



AFRL-RW-EG-TR-2012-064

Relational Information Space for Dynamic Systems

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15 May 2012

FINAL REPORT

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(96ABW-2012-0196)

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REPORT DOCUMENTATION PAGE				Form Approved OMB No. 0704-0188	
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1. REPORT DATE 04-07-2012		2. REPORT TYPE Final		3. DATES COVERED (From - To) (1 Jan 2011)-(15 May 2012)	
4. TITLE AND SUBTITLE Relational Information Space for Dynamic Systems				5a. CONTRACT NUMBER n/a	
				5b. GRANT NUMBER n/a	
				5c. PROGRAM ELEMENT NUMBER 61102F	
6. AUTHOR(S) Robert A. Murphey				5d. PROJECT NUMBER 2304	
				5e. TASK NUMBER AW	
				5f. WORK UNIT NUMBER 95	
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) Air Force Research Laboratory, Munitions Directorate AFRL/RWW 101 West Eglin Boulevard Eglin AFB, FL 32542-6810				8. PERFORMING ORGANIZATION REPORT NUMBER AFRL-RW-EG-TR-2012-064	
9. SPONSORING / MONITORING AGENCY NAME(S) AND ADDRESS(ES) Air Force Research Laboratory, Munitions Directorate AFRL/RWG 101 West Eglin Boulevard Eglin AFB, FL 32542-6810				10. SPONSOR/MONITOR'S ACRONYM(S) AFRL-RW-EG	
				11. SPONSOR/MONITOR'S REPORT NUMBER(S) AFRL-RW-EG-TR-2012-064	
12. DISTRIBUTION / AVAILABILITY STATEMENT DISTRIBUTION A. Approved for public release, distribution unlimited. 96ABW-2012-0196. 12 Jun 2012.					
13. SUPPLEMENTARY NOTES DISTRIBUTION STATEMENT INDICATING AUTHORIZED ACCESS IS ON THE COVER PAGE AND BLOCK 12 OF THIS FORM. DATA RIGHTS RESTRICTIONS AND AVAILABILITY OF THIS REPORT ARE SHOWN ON THE NOTICE AND SIGNATURE PAGE.					
14. ABSTRACT Cooperative decentralized control of autonomous vehicles continues to be an important research subject for many military applications. Vehicles communicate with each other and exchange information about their relative environment and use that data to develop decentralized, coordinated control policies. Communication is often represented by an graph, and information exchange is modeled by a discrete-time dynamical system, known as the information loop. When vehicles agree on the information state they have reached an information consensus. In this work a topological manifold for representing complex networks of dynamical entities is shown to be an effective way to represent non-entropic measures of information as low dimensional embeddings in a high dimensional lifted space. A 2 dimensional embedding was developed that demonstrates an efficient frontier of graphs that dominate all others in their ability to reject disturbances and converge rapidly to a consensus.					
15. SUBJECT TERMS DYNAMICS, DIMENSIONAL REDUCTION, INFORMATION THEORY, CONSENSUS, NETWORKS					
16. SECURITY CLASSIFICATION OF:			17. LIMITATION OF ABSTRACT UL	18. NUMBER OF PAGES 30	19a. NAME OF RESPONSIBLE PERSON Robert A. Murphey
a. REPORT UNCLASSIFIED	b. ABSTRACT UNCLASSIFIED	c. THIS PAGE UNCLASSIFIED			19b. TELEPHONE NUMBER (include area code) (850) 882-4033

RELATIONAL INFORMATION SPACE FOR DYNAMICAL SYSTEMS

by

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ABSTRACT

Cooperative decentralized control of autonomous vehicles continues to be an important research subject for many military and civilian applications. Vehicles can communicate with each other and exchange information about their relative positions, target, environment, and use that data to develop decentralized but coordinated control policies. Communication is often represented by an information graph, and information exchange is modeled by a discrete-time dynamical system, known as the information loop. When the vehicles all agree on the information state it is said that they have reached an information “consensus,” which is equivalent to conditional stability of the information loop. Often consensus control is slow to converge or easily destabilized. Being able to assess the quality of communication topologies (information graphs) is critical to determining the quality of a consensus solution.

In this work a topological manifold approach for representing complex networks of dynamical entities is shown to be an effective way to represent non-entropic measures of information as low dimensional embeddings in a high dimensional lifted space. A 2 dimensional embedding (stability margin - convergence rate) was developed that demonstrates an efficient frontier of graph topologies that dominate all others in their ability to reject disturbances and converge rapidly to a consensus.

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Introduction

The study of information dynamics is important for understanding complex networks of dynamical systems with information flows and shared or coordinated control policies. Information dynamics is essentially the study of information flows in a network when modeled as a discrete-time dynamical system. Control policies that shape the dynamics of the information flows in-turn shape the system dynamics of the physical entities within the network (e.g. formations, shared tasks). Vehicle communication is often represented by a communication or information graph, and because of possible delays in information processing and transmission, information exchange is modeled by a discrete-time dynamical system, known as the information loop. Ensuring desired stability and convergence properties of the information loop is critical to efficient performance of a cooperative system. When the vehicles all agree on the information state it is said that they have reached an information “consensus”

Optimizing the convergence rate of the information flow in consensus problems for various networks has long been an active research venue. On the other hand, stability of information flow in application to cooperative control of vehicle formation was comprehensively investigated, and a general method for deriving transfer functions for closed-loop multi-agent systems was recently suggested. However, often improvements of the convergence rate lead to degrading stability and vice-versa. Both stability and convergence are important characteristics of the information flow and should be analyzed together. This work develops an optimization framework for stability and convergence of the information flow in cooperative systems and also investigates the impact of the topology of the communication graph on the stability margin and convergence rate. The set of all graphs that that dominate all others in their ability to reject

disturbances and converge rapidly to a consensus was computed. This set is the efficient frontier or Pareto solution set. A high dimension “information space” may be constructed such that a point in this space corresponds to one possible graph and all possible graphs on n -nodes spans the space. The Pareto solution set is shown to be a 2 dimensional manifold on the information space.

The problem to be addressed is formulated as follows. Suppose there are n vehicles in a cooperative system. Let vector $x_i = (x_{i1}, \dots, x_{im})^T$ determine position of vehicle i in m -dimensional space, and let $X = (x_1, \dots, x_n)$ be an $m \times n$ matrix describing position of the whole system. Communication in the system is represented by a directed communication graph $G = (V, E)$ with V and E being the sets of vertices and edges, respectively, where node i represents vehicle i and the edge from i to j shows that vehicle j receives information from vehicle i (or “watches” vehicle i). Let N_i be the set of outgoing edges of vertex i with $|N_i|$ the cardinality of N_i . The normalized adjacency matrix G and the normalized Laplacian L of G are defined as follows:

$$G = \{g_{ij}\}_{i,j=1}^n, \quad g_{ij} = \begin{cases} |N_i|^{-1}, & j \in N_i, \\ 0, & j \notin N_i \cup \{i\}, \end{cases}$$

$$L = I - G, \tag{1}$$

where I is the identity matrix.

Let $y_k = (y_{1k}, \dots, y_{nk})$ be an error vector, in which component y_{ik} represents the error between an internal state measurement of vehicle i and a time-varying offset function $h_i(k)$ relative to an arbitrary reference at time moment $t = t_k$. For example, $y_{ik} = \|Cx_i(k) - h_i(k)\|$, where C is a matrix and $x_i(k)$ is the position of vehicle i at $t = t_k$. Also, let vector p_k denote information transmitted to

the vehicles at $t = t_k$. The information flow in the cooperative system can be represented by a discrete-time linear dynamical system (information loop)

$$\begin{aligned} q_{k+1} &= \sum_{j=0}^M a_j q_{k-j} + G p_k + L y_k, \quad k = 0, 1, \dots \\ p_k &= \sum_{j=0}^M b_j q_{k-j}, \quad k = 0, 1, \dots \end{aligned} \tag{2}$$

with $q_k = 0$ for $k = -M, \dots, 0$; see [7].

We pose the following questions:

- (i) Given a communication graph G , what is the best possible convergence rate for the information loop in (2)?
- (ii) Given a communication graph G , what is the tradeoff between the convergence rate and stability margin as a function of the information control gains $a_j, b_j, j = 0, \dots, M$?
- (iii) Given a finite set of graphs on “ n ” vertices, what is the best topology of the communication graph G with respect to both the convergence rate and stability margin? Find an ordering of these graphs, from best to worst, that illustrates how some graphs can dominate others.

Convergence Rate.

Conditional convergence for a discrete LTI system is given as follows: G has exactly 1 eigenvalue $\lambda_1=1$ with eigenvector $\mathbf{1}_N$, all other eigenvalues are strictly within the unit disk.

Conditional convergence is equivalent to “consensus” for an LTI information dynamical system.

$$\text{Let } \lim_{k \rightarrow \infty} p_k = p^*, \quad \lim_{k \rightarrow \infty} q_k = q^*, \quad \lim_{k \rightarrow \infty} y_k = y^*, \quad a = \sum_{j=0}^M a_j, \quad b = \sum_{j=0}^M b_j \text{ and } c = (1-a)/b$$

$$\text{Then } q^* = a q^* + G p^* + L y^*, \quad p^* = b q^*$$

If c is an eigenvalue of G it must be 1 and unique with e.vector $\mathbf{1}_N$, can be shown

$$p^* = y + \gamma \mathbf{1}_N \quad \text{with } \gamma \text{ scalar multiplier that determines convergence}$$

Define the block diagonal matrix

$$Q = \begin{bmatrix} N_0 & N_1 & \cdots & N_{M-1} & N_M \\ I & 0 & \cdots & 0 & 0 \\ 0 & I & \cdots & 0 & 0 \\ \vdots & \vdots & \cdots & \vdots & \vdots \\ 0 & 0 & \cdots & I & 0 \end{bmatrix} \quad \text{where } \begin{matrix} N_j = a_j I + b_j G \\ \sum_{j=0}^M (a_j + b_j) = 1 \end{matrix} \quad (3)$$

If Q meets conditional stability (simple eigenvalue of 1, all others within unit disk) then p^* is guaranteed to converge to $p^* = y^* - \tau y^* \mathbf{1}_n$ with τ left eigenvector of G : $\tau \mathbf{1}_n = 1$

$n(M+1)$ eigenvalues of matrix Q found from roots of characteristic polynomials:

$$P_k(s) = s^{M+1} - \sum_{j=0}^M (a_j + \lambda_k b_j) s^{M-j} = 0 \quad \text{for } k = 1, 2, \dots, n$$

with roots s_{kj} such that $s_{11} = 1$, and otherwise $|s_{kj}| < 1$ when conditionally stable

Now define generalized convergence rate as:

$$\varepsilon = 1 - \max_{s_{kj} \neq s_{11}=1} |s_{kj}| \quad (4)$$

which has exact expressions for low order ($M=0$ or 1) controllers but becomes intractable for higher orders (however, it is conjectured that higher order controllers would have limited additional benefit). For instance, for $M=0$

$$\varepsilon = 1 - \max_{k=2,\dots,n} |1 - b_0 + \lambda_k b_0| \quad (5)$$

The maximal convergence ε^* can be found over all strongly connected graphs by solving a quadratic optimization program. It was also proven that only the complete graph has the fastest convergence, $\varepsilon=1$.

Stability Margin

To obtain a measure of stability margin without resorting to gain and phase margins, we first obtain a closed loop transfer function by taking Z-transform as:

$$P(z) = \left(\sum_{j=0}^M b_j z^{-j} \right) \left(\left(z - \sum_{j=0}^M a_j z^{-j} \right) I - \left(\sum_{j=0}^M b_j z^{-j} \right) G \right)^{-1} LY(z) \quad (6)$$

$$P(z) = F(z)Y(z) \text{ where } P(z) = \sum_{k=0}^{\infty} p_k z^{-k}, \text{ and similar for } Q(z), Y(z)$$

The open loop (forward path) transfer function is then:

$$F(z) = (I + \Phi(z))^{-1} \Phi(z), \text{ or } \Phi(z) = F(z)(I - F(z))^{-1} \quad (7)$$

Now compute the inverse of the sensitivity function (defined as the magnitude of this vector from -1 to the closest point on the Nyquist curve plotted for the open loop transfer function):

$$S = (I + \Phi(z))^{-1}, \text{ with } S_{\max} = \max_{|z|=1} |(I + \Phi(z))^{-1}| \text{ so } \delta_m = \min_{|z|=1} |I + \Phi(z)|$$

From this the stability margin is defined as:

$$\delta = \min_{k=2, \dots, n} \min_{|z|=1} \left| \frac{P_k(z)}{P_1(z)} \right| \quad (8)$$

Which again is easily computed for low order controllers (M=0,1,2) but not so easily for higher orders. For example, for M=0,

$$\delta = \min \left| \frac{\operatorname{Re}[1 - \lambda_k]}{[1 - \lambda_k]} - \frac{b_0}{2} |1 - \lambda_k| \right|, \quad a_0 = 1 - b_0 \quad (9)$$

Pareto Framework.

Now we turn to constructing the 2-dimensional manifold or efficient frontier of convergence rate and stability margin. For a graph G , we can formulate the following constrained optimization problem:

$$\begin{aligned} \delta_G^*(\epsilon) = \max_{\substack{a_0, \dots, a_M \\ b_0, \dots, b_M}} \min_{k=2, \dots, n} \min_{|z|=1} \left| \frac{P_k(z)}{P_1(z)} \right| \\ \text{s.t. } |s_{1i}| \leq 1 - \epsilon, \quad P_1(s_{1i}) = 0, \quad i = 2, \dots, M+1, \quad M \geq 1, \\ |s_{ki}| \leq 1 - \epsilon, \quad P_k(s_{ki}) = 0, \quad i = 1, \dots, M+1, \quad k = 2, \dots, n, \quad M \geq 0, \\ \sum_{j=0}^M (a_j + b_j) = 1, \end{aligned} \tag{10}$$

Which has a solution that optimizes controller gains a_j and b_j to find the maximal stability margin $\delta^*G(\epsilon)$ for $\epsilon \in (0, \epsilon^*]$. This is the efficient frontier.

Results.

An efficient frontier was computed for the example graphs in Figure 1. The results are in Figure 2 and 3.

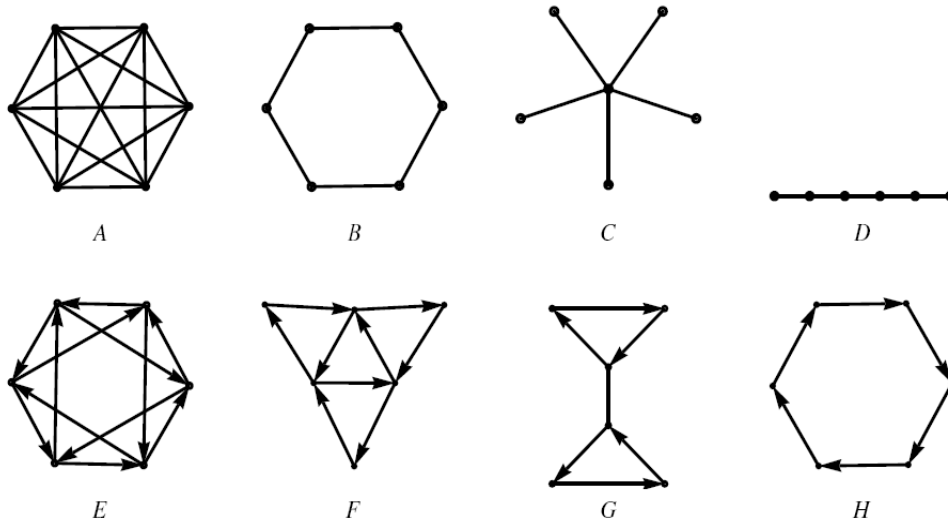


Figure 1: Example Graph Topologies on 6 Nodes.

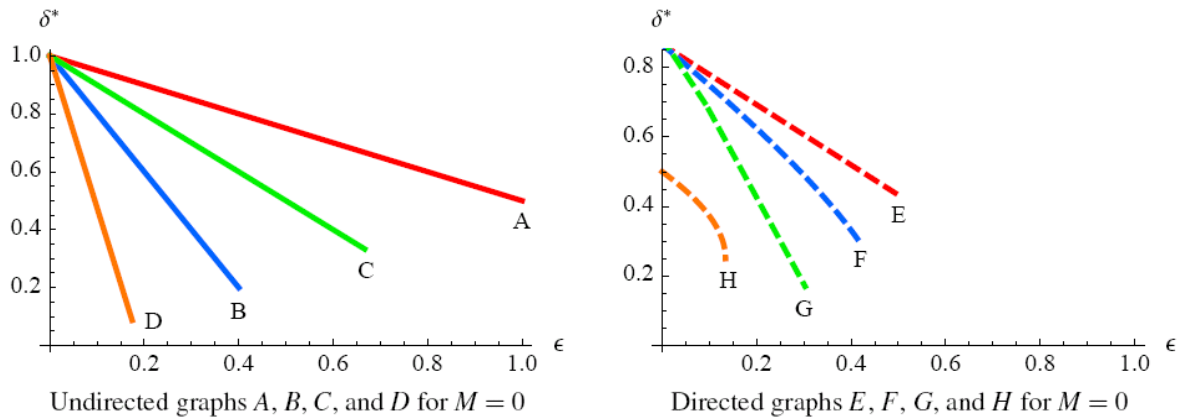


Figure 2. Efficient Frontier For Graphs in Figure 1 with $M=0$

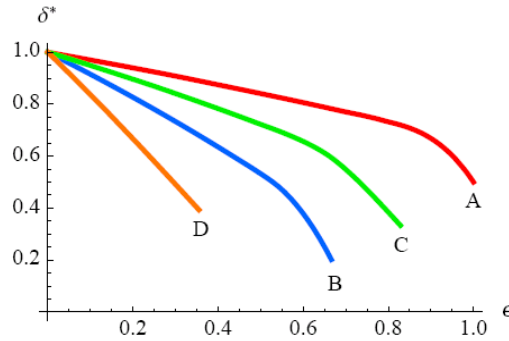


Figure 3. Efficient Frontier For Graphs in Figure 1 with $M=1$

As can be seen, the complete graph always dominates but other graphs do show dominating effects as well. These results show how stability margin can be traded for convergence rate and vice versa. For the zero-order information loop and all strongly connected communication graphs, efficient frontiers have been found analytically, while for the first-order information loop and undirected communication graphs, they have been evaluated numerically. The result that the complete graph has the highest convergence rate and the best efficient frontier can be related to the fact that the normalized adjacency matrix of the complete graph has the minimal number of distinct eigenvalues. In other words, the more distinct eigenvalues the normalized adjacency matrix of a graph has, the more constraints on control gains in the information loop are imposed, and consequently, the lower maximal convergence rate and maximal stability margin are. The complete graph is the primal choice for vehicle communication. However, if for some reason, it cannot be afforded, numerical results show that the “star” graph is the next best choice.

Conference presentation at Conference for Dynamics of Information Systems, Feb 3 2011, Gainesville, FL.

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Trends in Information Dynamics and Autonomy

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Introduction



- **TREND #1. Increasing need to analyze and design complex networked control systems**
 - Systems of systems
 - Blending computation, communications, machine intelligence, control, and human-machine shared knowledge
 - Goal: Faster, more effective complex behaviors
- **TREND #2: Increasing desire to “automate” networks**
 - *Air Force Tech Horizons*
 - Goal: Faster, expanded capabilities (incl. non human friendly)
 - But at what cost?
 - Trust: V&V, role of humans

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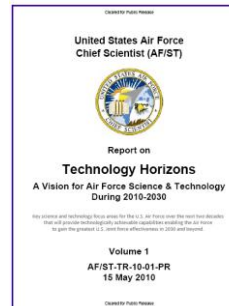


Technology Horizons on Autonomy: “#1 Essential Focus Areas for Air Force S&T Investment”



Excerpts from Werner J.A. Dahm, Chief Scientist of the U.S. Air Force (AF/ST); ltr 15 May 2010:

- Two key areas in which significant advances are possible in the next decade with properly focused Air Force investment are: (i) *increased use of autonomy and autonomous systems*, and (ii) *augmentation of human performance*
- Flexibly autonomous systems can be applied far beyond remotely-piloted aircraft, operational flight programs, and other implementations in use today; *dramatically increased use of autonomy* ...
- Greater use of *highly adaptable and flexibly autonomous systems and processes* can provide significant time-domain operational advantages over adversaries who are limited to human planning and decision speeds; the increased operational tempo that can be gained through greater use of autonomous systems itself represents a significant capability advantage.
- ... will require developing new methods to establish “*certifiable trust in autonomy*” through verification and validation (V&V) of the near-infinite state systems that result from high levels of adaptability
- Developing *V&V methods for highly adaptive autonomous systems* is a major challenge facing the field of control science that may require a decade or more to solve.
- ... natural human capacities are becoming increasingly mismatched to the enormous data volumes, processing capabilities, and decision speeds that technologies offer or demand; *closer human-machine coupling* and augmentation of human performance will become possible and essential.



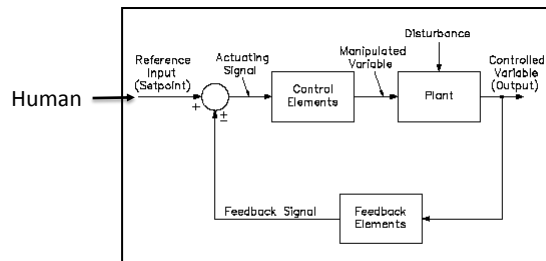
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Evolution of Network Control from Automatic Control to “Systems of Systems”



“Autonomous” within the boundary of the system

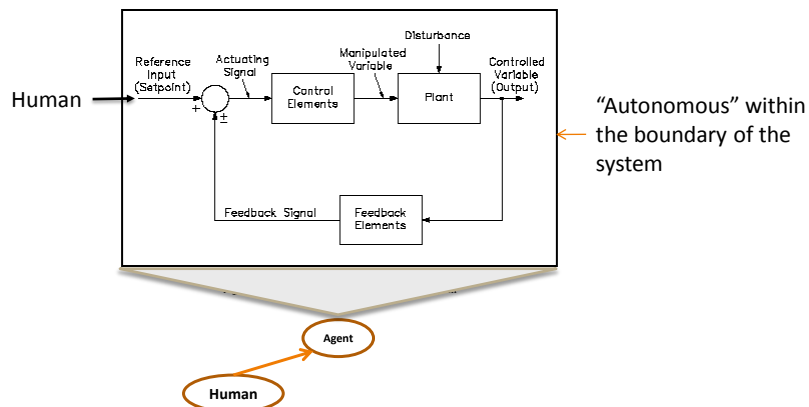
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Evolution of Network Control from Automatic Control to “Systems of Systems”



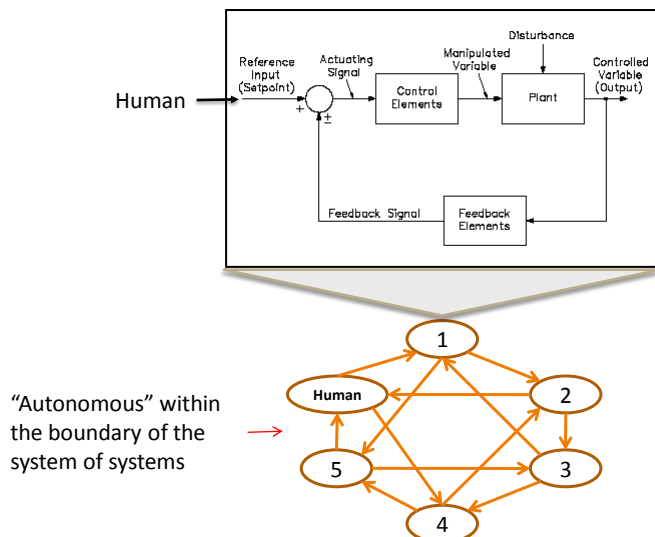
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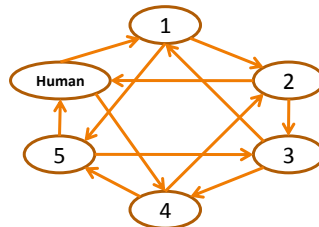
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Questions



#1. Does adding a link from a human node to an agent node, A_i , make the system less autonomous?



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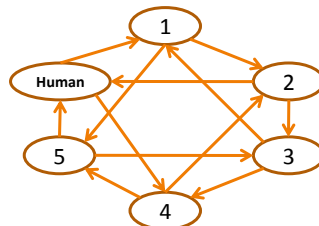


Questions



#1. Does adding a link from a human node to an agent node, A_i , make the system less autonomous?

Answer: No. Autonomy is defined on the boundary of the system of systems.



Probably not what they mean. Imagine a network of all human agents!

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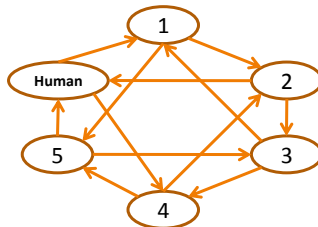


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Questions



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Questions



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Questions



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Answer: No. Autonomy is defined on the boundary of the system of systems.

#2. Does adding a link from a human node to an agent node, A_i , make agent A_i less autonomous?

Answer: it depends – on whether or not agent A_i can choose if and how to use the information.

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“Autonomy”



From Greek αὐτο- auto- "self" + νόμος nomos, "law"
"one who gives oneself their own law"

A concept found in political and bioethical philosophy.
Within these contexts, it refers to the capacity of a
rational individual to make an informed, un-coerced
decision.

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Levels of Autonomy



Essentials:

- **No Autonomy:** agent is compelled to use information
- **Full Autonomy:** agent may use information according to its own best (self) interests
- *For simplicity, assume it is a measure, $\omega \in \Omega$, on the closed unit interval $[0,1]$*

Some Possibilities:

Single agent, static autonomy:

$$\Omega = \{0, 1\}$$

Single agent, dynamic autonomy:

$$\Omega = \left\{0, \frac{1}{K}, \frac{2}{K}, \dots, \frac{K-1}{K}, 1\right\}$$

N agents, static autonomy:

$$\Omega = \left\{0, \frac{1}{n}, \frac{2}{n}, \dots, \frac{n-1}{n}, 1\right\}$$

N agents, dynamic autonomy:

$$\Omega = \left\{0, \frac{1}{nK}, \frac{2}{nK}, \dots, \frac{nK-1}{nK}, 1\right\}$$

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How Does Autonomy Relate to our Measures on Information Dynamical Systems?



An autonomous agent has 2 options with information: use it or ignore it. The question is; *when is agent autonomy in the best interests of the system?*

- Consensus is a well established measure on information dynamics
- Results on speed, stability of consensus [Murphey, Zabrankin, Murray 2010]
- Assume agent's value function is not strictly a consensus goal (otherwise solt'n is trivial: always leads to coerced - non autonomous - result)

Given these measures, when is autonomy not a good idea (i.e. degrades consensus)?

Consider autonomous agent that may choose whether or not to use information from human node.

Case 1: information would degrade consensus but improves agent's overall value function. *Result: agent uses information which then degrades consensus. However the autonomous result is same as coerced result (uses information). So extending autonomy is of neutral benefit.*

Case 2: information would improve consensus value but degrades agent's overall value function. *Result: agent ignores information which degrades consensus. Extending autonomy is not desirable. All other cases, autonomy is desirable.*

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Information Dynamics & Consensus



- Treat information flows as (discrete time) dynamical entity
- Develop a control policy to shape information flows, in-turn shape system dynamics

$$q_{k+1} = \sum_{j=0}^M a_j q_{k-j} + G p_k + L y_k, \quad k = 0, 1, \dots$$

$$p_k = \sum_{j=0}^M b_j q_{k-j}, \quad k = 0, 1, \dots$$

- $p_k = \{p_{ik}\}, i=1,2,\dots,n$: information sent to vehicle i during time step k
- $y_k = \{y_{ik}\}, i=1,2,\dots,n$: error between vehicle i and a time varying offset function h_{ik}
- G is the normalized adjacency matrix of a directed graph.
- L is the Laplacian of G defined as $L=I-G$, $\lambda_k, k=1,2,\dots,n$ are the eigenvalues of G
- Information flow law: $(a_j, b_j) j=0..M$ M -order polynomial controllers are possible

$$\text{Let } \lim_{k \rightarrow \infty} p_k = p^*, \quad \lim_{k \rightarrow \infty} q_k = q^*, \quad \lim_{k \rightarrow \infty} y_k = y^*, \quad a = \sum_{j=0}^M a_j, \quad b = \sum_{j=0}^M b_j \quad \text{and } c = (1-a)/b$$

If c is an eigenvalue of G it must be 1 and unique with e.vector $\mathbf{1}_N$, can be shown

$$p^* = y + \gamma \mathbf{1}_N \quad \text{THIS IS CALLED CONSENSUS}$$

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Stability Margin and Convergence Rate of Consensus: Zero Order Controller



Stability Margin

$$\delta = \min \left| \frac{\operatorname{Re}[1 - \lambda_k]}{[1 - \lambda_k]} - \frac{b_0}{2} |1 - \lambda_k| \right|, \quad a_0 = 1 - b_0$$

Convergence Rate

- (a) $a_0 = 1 - b_0$ and $\varepsilon = 1 - \max_{k=2,3,\dots,n} |1 - b_0 + \lambda_k b_0|$ is defined as **convergence rate**
- (b) If $b_0 \leq 0$ then p^* does not converge for any graph
- (c) If $b_0 \in (0,1)$ then p^* converges for any strongly connected graph
- (d) $\varepsilon=1$ if and only if G is complete, where $b_0 = (n-1)/n$ and $p^* = p^1$

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How Does Autonomy Relate to our Measures on Information Dynamical Systems?



An autonomous agent has 2 options with information: use it or ignore it. The question is; *when is agent autonomy in the best interests of the system?*

- Consensus is a well established measure on information dynamics
- Results on speed, stability of consensus [Murphey, Zabrankin, Murray 2010]
- Assume agent's value function is not strictly a consensus goal (otherwise solt'n is trivial: always leads to coerced - non autonomous - result)

Given these measures, when is autonomy not a good idea (i.e. degrades consensus)?

Consider autonomous agent that may choose whether or not to use information from human node.

Case 1: information would degrade consensus but improves agent's overall value function. Result: agent uses information which then degrades consensus. However the autonomous result is same as coerced result (uses information). So extending autonomy is of neutral benefit.

Case 2: information would improve consensus value but degrades agent's overall value function. Result: agent ignores information which degrades consensus. Extending autonomy is not desirable. **All other cases, autonomy is desirable.**

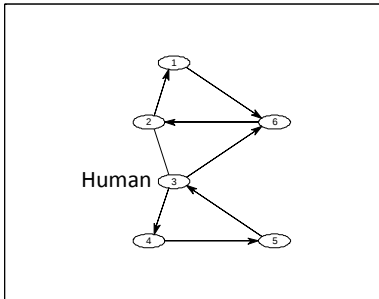
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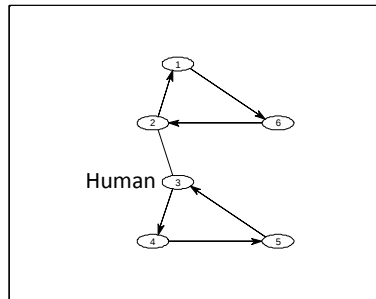
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Some Quick Results



Agent 6 Value Fn: 0.42
Stability margin: 0.81
Convergence rate: 0.04



Agent 6 Value: 0.37
Stability margin: 0.81
Convergence rate: 0.03

Using information would increase value function. Therefore agent 6 uses information and consensus only very slight degraded.

Autonomy Desirable

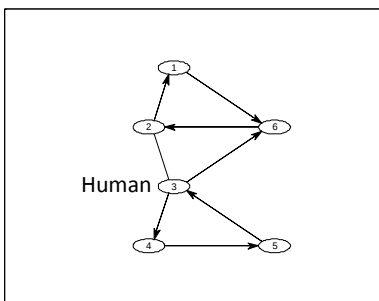
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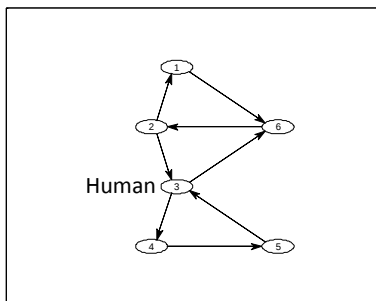
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Some Quick Results



Agent 2 Value Fn: 0.42
Stability margin: 0.81
Convergence rate: 0.04



Agent 2 Value: 0.58
Stability margin: 0.70
Convergence rate: 0.02

Using information would degrade Value fn. Therefore, agent 2 ignores information and consensus is degraded.

Autonomy Not Desirable.

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Consensus is great. But what about other global goals for a “system of systems?”



1. Includes complex behaviors in time and space?
 - Non-linear dynamics, highly non-linear coupling
 - Continuous/Discrete
 - Synchronized as needed but not dependent on it
 - Contains machine (and human) intelligence that will essentially, *redesign itself*
2. Encapsulates uncertainty in both the goal and its execution?
 - Ambiguities in the goal
 - Poor model of environment
 - Non-smooth communications (not a graceful degradation!)
 - System and subsystem faults
3. Ensures real-time constraints in computing and communications are met?
 - Parsing goal into multiple languages and spatial/temporal contexts
 - Verify what is “coded” is actually intended by goal
4. Validates the models that are (in some cases) being created for the first time during execution of the system and serve as the basis for designing new control policies?

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How is a global goal for a “systems of systems” specified that :



1. Includes complex behaviors in time and space?
 - Non-linear dynamics, highly non-linear coupling
 - Continuous/Discrete
 - Synchronized as needed but not dependent on it
 - Contains machine (and human) intelligence that will essentially, *redesign itself*
2. Encapsulates uncertainty in both the goal and its execution?
 - Ambiguities in the goal
 - Poor model of environment
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 - System and subsystem faults
3. Ensures real-time constraints in computing and communications are met?
 - Parsing goal into multiple languages and spatial/temporal contexts
 - Verify what is “coded” is actually intended by goal
4. Validates the models that are (in some cases) being created for the first time during execution of the system and serve as the basis for designing new control policies?

These goals are relevant because they relate to “autonomy”

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Some promising Trends



- Temporal logic
- Lyapunov analysis, LMIs, sum of squares
- Rapidly exploring trajectories (trees)
- Risk Measures – Risk Optimization
- Model checking proofs
- Graph theory, spectral graph theory
- Dynamic Data Driven App Systems
- Human-Machine Cognition

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Conclusions



- Information dynamic networked systems becoming more and more prevalent
 - E.g. System of systems
- Increasing desire to “automate” networks to gain efficiencies and expand roles
- Looming barrier to both is trust, validation, and verification of models, performance, value
- Need more precise definitions of autonomy
 - Initial attempt shows that autonomy can “flex” from full to none based upon conditions set on consensus global goals
 - Autonomy definition can actually clarify/specify goals for these networked systems
 - Autonomy conditions (on global goals) could be specified with time average degradation, network average, many others!

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Acknowledgment/Disclaimer

This work was sponsored (in part) by the Air Force Office of Scientific Research, USAF. The views and conclusions contained herein are those of the authors and should not be interpreted as necessarily representing the official policies or endorsements, either expressed or implied, of the Air Force Office of Scientific Research or the U.S. Government.

Personnel Supported During Duration of Grant

Robert Murphey PI, Munitions Directorate, AFRL

Publications

“Optimization Framework for Stability and Convergence of Information Flow in Cooperative Systems,” Zabarankin, M., Murphey, R., Murray, R., A, accepted as technical note 2011.

“Stability and Convergence of Information Flow in Cooperative Systems,” Zabarankin, M., Murphey, R., Murray, R., A, accepted as full paper 2012.

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