4.1). The evolution in ICE₆₈ is thus consistent with the results of RMN10, i.e. the shear-induced frustration of inflow layer θ_e plays a crucial role in the intensity evolution in ICE₆₈. Furthermore, it will be argued in section 4.2 that this rapid weakening is consistent with the frictional spindown of an axisymmetric vortex due to a significant reduction of the inner-core convective mass flux.

3.3 Evolution of vortex tilt

Following RMN10, the tilt of the vortex is defined here as the vector difference between the vorticity centroids at 10 km and 1 km height. Details on the calculation of the vorticity centroids are given in RMN10.

A detailed examination of the tilt evolution in RMN₆₈ was given in section 5.1 of RMN10. There, evidence was presented that the tilt evolution is governed to zero order by asymmetric-balance dynamics. The TC in RMN₆₈ settles into a quasi-equilibrium tilt direction to the downshear-left (south) shortly after shear is imposed (approx. within 3 h). A quasi-equilibrium tilt direction may be achieved when the cyclonic precession of the tilted vortex cancels the differential advection by the vertical shear flow. This quasi-equilibrium vortex tilt can be described in a first approximation by the balanced dynamics of an initially barotropic, dry TC-like vortex (Jones, 1995; Reasor et al., 2004).

In RMN₆₈, the tilt amplitude decreases while maintaining the quasi-equilibrium tilt direction. The TC virtually re-aligns within approx. 24 h, i.e. after this time the tilt amplitude is comparable to the tilt amplitude of the TC in the no-shear benchmark experiment (see Fig. 5 in RMN10). Once the tilt amplitude has decreased considerably, a high variability in the tilt direction ensues, indicative of a high-frequency precession of the vortex.

Figures 3 and 4 demonstrate that the general characteristics of the tilt evolution are similar in all of our experiments in the first 24 h - 30 h after vertical wind shear is imposed. All TCs are resilient during this time and the tilt direction is predominantly to the South (180°). In CBLAST₆₈, the maximum tilt magnitude, as well as the temporal tilt evolution, is very similar to that of RMN₆₈. The only exception being that the local maximum at 23 h is more pronounced and, thereafter, the tilt magnitude remains 3 km - 5 km larger. As can be expected from the discussion in Sec. 3.1, the weaker TCs in RMN₅₄ and CBLAST₅₄ clearly exhibit a larger tilt magnitude in the first 24 h than the more intense TCs in RMN₆₈, CBLAST₆₈, and ICE₆₈. Maximum tilt amplitudes reach 40 km in RMN₅₄ and 30 km in CBLAST₅₄. Both TCs eventually re-align.

The most striking feature in the tilt evolution is the disruption of the TC vortex after 30 h in ICE₆₈ (Fig. 3). Until this time the TC tends to re-align slowly: the local tilt maximum and minimum at 25 h and 30 h, respectively, are smaller than their respective predecessors at 9 h and 15 h. At 30 h, intensity has decreased by over 30 ms⁻¹ as compared to the time when vertical wind shear is

imposed and has reached the smallest absolute value in all experiments (approx. 35 ms^{-1} , Fig. 2). Based on the discussion in Sec. 3.1, it is plausible that the significantly weakened TC can no longer
 395 withstand the differential advection associated with the vertical wind shear. Note that the distinct weakening in the first 20 h precedes the disruption of the TC by more than 10 h. After 30 h, the TC remains as a coherent entity with smaller vertical extent: the tilt as inferred from the vorticity centroid at 9 km height instead of 10 km height does not exceed 35 km (not shown). Arguably, the survival as a vertically less extensive system allows for the rapid re-intensification of the TC after
 400 the inflow layer θ_e values have recovered (Sec. 4.1).

The tilt magnitude in $_{10}\text{ICE}_{68}$ remains below 10 km and quickly reduces to values smaller than 6 km after 12 h. Despite this small tilt magnitude a southerly tilt direction is preferred until late in the experiment. Although the evolution of the tilt magnitude is similar in $_{10}\text{RMN}_{68}$, the tilt direction in $_{10}\text{RMN}_{68}$ exhibits more variability after 30 h when the tilt magnitude is small (not shown).

405 3.4 SBC formation and downward flux of low- θ_e air into the inflow layer

A metric for the downward flux of low- θ_e air into the inflow layer (DFX) has been defined in RMN10 (their Sec. 4.2.1) as

$$\text{DFX} \equiv w_- \theta'_e, \quad (4)$$

where w_- denotes downward vertical motion and θ'_e the perturbation from the azimuthal mean of
 410 θ_e . DFX is evaluated at 1.5 km, the approximate top of the axisymmetric inflow layer.

The time-averaged structure of the SBC, represented by low-level upward motion, and the distribution of DFX shortly after the time when vertical wind shear is imposed is depicted in Fig. 5. In this early stage of the evolution, the general structure of the SBC and the distribution of DFX is consistent in all experiments. The SBC forms in the downshear-right quadrant extending radially
 415 outwards to 150 km - 200 km. Small to moderate DFX values occur over a broad, banded region downwind of the SBC, from the downshear quadrant through downshear-left, and into the upshear quadrant. In all experiments, azimuthal vertical cross-sections (as Fig. 18 in RMN, not shown here) indicate that the associated downdrafts form underneath the helical updrafts of the SBC.

It is of interest to note that the SBCs in RMN_{54} , ICE_{68} , and $_{10}\text{ICE}_{68}$, respectively, extend further
 420 into the upshear quadrant than their counterparts in RMN_{68} , CBLAST_{68} , and CBLAST_{54} . In the former experiments, the tilt direction at early times exhibits a greater downshear (westerly) component than in the latter experiments (Fig. 4). The low-level vorticity anomaly associated with the tilted vortex can thus be expected to extend into the upshear quadrant. RMN10 have shown evidence that frictional convergence due to the low-level vorticity anomaly associated with the tilted vortex
 425 contributes to the forcing of the SBC. The correlation of the SBC formation location and the tilt direction in our experiments presented here provides further support for RMN10's interpretation.

A distinct maximum of DFX is found in the upshear quadrant close to the eyewall. This maximum is most pronounced in the ICE experiments (Fig. 5(e) and 5(f)). In RMN10, this DFX maximum

was not given special attention. A pronounced maximum in the upshear quadrant occurred in the
 430 20mps case of RMN10 (their Fig. 10(d)). RMN10 further noted a localized region of downdrafts in
 the upshear region close to the eyewall after the TCs in the 10mps and 15mps cases have re-aligned
 (their Fig. 11(a) and associated discussion).

The DFX maximum is located at the downwind end of the banded region of positive DFX values.
 A pronounced θ_e depression is found at the top of the inflow layer in this region (not shown). Large,
 435 negative values of θ'_e therefore contribute to high values of DFX (Eq. 4). Downward motion into
 the inflow layer, however, is particularly strong in this region also (not shown). A preliminary ex-
 amination of the distributions of vertical motion, hydrometeors, and θ_e suggests that the downdrafts
 close to the eyewall may form by evaporation of precipitation falling out of the tilted eyewall. To us,
 however, it is not clear whether the more pronounced localized maximum in the ICE experiments is
 440 solely due to the inclusion of ice microphysics or to what extent the differences in the radial structure
 of the TC vortex contribute. Clearly, more research is needed to clarify the formation mechanism of
 these downdrafts and the relative importance of the confined DFX maximum and the broad region
 of moderate DFX for TC intensity evolution.

3.5 Vortex-tilt induced dynamic instability?

445 A non-linear, Kelvin-Helmholtz type instability in the inner core of a tilted, dry TC-like vortex has
 been found in a numerical experiment by Reasor et al. (2004, their Sec. 5a). In their experiment,
 this instability contributed to enhanced localized, three-dimensional mixing. Such mixing is one
 pathway to dissipate kinetic energy in the TC's inner core. The role of this mixing for the intensity
 evolution of TCs in vertical wind shear is hitherto unexplored.

450 The necessary condition for such an instability is that the gradient Richardson number, $\mathcal{R}$, drops
 below unity (Abarbanel et al., 1986). Here, $\mathcal{R}$ is calculated as

$$\mathcal{R} = N^2 / ((du/dz)^2 + (dv/dz)^2), \quad (5)$$

where N is the (dry) vertical static stability, and u and v are the radial and tangential wind compo-
 nents¹⁰, respectively. The tilt of the vortex may lead to a high *local* vertical shear of the swirling
 455 winds in the inner core. Thus, in such regions, the gradient Richardson number may reach small
 values.

In all of our (moist) TC experiments, the potential for a Kelvin-Helmholtz type instability and
 the associated three-dimensional, turbulent mixing in the inner core is an element of vertical-shear
 interaction. Underneath the eyewall and the SBC, $\mathcal{R} < 1$ is an ubiquitous feature within the layer of
 460 strong, frictionally-driven inflow (not shown). Above this inflow layer, localized regions of $\mathcal{R} < 1$
 occur, at least temporarily, in all experiments presented in this study within the first 6 h after shear

¹⁰Normally, the definition of $\mathcal{R}$ involves the zonal and meridional wind components. Our calculation of $\mathcal{R}$ is equivalent to
 this definition.

is imposed. These regions are located within the eyewall in the downshear-left to upshear quadrant (exemplified in Fig. 6 for RMN₆₈ and ICE₆₈). This feature is most pronounced in RMN₆₈ and least pronounced in RMN₅₄, as might be expected for the weaker vortex in RMN₅₄. The regions of $\mathcal{R} < 1$ are frequently located radially inwards (within 20 km - 30 km) of regions of high DFX (exemplified in Fig. 6). Due to this proximity, it seems justified to hypothesize that enhanced mixing associated with the tilt-induced instability locally modifies the downward flux of low- θ_e air into the inflow layer. A quantitative diagnostic of this mixing process is deferred to future work.

3.6 Inflow layer θ_e depression

3.6.1 θ_e depression outside of the eyewall

A snapshot of the height-averaged inflow layer θ_e distribution after 5 h into the shear experiments is presented in Fig. 7. As can be expected from the DFX patterns discussed above, the inflow layer θ_e distribution is similar in all experiments at this time: Low- θ_e air wraps cyclonically from the downshear quadrant into the upshear quadrant. Also evident in all cases is the pronounced wave-number 1 signature of the SBC in the vertical motion field at low levels above the inflow layer.

To facilitate the intercomparison of the experiments we consider now the deviation from the axisymmetric mean θ_e distribution at the time when shear is imposed in the respective experiment (Fig. 8). This figure depicts time-averaged values from 4 h - 9 h after shear is imposed. In all cases the inflow layer θ_e values outside of the inner-core updrafts are significantly depressed. A depression of up to 15 K can be found in RMN₆₈, RMN₅₄, and ICE₆₈. Minimum θ_e values are generally found to the southeast of the centre (upshear to downshear-left). This location is consistent with the DFX maximum in this region and the continuous depression of θ_e values along the spiralling inflow leg, as hypothesised by RMN10 (their Fig. 11a). The inflow layer θ_e depression extends into the downshear-right quadrant also, outwards to a radius of 100 km - 150 km. In the absence of downward flux of low θ_e in this region (cf. Fig. 5) the inflow layer θ_e values gradually recover while air parcels circle from the upshear quadrant to the upshear-right quadrant.

The inflow layer θ_e depression outside of the eyewall in the CBLAST experiments is less pronounced than in the comparable RMN experiments. While the minima in RMN exceed -13 K, the minima in CBLAST have values of approx. -10 K. This less pronounced θ_e depression is consistent with smaller average DFX in CBLAST₆₈ and CBLAST₅₄ as compared to RMN₆₈ and RMN₅₄, respectively (Fig. 5). The smaller DFX values in CBLAST are associated with a weaker general downdraft activity (see section 3.7 and Fig. 10 for supporting evidence).

In the ICE experiments, the spatial pattern of the θ_e depression is radially more confined than in the warm-rain experiments. This is consistent with the DFX pattern. As discussed at the end of Sec. 3.4, it is not evident to us to what extent this greater radial confinement can be attributed to differences in the cloud microphysics or to differences in the radial structure of the TC vortices.

3.6.2 θ_e depression underneath the inner-core updrafts

An axisymmetric view of the inflow layer and eyewall θ_e distribution is presented in RMN10. In this axisymmetric view a tongue of low- θ_e air effectively intrudes into the inflow layer from above and radially inwards towards the eyewall. The θ_e values of air rising in the eyewall of the sheared TCs are several degrees smaller than in the experiment without vertical shear (Fig. 9 in RMN10). The same general characteristics of the axisymmetric inflow layer and adjacent eyewall structure are found in the additional experiments considered in this study (not shown). When viewed from the simplified perspective of an idealised Carnot-cycle a weakening of the sheared TCs can thus be expected. As noted in RMN10, however, it is an open question whether an axisymmetric viewpoint is sufficient in the presence of pronounced wave-number 1 asymmetries in the inflow layer θ_e distribution and the eyewall updrafts of a TC in vertical wind shear.

In the present study we complement the axisymmetric view by the examination of the horizontal distribution of inflow layer θ_e and low-level eyewall updrafts. For the following discussion the eyewall updrafts are defined as the contiguous region within the 1 ms^{-1} vertical velocity isotach near the centre in Fig. 8. We consider the θ_e values within this region to be a good approximation for the θ_e values of air rising out of the boundary/ sub-cloud layer in the eyewall updrafts. Upon examining the results, it is obvious that in all cases the inner-core updrafts exhibit a pronounced wave-number 1 asymmetry and that the eyewall is not closed.

By visual inspection we estimate the average θ_e depression underneath the eyewall (averaged from 4 h - 9 h) to be 0 K for CBLAST₅₄, 2 K - 3 K for RMN₆₈ and CBLAST₆₈, 3 K - 5 K for RMN₅₄ and ₁₀ICE₆₈, and 6 K - 7 K for ICE₆₈. These values correlate well with the intensity evolution of the respective TCs. The TC in CBLAST₅₄ does not weaken until 7 h after shear is imposed (Fig. 2(c)). The TCs in RMN₆₈ and CBLAST₆₈ show a very similar weakening in the first 12 h while RMN₅₄ and ₁₀ICE₆₈ exhibit slightly faster weakening rates. The pronounced and rapid weakening of the TC in ICE₆₈ is associated with the most pronounced depression of θ_e underneath the eyewall. This correlation supports RMN10's result that the intensity evolution of resilient TCs in vertical shear is governed to first order by the systematic depression of θ_e in the inflow layer.

The inflow layer θ_e depression *outside* of the eyewall in CBLAST₆₈ is less pronounced than in RMN₆₈. The θ_e depression underneath the eyewall, however, is very similar in both experiments. Consistently, the intensity decrease is very similar in CBLAST₆₈ and RMN₆₈ in the first 12 h. It can therefore be inferred that the replenishment of inflow air spiralling towards the eyewall is more complete in RMN than in CBLAST. As discussed in the Introduction, the smaller value of C_D in CBLAST may lead to weaker frictional inflow as compared to RMN and thus to a longer replenishment time. Here, this effect of a smaller C_D value is apparently overruled by the reduced extraction of heat from the ocean surface due to a smaller value of C_K . It is difficult to examine this aspect in RMN₅₄ and CBLAST₅₄ because the θ_e depression underneath the eyewall is different at this early time in the experiment.

The replenishment time of air with depressed θ_e values may depend considerably on the *azimuthal* location. The radial velocity averaged over the lowest 1 km exhibits a pronounced wave-number 1 asymmetry in all experiments (Fig. 8). In the downshear semicircle the maximum height-averaged radial inflow is approx. 20 ms^{-1} while in the upshear semicircle the height-averaged radial velocity is very small or is even directed *outwards* (e.g. in RMN₅₄ (Fig. 8(c))). Figure 8 indicates that the bulk of the depressed inflow layer θ_e spirals around the centre before entering the inner core updrafts in the downshear-right quadrant (e.g. Figs. 8(a) and 8(f)). In RMN₅₄ and ICE₆₈, in contrast, it is indicated that low- θ_e air from the downshear quadrant enters the eyewall updrafts on a much more direct pathway in the downshear to downshear-left quadrant also (Figs. 8(c) and 8(e)). The replenishment of inflow layer θ_e along this more direct pathway can be expected to be less complete than along the longer inflow spiral. In the presence of a pronounced wave-number 1 asymmetry of the inflow, it stands to reason that the (azimuthal) *location* of the flushing of the inflow layer with low- θ_e air may be of importance for the intensity evolution also, and not only the magnitude of the θ_e depression in the azimuthal mean.

3.7 Vertical motion characteristics

The formation of the SBC and the associated downdrafts that flush low- θ air into the inflow layer are two central aspects of RMN10's framework. We here examine the general characteristics of vertical motion in our suite of experiments using so-called contoured frequency by altitude diagrams (CFADs Yuter and Houze, 1995). These diagrams depict the frequency of the occurrence of vertical motion of a given magnitude, here binned in 0.5 ms^{-1} intervals, within a given region and at a given altitude. It is very difficult to focus specifically on the SBC and on regions where shear-induced downdrafts form. We therefore consider all vertical motion within a radius of 160 km.

A comparison of the RMN and ICE experiments is presented in Fig. 9. Without vertical wind shear (Figs. 9(a) and 9(b)) strong up- and downdrafts occur more frequently in the ICE experiment. Under the influence of vertical shear (Figs. 9(c) and 9(d)), the frequency distribution broadens considerably below 5 km - 6 km as compared to the respective no-shear experiment. For both, the warm rain and ice microphysics configurations, vertical wind shear increases the frequency of the strongest up- and downdrafts at midlevels and below. At upper levels the increase of downdraft frequency is less pronounced and the frequency of strong updrafts tends to decrease, except for the strongest updrafts in ICE₆₈. It is evident also that strong downdrafts below 5 km occur considerably more frequently in ICE₆₈ than in RMN₆₈ (cf. Figs. 9(c) and 9(d)). The more pronounced downdraft activity in the ICE experiments is consistent with the tenet that the cooling associated with the melting of ice particles may initiate or strengthen existing downdrafts (Srivastava, 1987).

In CBLAST, the imposed vertical wind shear leads to a broadening of the frequency distribution also (not shown). The differences between CBLAST and RMN experiments are less pronounced than between ICE and RMN. The differences are depicted in Fig. 10 as the ratio of the frequen-

570 cies in RMN₆₈ and CBLAST₆₈ (Fig. 10(a)) and RMN₅₄ and CBLAST₅₄ (Fig. 10(b)). The results are very similar for RMN and CBLAST without imposed vertical shear (not shown). Apparently, the frequency of the strongest downdrafts is more than 275 % greater in RMN than in CBLAST. Strong updrafts tend to be more frequent in RMN also, in particular so in RMN₅₄ as compared to CBLAST₅₄.

575 Differences in the thermodynamic properties of the ambient air in which downdrafts occur may contribute to the observed differences in downdraft activity. The strength of a downdraft depends, inter alia, on the buoyancy difference between the descending air parcel and the ambient air along the parcel's downward path. A vertically integrated measure of this buoyancy difference is the downdraft convective available potential energy (DCAPE, Emanuel, 1994, his Sec. 6.3). The derivation of
580 DCAPE assumes the following two-stage process. First, evaporation of precipitation cools an air parcel isobarically through a wet-bulb process, i.e. until saturation is reached. Then, the parcel descends pseudo-adiabatically with just enough evaporation to keep the parcel saturated.

We have calculated DCAPE using the azimuthal mean soundings at the time when shear is imposed. Because it is not entirely clear which radius is most appropriate to examine the downdrafts
585 underneath the SBC we considered a number of different radii and radial averages between 60 km and 150 km (not shown). For all of these regions, a clear relationship between the DCAPE values and the downdraft activity, respectively the downward flux of low- θ_e air into the inflow layer, is not found. In particular, DCAPE values below 500 hPa in CBLAST₅₄ are higher than in RMN₅₄, *in contrast* to the more pronounced downdraft activity in RMN₅₄.

590 Apparently, consideration of solely thermodynamic properties of the air in which the downdrafts occur is insufficient to explain the observed differences in downdraft activity. We propose the following alternative explanation that focuses on the dynamic coupling of the convection with the frictional boundary layer. First, we note that the weaker downdrafts in CBLAST₆₈ and CBLAST₅₄ are associated with weaker updraft activity. This may be expected because a prominent downdraft formation
595 mechanism is the evaporation of precipitation that is formed in the updrafts and falls into unsaturated air. Both the smaller value of C_D and C_K in CBLAST may contribute to weaker updrafts. Ascent out of the boundary layer forced by frictional convergence, either underneath the eyewall or underneath the vorticity anomaly associated with the tilt of the outer vortex (RMN10, their Fig. 17), can be expected to decrease for decreasing C_D . For example, in simple Ekman pumping theory the vertical
600 motion at the top of the boundary layer is proportional to $\sqrt{C_D}$ (e.g. Holton, 2004, his Eq. 5.38). The smaller value of C_K in CBLAST decreases the rate by which heat is extracted from the ocean surface. These reduced surface fluxes destabilise the boundary layer in CBLAST to a lesser extent than in RMN. Less vigorous updrafts can be expected to occur in such a more stable stratification. Our foregoing argument is supported by the results of the CBLAST and RMN no-shear experiments
605 (not shown). Without vertical shear, the activity of *transient* rain bands and the associated localized downward flux of low θ_e into the inflow layer in CBLAST are also less pronounced than in the

no-shear RMN experiment.

In all experiments, vertical wind shear increases the frequency of moderate to strong downdrafts. It is clear that CBLAST has the lowest frequency of strong downdrafts and that ICE has the highest frequency. The downdraft activity as seen in the CFADs is consistent with the magnitude of the inflow layer θ_e depression outside of the eyewall (cf. Fig.8). Therefore, the examination of the CFADs provides additional support for the hypothesis that the distinct depression of the inflow layer θ_e values are caused by downdrafts induced by the imposed vertical wind shear.

4 A closer look at the ICE₆₈ experiment

The weakening of the TC in ICE₆₈ is much more pronounced than in the comparable warm-rain experiments RMN₆₈ and CBLAST₆₈. In the previous sections it has been shown that the general structural changes in the first 20 h are nevertheless very similar in all experiments. We now take a closer look at ICE₆₈ to further confirm that the intensity evolution in this case is consistent with the shear-induced thermodynamic modification of the inflow layer. First, the inflow layer θ_e distribution is examined during periods of distinct intensity changes. Then, we will provide evidence based on axisymmetric spindown theory that the rapid weakening in the first 20 h is consistent with the spindown of the TC vortex due to a significant decrease of the inner core convective mass flux.

4.1 Intensity evolution and inflow layer θ_e

It has been shown in section 3.6 (Fig. 7(e)) that the rapid weakening is associated with a significant depression of inflow layer θ_e soon after shear is imposed. Here we emphasize that a significant part of the depressed θ_e -air apparently intrudes from the downshear quadrant into the inner-core updrafts on a direct pathway (Fig. 11(a), at 7 h). Over half of the area underneath the inner-core updrafts at this time has θ_e values lower than 355 K, as compared to approx. 363 K before shear is imposed (not shown). Along with this significant frustration of the θ_e values in the inner-core region the vertical mass flux at midlevels (5 km) decreases in the first 10 h by 60 % from $50 \times 10^6 \text{ kg s}^{-1}$ to approx. $20 \times 10^6 \text{ kg s}^{-1}$ (not shown).

We now consider the two distinct, short-lived local intensity maxima at 22 h and 44 h, prominent features of the intensity evolution in ICE₆₈ (Fig. 2(b), the maxima are found at 64 h and 86 h because this figure includes the 42 h spinup period). Both periods of temporary re-intensification are preceded by relatively high inflow layer θ_e values in the downshear to downshear-right quadrants while the very pronounced θ_e depression at these times is mostly confined to the upshear semicircle (at 20 h (Fig. 11(b)) and at 40 h (Fig. 11(d))). Due to the distinct wave-number 1 inflow asymmetry discussed previously (Fig. 8), it can be expected that, at these times, the eyewall updrafts are fed to a large extent by the relatively high- θ_e air in the downshear semicircle. Eyewall θ_e values may then temporarily increase and the TC may intensify. The temporary intensification ensues until the very

low θ_e air from the upshear semicircle wraps around the centre and limits considerably the supply of relatively high θ_e (exemplified at 23 h (Fig. 11(c)) and at 45 h (Fig. 11(e))).

At the end of our experiment a robust re-intensification is indicated in the intensity time series (Fig. 2(b)). As in the experiments examined in RMN10, this final re-intensification is associated
645 with an almost complete recovery of the inflow layer θ_e (Fig. 11(f)).

As indicated in Figs. 11(b) - 11(e), low- θ_e air in the inflow layer may wrap around the centre into the downshear-right quadrant. This low- θ_e air tends to suppress the convection of the SBC. Furthermore, after 20 h in ICE₆₈ the vortex tilt is no longer in the approximate left-of-shear equilibrium direction but starts to precess. In accordance with this precession, the vorticity anomaly associated
650 with the tilt of the outer vortex then starts to move also and thus no longer provides persistent forcing for the SBC in the downshear-right quadrant. It is interesting to note that a narrow band of convection preferably occurs in the downshear quadrant at these later times (Figs. 11(b) - 11(e)). Frequently, one observes significant downward flux of low θ_e associated with this remnant SBC (not shown).

655 4.2 A timescale for vortex spindown

Within the simplified framework of an idealised Carnot cycle, and based on the idea that environmental vertical wind shear leads to the frustration of such a thermodynamic cycle, Tang and Emanuel (2010) have derived a theory for the storm's reduced *steady-state* intensity. Such a theory, however, does not provide information about the *temporal evolution* of storm intensity, i.e. how rapidly a TC
660 weakens. A well-known concept for the weakening of a TC is the axisymmetric, frictionally-induced spindown of the TC vortex. Frictional convergence forces ascent out of the inflow layer. When the vertical convective mass flux is smaller than the frictionally forced vertical mass flux, some of the air has to diverge above the inflow layer due to mass continuity (Willoughby, 1979). Under the assumption that air parcels approximately conserve their angular momentum above the frictional
665 inflow layer, this divergence implies a decay of the tangential winds, i.e. the TC weakens.

A timescale for the frictional spindown of an *axisymmetric* vortex *without* convective mass flux has been derived by Elliassen and Lystad (1977). Their model assumes a neutral stratification above the layer of strong frictional inflow which is a reasonable assumption in the inner core of a TC because isosurfaces of θ_e and angular momentum are approximately congruent in this region. Montgomery et al. (2001) have verified by numerical experiments that the theory gives reasonable results
670 for the spindown of TC-like vortices, even beyond the formal validity of the theory. The half-time t_{half} , i.e. the time that is required to reduce the initial tangential velocity v by a factor of 2, is given by Elliassen and Lystad's theory as

$$t_{half} = \frac{H - h}{\chi^2 C_D v}. \quad (6)$$

675 Here, H is the fluid depth, h the height of the boundary layer, and χ a reduction factor defined by Elliassen and Lystad as the ratio of the tangential winds at the top of the surface layer to the tangential

winds at the top of the Ekman layer. Estimating $H - h = 10^4$ m, $\chi = 0.8$, and using $C_D = 3.8 \times 10^{-3}$ from Deacon's formula with $v = 68 \text{ ms}^{-1}$ yields a half-time $t_{half} = 16.8$ h.

The weakening of the TC in ICE₆₈ is remarkable: intensity decreases from 68 ms^{-1} at 42 h to
680 33 ms^{-1} at 68 h (Fig. 2(b)), corresponding to a weakening rate of 35 ms^{-1} in 26 h; or a half-time
of approx. 25 h. This value is consistent with a *partial* shutdown of the convective mass flux. As
noted above, concurrently with the frustration of the inflow layer θ_e and the rapid weakening, the
vertical mass flux at 5 km height decreases by approx. 60%. Consequently, it can be argued that the
significant reduction of the convective vertical mass flux by the severe depression of the inflow layer
685 θ_e values broadly governs the rapid weakening in ICE₆₈.

5 Conclusions

In the light of a new framework developed in a recent study (RMN10), the current study further
examines the evolution of TCs exposed to environmental vertical wind shear. The new framework
has been developed based on idealized numerical experiments for which we have deliberately chosen
690 a simple set of physical parameterisations to minimize the complexity of the problem. In the current
study, we survey and diagnose five additional numerical experiments with some modifications of the
experimental setup to assess the robustness of our previous results.

The modifications of the experimental setup focus on parameters that are important for structure
change and intensity evolution of numerically simulated TCs and the storms' evolution in vertical
695 wind shear, discussed in some detail in the Introduction in Sec. 1.2. Specifically, in comparison
to RMN10, we here consider weaker, but still mature TCs; employ values for the exchange coeffi-
cients of surface heat and momentum fluxes that are in better agreement with recent observational
results; and complement our previous warm-rain experiments with experiments that employ an ice
microphysics scheme.

700 The ability of TC-like vortices to withstand the differential advection by vertical wind shear and to
eventually re-align depends on the radial profile of the swirling winds (discussed in detail in Sec.3.1).
Some differences in this radial structure arise in the individual experiments *before* interacting with
the imposed vertical wind shear. The most notable differences are found in the experiment with ice
microphysics in which the TC, inter alia, features a radius of maximum winds that is approx. 25 %
705 smaller than in the warm-rain experiments. Differences in the radial vortex structure complicate the
attribution of differences in the TC evolution to, e.g., the inclusion of ice microphysics alone.

The differences in the vortex structure notwithstanding, in all experiments the TCs exhibit the
same general structural changes when exposed to vertical wind shear. The structural changes are
consistent with RMN10's new framework and comprise a vortex tilt predominantly to the downshear-
710 left for 20 h - 24 h, the formation of a pronounced wave-number 1 convective asymmetry *outside*
of the eyewall (reminiscent of a stationary band complex), and downward flux of low- θ_e air into the

inflow layer in the downshear-left semicircle. A significant depression of the inflow layer θ_e values ($\mathcal{O}(10\text{ K})$) occurs in all experiments.

Furthermore, for all experiments the potential for a non-linear, Kelvin-Helmholtz type instability in the inner core of the tilted TC-vortex is diagnosed. Such an instability would contribute to enhanced dissipation of kinetic energy and may modify the flux of low- θ_e air into the inflow layer. A quantitative analysis of the mixing process associated with the potential instability, however, is deferred to future work.

Two additional diagnostics are considered in the current study that have not been considered in RMN10, namely the θ_e values underneath the *asymmetric* inner-core updrafts, and so-called contoured frequency by altitude diagrams to examine the general characteristics of vertical motion. The magnitude of the θ_e depression underneath the *asymmetric* inner-core updrafts early in the respective shear experiment correlates well with the ensuing weakening of the TC, supporting the idea that it is the depression of the inflow layer θ_e that governs the intensity evolution to first order. For all experiments, vertical wind shear increases the frequency of strong downdrafts as compared to the no-shear experiments. The magnitude of the θ_e depression *outside* of the eyewall is consistent with the frequency of strong downdrafts, supporting the idea that it is the shear-induced downdrafts that flush low- θ_e air into the inflow layer. Consequently, both additional diagnostics corroborate RMN10's framework.

In one of our experiments employing ice microphysics, a very rapid weakening of the TC occurs. This intensity evolution is distinct from the intensity evolution in our warm-rain experiments. Therefore, a question may naturally arise whether ice microphysics, as represented in the RAMS model, introduces an important mechanism for intensity change that is not considered in RMN10's framework. As noted above, the structural changes caused by the vertical wind shear in the experiment with ice microphysics are very similar as in the warm-rain experiments. In the ice experiment, the general downdraft activity, the flux of low- θ_e air into the inflow layer, and the θ_e depression underneath the inner-core updrafts are all the most pronounced in our suite of experiments. The inner-core θ_e depression that accompanies the initial rapid weakening is more than twice as high than in the comparable experiments employing warm-rain microphysics (6 K - 7 K as compared to 2 K - 3 K). Axisymmetric spindown theory (Elliasen and Lystad, 1977; Montgomery et al., 2001) further supports the hypothesis that the rapid initial weakening is due to a substantial decrease of the convective mass flux associated with the significant depression of the inflow layer θ_e by shear-induced downdrafts. In addition, we have documented a close relationship between the evolution of the inflow layer θ_e values and two transient intensity maxima that occur at 22 h and 44 h after vertical wind shear is imposed. The final re-intensification of the TC in this experiment, as in RMN10, is associated with a near-complete replenishment of the inflow layer θ_e values also.

Based on the evidence presented here, we conclude that RMN10's framework for the intensity modification of TCs in vertical wind shear is robust to the presented changes in the setup of the

numerical experiment. We advocate further study and tests of this framework with case studies and
750 real atmospheric data.

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References

- Abarbanel, H. D. I., Holm, D. D., Marsden, J. E., and Ratiu, T.: Nonlinear stability of incompressible stratified flow, *Phil. Trans. Roy. Soc.*, A318, 349–409, 1986.
- 760 Bell, M. M.: Air – sea enthalpy and momentum exchange at major hurricane wind speeds, Ph.D. thesis, Naval Postgraduate School, Monterey, California, USA, 2010.
- Bender, M. A.: The effect of relative flow on the asymmetric structure in the interior of hurricanes, *J. Atmos. Sci.*, 54, 703–724, 1997.
- Black, P. G., D’Asaro, E. A., Drennan, W. M., French, J. R., Niiler, P. P., Sanford, T. B., Terrill, E. J., Walsh, E. J., and Zhang, J. A.: Air-sea exchange in hurricanes: Synthesis of observations from the Coupled Boundary Layer Air-Sea Transfer experiment, *Bull. Am. Meteorol. Soc.*, 88, 357–374, 2007.
- 765 Braun, S. A. and Tao, W. K.: Sensitivity of high-resolution simulations of Hurricane Bob (1991) to planetary boundary layer parameterizations, *Mon. Wea. Rev.*, 128, 3941–3961, 2000.
- Bui, H. H., Smith, R. K., Montgomery, M. T., and Peng, J.: Balanced and unbalanced aspects of tropical-cyclone intensification, *Q. J. R. Meteorol. Soc.*, 135, 1715–1731, 2009.
- 770 Cotton, W. R. and Coauthors: RAMS 2001: Current status and future directions, *Meteor. Atmos. Phys.*, 82, 5–29, 2003.
- DeMaria, M.: The effect of vertical shear on tropical cyclone intensity change, *J. Atmos. Sci.*, 53, 2076–2088, 1996.
- 775 Eliassen, A. and Lystad, M.: On the Ekman layer in a circular vortex: A numerical and theoretical study., *Geophys. Norv.*, 31, 1977.
- Emanuel, K. A.: Atmospheric convection, pg. 172, Oxford University Press, New York, 1994.
- Fovell, R. G., Corbosiero, K. L., and Kuo, H.-C.: Cloud Microphysics Impact on Hurricane Track as Revealed in Idealized Experiments, *J. Atmos. Sci.*, 66, 1764–1778, 2009.
- 780 Frank, W. M. and Ritchie, E. A.: Effects of vertical wind shear on the intensity and structure of numerically simulated hurricanes, *Mon. Wea. Rev.*, 129, 2249–2269, 2001.
- Hill, G. E.: Factors controlling the size and spacing of cumulus clouds as revealed by numerical experiments, *J. Atmos. Sci.*, 31, 646–673, 1974.
- Holton, J.: An introduction to dynamic meteorology, pg 132, Academic Press, London, 2004.
- 785 Jones, S. C.: The evolution of vortices in vertical shear. I: Initially barotropic vortices, *Q. J. R. Meteorol. Soc.*, 121, 821–851, 1995.
- Kessler, E.: On the distribution and continuity of water substance in atmospheric circulations, *Meteor. Monogr.* 32, Amer. Meteor. Soc., 1969.
- Lilly, D. K.: On the numerical simulation of buoyant convection, *Tellus*, 14, 148–172, 1962.
- 790 Meyers, M., Walko, R., Harrington, J., and Cotton, W.: New RAMS cloud microphysics parameterization. Part II: The two-moment scheme., *Atmos. Res.*, 45, 3–39, 1997.
- Montgomery, M. T., Snell, H. D., and Yang, Z.: Axisymmetric Spindown Dynamics of Hurricane-like Vortices, *J. Atmos. Sci.*, 58, 421–435, 2001.
- Montgomery, M. T., Smith, R. K., and Nguyen, S. V.: Sensitivity of tropical cyclone models to the surface drag coefficient, *Q. J. R. Meteorol. Soc.*, 136, 1945–1953, 2010.
- 795 Pielke, R. A. and Coauthors: A comprehensive meteorological modeling system – RAMS, *Meteor. Atmos.*

Phys., 49, 69–91, 1992.

Reasor, P. D., Montgomery, M. T., and Grasso, L. D.: A new look at the problem of tropical cyclones in vertical shear flow: Vortex resiliency, *J. Atmos. Sci.*, 61, 3–22, 2004.

800 Riemer, M. and Montgomery, M. T.: Simple kinematic models for the environmental interaction of tropical cyclones in vertical wind shear, *Atmos. Chem. Phys.*, 11, 9395–9414, <http://www.atmos-chem-phys.net/11/9395/2011/>, 2011.

Riemer, M., Montgomery, M. T., and Nicholls, M. E.: A new paradigm for intensity modification of tropical cyclones: thermodynamic impact of vertical wind shear on the inflow layer, *Atmos. Chem. Phys.*, 10, 3163–
805 3188, <http://www.atmos-chem-phys.net/10/3163/2010/>, 2010.

Schecter, D. A. and Montgomery, M. T.: On the symmetrization rate of an intense geophysical vortex, *Dyn. Atmos. Oceans*, 37, 55–88, 2003.

Smagorinsky, J.: General circulation experiments with the primitive equations, *Mon. Wea. Rev.*, 91, 99–164, 1963.

810 Smith, R. K. and Thomsen, G. L.: Dependence of tropical-cyclone intensification on the boundary-layer representation in a numerical model, *Q.J.R. Meteorol. Soc.*, 136, 1671–1685, 2010.

Smith, R. K., Montgomery, M. T., and Thomsen, G.: Sensitivity of tropical cyclone models to the surface drag coefficient in different boundary-layer schemes, *Q.J.R. Meteorol. Soc.*, p. in review, 2011.

Srivastava, R. C.: A Model of Intense Downdrafts Driven by the Melting and Evaporation of Precipitation, *J. Atmos. Sci.*, 44, 1752–1774, 1987.
815

Tang, B. and Emanuel, K. A.: Midlevel ventilation’s constraint on tropical cyclone intensity, *J. Atmos. Sci.*, 67, 1817–1830, 2010.

Tripoli, G. J. and Cotton, W. R.: The use of ice-liquid water potential temperature as a thermodynamic variable in deep atmospheric models, *Mon. Wea. Rev.*, 109, 1094–1102, 1981.

820 Verlinde, J., Flatau, P., and Cotton, W.: Analytical solutions to the collection growth equation: Comparison with approximate methods and application to cloud microphysics parameterization schemes, *J. Atmos. Sci.*, 47, 2871–2880, 1990.

Walko, R., Cotton, W., Harrington, J., and Meyers, M.: New RAMS cloud microphysics parameterization. Part I: The single-moment scheme, *Atmos. Res.*, 38, 29–62, 1995.

825 Willoughby, H. E.: Forced secondary circulations in hurricanes, *J. Geophys. Res.*, 84, 3173–3183, 1979.

Willoughby, H. E., Marks, F. D., and Feinberg, R. J.: Stationary and moving convective bands in hurricanes, *J. Atmos. Sci.*, 41, 3189–3211, 1984.

Wong, M. L. M. and Chan, J. C. L.: Tropical cyclone intensity in vertical wind shear, *J. Atmos. Sci.*, 61, 1859–1876, 2004.

830 Yuter, S. E. and Houze, R. A.: Three-Dimensional Kinematic and Microphysical Evolution of Florida Cumulonimbus. Part II: Frequency Distributions of Vertical Velocity, Reflectivity, and Differential Reflectivity, *Mon. Wea. Rev.*, 123, 1941–1963, 1995.

Zhang, J. A., Black, P. G., French, J. R., and Drennan, W. M.: First direct measurements of enthalpy flux in the hurricane boundary layer: The CBLAST results, *Geophys. Res. Lett.*, 35, 2008.

Table 1. Overview of the experiments that are considered in this study. The experiments RMN_{68} and ${}_{10}\text{RMN}_{68}$ are described in detail in RMN10. In column C_K , 'Deacon' denotes that Deacon's formula (see section 2.3) is used to determine the exchange coefficients. The last column gives the TC's intensification rate just before vertical shear is imposed.

Experiment	'initial' intensity [ms^{-1}]	C_K	C_K/C_D	microphysics	shear [$\text{ms}^{-1}/12 \text{ km}$]	preceding int. rate [ms^{-1}/h]
RMN_{68}	68	Deacon	1	warm	15	1.8
${}_{10}\text{RMN}_{68}$	68	Deacon	1	warm	10	1.8
RMN_{54}	54	Deacon	1	warm	15	0.0
CBLAST_{68}	68	1.16×10^{-3}	0.65	warm	15	1.1
CBLAST_{54}	54	1.16×10^{-3}	0.65	warm	15	0.0
ICE_{68}	68	Deacon	1	ice	15	2.5
${}_{10}\text{ICE}_{68}$	68	Deacon	1	ice	10	2.5

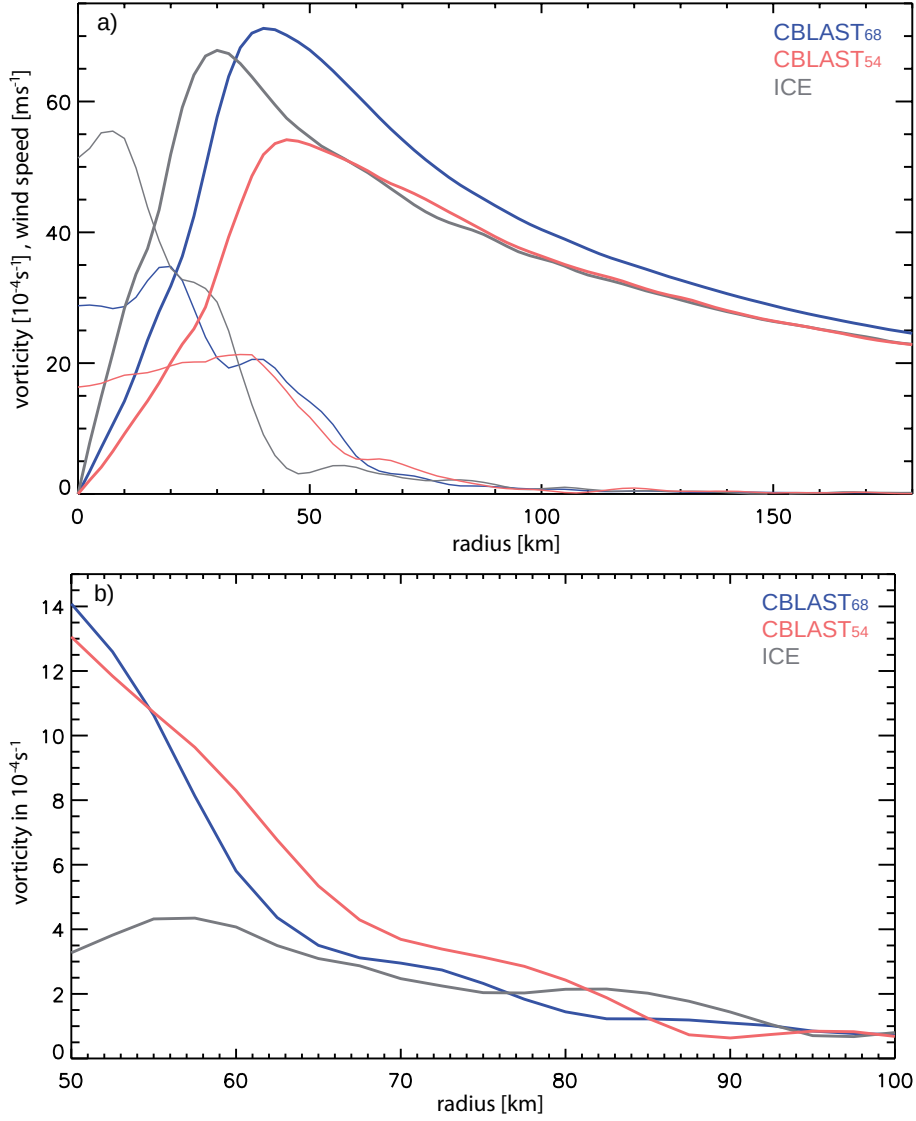


Fig. 1. (a) Radial profiles of azimuthal mean vorticity at 2 km (thin) and azimuthal mean tangential wind at the radius of maximum winds at 1 km height (thick) at the time when vertical wind shear is imposed in RMN₅₄ (red), CBLAST₆₈ (blue), and ICE₆₈ (grey), respectively. (b) Radial vorticity profiles as in (a) but zoomed in on the “skirt” region between 50 km and 100 km.

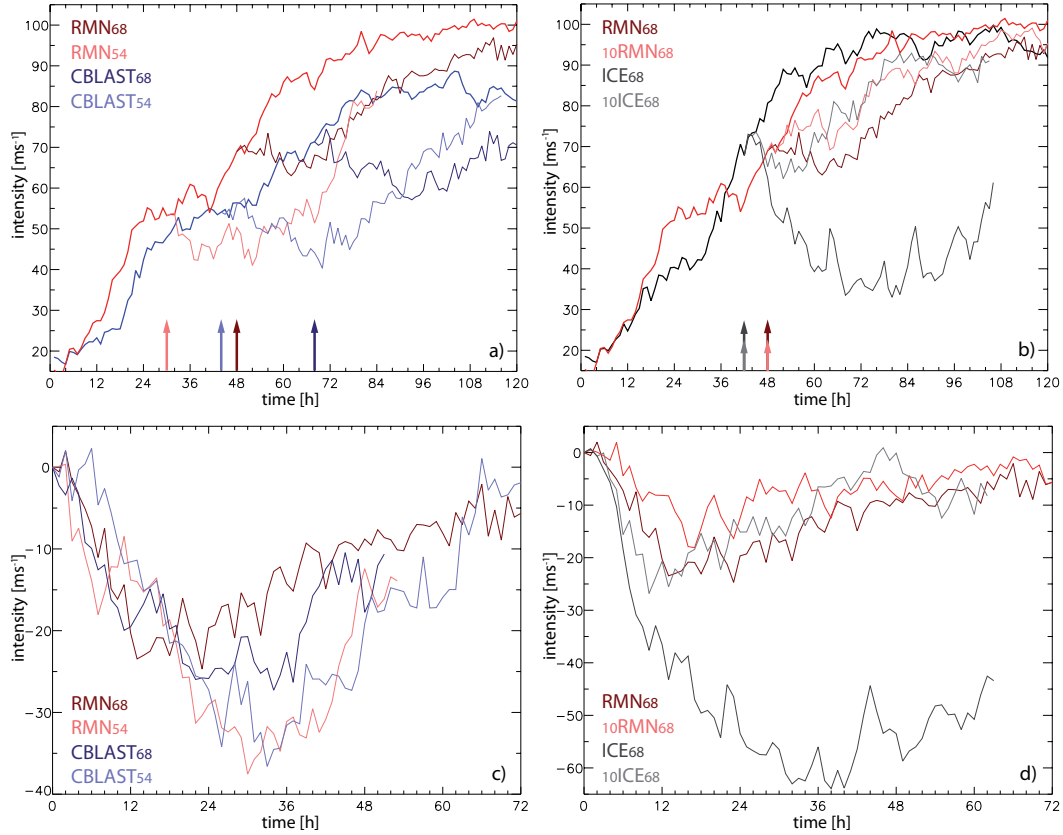


Fig. 2. a) Intensity time series for the RMN no-shear experiment (red), RMN₅₄ (light red), RMN₆₈ (dark red), the CBLAST no-shear experiment (blue), CBLAST₅₄ (light blue), and CBLAST₆₈ (dark blue). The colour-coded arrows denote the time when vertical wind shear is imposed in the respective experiment. b) As in a), but for the RMN no-shear experiment (red), RMN₆₈ (dark red), ₁₀RMN₆₈ (light red), the ICE no-shear experiment (black), ICE₆₈ (dark grey), and ₁₀ICE₆₈ (light grey). c) Time series of the difference between the intensity in RMN₅₄ (light red), RMN₆₈ (dark red), CBLAST₅₄ (light blue), and CBLAST₆₈ (dark blue) and the respective no-shear experiment. Time 0 h denotes the time when vertical wind shear is imposed in the respective experiment. d) As in c), but for RMN₆₈ (dark red), ₁₀RMN₆₈ (red), ICE₆₈ (dark grey), and ₁₀ICE₆₈ (light grey).

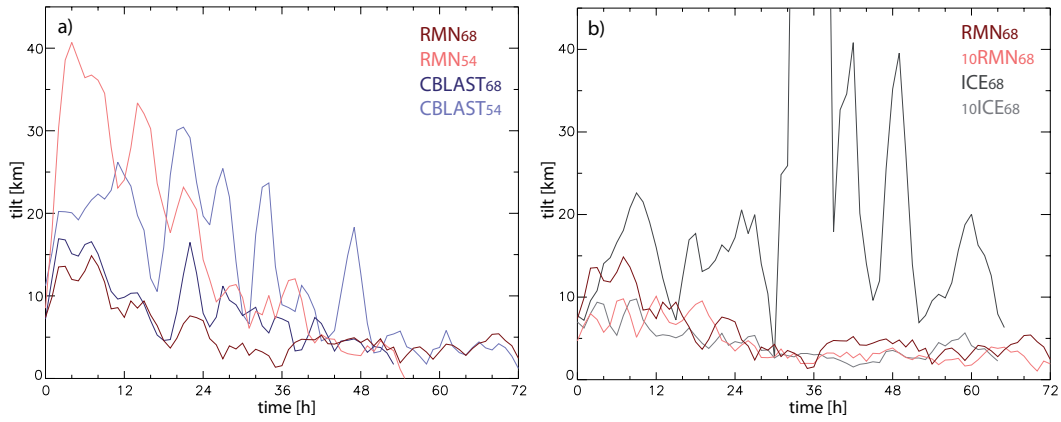


Fig. 3. a) Time series of the tilt magnitude for RMN_{54} (light red), RMN_{68} (dark red), CBLAST_{54} (light blue), and CBLAST_{68} (dark blue). Vortex tilt is defined as the vector difference between the vorticity centroids at 10 km and 1 km height. For visual clarity, the 3 h running mean of the time series is shown. b) As in a) but for RMN_{68} (dark red), 10RMN_{68} (light red), ICE_{68} (dark grey), and 10ICE_{68} (light grey). Note that the tilt magnitude for ICE_{68} goes off the scale between 33 h and 38 h reaching a maximum value of 195 km (not shown).

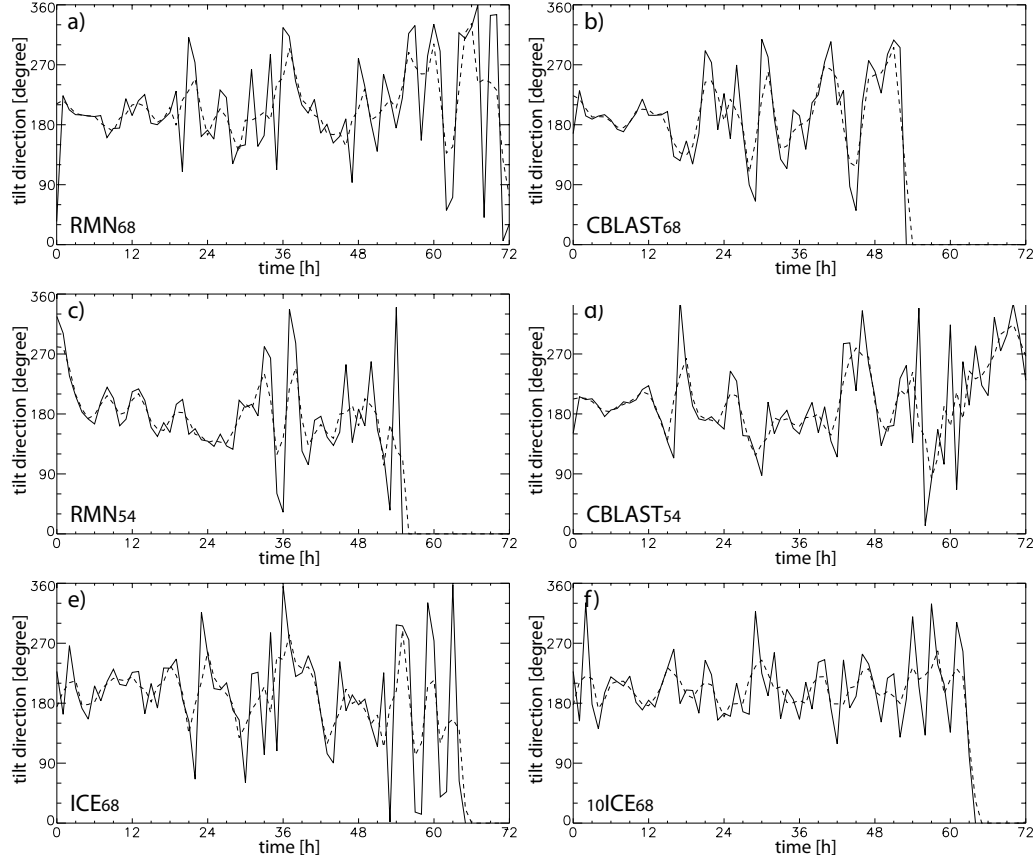


Fig. 4. Time series of the tilt direction for RMN₆₈ (a), CBLAST₆₈ (b), RMN₅₄ (c), CBLAST₅₄ (d), ICE₆₈ (e), and 10ICE₆₈ (f). Vortex tilt is defined as the vector difference between the vorticity centroids at 10 km and 1 km height. Dashed line denotes the 3 h running mean.

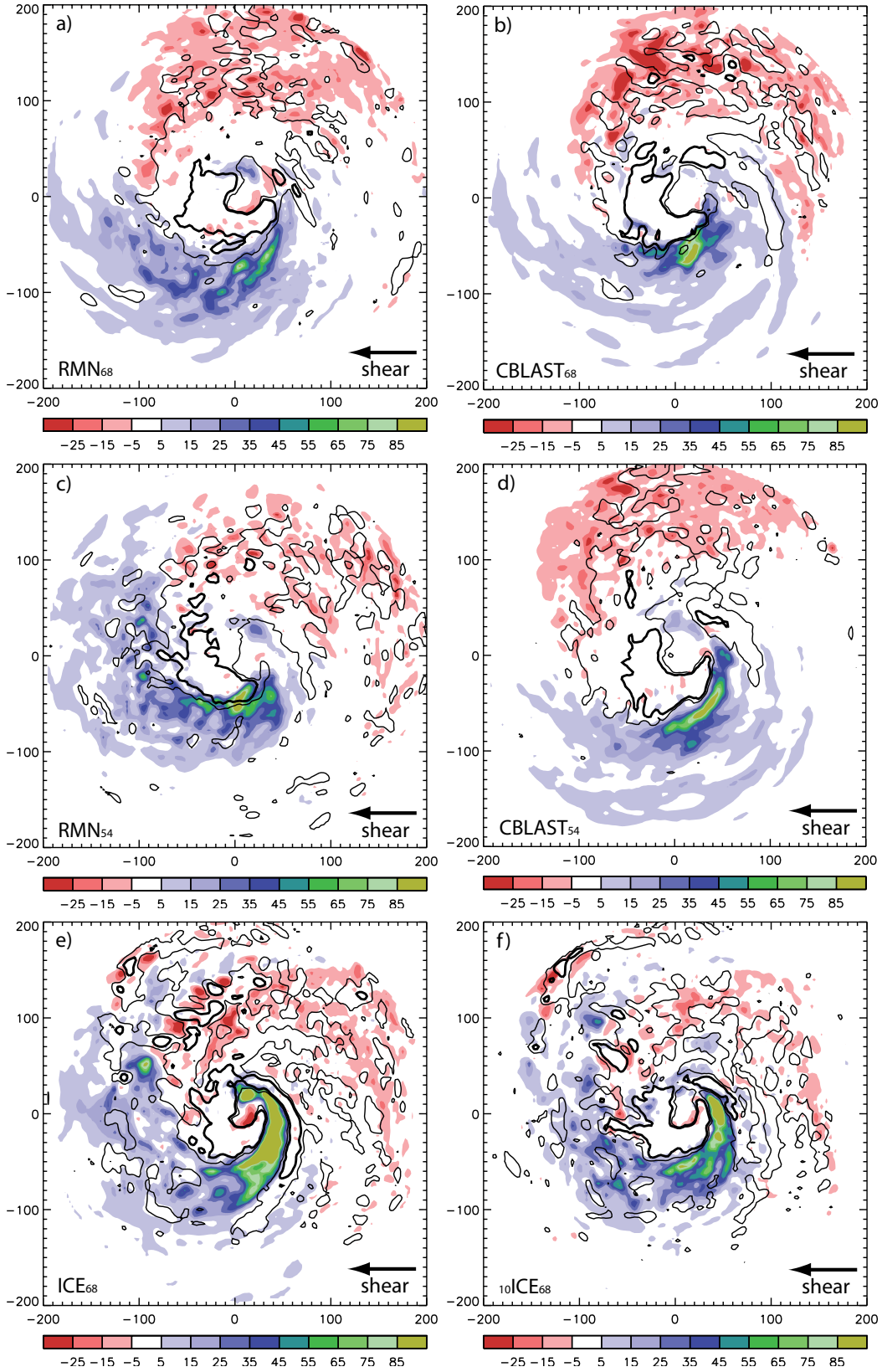


Fig. 5. Downward flux of θ'_e , DFX (colour, in 0.1 Kms^{-1} , see text for definition), at the top of the axisymmetric inflow layer, defined as 1.5 km, and low-level upward motion (thin contour: 0.25 ms^{-1} , thick contour: 1 ms^{-1} , averaged from 1.25 km - 2 km height) both averaged from 1 h - 6 h after vertical shear is imposed for a) RMN₆₈, b) CBLAST₆₈, c) RMN₅₄, d) CBLAST₅₄, e) ICE₆₈, and f) 10ICE₆₈. The arrow indicates the direction of the deep-layer shear. The horizontal scale is in km

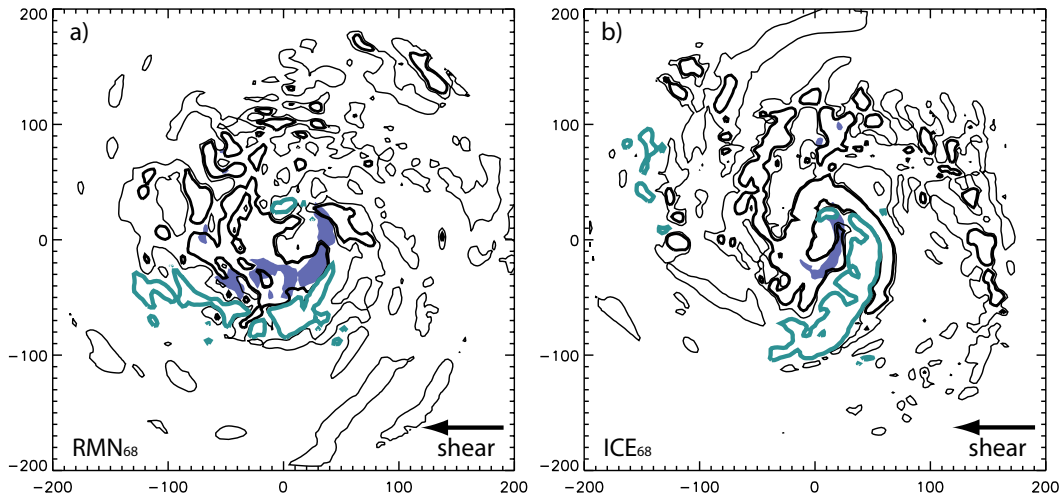


Fig. 6. Snapshots of the gradient Richardson number at 3 h after vertical shear is imposed (shaded for values below 1) in (a) RMN_{68} and (b) ICE_{68} . Upward motion is depicted in black contours (thin for 0.25 ms^{-1} , thick for 1 ms^{-1}). The cyan contour denotes regions of strong downward flux of low- θ_e air into the inflow layer (DFX at 1.5 km height, the contour depicts the 4.5 Kms^{-1} isoline). The horizontal scale is in km.

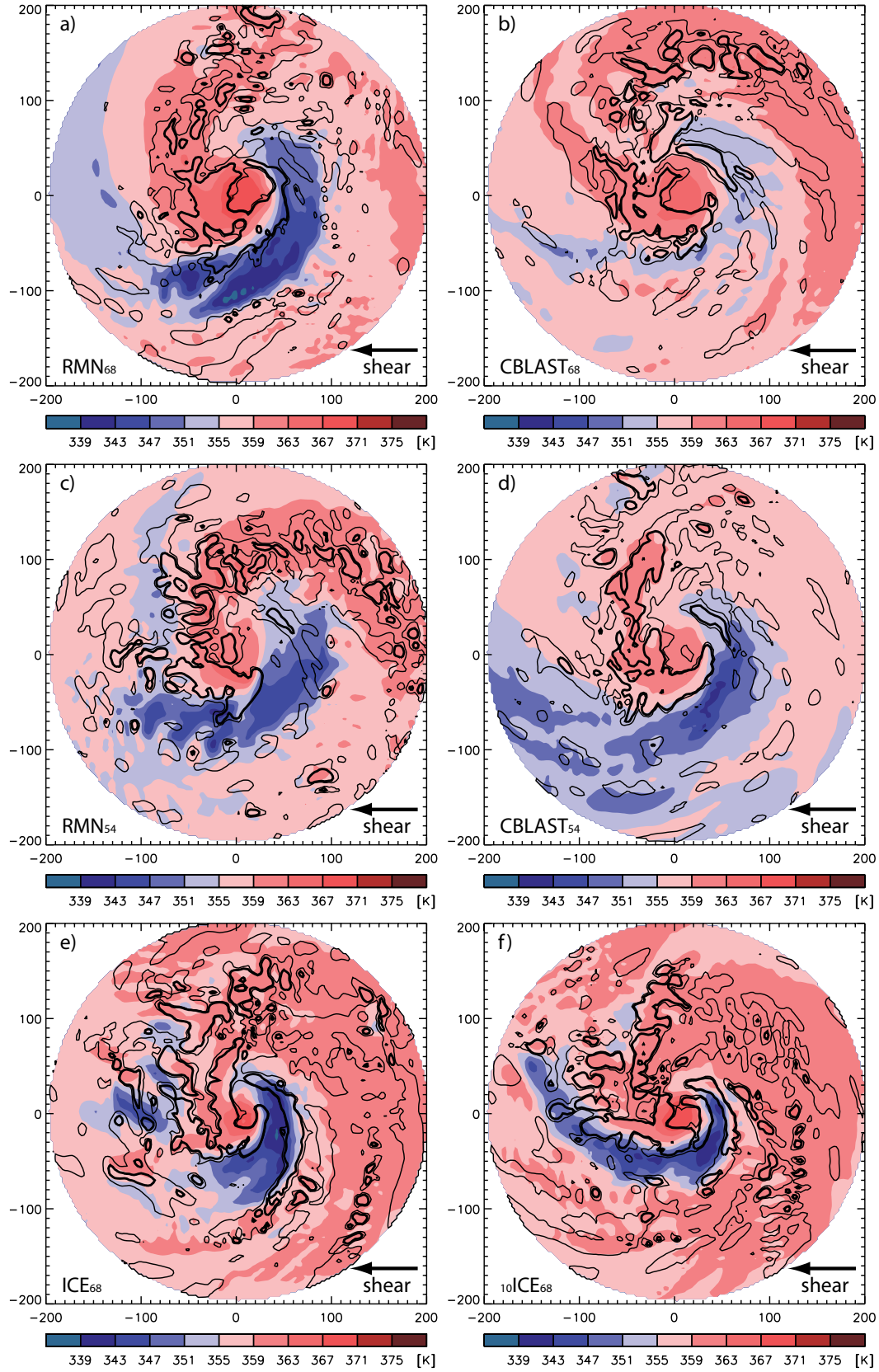


Fig. 7. As Fig. 5, but for a snapshot of inflow layer θ_e (colour, averaged over lowest 1 km) and low-level updrafts at 5 h after vertical shear is imposed for a) RMN₆₈, b) CBLAST₆₈, c) RMN₅₄, d) CBLAST₅₄, e) ICE₆₈, and f) 10ICE₆₈. The depicted time is representative for the early part of the experiments.

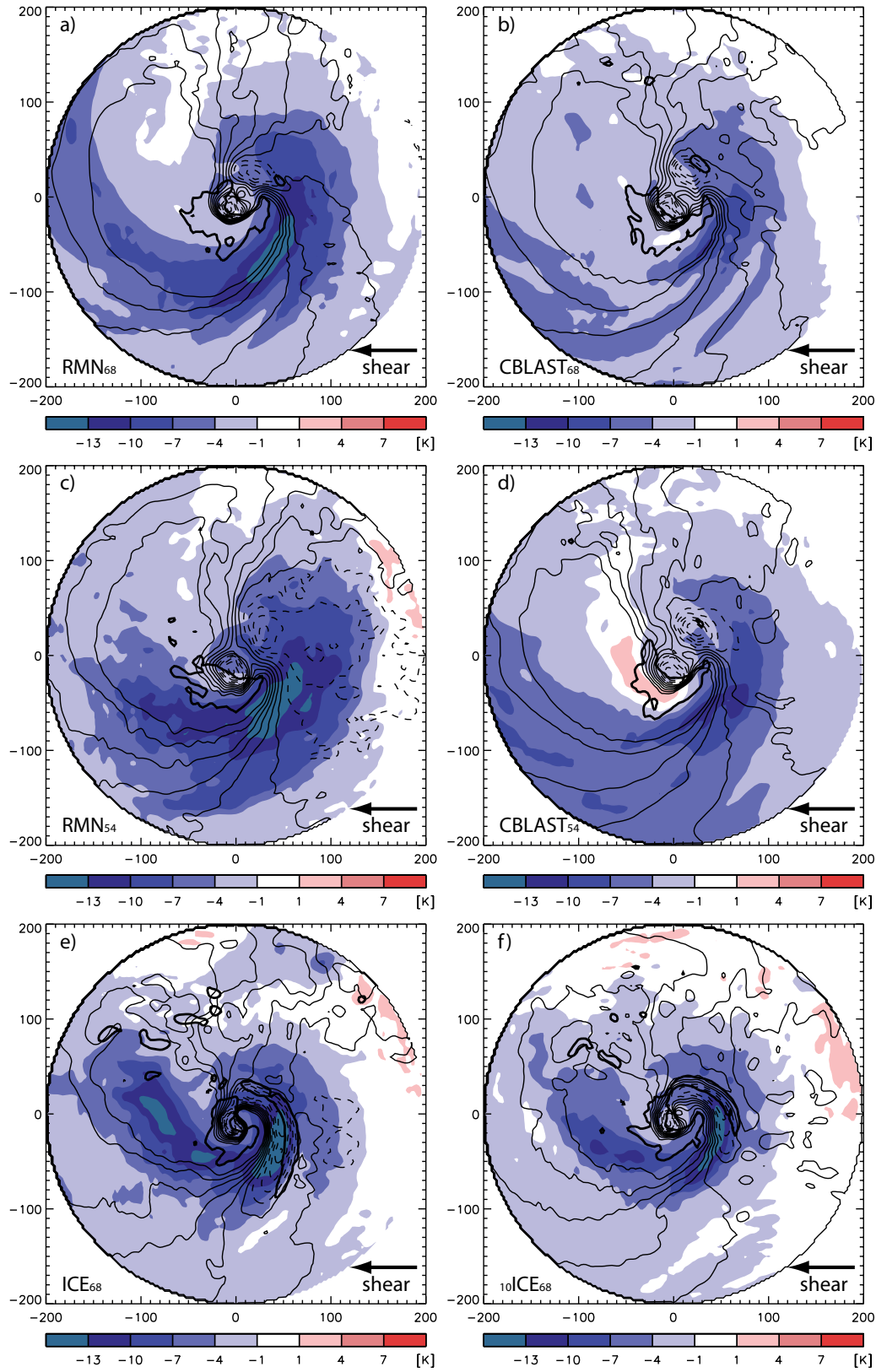


Fig. 8. Depression of inflow layer θ_e (averaged over the lowest 1 km and from 4 h - 9 h) relative to the axisymmetric mean at the time when vertical wind shear is imposed (colours). Thin contours depict the radial flow averaged over the lowest 1 km (every 4 ms⁻¹, starting at 2 ms⁻¹, dashed for negative values (outflow)). Thick contour denotes low-level updrafts (1 ms⁻¹, averaged from 1.25 km - 2 km height). a) RMN₆₈, b) CBLAST₆₈, c) RMN₅₄, d) CBLAST₅₄, e) ICE₆₈, and f) ₁₀ICE₆₈

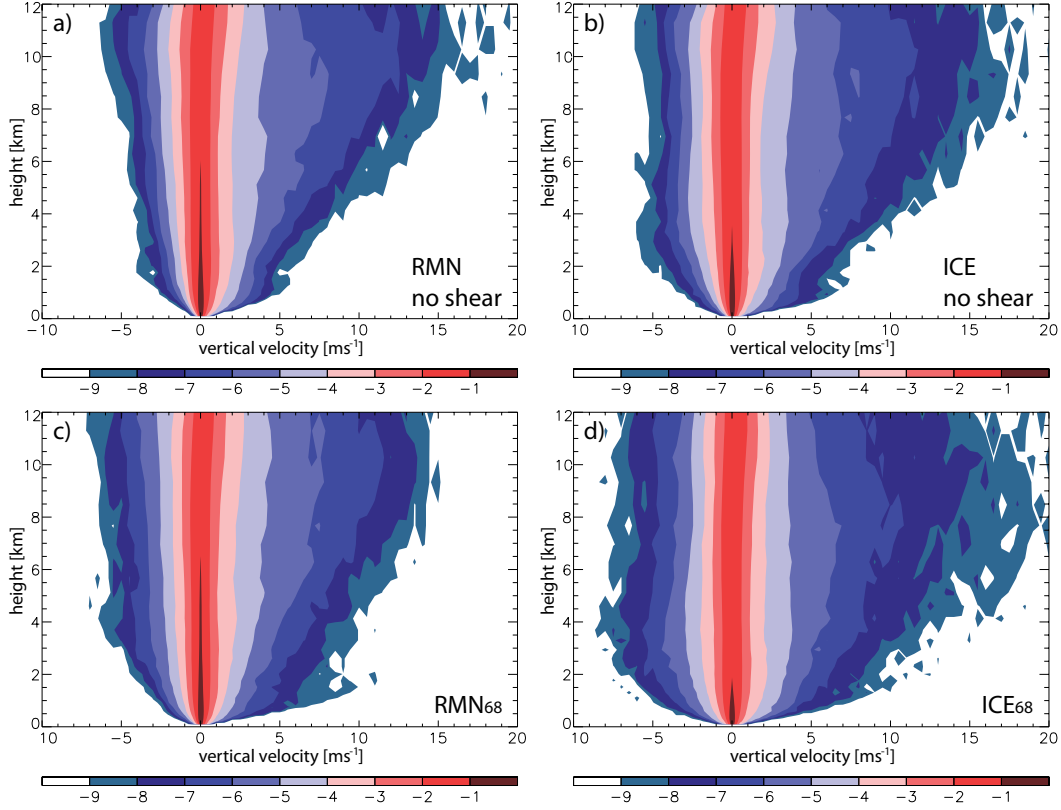


Fig. 9. Contoured frequency by altitude diagrams of vertical motion within 160 km radius of the centre. Vertical motion is binned into intervals of 0.5 ms^{-1} , centred on the values given on the x-axis. The colour-coded value denotes the logarithm of the frequency. With each contour the frequency decreases by a factor of $1/e$. Before taking the logarithm of the frequency a small positive value ($10^{-5} \approx e^{-11.5}$) has been added to ensure that the logarithm is well defined everywhere. For the no-shear cases of RMN (a) and ICE (b) the 6 h time period after vertical wind shear is imposed in the respective shear runs is considered. For RMN_{68} (c) and ICE_{68} (d) the times 4 h - 9 h are considered.

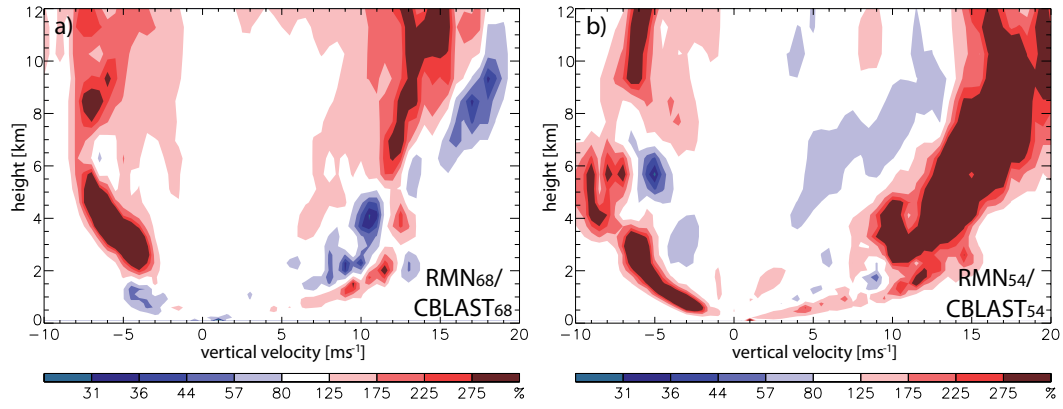


Fig. 10. As Fig. 9, but for the ratio of vertical motion frequency of RMN₆₈/CBLAST₆₈ (a) and RMN₅₄/CBLAST₅₄ (b).

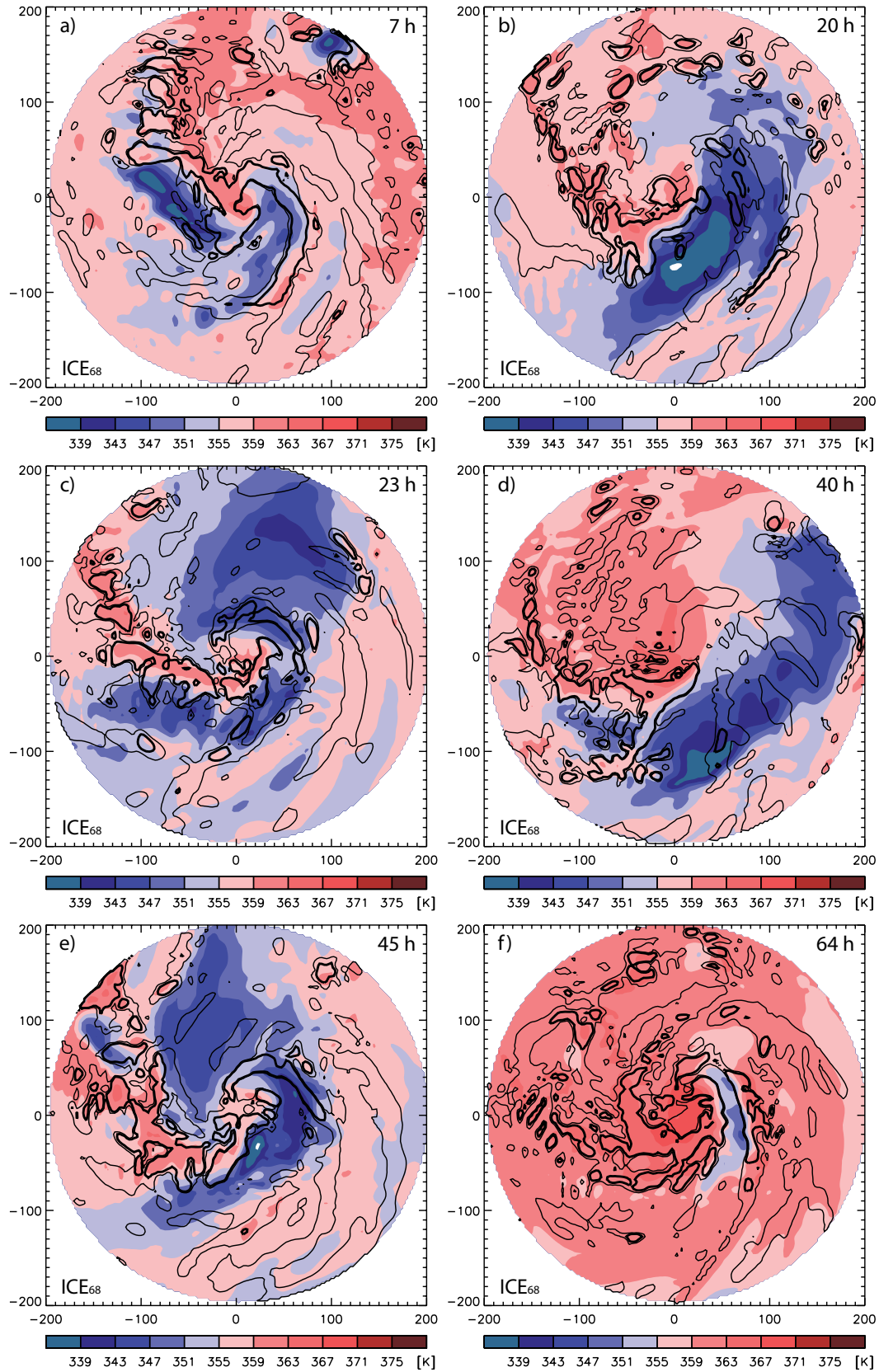


Fig. 11. As Fig. 7, but for ICE_{68} at a) 7 h, b) 20 h, c) 23 h, d) 40 h, e) 45 h, and f) 64 h.