



Granger Causality and National Procurement Spending

Applications to the CC130 Hercules Fleet Performance

David W. Maybury
Materiel Group Operational Research

DRDC CORA TM 2011-154
September 2011

Defence R&D Canada
Centre for Operational Research and Analysis

Materiel Group Operational Research
Assistant Deputy Minister (Materiel)



National
Defence

Défense
nationale

Canada

Granger Causality and National Procurement Spending

Applications to the CC130 Hercules Fleet Performance

David W. Maybury
Materiel Group Operational Research

Defence R&D Canada – CORA

Technical Memorandum

DRDC CORA TM 2011-154

September 2011

Principal Author

Original signed by David W. Maybury

David W. Maybury

Approved by

Original signed by R.M.H. Burton

R.M.H. Burton

Section Head (Joint Systems Analysis)

Approved for release by

Original signed by P. Comeau

P. Comeau

Chief Scientist

© Her Majesty the Queen in Right of Canada as represented by the Minister of National Defence, 2011

© Sa Majesté la Reine (en droit du Canada), telle que représentée par le ministre de la Défense nationale, 2011

Abstract

Using Granger causality tests, we look for relationships in performance and National Procurement spending time series data that can improve forecasting capabilities with the CC130 fleet. We find that no meaningful relationships exist between spending and performance indicators within the spending envelope studied. Our results concord with earlier work based on random matrix theory and minimal spanning trees, which suggest the fleet is robust to spending shocks. We conclude that NP spending changes do not correlate with subsequent CC130 Hercules aircraft performance changes and vice versa. Granger causality tests represent a powerful tool which can be used with future fleet studies.

Résumé

Nous avons recours à des tests de causalité à la Granger pour établir des liens entre les données de séries chronologiques sur le rendement et les dépenses d'approvisionnement national qui permettraient d'améliorer les capacités de prévision pour la flotte des CC130. Nous constatons qu'il n'existe aucun lien significatif entre les dépenses et les indicateurs de rendement performance au sein de l'enveloppe de dépenses étudiée. Nos résultats sont conformes à ceux de recherches antérieures fondées sur la théorie des matrices aléatoires et sur les arbres de poids minimum, et selon lesquelles la flotte résiste aux réductions des dépenses. Nous pouvons conclure que les fluctuations des dépenses d'approvisionnement national et les fluctuations ultérieures du rendement des avions CC130 Hercules ne sont pas corrélées, et inversement. Les tests de causalité à la Granger constituent un puissant outil qui pourra servir dans les futures études de flotte.

This page intentionally left blank.

Executive summary

Granger Causality and National Procurement Spending

David W. Maybury; DRDC CORA TM 2011-154; Defence R&D Canada – CORA; September 2011.

ADM(Mat) has sought a deeper understanding of the relationship between National Procurement (NP) spending and fleet performance across the Canadian Forces for the last eight years. Senior decision-makers have hoped that insight into spending effects on fleet operations would eventually lead to better sparing methodologies, more efficient maintenance activities and schedules, along with a deeper understanding of end-of-life issues. Using the CC130 NP spending and performance data, we re-examine the results in [2] by applying econometric times series methods.

We search for relationships between time series by using Granger causality tests, which tells us if the mean squared forecasting error of one time series can be reduced through knowledge of another time series. This study provides a complement to [2] and we show that NP spending does not improve the predictability of any time series. We find that no meaningful relationships exist between spending and performance indicators within the spending envelope studied.

We should stress that not discovering Granger causality in spending and fleet performance data does not imply inefficiency. In fact, an efficiently maintained fleet should not show a strong correlation between routine spending and performance changes. On the other hand, we caution that these results do not imply that the underlying supply chain is optimal – the robustness to spending shocks may simply arise from non-optimally high inventory levels. We cannot address supply chain issues or optimal sparing through Granger causality tests. From the analysis in this study, we can only conclude that NP spending changes do not correlate with subsequent performance changes and vice versa. Further analysis is warranted on the supply chain to understand the reasons behind the lack of Granger causality.

Sommaire

Granger Causality and National Procurement Spending

David W. Maybury ; DRDC CORA TM 2011-154 ; R & D pour la défense Canada – CARO ; septembre 2011.

Au cours des huit dernières années, le SMA(Mat) a voulu mieux comprendre les liens entre les dépenses d'approvisionnement national et le rendement de la flotte dans l'ensemble des Forces canadiennes. Les décideurs principaux espéraient que de mieux comprendre les effets des dépenses sur la flotte permettrait de mieux définir les quantités optimales de pièces de rechange à garder en stock, d'améliorer l'efficacité des activités et des calendriers d'entretien et de mieux comprendre les problèmes associés à la fin de vie utile. À l'aide des données sur le rendement de la flotte de CC130 et sur les dépenses d'approvisionnement national connexes, nous réexaminons les résultats obtenus [2] en appliquant les méthodes économétriques de séries chronologiques.

Nous vérifions s'il existe des liens entre les séries chronologiques au moyen des tests de causalité à la Granger, qui permettront de déterminer si l'erreur quadratique moyenne de prévision d'une série chronologique peut être réduite par l'introduction d'une autre série chronologique. La présente étude se veut un complément de [2], et nous y démontrons que les dépenses d'approvisionnement national n'améliorent pas la prévisibilité des séries chronologiques. Nous constatons qu'il n'existe aucun lien significatif entre les dépenses et les indicateurs de rendement performance au sein de l'enveloppe de dépenses étudiée.

Nous devons souligner que l'absence d'un lien de causalité à la Granger entre les dépenses et le rendement de la flotte n'est pas synonyme d'inefficacité. En fait, dans le cas d'une flotte entretenue de façon efficiente, une forte corrélation entre les dépenses courantes et les fluctuations du rendement ne devrait pas être observée. Une mise en garde s'impose toutefois : les résultats ne devraient pas porter à croire que la chaîne d'approvisionnement sous jacente est optimale - la résistance aux chocs de dépenses peut simplement s'expliquer par des stocks trop grands. Les tests de causalité à la Granger ne permettent pas de traiter les questions relatives à la chaîne d'approvisionnement ou aux quantités optimales de pièces de rechange à garder en stock. La seule conclusion pouvant être tirée de la présente analyse est que les dépenses d'approvisionnement national et les fluctuations ultérieures du rendement ne sont pas corrélées, et inversement. D'autres études sur la chaîne d'approvisionnement devront chercher à comprendre l'absence d'un lien de causalité à la Granger.

Table of contents

Abstract	i
Résumé	i
Executive summary	iii
Sommaire	iv
Table of contents	v
Acknowledgements	vi
1 Introduction	1
1.1 Background	1
1.2 Scope	2
2 Results	3
2.1 Data selection	4
2.2 Analysis	5
3 Conclusions	10
References	12
Annex A: Time series and Granger causality	13
Annex B: Fleet indicator definitions	17
List of Acronyms	22

Acknowledgements

I would like to thank Dr. Ben Solomon for useful discussions and his encouragement during this project.

1 Introduction

It would be nice to use a non-parametric approach – just use histograms to characterize the joint density ... Unfortunately, we will not have enough data to follow this approach in macroeconomics for 2000 years or so.

— John H. Cochrane

1.1 Background

ADM(Mat) has sought a deeper understanding of the relationship between National Procurement (NP) spending and fleet performance across the Canadian Forces for the last eight years. Senior decision-makers have hoped that insight into spending effects on fleet operations would eventually lead to better sparing methodologies, more efficient maintenance activities and schedules, along with a deeper understanding of end-of-life issues. In a period of budget restraints, ADM(Mat) requires an analysis of the effect that changes in NP spending have on DND fleets. In response to ADM(Mat)'s concerns, the Directorate of Materiel Group Operational Research (DMGOR) has applied numerous technical methods to fleet data over the last five years, including neural networks trained on performance and costing data, generalized filter methods, and asymptotic methods based on equilibrium relaxation of coupled differential equations [1]. Despite the incredible efforts, each method has failed to identify a compelling link between high level performance indicators and NP spending.

Last year, the DMGOR undertook a study to elucidate spending linkages with performance data by examining the correlation structure of NP spending and performance time series data with the CC130 fleet. In [2], the DMGOR found that the correlation matrix for CC130 fleet performance with NP spending data contained a significant amount of noise dressing, which impedes the development of a general filter method. By constructing a minimal spanning tree on an ultrametric space in which the performance indicators and NP spending formed nodes, the DMGOR found that NP spending did not form a hub or cluster with the performance data. As a result, it was concluded in [2] that NP spending changes do not provide a meaningful input to predicting future performance changes.

While the problem seems well posed and the result of [2] counterintuitive, any potential analysis that attempts to isolate the effect of spending levels on fleet performance faces extreme hurdles. Since spending connects to a myriad of exogenous economic factors, such as inflation, price fluctuations in materiel, and worldwide supply chain pressures, a simple one-to-one map cannot exist between spending and any performance measure¹. For example, in any one period, spending may rise as the result of an increase in the cost of lubricants

¹We suffer from simultaneous equation bias under which the error term in a regression analysis is correlated with the explanatory variable. Simultaneous equation bias plagues the social sciences as we cannot usually perform a controlled experiment.

while performance may decline due to the discovery of an unexpected aging effect. The problem of connecting NP spending to fleet performance must rely on a statistical analysis of changes in both fleet indicators and costs as primary inputs.

This paper re-examines the results in [2]. Instead of focusing on the correlation matrix's structure, we search for relationships in vector autoregressive models of the performance and NP spending time series data. In particular, we apply statistical tests that identify if knowledge of the NP time series improves the prediction of the high level performance indicators. This study provides a complement to [2] and we show that NP spending does not improve the predictability of any CC130 performance time series.

1.2 Scope

ADM(Mat) requires a study to identify possible exploitable information between NP spending and fleet performance. In particular, a former COS(Mat) [3] tasked the DMGOR to search for a methodology that would allow a more logical articulation of the linkage between the resources allocated to National Procurement. In discussions with the former DCOS(Mat), the CC130 Hercules fleet was identified as a priority for the previous study [2]. We extend the analysis in [2] using time series techniques. Our modelling methods aim to:

- use the theory of time series to identify if the mean squared error (MSE) in the prediction of changes in the performance time series data are reduced through knowledge of changes in total NP spending; and
- identify how the results of [2] concord with this study

We obtained all performance data on the CC130 from the AEPM PERFORMA database [4] and NP data from Financial and Managerial Accounting System (FMAS) [5].

We organize the paper in two parts. Following the introduction we informally discuss Granger causality and display key results. Section 3, contains the conclusions and discusses future avenues for research. We reserve the Annex A and annex B for technical discussions on time series statistical test, and for definitions of the performance indicators respectively.

2 Results

In [2], it was determined through random matrix theory that the univariate innovations in changes in NP spending did not correlate with subsequent univariate innovations in the performance change data. The analysis told us that the majority of observed cross-correlations were spurious and could mostly be explained through noise dressing. Furthermore, NP spending did not form a central hub in the minimal spanning tree analysis [2]. These observations suggest that knowledge of changes in NP spending does not improve forecasting changes in the performance time series data.

We seek a further understanding of relationships in the performance and NP spending data using the theory of time series analysis. In particular, we use Granger causality tests [6] to search for information in one time series that can improve the forecast of another time series. We will see that Granger causality tests provide an excellent complement to the work in [2].

The concept of Granger causality rests on the ability to use the past knowledge in one time series to help improve the forecast of another time series. It is true that if one time series actually causes another time series then knowledge of the driving time series will improve the forecasts, but Granger causality does not give us actual causal information. In fact, causality is not something that we can test for statistically, but must be known a priori. An example will help illustrate Granger causality.

Imagine that we have built a crude home-made weather station that we use to predict the weather. We make observations and compare our recordings with our predictions. Our only source of information to make forecasts comes from our weather station, which includes all past observations. Now, suppose that we decide to include Environment Canada's weather observations in our information set when we make a forecast. Given that Environment Canada has state-of-the-art meteorological equipment, the inclusion of their observations in our forecast will almost certainly improve our prediction of the weather. From a time series perspective, Environment Canada's observations Granger cause the weather time series generated by our home-made weather station – we can improve our forecast through the knowledge of Environment Canada's data. The improved weather forecast does not mean that Environment Canada actually causes the weather (after all, shooting the weatherman will not stop the weather), but positive Granger causality effects between the time series imply that we have found a mechanism for reducing the MSE in our forecasts. Clearly, we should use this extra information if we are serious about predicting the weather. Granger causality tests help us establish relevant information and relationships within multiple time series data.

Armed with Granger causality tests, we can now rephrase the problem and search for relationships that extend the findings of the random matrix theory approach and minimal spanning tree technique. Using the theory of time series will provide us with a more refined

analysis and allow us to dive deeper into the data as we search for meaningful relationships. Granger causality methods can be applied generally at CORA across problems which have multiple time series data.

2.1 Data selection

This study uses two data sources for the CC130 fleet: the PERFORMA database for fleet performance indicators, and FMAS for NP spending levels. In total, we select the same 13 high level performance indicators in [2], and we search for connections in the time series data. Furthermore, we break down the NP spending into spares and R&O to help identify relationships within spending subsets. For this study, we use cost centres:

- 8485QA: CC130 Spares;
- 8485QB: T56 Engine Spares;
- 8485QH: CC130 Airframe Repair and Overhaul;
- 8485QJ: CC130 Miscellaneous Engine;
- 8485QL: CC130 T56 Engine Repair and Overhaul;
- 8485TM: Repair and Overhaul Flight Navigation Communication Equipment and;
- 8485UQ: CC130 Ties.

In the total NP part of the study, we used the data from all cost centres while in the spares/R&O breakdown part of the study we use 8485QA, 8485QB, and 8485QH, 8485QJ, 8485QL respectively.

We use the PERFORMA database to extract 10 years of monthly data (December of 1998 to November 2008, representing the same data set as [2]) for the performance indicators, thereby giving us 120 measurements. In the data selection process, we need to ensure that time series data captures the fleet's performance at a high level with an expectation that NP spending has an effect on the indicators themselves. The performance indicators we use are:

1. All failures
2. A_o – Overall operational availability
3. Corrective maintenance person-hours rate
4. First level A_o
5. Flying hours

6. Mean flying time between on aircraft corrective forms
7. Mean flying time between on aircraft preventive forms
8. Mean flying time between downing event
9. Off aircraft maintenance person-hour rate
10. On aircraft maintenance person-hour rate
11. On aircraft robs maintenance person-hour rate
12. Operation mission abort rate
13. Preventive maintenance person-hour rate

A full description of each performance indicator can be found in Annex B. The data we select from the PERFORMA database concords with the type of data examined in past attempts that address the NP allocation problem. Applying time series methods to the data expands not only on the work in [1], but also on previous (unpublished) work that focused on A_o as the main object to connect with NP spending [1].

We obtained the financial data from FMAS broken down by spares and R&O. The data covers the same time frame (in monthly form) as the performance indicator data. The financial data are placed inside a 13 month year to account for spending invoiced at the end of one fiscal year but expensed in the following fiscal year. We correct for the 13 month year by placing the data from the 13th month into the first month of the new fiscal year. We understand that from an accounting perspective the 13th month represents a separate entity to capture actual previous fiscal year spending relationships, but for our study, we need to treat spending as a continuous process. Moving the 13th month spending into the first fiscal month of the following year has the effect of removing the artificial discontinuous seasonal jump that we see in the spending data at fiscal year changes. Since we desire a relationship between incremental changes in the data, we must ensure that we make appropriate comparisons with continuous time. We treat spending on spares, spending on R&O, and total NP spending separately in the analysis.

2.2 Analysis

We break the analysis down into three parts: performance indicators with total NP spending, performance indicators with spares spending, and performance indicators with R&O spending. Before we apply time series modelling, we need to put the data in a standard form through the transformation,

$$\tilde{y}_i(t) = \log \left(\frac{x_{i+1}}{x_i} \right), \quad (1)$$

where x_i denotes the individual time series values. As we are not interested in absolute levels², eq.(1) ensures that we compare changes in NP spending to changes in performance time series. In the small change approximation, eq.(1) expresses the percent change in the time series level. The effect of changes represent the relationships that we wish to examine. To perform our analysis, we use MATLAB®'s Econometrics Toolbox, and Statistics Toolbox which contain all the routines needed for detailed time series analysis.

We test the transformed data for stationarity by using the augmented Dickey-Fuller test (see [7] for details) with lags from 0 to 14 to assess the null hypothesis of a unit root with and without drift. We find that we can reject the null hypothesis at the 95% confidence level for all of the time series studied. Thus, we accept that each time series is stationary.

Next, we create 14 bivariate time series, pairing NP spending with each performance indicator. Using the Akaike information criterion, we determine the best fit bivariate model for each of the 14 cases. In each case, we test the residuals of the best fit model for heteroskedasticity using Engle's ARCH test to detect model misspecification. We find that we cannot reject the null hypothesis of no ARCH effects at the 95% confidence level in each case of the 14 cases and thus we accept each best fit VAR model.

Using the F-test, we test each VAR model for Granger causality under the null hypothesis that NP spending does not Granger cause any performance time series. Since we perform 14 F-tests in each spending-performance time series analysis, we use the 99% critical value of the F-test to prevent rejecting the null hypothesis through type I errors.

In Table 1, we show the F-test results for Granger causality on all bivariate models of performance with NP, spares and R&O spending. For total NP spending, we cannot reject the null hypothesis of no Granger causality at the 99% confidence level (or at the 95% confidence level). Thus, changes in NP spending do not Granger cause any of the changes in performance indicators, which means that we cannot improve the linear forecast of performance based on knowledge of the changes in the NP spending time series. We also see that changes in spending on spares do not Granger cause changes in performance. For each case, we test the robustness of the results by changing the lags in the best fit models by two units in each direction around the Akaike information criterion. In all cases, the acceptance of the null for NP and spares spending is maintained. However, at the 99% confidence level, we see that changes in R&O spending allow us to reject the null hypothesis of no Granger causality for changes in Flying Hours (TS5) and changes in Operation Mission Abort Rate (TS12). While the result suggests that we can use R&O spending to help improve the forecast of Flying Hours and Operation Mission Abort Rate, the results are not robust under a sensitivity analysis around the minimum of the Akaike information criterion. If we change the best fit model by two lags in either direction, the rejection of the null hypothesis disappears. Since we have no underlying model linking any of the performance indicators to R&O spending, the lack of robustness in the result tells us that we

²The client is concerned with the effect of changes in performance from changes in spending.

Table 1: Granger causality F-test (Spending Granger causing performance)

F value	TS1	TS2	TS3	TS4	TS5	TS6	TS7	TS8	TS9	TS10	TS11	TS12	TS13
Total NP Spending													
$F_{0,99}$	2.4093	3.2002	2.3638	3.2002	2.7064	2.7064	2.8292	3.2002	3.2002	2.7064	3.2002	2.9877	2.7064
F -value	0.8181	0.6186	1.4290	0.5348	1.7829	1.3435	1.3641	1.6711	0.3447	0.9124	0.4707	1.1610	0.443
Spares Spending													
$F_{0,99}$	2.3258	3.2002	2.3258	3.2002	2.3258	2.7064	2.7064	3.2002	2.3258	2.7064	2.3258	2.3258	2.3638
F -value	0.9060	0.9330	0.5890	0.9539	0.6363	1.6719	1.0322	0.9780	0.7059	1.6759	1.1728	0.8816	0.8472
R&O Spending													
$F_{0,99}$	2.3258	2.9877	2.3638	3.2002	2.7064	2.7064	2.8292	3.2002	3.2002	2.7064	3.2002	2.5291	2.4637
F -value	0.9849	1.0728	1.9753	0.8868	2.7165	1.9515	1.5998	2.9922	1.8439	1.3955	0.4714	2.9525	1.8261

should cautiously reject the conclusion that R&O spending Granger causes Flying Hours or the Operation Mission Abort Rate. These two time series should be flagged for future analysis.

Finally, we turn the problem around to see if changes in one of the performance indicators Granger cause spending changes. In table 2 we see that we cannot reject the null hypothesis of no Granger causality. Again, the results are robust under changing the lags by two unit in each direction.

Table 2: Granger causality F-test (Performance Granger causing spending)

F value	TS1	TS2	TS3	TS4	TS5	TS6	TS7	TS8	TS9	TS10	TS11	TS12	TS13
Performance on NP Spending													
$F_{0.99}$	2.4093	3.2002	2.3638	3.2002	2.7064	2.7064	2.8292	3.2002	3.2002	2.7064	3.2002	2.9877	2.7064
F -value (NP)	2.0627	0.9954	0.6721	0.4302	1.4381	1.4644	0.4310	0.6445	0.7010	1.2509	1.2763	1.3095	0.9124
Performance on Spare Spending													
$F_{0.99}$	2.3258	3.2002	2.3258	3.2002	2.3258	2.7064	2.7064	3.2002	2.3258	2.7064	2.3258	2.3258	2.3638
F -value	1.7456	0.3367	1.1387	0.5586	0.9319	1.1523	1.7251	0.7634	1.4766	1.4690	1.5450	0.7760	1.0909
Performance on R&O Spending													
$F_{0.99}$	2.3258	2.9877	2.3638	3.2002	2.7064	2.7064	2.8292	3.2002	3.2002	2.7064	3.2002	2.5291	2.4637
F -value	1.3244	0.7934	0.4040	0.2682	1.2073	1.5114	0.7497	0.4396	0.9313	0.4846	0.8499	1.4659	0.7075

3 Conclusions

Searching for a connection between NP spending and fleet performance indicators represents a difficult problem. Past attempts, based largely on filter methods, have met defence scientists with frustration. In 2010, the DMGOR re-analyzed the problem from a random matrix theory and a minimal spanning tree approach [2] and found that NP spending was not strongly linked to any performance indicator. In particular, [2] discovered that the univariate spending innovations were not correlated with subsequent performance time series innovations in any meaningful way.

The application of Granger causality test provides a new method for looking at spending and performance data. Granger causality tells us which time series contain information that allow us to reduce the MSE forecasting error in another time series. The application of this technique to spending and CC130 fleet performance data from December 1998 to November 2008 confirms the results in [2] and provides the CF with a new tool to help search for relationships in time series data. In our analysis, we found that (R&O) spending potentially Granger causes Flying Hours and the Operation Mission Abort Rate, yet the effect disappears under slight model respecifications. This result suggests that we focus on these time series in future analysis. Interestingly, the Operation Mission Abort Rate appears close to (R&O) spending in the dendrogram in [2] (although not part of a central hub).

We must stress that Granger causality does not tell us anything about actual causality or the direction of any causal relationships. For example, it has been shown (see [7]) that stock prices Granger cause dividends when in reality it is the market's assessment of dividend policies that set stock prices. This observation shows that Granger causality can mix up the real underlying causal direction. Granger causality tests can help us understand forward looking effects in the data. In the stock price and dividend example, Granger causality tells us that stock prices are forward looking and hence they cannot be predicted based on observing other time series, such as dividends, even if the other time series are known entities in stock price formation. In spending and fleet performance issues, we can use the same tests to uncover forward looking spending effects on maintenance. If future analysis show that R&O spending continue to Granger cause Flying Hours and the Operation Mission Abort Rate, we must guard against the interpretation that changes in R&O spending cause changes in the other time series. The fleet may have forward looking behaviour under which known problems that will reduce future Flying Hours or cause a higher Operation Mission Abort Rate induce decision makers to act. In this case, the causality runs in the opposite direction to the Granger causality finding.

We should stress that not discovering Granger causality in spending and fleet performance data does not imply inefficiency. In fact, an efficiently maintained fleet should not show a strong correlation between routine spending and performance changes. On the other hand, we caution that these results do not imply that the underlying supply chain is optimal

– the robustness to spending shocks may simply arise from non-optimally high inventory levels. We cannot address supply chain issues or optimal sparing through Granger causality tests. From the analysis in this study, we can only conclude that NP spending changes do not correlate with subsequent performance changes and vice versa within the fluctuations observed of the data. Further analysis is warranted on the supply chain to understand the reasons behind the lack of Granger causality.

References

- [1] Dr. P. E. Desmier , Private communication, (February 1, 2009).
- [2] D. W. Maybury, A Random Matrix Theory Approach to National Procurement Spending, DRDC CORA TM 2010-168, (August 2011).
- [3] K. F. Ready, Private communication, (February 06, 2003).
- [4] InnoVision Consulting Inc., AEPM PERFORMA, DV6000.4000.6052.
- [5] Financial Managerial Accounting System, <http://DRMIS-SIGRD.MIL.CA>
- [6] C. W. J. Granger, Investigating Causal Relations by Econometric Models and Cross-Spectral Methods, *Econometrica* (*Econometrica*, Vol. 37, No. 3) 37 (3): 424-438, (1969).
- [7] J. D. Hamilton, *Time Series Analysis*, Princeton University Press, (1994).
- [8] P. J. Brockwell, and R.A. Davis, *Introduction to Time Series*, Springer, (2001).

Annex A: Time series and Granger causality

In this study, we focus on vector autoregression (VAR) to describe the time series data of the CC-130 fleet. The theory of times series analysis (see for example, [7], [8]) is a vast subject and it is not the intention of this paper to develop the theory in any detail. We refer the interested reader to the references to see a careful construction of the theoretical details. The basic building block for our time series modelling is the white noise process,

$$\varepsilon_t \sim \text{i.i.d. } \mathcal{N}(0, \sigma_\varepsilon), \quad (\text{A.1})$$

with the implications:

- $\mathbb{E}(\varepsilon_t) = \mathbb{E}(\varepsilon_t | \varepsilon_{t-1}, \varepsilon_{t-2}, \varepsilon_{t-3}, \dots) = \mathbb{E}(\varepsilon_t | \text{all information at } t-1) = 0$;
- $\mathbb{E}(\varepsilon_t \varepsilon_{t-j}) = 0$; and
- $\text{var}(\varepsilon_t) = \text{var}(\varepsilon_t | \varepsilon_{t-1}, \varepsilon_{t-2}, \varepsilon_{t-3}, \dots) = \text{var}(\varepsilon_t | \text{all information at } t-1) = \sigma_\varepsilon^2$.

The central idea behind our white noise process stands on the lack of predictability or serial correlation and on homoscedastic variance (*i.e.*, the variance does not change with time). More general white noise processes exist, but we will only need the above process for this study.

Univariate time series models are based on linear projections on to past information. Imagine that we wish to forecast a random variable Y_{t+1} based on the information in $\mathbf{X}_t$. As an example, $\mathbf{X}_t$ might be the last m values of Y_{t+1} , in which case $\mathbf{X}_t$ is a vector of a constant plus $Y_t, Y_{t-1}, Y_{t-2}, \dots, Y_{t-m+1}$. To determine the usefulness of the forecast, Y_{t+1}^* , we require a loss function that tells us how much the forecast deviates from moment to moment. The most useful function for our purposes is the quadratic loss function,

$$\mathbb{E}(Y_{t+1} - Y_{t+1|t}^*)^2, \quad (\text{A.2})$$

which we seek to minimize. Eq.(A.2) is the mean squared error (MSE) associated with our forecast. We can show that the forecast that minimizes the MSE reads,

$$Y_{t+1}^* = \mathbb{E}(Y_{t+1} | \mathbf{X}_t). \quad (\text{A.3})$$

If we now restrict ourselves to linear forecasts such that,

$$Y_{t+1|t}^* = \alpha' \mathbf{X}_t, \quad (\text{A.4})$$

where α is a coefficient vector, then the linear project determines α through

$$\mathbb{E}[(Y_{t+1} - \alpha' \mathbf{X}_t) \mathbf{X}_t'] = \mathbf{0}. \quad (\text{A.5})$$

We can view the expectation operator as a generalized inner product, and we see that the error in the linear forecast is orthogonal to the vector containing the information at time t . Thus, we have

$$\alpha' = \mathbb{E}(Y_{t+1}\mathbf{X}_t')[\mathbb{E}(\mathbf{X}_t\mathbf{X}_t')]^{-1} \quad (\text{A.6})$$

which closely follows the ordinary least squares (OLS) construction³. We denote the linear projection as,

$$\hat{P}(Y_{t+1}|\mathbf{X}_t) = \alpha'\mathbf{X}_t, \quad (\text{A.7})$$

and if we include a constant term, we write,

$$\hat{E}(Y_{t+1}|\mathbf{X}_t) \equiv \hat{P}(Y_{t+1}|1, \mathbf{X}_t). \quad (\text{A.8})$$

The linear forecasts are built from linear combinations of white noise processes. Univariate examples include,

- AR(1): $y_t = \phi_1 y_{t-1} + \varepsilon_t$;
- AR(p): $y_t = \phi_1 y_{t-1} + \phi_2 y_{t-2} + \dots + \phi_p y_{t-p} + \varepsilon_t$;
- MA(1): $y_t = \varepsilon_t + \theta_1 \varepsilon_{t-1}$;
- MA(q): $y_t = \varepsilon_t + \theta_1 \varepsilon_{t-1} + \theta_2 \varepsilon_{t-2} + \dots + \theta_q \varepsilon_{t-q}$; and
- ARMA(p,q): $y_t = \phi_1 y_{t-1} + \phi_2 y_{t-2} + \dots + \phi_p y_{t-p} + \varepsilon_t + \theta_1 \varepsilon_{t-1} + \theta_2 \varepsilon_{t-2} + \dots + \theta_q \varepsilon_{t-q}$,

where AR and MA denote autoregressive and moving average respectively. A convenient notation uses lag operators to represent the time series,

$$Ly_t = y_{t-1}. \quad (\text{A.9})$$

Thus, we can write an AR(p) process as,

$$(1 - \phi_1 L - \phi_2 L^2 - \dots - \phi_p L^p)y_t = \varepsilon_t, \quad (\text{A.10})$$

and an MA(q) process as

$$y_t = (1 + \theta_1 L + \theta_2 L^2 + \dots + \theta_q L^q)\varepsilon_t. \quad (\text{A.11})$$

In a more compact form, we can write the lag polynomials $a(L) = (1 - \phi_1 L - \phi_2 L^2 - \dots - \phi_p L^p)$ and $b(L) = (1 + \theta_1 L + \theta_2 L^2 + \dots + \theta_q L^q)$ respectively. By promoting y_t to a vector of observations $(y_{1t}, y_{2t}, \dots)$, we can write the autoregressive lag polynomial as a vector equation,

$$\mathbf{y}_t = \mathbf{c} + \Phi_1 \mathbf{y}_{t-1} + \Phi_2 \mathbf{y}_{t-2} + \dots + \Phi_p \mathbf{y}_{t-p} + \varepsilon_t, \quad (\text{A.12})$$

³The comparison with OLS rests on the stationary and ergodicity. For details see [7].

where each coefficient, Φ_i , has been promoted to a matrix and $\mathbf{c}$ represents a constant vector. In this study, we will focus on applying the vector autoregression of eq.(A.12) to the CC130 data set. Provide that we have an invertible process, we can always convert an (vector) autoregressive process into a pure (vector) moving average process by inverting the lag polynomials. Thus, if an invertible process contains a moving average component, we can rewrite the same process as an autoregressive process. For more details on invertability, see [7].

Imagine that we have a pair of time series written in vector autoregressive form,

$$\begin{bmatrix} y_{1,t} \\ y_{2,t} \end{bmatrix} = \begin{bmatrix} c_1 \\ c_2 \end{bmatrix} + \begin{bmatrix} \phi_{11}^{(1)} & \phi_{12}^{(1)} & y_{1,t-1} \\ \phi_{21}^{(1)} & \phi_{22}^{(1)} & y_{2,t-1} \end{bmatrix} + \dots + \begin{bmatrix} \phi_{11}^{(p)} & \phi_{12}^{(p)} \\ \phi_{21}^{(p)} & \phi_{22}^{(p)} \end{bmatrix} \begin{bmatrix} y_{1,t-p} \\ y_{2,t-p} \end{bmatrix} + \begin{bmatrix} \varepsilon_{1,t} \\ \varepsilon_{2,t} \end{bmatrix}. \quad (\text{A.13})$$

As a point of investigation, we may wish to know if knowledge of one of the component time series improves the forecast of the other component time series. Specifically, if we find that the mean squared error of the linear projection of the first time series, $y_{1,t}$, on all the available information does not depend on knowledge in the second time series, $y_{2,t}$ namely,

$$\text{MSE}[\hat{E}(y_{1,t+s}|y_{1,t}, y_{1,t-1}, \dots)] = \text{MSE}[\hat{E}(y_{1,t+s}|y_{1,t}, y_{1,t-1}, \dots, y_{2,t}, y_{2,t-1}, \dots)], \quad (\text{A.14})$$

then we say that the time series $y_{2,t}$ is not linearly informative about the future of $y_{1,t}$. On the other hand, if $y_{2,t}$ can improve the forecast of $y_{1,t}$, we say that $y_{2,t}$ *Granger causes* $y_{1,t}$.

In the bivariate VAR representation, y_2 does not Granger cause y_1 if the coefficient matrices Φ_j of eq.(A.13) are all lower triangular. We can test for Granger causality by recognizing that eq.(A.12) implies,

$$y_{1,t} = c_1 + \alpha_1 y_{1,t-1} + \alpha_2 y_{1,t-2} + \dots + \alpha_p y_{1,t-p} + \beta_1 y_{2,t-1} + \beta_2 y_{2,t-2} + \dots + \beta_p y_{2,t-p} + \varepsilon_t. \quad (\text{A.15})$$

If we make the null hypothesis that,

$$H_0 : \beta_1 = \beta_2 = \dots = \beta_p = 0, \quad (\text{A.16})$$

then we can use an F -test on the residuals to accept or reject the hypothesis. Specifically, we use the squared residuals of eq.(A.15),

$$RSS_1 = \sum_{t=1}^T \hat{\varepsilon}_t^2, \quad (\text{A.17})$$

with the univariate squared residual for $y_{1,t}$,

$$RSS_0 = \sum_{t=1}^T \hat{e}_t^2, \quad (\text{A.18})$$

where

$$y_{1,t} = c_0 + \gamma_1 y_{1,t-1} + \gamma_2 y_{1,t-2} + \dots + \gamma_p y_{1,t-p} + e_t, \quad (\text{A.19})$$

to give the $F(p, T - 2p - 1)$ distributed test statistic

$$S = \frac{(RSS_0 - RSS_1)/p}{RSS_1/(T - 2p - 1)}, \quad (\text{A.20})$$

(see [7] for details.) The essential idea behind the test for Granger causality rests on our ability to reject the null hypothesis that the coefficient matrices Φ_j are lower triangular. We should stress that the test for Granger causality can be surprisingly sensitive to the number of lags used in the autoregression. In this paper, we use the Akaike information criteria (see [8]) for the construction) to set the number of lags in our analysis, and we perform a sensitivity analysis around the best fit model.

Annex B: Fleet indicator definitions

This Annex contains the definitions of the fleet indicators used in the analysis provided in this paper. The definitions listed below are taken verbatim from the PERFORMA database. Further technical information can be found in the PERFORMA database[4].

All Failures

Definition: All Failures are the sum of the On-A/C Failures and the Off-A/C Failures.

- On-A/C Failures: Total number of failures recorded on a CF 349 form against a piece of equipment installed on an Aircraft. Those are determined from all entries recorded on the On-A/C CF 349 maintenance forms against any valid WUC, where the equipment had to be replaced or repaired in order to return the Aircraft to a serviceable status. This includes all valid Sequence 1 and 2 line entries.
- Off-A/C Failures: Total number of failures recorded against uninstalled equipment. An Off-A/C form is defined as a CF 349 form without an Aircraft number or a CF 543 form. A failure will have a Fix = 3 or for non-serialized items, the Fix = 6 with a contractor Fixer Unit Code (3 letters) and a supplementary data of TLRO/TLIR/TLM.

Ao – Operational Availability as % of time

Definition: (Ao) Operational Availability as % of time is the proportion of observed time that a group of Aircraft is in an operable state (not undergoing maintenance) in relation to the total operational time available during a stated period. Operational Availability as percentage of time is calculated using: $Ao = \text{Up Time} / (\text{Up Time} + \text{Down Time})$ Where: “Up Time” is the total actual number of calendar hours where the selected Aircraft are not undergoing any maintenance action during the chosen period (no open CF 349) and the Allocation Code is not “LX”. And: “Up Time + Down Time” is the total number of calendar hours included in the selected period of the analysis. In calculating all downtimes and uptimes, the date and time are translated to the nearest hour based on 24/7 operations.

Corrective Maintenance Person-Hours Rate

Definition: Total number of “Maintenance Person-Hours” reported on CF 349 and CF 543 corrective maintenance forms for every 1000 hours flown by a specific fleet. This calculation involves three defaults when examining MPHRs for a particular component.

- Installation Factor (IF): Quantity of the same item that is installed on a single Aircraft (e.g. there are two engines on the Aircraft). The Installation Factor information is not available so 1 is used as default.

- Fitment Factor (FF): Proportion of a fleet onto which equipment is fitted (e.g. EW equipment is not installed on all Aircraft). The FF information is not available so 1 is used as default (for 100% of fleet).
- Duty Cycle (DC): Proportion of time a piece of equipment is on when an Aircraft is operating (e.g. even when installed, EW equipment does not operate for the entire duration of a flight). The DC information is not available so 1 is used as default (for 100% of mission time).

First Level Availability

Definition: First Level Availability (First Level Ao) is the proportion of observed time where routine maintenance is not carried out on the group of “First Level Aircraft” (First Level Up Time), in relation to the total cumulative time where those Aircraft could have been available (First Level Total Time). The First Level Availability is based on the time that an aircraft is considered to be in First Level and not on calendar time. Therefore, an aircraft may be in First Level for only two days in one month and have First Level Availability of 80% for that month if it was available for 80% of the time that it was in First Level. First Level Availability is an availability calculation done specifically for the group of “First Level Aircraft” which are those that are considered to be used for the daily flying; they are owned by military units, have an allocation code “CX” or “GX” and can either be serviceable or be undergoing “First Level maintenance”, generally 1st level of maintenance. First Level Availability is calculated using: $\text{First Level Ao} = (\text{First Level Uptime}) / (\text{First Level Total Time})$ Where: The “First Level Total Time” is calculated using: $\text{First Level Total Time} = (\text{First Level Uptime} + \text{First Level Downtime})$

Note that the First Level Total Time is not necessarily the complete calendar time for the query expression but the calendar time during which an aircraft was considered to be in first level. The downtimes excluded from the “First Level Total Time” calculation are the downtimes for a distinct tail number where the CF 349s reporting On-A/C maintenance work are from one of the following categories:

- “Non-routine maintenance” action (see list below);
- “Routine maintenance” (see list below) occurring simultaneously with a non-routine; maintenance action (i.e. put u/s date of the "routine maintenance" is during a “non-routine maintenance” form downtime);
- Maintenance action reported by 2nd or 3rd line (i.e. How Found = D); and
- Maintenance action reported by a non-military fixer unit (i.e. alphanumeric fixer unit)

The “First Level Downtime” is calculated from the downing events for a distinct tail number where the CF 349s reporting On-A/C maintenance work are not from the four categories

listed above. The downtimes for all these downing events are calculated for each distinct tail number and added up to get the total “First Level Downtime”. A downing event downtime is composed of a single or a group of CF 349s reporting work performed On-A/C (i.e. CF 349s must have a tail number) from the time the Aircraft was first put u/s to the completion of the maintenance work that brings the Aircraft to a serviceable status. The downtime calculation for any downing event starts when a CF 349 form is opened against a distinct tail number (put u/s date-time when the Aircraft becomes unserviceable) and ends when the last CF 349 is closed ’ (last certified serviceable date-time bringing the Aircraft back to a serviceable status) The “First Level Up Time” is defined as any period where a First Level Aircraft is not undergoing maintenance.

Flying Hours

Definition: Total flying hours recorded by the aircrew during a given time period as reported via the monthly AUSR report.

Mean Flying Time Between On-A/C Corrective Forms

Definition: Average elapsed flying time between two consecutive On-A/C Corrective Forms. This is determined by dividing the total operating hours of a piece of equipment over a given period by the total number of On-A/C Corrective Forms recorded against that equipment. For periods with no forms or events occurring, the operating hours will be shown.

Mean Flying Time Between On-A/C Preventive Forms

Definition: Average elapsed flying time between two consecutive On-A/C Preventive Forms. This is determined by dividing the total operating hours of a piece of equipment over a given period by the total number of On-A/C Preventive Forms recorded against that equipment. For periods with no forms or events occurring, the operating hours will be shown. This parameter is more suitable for analysis at the system or component level.

Mean Flying Time Between Downing Events

Definition: MFTBDE indicates the average flying hours between two consecutive Aircraft Downing Events. A downing event refers to any single occurrence, or group of occurrences, where an Aircraft is brought from a Serviceable/Operational status to an Unserviceable/Repair status. These include both Preventive and Corrective Maintenance Actions reported against an operational Aircraft. Only forms with a numerical fixer unit are included in an event. A downing event may include several failures that are all repaired following the single downing event.

Off-A/C Maintenance Person-Hours Rate

Definition: Total number of “Maintenance Person-Hours” reported on “Off-A/C” forms for every 1000 hours flown by a specific fleet or selected Aircraft.

This calculation involves three defaults when examining MPHRS for a particular component.

- **Installation Factor (IF):** Quantity of the same item that is installed on a single Aircraft (e.g. there are two engines on the Aircraft). The Installation Factor information is not available so 1 is used as default.
- **Fitment Factor (FF):** Proportion of a fleet onto which equipment is fitted (e.g. EW equipment is not installed on all Aircraft). The FF information is not available so 1 is used as default (for 100% of fleet).
- **Duty Cycle (DC):** Proportion of time a piece of equipment is on when an Aircraft is operating (e.g. even when installed, EW equipment does not operate for the entire duration of a flight). The DC information is not available so 1 is used as default (for 100% of mission time).

On-A/C Maintenance Person-Hours Rate

Definition: Total number of “Maintenance Person-Hours” reported on “On-A/C” forms for every 1000 hours flown by a specific fleet or selected Aircraft.

This calculation involves three defaults when examining MPHRS for a particular component.

- **Installation Factor (IF):** Quantity of the same item that is installed on a single Aircraft (e.g. there are two engines on the Aircraft). The Installation Factor information is not available so 1 is used as default.
- **Fitment Factor (FF):** Proportion of a fleet onto which equipment is fitted (e.g. EW equipment is not installed on all Aircraft). The FF information is not available so 1 is used as default (for 100% of fleet).
- **Duty Cycle (DC):** Proportion of time a piece of equipment is on when an Aircraft is operating (e.g. even when installed, EW equipment does not operate for the entire duration of a flight). The DC information is not available so 1 is used as default (for 100% of mission time).

On Aircraft Robs Maintenance Person-Hour Rate

Definition: Number of “Maintenance Person-Hours” reported against a ROB on “On-A/C forms” for every 1000 hours flown by a specific fleet or selected Aircraft. This calculation involves three defaults when examining MPHRS for a particular component.

- **Installation Factor (IF):** Quantity of the same item that is installed on a single Aircraft (e.g. there are two engines on the Aircraft). The Installation Factor information is not available so 1 is used as default.

- Fitment Factor (FF): Proportion of a fleet onto which equipment is fitted (e.g. EW equipment is not installed on all Aircraft). The FF information is not available so 1 is used as default (for 100% of fleet).
- Duty Cycle (DC): Proportion of time a piece of equipment is on when an Aircraft is operating (e.g. even when installed, EW equipment does not operate for the entire duration of a flight). The DC information is not available so 1 is used as default (for 100% of mission time).

Ops Mission Aborts Rate

Definition: Total number of “Ops Mission Aborts” reported for every 1000 hours flown by a specific fleet.

Rate calculations involve three defaults.

- Installation Factor (IF): Quantity of the same item that is installed on a single Aircraft (e.g. there are two engines on the Aircraft). The Installation Factor information is not available so 1 is used as default.
- Fitment Factor (FF): Proportion of a fleet onto which equipment is fitted (e.g. EW equipment is not installed on all Aircraft). The FF information is not available so 1 is used as default (for 100% of fleet).
- Duty Cycle (DC): Proportion of time a piece of equipment is on when an Aircraft is operating (e.g. even when installed, EW equipment does not operate for the entire duration of a flight). The DC information is not available so 1 is used as default (for 100% of mission time).

Preventive Maintenance Person-Hours Rate

Definition: Total number of “Maintenance Person-Hours” reported on CF 349 and CF 543 preventive maintenance forms for every 1000 hours flown by a specific fleet. This calculation involves three defaults when examining MPHRs for a particular component.

- Installation Factor (IF): Quantity of the same item that is installed on a single Aircraft (e.g. there are two engines on the Aircraft). The Installation Factor information is not available so 1 is used as default.
- Fitment Factor (FF): Proportion of a fleet onto which equipment is fitted (e.g. EW equipment is not installed on all Aircraft). The FF information is not available so 1 is used as default (for 100% of fleet).
- Duty Cycle (DC): Proportion of time a piece of equipment is on when an Aircraft is operating (e.g. even when installed, EW equipment does not operate for the entire duration of a flight). The DC information is not available so 1 is used as default (for 100% of mission time).

List of Acronyms

ADM(Mat)	Assistant Deputy Minister (Materiel)
A_o	Operational Availability
AUSR	Aircraft Utilization Statistical Report
CORA	Centre for Operational Research and Analysis
COS(Mat)	Chief of Staff (Materiel)
DCOS(Mat)	Deputy Chief of Staff (Materiel)
DMGOR	Directorate Materiel Group Operational Research
DND	Department of National Defence
DRDC	Defence Research and Development Canada
FMAS	Financial and Managerial Accounting System
ILS	Integrated Logistics Support
MSE	Mean Squared Error
NP	National Procurement
R&O	Repair and Overhaul
TLRO	Third Line Repair and Overhaul
TLIR	Third Line Inspection and Repair
TLM	Third Line Maintenance
VAR	Vector Autoregression
WUC	Work Unit Code

DOCUMENT CONTROL DATA		
(Security classification of title, body of abstract and indexing annotation must be entered when document is classified)		
1. ORIGINATOR (The name and address of the organization preparing the document. Organizations for whom the document was prepared, e.g. Centre sponsoring a contractor's report, or tasking agency, are entered in section 8.) Defence R&D Canada – CORA Dept. of National Defence, MGen G.R. Pearkes Bldg., 101 Colonel By Drive, Ottawa, Ontario, Canada K1A 0K2	2. SECURITY CLASSIFICATION (Overall security classification of the document including special warning terms if applicable.) UNCLASSIFIED	
3. TITLE (The complete document title as indicated on the title page. Its classification should be indicated by the appropriate abbreviation (S, C or U) in parentheses after the title.) Granger Causality and National Procurement Spending		
4. AUTHORS (Last name, followed by initials – ranks, titles, etc. not to be used.) Maybury, D.W.		
5. DATE OF PUBLICATION (Month and year of publication of document.) September 2011	6a. NO. OF PAGES (Total containing information. Include Annexes, Appendices, etc.) 32	6b. NO. OF REFS (Total cited in document.) 8
7. DESCRIPTIVE NOTES (The category of the document, e.g. technical report, technical note or memorandum. If appropriate, enter the type of report, e.g. interim, progress, summary, annual or final. Give the inclusive dates when a specific reporting period is covered.) Technical Memorandum		
8. SPONSORING ACTIVITY (The name of the department project office or laboratory sponsoring the research and development – include address.) Defence R&D Canada – CORA Dept. of National Defence, MGen G.R. Pearkes Bldg., 101 Colonel By Drive, Ottawa, Ontario, Canada K1A 0K2		
9a. PROJECT NO. (The applicable research and development project number under which the document was written. Please specify whether project or grant.) N/A	9b. GRANT OR CONTRACT NO. (If appropriate, the applicable number under which the document was written.)	
10a. ORIGINATOR'S DOCUMENT NUMBER (The official document number by which the document is identified by the originating activity. This number must be unique to this document.) DRDC CORA TM 2011-154	10b. OTHER DOCUMENT NO(s). (Any other numbers which may be assigned this document either by the originator or by the sponsor.)	
11. DOCUMENT AVAILABILITY (Any limitations on further dissemination of the document, other than those imposed by security classification.) (X) Unlimited distribution () Defence departments and defence contractors; further distribution only as approved () Defence departments and Canadian defence contractors; further distribution only as approved () Government departments and agencies; further distribution only as approved () Defence departments; further distribution only as approved () Other (please specify):		
12. DOCUMENT ANNOUNCEMENT (Any limitation to the bibliographic announcement of this document. This will normally correspond to the Document Availability (11). However, where further distribution (beyond the audience specified in (11)) is possible, a wider announcement audience may be selected.)		

13. ABSTRACT (A brief and factual summary of the document. It may also appear elsewhere in the body of the document itself. It is highly desirable that the abstract of classified documents be unclassified. Each paragraph of the abstract shall begin with an indication of the security classification of the information in the paragraph (unless the document itself is unclassified) represented as (S), (C), (R), or (U). It is not necessary to include here abstracts in both official languages unless the text is bilingual.)

Using Granger causality tests, we look for relationships in performance and National Procurement spending time series data that can improve forecasting capabilities with the CC130 fleet. We find that no meaningful relationships exist between spending and performance indicators within the spending envelope studied. Our results concord with earlier work based on random matrix theory and minimal spanning trees, which suggest the fleet is robust to spending shocks. We conclude that NP spending changes do not correlate with subsequent CC130 Hercules aircraft performance changes and vice versa. Granger causality tests represent a powerful tool which can be used with future fleet studies.

14. KEYWORDS, DESCRIPTORS or IDENTIFIERS (Technically meaningful terms or short phrases that characterize a document and could be helpful in cataloguing the document. They should be selected so that no security classification is required. Identifiers, such as equipment model designation, trade name, military project code name, geographic location may also be included. If possible keywords should be selected from a published thesaurus. e.g. Thesaurus of Engineering and Scientific Terms (TEST) and that thesaurus identified. If it is not possible to select indexing terms which are Unclassified, the classification of each should be indicated as with the title.)

Granger causality
Fleet performance
National procurement spending
Time Series



www.drdc-rddc.gc.ca