

PROPERTIES OF SEQUENTIAL CHROMOSPHERIC BRIGHTENINGS AND ASSOCIATED FLARE RIBBONS (POSTPRINT)

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Interim Report

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PROPERTIES OF SEQUENTIAL CHROMOSPHERIC BRIGHTENINGS AND ASSOCIATED FLARE RIBBONS

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ABSTRACT

We report on the physical properties of solar sequential chromospheric brightenings (SCBs) observed in conjunction with moderate-sized chromospheric flares with associated Coronal mass ejections. To characterize these ephemeral events, we developed automated procedures to identify and track subsections (kernels) of solar flares and associated SCBs using high-resolution $H\alpha$ images. Following the algorithmic identification and a statistical analysis, we compare and find the following: SCBs are distinctly different from flare kernels in their temporal characteristics of intensity, Doppler structure, duration, and location properties. We demonstrate that flare ribbons are themselves made up of subsections exhibiting differing characteristics. Flare kernels are measured to have a mean propagation speed of 0.2 km s^{-1} and a maximum speed of 2.3 km s^{-1} over a mean distance of $5 \times 10^3 \text{ km}$. Within the studied population of SCBs, different classes of characteristics are observed with coincident negative, positive, or both negative and positive Doppler shifts of a few km s^{-1} . The appearance of SCBs precedes peak flare intensity by ≈ 12 minutes and decay ≈ 1 hr later. They are also found to propagate laterally away from flare center in clusters at 45 km s^{-1} or 117 km s^{-1} . Given SCBs' distinctive nature compared to flares, we suggest a different physical mechanism relating to their origin than the associated flare. We present a heuristic model of the origin of SCBs.

Key words: Sun: chromosphere – Sun: flares

1. INTRODUCTION

The solar chromosphere exhibits three different classes of small-scale intensity brightenings: flare, plage, and compact brightenings. Although each is characterized by an enhanced temporal $H\alpha$ brightness relative to a background quiet Sun, they each have distinct physical processes governing their spatial and temporal evolution. Typically, brightenings have been identified and characterized manually from a single data source (e.g., Kurt et al. 2000; Ruzdjak et al. 1989; Veronig et al. 2002). However, in order to form a better understanding of the underlying dynamics, data from multiple sources must be utilized and numerous similar features must be statistically analyzed.

This work focuses on flare brightenings and associated compact brightenings called sequential chromospheric brightenings (SCBs). SCBs were first observed in 2005 and appear as a series of spatially separated points that brighten in sequence (Balasubramaniam et al. 2005). SCBs are observed as multiple trains of brightenings in association with a large-scale eruption in the chromosphere or corona and are interpreted as progressive propagating disturbances. The loci of brightenings emerge predominantly along the axis of the flare ribbons. SCBs are correlated with the dynamics which cause solar flares, coronal restructuring of magnetic fields, halo Coronal mass ejections (CMEs), EIT waves, and chromospheric sympathetic flaring (Balasubramaniam et al. 2005). Pevtsov et al. (2007) demonstrate that SCBs have properties consistent with aspects of chromospheric evaporation.

This article presents a new description of the dynamical properties of SCBs resulting from applying a new automated method (Kirk et al. 2011) of identifying and tracking SCBs and associated flare ribbons. This tracking technique differs from previous flare tracking algorithms in that it identifies and tracks spatial and temporal subsections of the flare and all related brightenings from pre-flare stage, through the impulsive brightening stage,

and into their decay. Such an automated measurement allows for tracking dynamical changes in intensity, position, and derived Doppler velocities of each individual subsection. The tracking algorithm is also adapted to follow the temporal evolution of ephemeral SCBs that appear with the flare. In Section 2, we describe the data used to train the algorithm and the image processing involved in the detection routine. In Section 3, we present the results of tracking the evolution of flare kernels through an erupting flare. In Section 4, we present the application of the tracking algorithm to ephemeral SCBs. We present a physical interpretation of the SCBs and provide a heuristic model of the origin of SCBs in Section 5. Finally, in Section 6 we discuss implications of these results and provide future direction for this work.

2. DATA AND DATA PROCESSING

In this study, we use chromospheric $H\alpha$ ($6562.8 \text{ \AA}$) images from the USAF's *Improved Solar Observing Optical Network* (ISOON; Neidig et al. 1998) prototype telescope to study flare ribbons and SCBs. ISOON is an automated telescope producing 2048×2048 pixel full-disk images at a one-minute cadence. Each image has a $1''.1$ spatial sampling, is normalized to the quiet Sun, and corrected for atmospheric refraction (Figures 1(a), 2(a), and 3(a)). Nearly coincident to the spectral line center images, ISOON also records $H\alpha \pm 0.4 \text{ \AA}$ off-band Doppler images, from which Doppler signals are derived.

For this study, we chose to apply the brightening detection algorithms to three flares where Balasubramaniam et al. (2006) had previously identified SCB events (Table 1). Each of the events selected has a two-ribbon configuration and an associated halo CME. Of these, both the 2005 May 6 and 2005 May 13 events were both located near disk center, while the 2004 November 9 event was near the western limb. Images were extracted from the archive from ± 3.5 hr of the eruption start time, yielding a data cube with ≈ 400 images for each event.

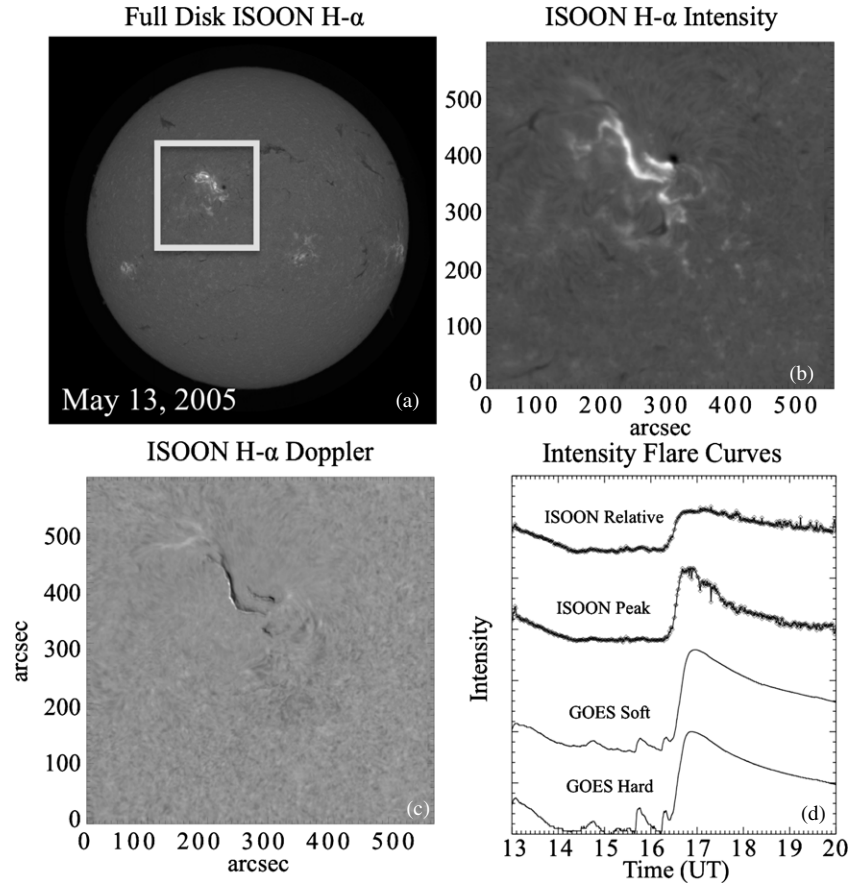


Figure 1. Two-ribbon flaring event from 2005 May 13. Panel (a) shows an example of a calibrated $H\alpha$ ISOON image with the ROI highlighted. The ISOON images are 2048×2048 pixels with each pixel having a $1''.1$ resolution. Panel (b) is the ROI after preprocessing. This ROI covers 576×576 pixels corresponding to 2.12×10^{11} km² on the solar surface. Panel (c) is a Doppler measure of the same ROI as part (b). The Doppler velocity image is created out of ISOON $H\alpha$ off-band images described in Section 2 where the velocity ranges from -26.6 to 21.5 km s⁻¹ from black to white. Panel (d) shows intensity curves over the time period of interest: 13:00–20:02 UT as described in detail in the text.

Table 1
Events Selected for Study

Date	Start Time (UT)	Duration (hr)	Flare Class	CME
2004 Nov 9	16:59	0.5	M8.9	Halo
2005 May 6	16:03	2.1	C8.5	Halo
2005 May 13	16:13	1.3	M8.0	Halo

Note. Each event was visually identified as having a two-ribbon configuration and SCBs associated with the flare.

An $H\alpha$ relative intensity curve, an $H\alpha$ maximum intensity curve, and *Geostationary Operational Environmental Satellites* (GOES) hard and soft X-ray fluxes are plotted to characterize the flare (Figures 1(d), 2(d), and 3(d)) as described in Kirk et al. (2011).

Each ISOON image is reconditioned to remove solar limb darkening. The images are then de-projected into conformal coordinates using a Gouy projection (an oblique aspect of the Peirce projection; Peirce 1879), which removes the projection effects of imaging the solar sphere. Each image is then cropped to the region of interest (ROI; Figures 1(b), 2(b), and 3(b)). The set of images are aligned using a cross-correlation algorithm eliminating the rotation effects of the Sun. Frames that contain bad pixels or excessive cloud interference are removed.

The red and blue wings of ISOON Doppler images are each preprocessed using the same technique as applied to the line

center images described above (Figures 1(c), 2(c), and 3(c)). In order to produce velocity measurements, a Doppler cancellation technique is employed in which red images are subtracted from blue images (for a modern example, see Connes 1985). Typically, red and blue images are separated by about 4 s and no more than 5 s. A mean zero redshift in the subtracted Doppler image in the quiet Sun serves as a reference. In dynamical situations such as solar flares, $H\alpha$ profiles are often asymmetric especially in emission making this Doppler technique invalid. To avoid asymmetric profiles, only values derived outside of the flaring region are considered such that the areas of interest at $\pm 0.4 \text{ \AA}$ are still in absorption even if raised in intensity (Balasubramaniam et al. 2004). The values from the subtracted images are translated into units of km s⁻¹ by comparison to a measured response in spectral line shifts, which are calibrated against an intensity difference for the ISOON telescope. In this context, we interpret the Doppler shift as a line-of-sight velocity. Thus, Doppler velocity [v_D] is defined as

$$v_D = k(\mathcal{I}_{\text{blue}} - \mathcal{I}_{\text{red}}), \quad (1)$$

where $\mathcal{I}$ is the measured intensity and k is a linear fitted factor that assumes the intensity changes due to shifts in the symmetric spectral line, which can be attributed to a Doppler measure as a first-order approximation. The linear factor [k] has been independently determined for the ISOON telescope by measuring the full $H\alpha$ spectral line Doppler shift across

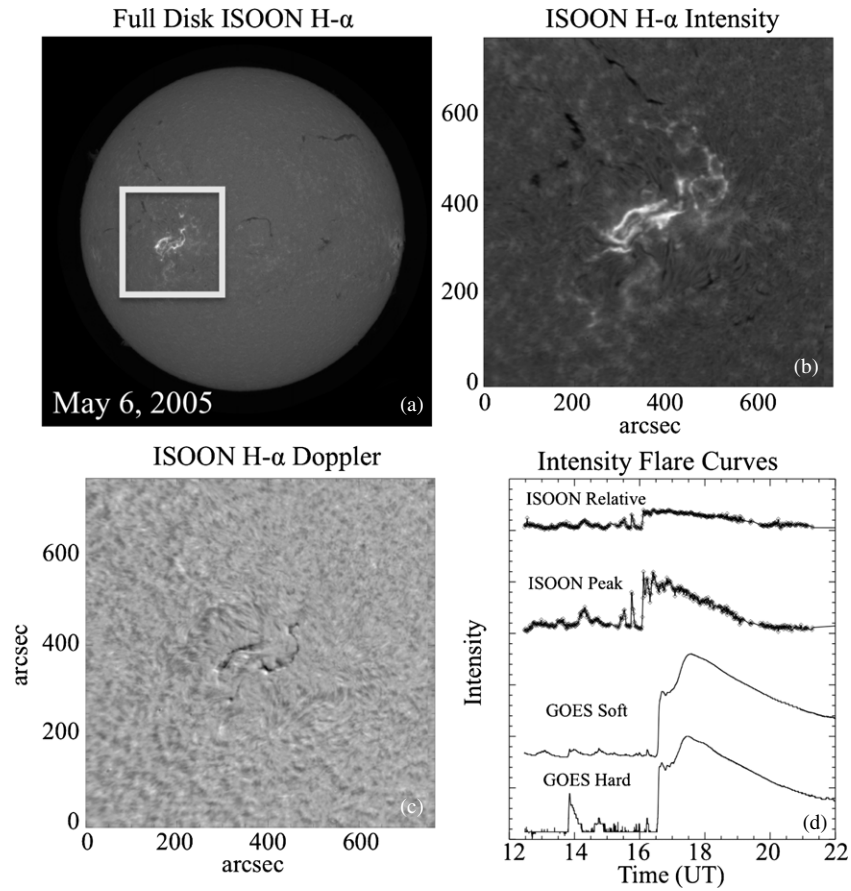


Figure 2. Two-ribbon flaring event from 2005 May 6. Panel (a) shows an example of a calibrated H α ISOON image with the region of interest (ROI) highlighted. The ISOON images are 2048×2048 pixels with each pixel having a $1''.1$ resolution. Panel (b) is the ROI after preprocessing. This ROI covers 768×768 pixels corresponding to 3.77×10^{11} km 2 on the solar surface. Panel (c) is a Doppler measure of the same ROI as part (b). The Doppler velocity image is created out of ISOON H α off-band images described in Section 2 where the velocity ranges from -12.5 to 6.9 km s $^{-1}$ from black to white. Panel (d) shows intensity curves over the time period of interest: 12:28–22:47 UT as described in detail in the text.

the entire solar disk (K. S. Balasubramaniam 2011, private communication).

2.1. Detection and Tracking

An animated time series of sequential images covering an erupting flare reveals several physical characteristics of evolving ribbons: the ribbons separate, brighten, and change their morphology. Adjacent to the eruption, SCBs can be observed brightening and dimming in the vicinity of the ribbons. Kirk et al. (2011) describe in detail techniques and methods used to extract quantities of interest such as location, velocity, and intensity of flare ribbons and SCBs. The thresholding, image enhancement, and feature identification are tuned to the ISOON data. The detection and tracking algorithms are specialized for each feature of interest and require physical knowledge (e.g., size, peak intensity, and longevity) of that feature being detected to isolate the substructure.

Briefly, the detection algorithm first identifies candidate bright kernels in a set of images. In this context, we define a kernel to be a locus of pixels that are associated with each other through increased intensity compared with the immediately surrounding pixels. Each kernel has a local maximum, must be separated from another kernel by at least one pixel, and does not have any predetermined size or shape. Next, the algorithm links time-resolved kernels between frames into trajectories. A filter is applied to eliminate inconsistent or otherwise peculiar

detections. Finally, characteristics of bright kernels are extracted by overlaying the trajectories over complementary data sets. To aid in this detection, tracking software developed by Crocker, Grier, and Weeks was used as a foundation and modified to fit the needs of this project⁵ (Crocker & Grier 1996).

In order to characterize a kernel, we calculate its integrated intensity, radius of gyration, and eccentricity. The eccentricity of the kernel (as defined by its semi-major (a) and semi-minor (b) axis) is calculated using

$$e = \sqrt{1 - \frac{b^2}{a^2}}. \quad (2)$$

The integrated intensity of a given kernel is defined by

$$m = \sum_{i^2+j^2 \leq \omega^2} \mathcal{A}(x+i, y+j), \quad (3)$$

where $\mathcal{A}(x+i, y+j)$ is the intensity of the pixel located at $(x+i, y+j)$, the kernel has a brightness-weighted centroid with coordinates (x, y) , and ω is the radius of the mask (Crocker & Grier 1996). The radius of the mask is chosen to be 8 pixels in this case. A radius of gyration, R_g , is related to the moment of

⁵ Crocker's software is available online at www.physics.emory.edu/~weeks/idl/.

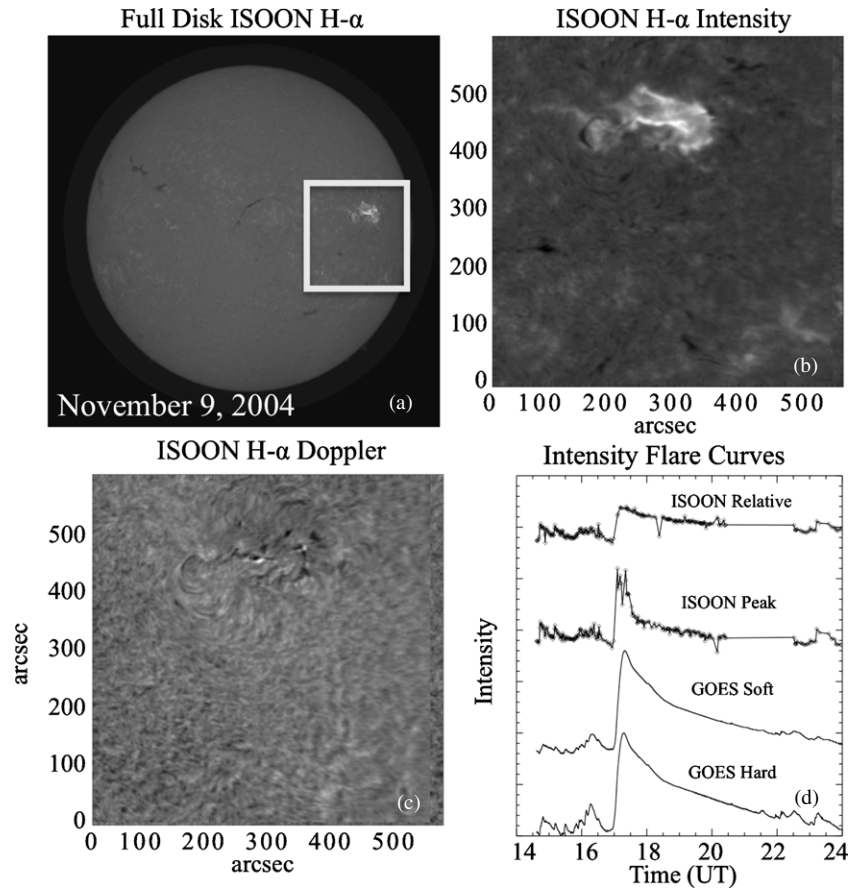


Figure 3. Two-ribbon flaring event from 2004 November 9. Panel (a) shows an example of a calibrated H α ISOON image with the ROI highlighted. The ISOON images are 2048×2048 pixels with each pixel having a $1''.1$ resolution. Panel (b) is the ROI after preprocessing. This ROI covers 600×600 pixels corresponding to 2.30×10^{11} km 2 on the solar surface. Panel (c) is a Doppler measure of the same ROI as part (b). The Doppler velocity image is created out of ISOON H α off-band images described in Section 2 where the velocity ranges from -9.3 to 14.6 km s $^{-1}$ from black to white. Panel (d) shows intensity curves over the time period of interest: 14:37–23:58 UT as described in detail in the text.

inertia [I] by using

$$I = \sum_k m_k r_k^2 = m R_g^2, \quad (4)$$

$$r = (a + b)/2, \quad (5)$$

where m_k is the mass of particle k , m is the total mass of the system, and r is the distance to the rotation axis. In this context, we interpret the radius of gyration to be

$$R_g^2 = \sum_k \frac{A_k r_k^2}{m}, \quad (6)$$

where m is the integrated intensity as defined in Equation (3) (Crocker & Grier 1996). Figure 4 diagrams a hypothetical kernel. The results of this algorithm identify and characterize several kernels in the flaring region (Figure 5). The total number of flare kernels detected is typically between 100 and 200, while the number of SCB kernels detected is typically three to four times that number.

3. FLARE RIBBON PROPERTIES

The properties of kernels identified in flare ribbons can be examined in two ways: (1) each kernel can be considered as an independent aggregation of compact brightenings or (2) kernels can be considered as dependent on each other as fragments

of a dynamic system. Each category brings about contrasting properties. If one considers the kernels as independent elements, this provides a way to examine changes to subsections of the flare and is discussed in Section 3.1. Associating kernels with their contextual surroundings allows a way to examine the total evolution of the flare without concern of how individual kernels behave. This type of examination is addressed in Section 3.2.

3.1. Qualities of Individual Kernels

A sample of six kernels from the 2005 May 13 event, letters U–X in Figure 6, is representative of the majority of flare kernels tracked. The kernels were selected from three different regions of this flare. The normalized H α intensity of each of these kernels is shown in Figure 7. In contrast with the integrated flare light curve, an individual flare kernel often has a shorter lifetime. This is because an individual kernel may first appear in the impulsive phase of the flare (as demonstrated in kernels W–Y), while other kernels may disappear as the flare begins to decay (as in kernels U and Z). Most likely these kernels merged with one another, at which point their unique identity was lost. Kernels W and X are the only two that show the characteristic exponential dimming found in the reference curves in Figure 1(d). All of these kernels have peak intensities within a few minutes of the peak of the total flare intensity and have sustained brightening above background levels for up to an hour.

The integrated speed of displaced kernels provides context to the evolution of intensities. We define the integrated speed

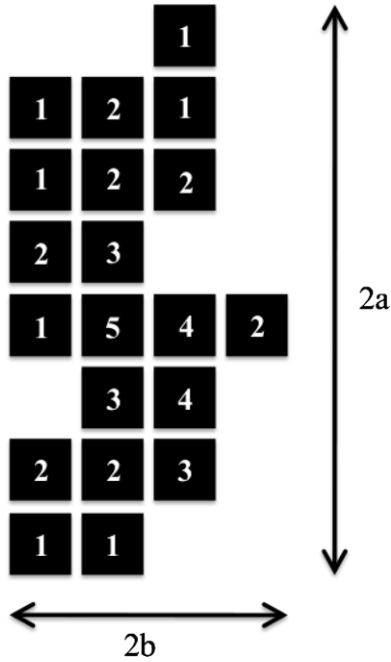


Figure 4. Diagram of a hypothetical kernel (either flare or SCB) used for classifications in this paper. Each pixel is labeled with a representative intensity $[A_i]$. The semi-major axis $[a]$ and semi-minor axis $[b]$ are shown. This kernel has the following properties: total intensity, $m_0 = 43$, semi-major axis, $a = 4$, semi-minor axis, $b = 2$, eccentricity, $e = 0.87$, centroid, $(x, y) = (0.26, 0.18)$, and radius of gyration, $R_g = 1.9$. The maximum intensity, in this case 5, is defined as having pixel coordinates $(0, 0)$.

of displacement to be the sum over all time steps of the measured velocity of an individual kernel and thus small velocity perturbations are minimized by the sum. The peak integrated speed measured for each kernel peaks at $\sim 2.3 \text{ km s}^{-1}$ and has a mean of $\sim 0.2 \text{ km s}^{-1}$. There is significant motion along the flare ribbons as well as outflow away from flare center. The motions are complex but generally diverge. The total spatial (angular) displacement of each flare kernel peaks at $\sim 20.7 \text{ Mm}$ and has a mean of $\sim 5.0 \text{ Mm}$. Flare kernels that exhibited the greatest speed did not necessarily have the greatest displacements. As

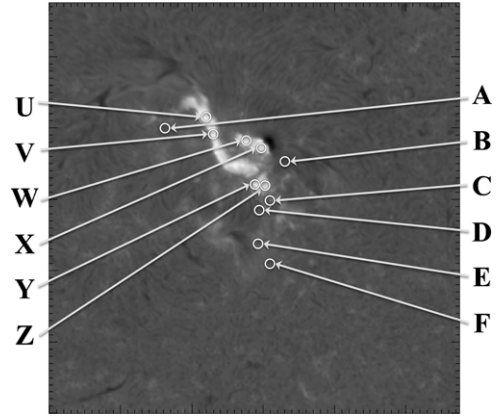


Figure 6. Image from the 2005 May 13 event. Letters A–F point to the locations several SCB kernels that are shown in more detail in Figure 7. Letters U–Z point to the locations of a sample of several flare kernels that are also shown in more detail in Figure 7. Note that since flare kernels move with the evolving flare ribbon, the locations of these kernels are only accurate for this image. In contrast, SCB kernels are stationary and remain in the same location in any image.

the flare develops, most of the motion in flare ribbons indicated is synchronous with the separation of the ribbons. A few tracked kernels indicate motion along flare ribbons. These flows along flare ribbons are consistently observed in all three flares.

3.2. Derived Flare Quantities

Examining trajectories of flare kernels offers insight into the motions of the flare ribbons as they evolve through the eruption. Figure 8 shows a time series of images centered about the peak time of the flare. The velocities of the detected flare kernels are superposed as vectors. Note the initial outflow of the two ribbons near the flare peak at 16:49 UT. But, as the flare continues to evolve, there is more motion along the flare ribbons. This is probably a result of the overarching loops readjusting after the reconnection event. Beneath each image is a histogram of the distribution of velocities at each time step. The mean apparent lateral velocity of each kernel remains below 0.5 km s^{-1} throughout the flare even though

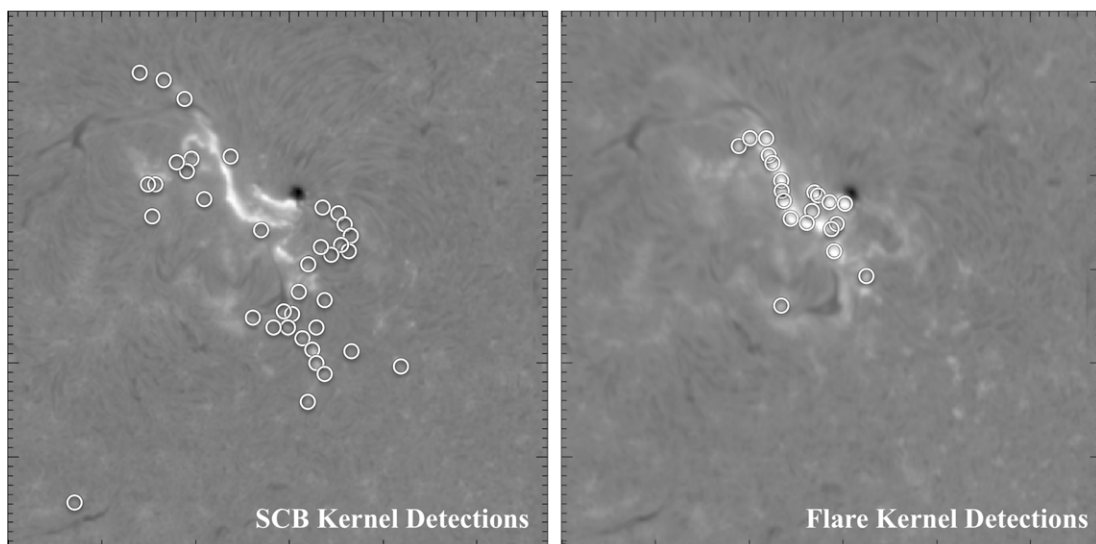


Figure 5. Example ISOON $H\alpha$ images from the 2005 May 13 two-ribbon flare. The detection algorithm is applied to the image series to extract either ribbon brightening or compact brightening. The left image shows one time slice of individual SCBs identified external to the flare ribbon. The right image shows the same time slice with brightenings identified along the flare ribbon. Each detection is made up of a small matrix of pixels associated with the brightening called a kernel.

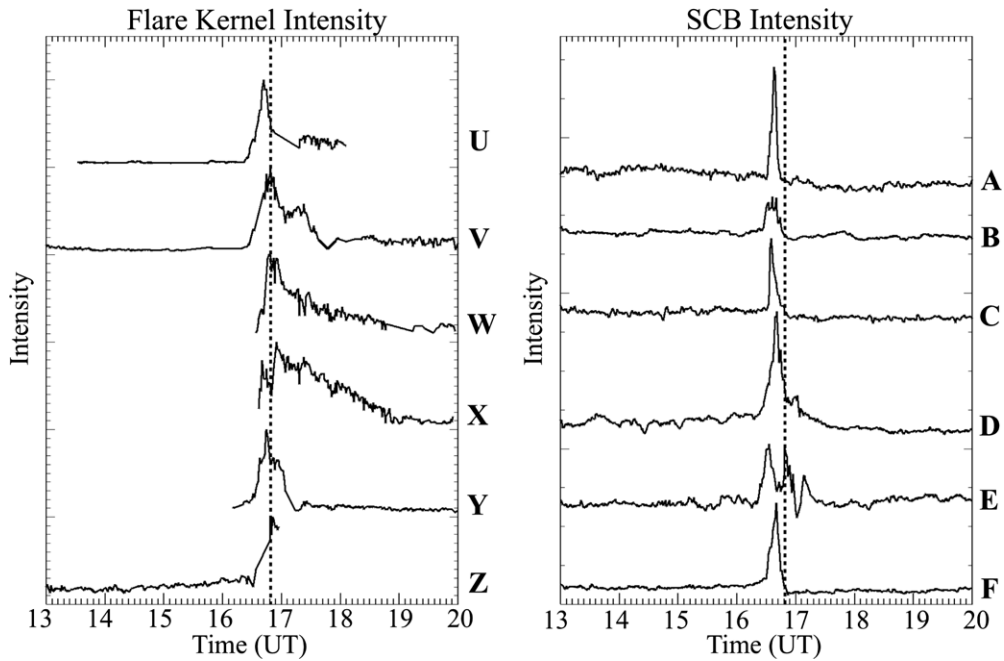


Figure 7. $H\alpha$ normalized intensity curves for each of the kernels indicated in Figure 6 by the associated letters. On the left, the tracked flare kernels are shown. The normalized intensity curves for the SCB kernels, shown on the right, are stationary and therefore tracked throughout the flaring window. In both panels, the vertical dashed line indicates the time at which the flare intensity peaks (16:49 UT) derived from integrating all flare kernel intensities at each time step.

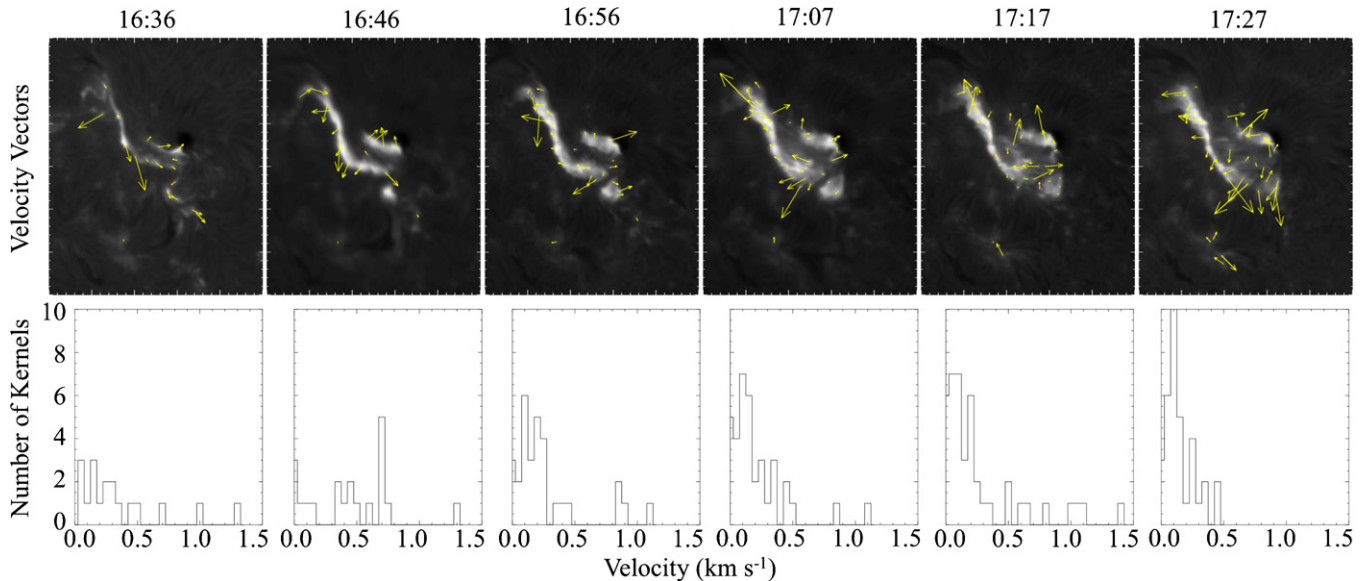


Figure 8. Time series of images with the apparent lateral velocity of each tracked flare kernel at that time step plotted over the $H\alpha$ flare ribbons. A histogram of the number of flare kernels as a function of velocity corresponding to each time step is plotted underneath.

the total velocity changes significantly. Qualitatively, the bulk of the apparent motion appears after the flare peak intensity at 16:49 UT.

Grouping the kernels' velocities into appropriate bins provides another way to analyze the dynamics of the flare (Figure 9). The kernels with apparent lateral speeds above 0.4 km s^{-1} are highly coincident with the peak intensity of the flare. The number of these fast-moving kernels peaks within a couple minutes of flare peak, and then quickly decays back to quiet levels. The velocity bins between 0.1 and 0.4 km s^{-1} show a different sub-structure. These velocity bins peak ≈ 30 minutes after the peak of the flare intensity. They show a much slower decay rate,

staying above the pre-flare velocity measured throughout the decay phase of the $H\alpha$ flare curve.

Figure 10 (left column) shows integrated unsigned kernel velocity (speed) for each image. In general, the evolution of the integrated kernel speed has a shape similar to the intensity curve. For the 2005 May 6 event, the speed curve is more similar to the *GOES* X-ray intensity curve than the $H\alpha$ curve. For the 2004 November event, the limb geometry of the flare, as well as the noise in the original data set, results in a noisy curve. Despite these difficulties, a clear increase in total speed is apparent near the peak of the flare. A continuum integrated speed level of $1\text{--}2 \text{ km s}^{-1}$ is consistent in each event, indicating the quality of

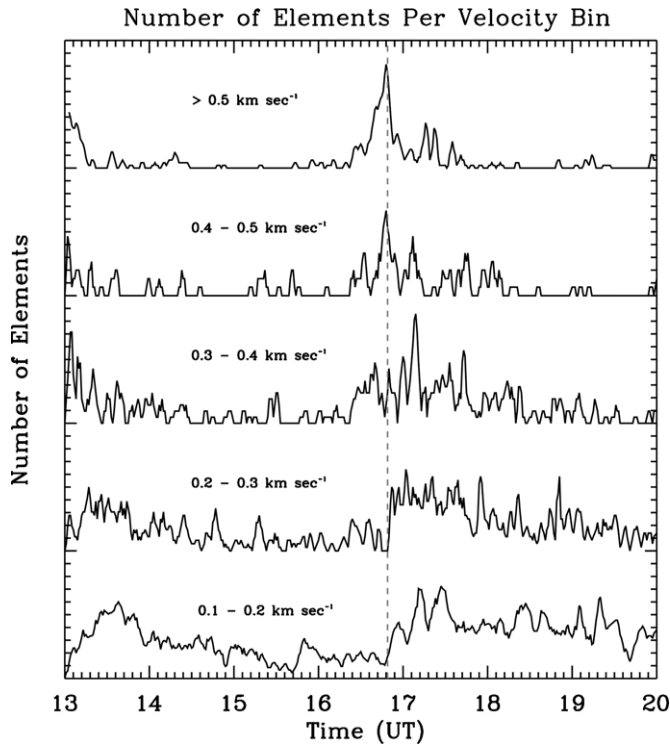


Figure 9. Number of elements in each apparent lateral velocity bin plotted as a function of time. The vertical dashed line marks the time of the peak flare intensity. The velocity bins are 0.1 km s^{-1} in width. The smallest bin, $0-0.1 \text{ km s}^{-1}$, is excluded because of a base level of noise inherent in the detection routine.

data and of the tracking software. The peak integrated speed is about 15 km s^{-1} for all three flares.

Examining the change in the speed of each kernel between successive images yields a derived acceleration for each tracked kernel. The integrated unsigned acceleration is plotted in Figure 10 (middle column). Both the 2005 May 13 and 2005 May 6 events show peak acceleration after the peak of the intensity curve. Hence, the majority of the acceleration in the apparent motion of the flare comes in the decay phase of $H\alpha$ emission, in concert with the formation of post-peak flare loops, as seen in movies of *Transition Region and Coronal Explorer* images of other flares. The peak acceleration appears uncorrelated with the strength of the flare since the peak of the M class May 13 event is just over 300 km s^{-2} , while the peak of the C-class flare on May 6 is nearly 400 km s^{-2} . The acceleration curve for the November 9 flare has too much noise associated with it to decisively determine the peak value.

The right column of Figure 10 shows a derived the kinetic energy associated with the measured motion of the flare kernels. This was accomplished by assuming a chromospheric density $[\sigma]$ of $10^{-5} \text{ kg m}^{-3}$ and a depth $[h]$ of 1000 km. The mass contained in each volume is then calculated by

$$m = \pi h \sigma R_g^2 \sqrt{1 - e^2}, \quad (7)$$

where R_g is defined in Equation (6) and e is defined in Equation (2). The kinetic energy under a kernel is defined in the standard way to be

$$E_k = \frac{1}{2} m v^2, \quad (8)$$

where v (speed) is a measured quantity for each kernel. The derived kinetic energy curves show a ≈ 30 -fold increase in

kinetic energy during the flare with a decay time similar to the decay rate of the $H\alpha$ intensity. The measure of a kernel's kinetic energy is imprecise because the measured motion is apparent motion of the underlying plasma. In the model of two ribbon solar flares put forth by Priest & Forbes (2002), the apparent velocity is a better indicator of rates of magnetic reconnection rather than of plasma motion. Despite this caveat, the derived kernel kinetic energy is a useful measure because it combines the size of the kernels with their apparent velocities to characterize the flare's evolution, thus representing the two in a quantitative way.

The non-thermal 25–50 keV emission between 16:42 and 16:43 UT from *RHESSI* (Lin et al. 2002) of the May 13 flare is contoured in Figure 11 over an $H\alpha$ image taken at 16:42 UT. The high-energy emission is centered over the flare ribbons but is discontinuous across the ribbon. There are three localized points from which the majority of the X-ray emission comes. The parts of the flare ribbons exhibiting the most displacement show generally lower X-ray intensity than the more stationary segments of the flare ribbons.

4. SCB PROPERTIES

The measured properties of SCBs can be studied using two scenarios: each SCB kernel is considered as independent and isolated compact brightenings; each compact brightening is considered to be fragments of a dynamic system that has larger structure. This is similar to the approach used for flares. Again, considering both scenarios has its benefits. Identifying kernels as independent elements reveals structural differences in compact brightenings and is discussed in Section 4.1. Associating kernels with their contextual surroundings provides some insight into the physical structure causing SCBs. An aggregate assessment of SCBs is addressed in Section 4.2. To mitigate the effects of false or marginal detections, only SCBs with intensities two standard deviations above the mean background intensity are considered for characterizing the nature of the ephemeral brightening.

4.1. Qualities of Individual SCBs

SCBs, although related to erupting flare ribbons, are distinctly different from the flare kernels discussed in Section 3. Six SCBs are chosen from the 2005 May 13 event as an example of these ephemeral phenomena. The locations of these six events are letters A–F in Figure 6. The $H\alpha$ normalized intensity of each of these kernels is shown in Figure 7. The SCB intensity curve is significantly different from the flare kernel curves shown on the left side of the figure. SCB curves are impulsive; they have a sharp peak and then return to background intensity in the span of about 12 minutes. Nearly all of the SCBs shown here peak in intensity before the peak of the flare intensity curve, shown as a vertical dashed line in Figure 7. SCBs B and E both appear to have more internal structure than the other SCBs and last noticeably longer. This is most likely caused by several unresolved SCB events occurring in succession.

Nearly all SCBs have $H\alpha$ line center intensities 40%–60% above the mean intensity of the quiet chromosphere (Figure 12). From this increased initial intensity, SCBs brighten to intensities 75%–130% above the quiet Sun.

Examining Doppler velocity measurements from the SCB locations reveals three distinct types of SCBs (Figure 12). A type Ia SCB has an impulsive intensity profile and an impulsive negative Doppler profile that occurs simultaneously or a few minutes after the peak brightening. In this study, a negative

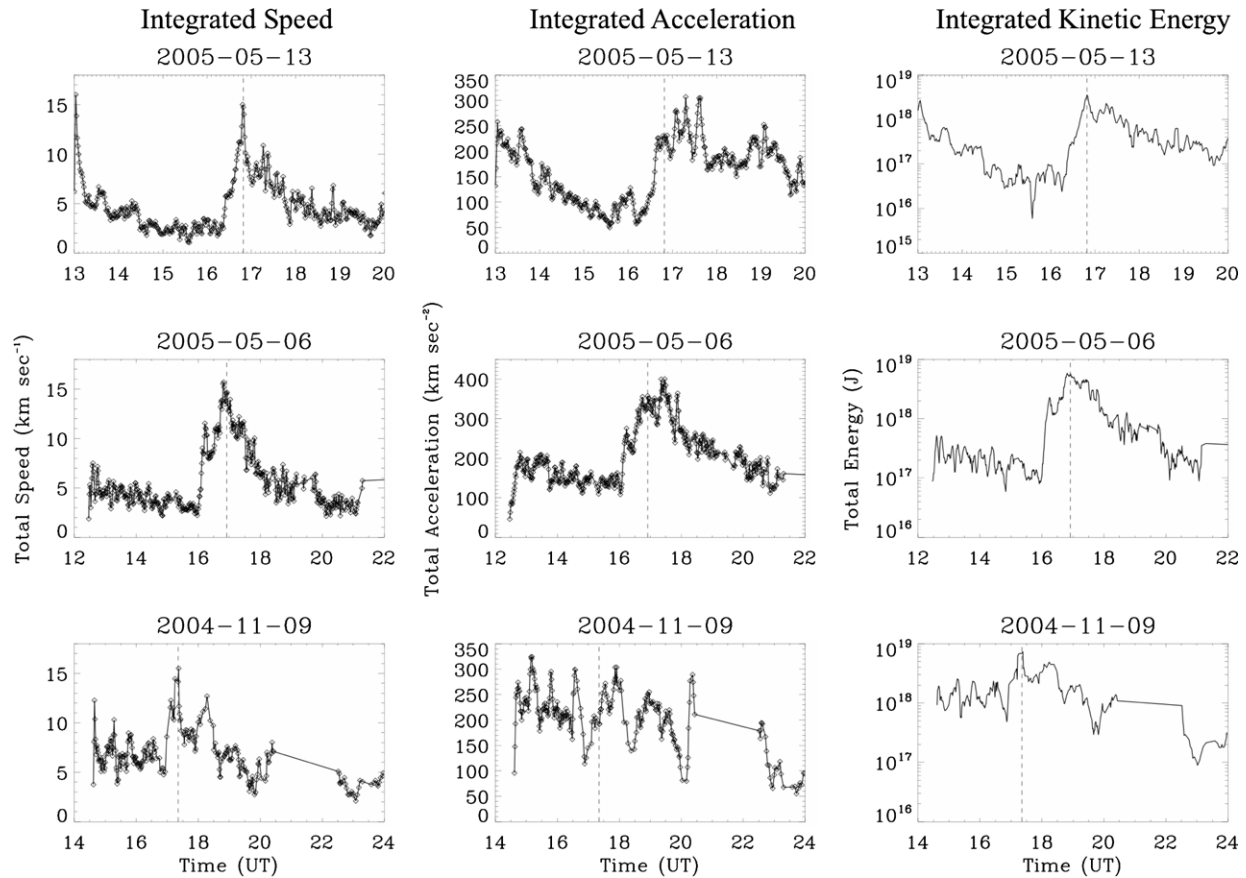


Figure 10. Integrated unsigned propagation speed, acceleration, and energy of flare kernels as a function of time for each of the three events studied. The vertical dashed line indicates the maximum flare intensity for the flaring event. The first column shows the integrated speed curves. The second column shows the acceleration of the flare ribbons. The third column shows the integrated kinetic energy, Equation (8), as a function of time for each of the three events studied. The 2004 flare had significant noise in the original data and a location on the limb contributing to the inconsistent measurements.

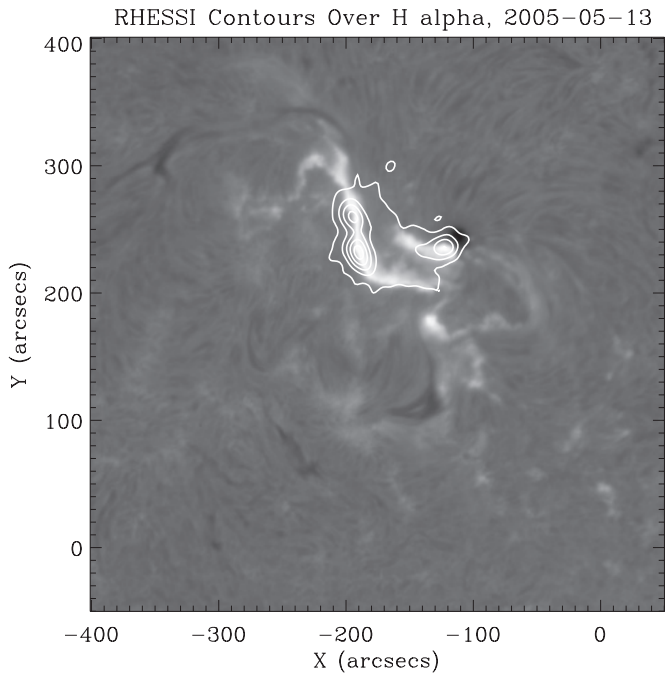


Figure 11. $H\alpha$ image of the 2005 May 13 flare at peak intensity is shown with the reconstructed *RHESSI* 25–50 keV pass band integrated between 16:42 and 16:43 UT contoured on top at 10%, 30%, 50%, 70%, and 90% of the maximum intensity. The field of view of the *RHESSI* image [−220:−95, 180:305] is confined within the flaring region.

velocity is associated with motion away from the observer and into the Sun. A type Ib SCB has a similar intensity and Doppler profile as a type Ia but the timing of the impulsive negative velocity occurs several minutes before the peak intensity of the SCB. The type Ib SCB shown in Figure 12 has a negative velocity that peaks 10 minutes before the peak intensity and returns to a stationary state before the $H\alpha$ line center intensity has decayed. A type II SCB has a positive Doppler shift perturbation that often lasts longer than the emission in the $H\alpha$ intensity profile. The timing of both are nearly coincidental. A type III SCB demonstrates variable dynamics. It has a broad $H\alpha$ intensity line center with significant substructure. A type III SCB begins with a negative Doppler profile much like a type I. Before the negative velocity perturbation can decay back to continuum levels, there is a dramatic positive velocity shift within three minutes with an associated line center brightening. In all types of SCBs the typical magnitude of Doppler velocity perturbation is between 2 and 5 km s^{−1} in either direction perpendicular to the solar surface.

Of all off-flare compact brightenings detected using the automated techniques, 59% of SCBs have no discernible Doppler velocity in the May 6 event and 21% in the May 13 event. Out of the SCBs that do have an associated Doppler velocity, the May 6 event has 35% of type I, 54% of type II, and 11% of type III. The May 13 event has 52% of type I, 41% of type II, and 17% of type III. When totaling all of the Doppler velocity associated SCBs between both events, 41% are of type I, 46% of type II, and 13% of type III. Both line center brightenings and

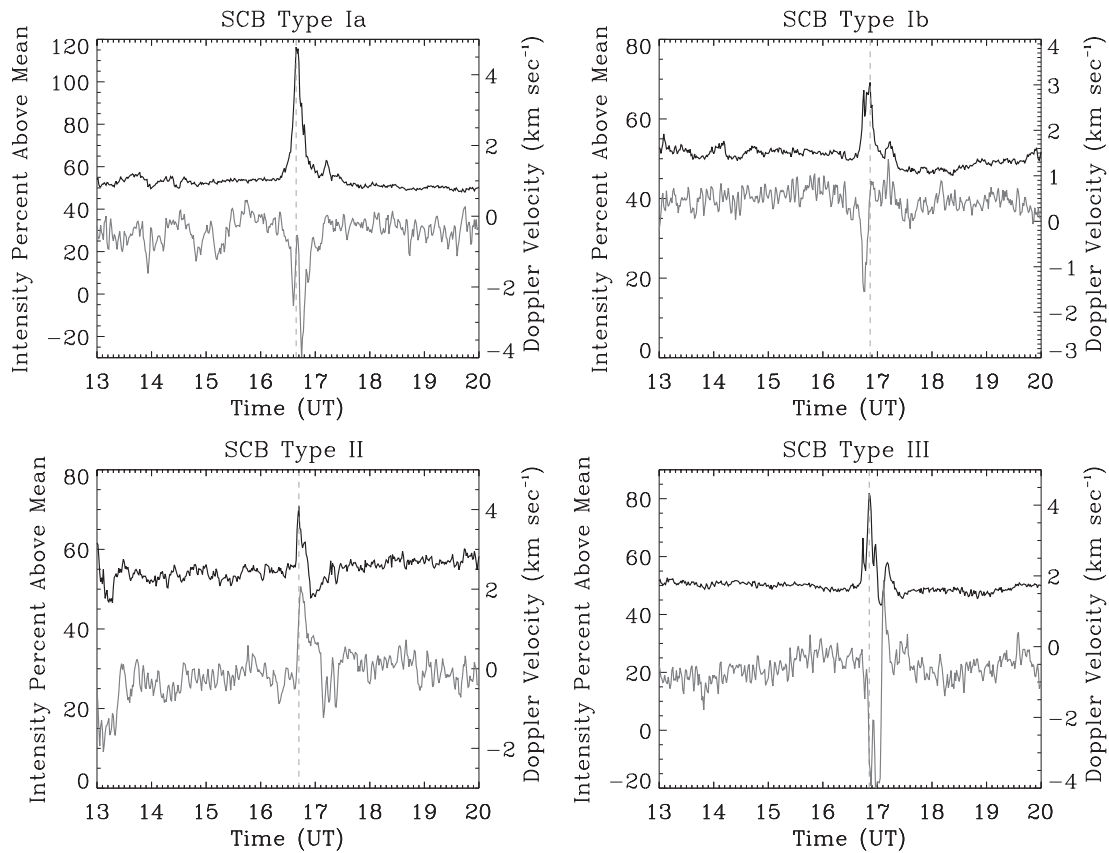


Figure 12. Line center intensity and Doppler velocity measurements for three different types of SCBs observed in both 2005 flares. The vertical dashed line marks the peak $H\alpha$ intensity of the associated SCB. A negative Doppler velocity is away from the observer and into the Sun.

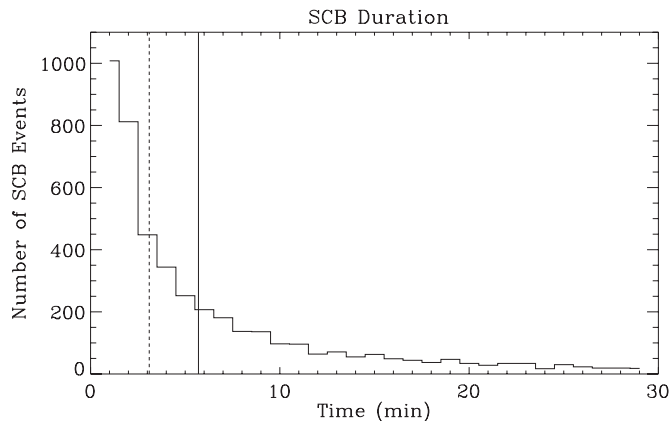


Figure 13. Histogram of the duration of all SCB detections in all three events. The SCBs have a measured mean duration of 5.7 minutes (dot-dashed line) and a median duration of 3.1 minutes (dashed line).

Doppler velocities are filtered such that positive detections have at least a two standard deviation peak above the background noise determined in the candidate detection (Kirk et al. 2011).

4.2. SCBs in Aggregate

Examining SCBs as a total population, the intensity brightenings have a median duration of 3.1 minutes and a mean duration is 5.7 minutes (Figure 13). The duration is characterized by the FWHM of the SCB intensity curve (examples of these curves are shown in Figure 6). A histogram of the distribution of the number of SCB events as a function of duration shows an

exponential decline in the number of SCB events between 2 and 30 minutes (Figure 13). The duration of SCBs is uncorrelated with both distance from flare center and the peak intensity of the SCB.

Examining individual SCBs' distance from the flare center as a function of time provides a way to extract the propagation trends of SCBs around the flare (Figure 14). The bulk SCBs appear between 1.2 and 2.5 Mm away from flare center in a 1 hr time window. At the extremes, SCBs are observed at distances up to ≈ 5 Mm and several hours after the flare intensity maximum. On the top two panels of Figure 14, the shade of the mark corresponds to the intensity of the SCB measured where the lighter the mark, the brighter the SCB. The center of the flare is determined by first retaining pixels in the normalized data set above 1.35. Then all of the images are co-added and the center of mass of that co-added image is set to be the “flare center.” The SCBs tend to clump together in the time–distance plot in both the May 6 and May 13 events. Generally, the brighter SCBs are physically closer to the flare and temporally occur closer to the flare peak. This intensity correlation is weak and qualitatively related to distance rather than time of brightening. Statistics from the 2004 November 9 event are dominated by noise.

Identifying SCBs with negative Doppler shifts within three minutes of the $H\alpha$ peak intensity limits SCBs to type I only. With this method of filtering, some trends become more apparent in a time–distance plot of SCBs (Figure 14, bottom panels). In this view of SCBs, they tend to cluster together in time as well as distance, with two larger groups dominating the plots.

To fit a slope to these populations, a forward-fitting technique is employed similar to a linear discriminate analysis.

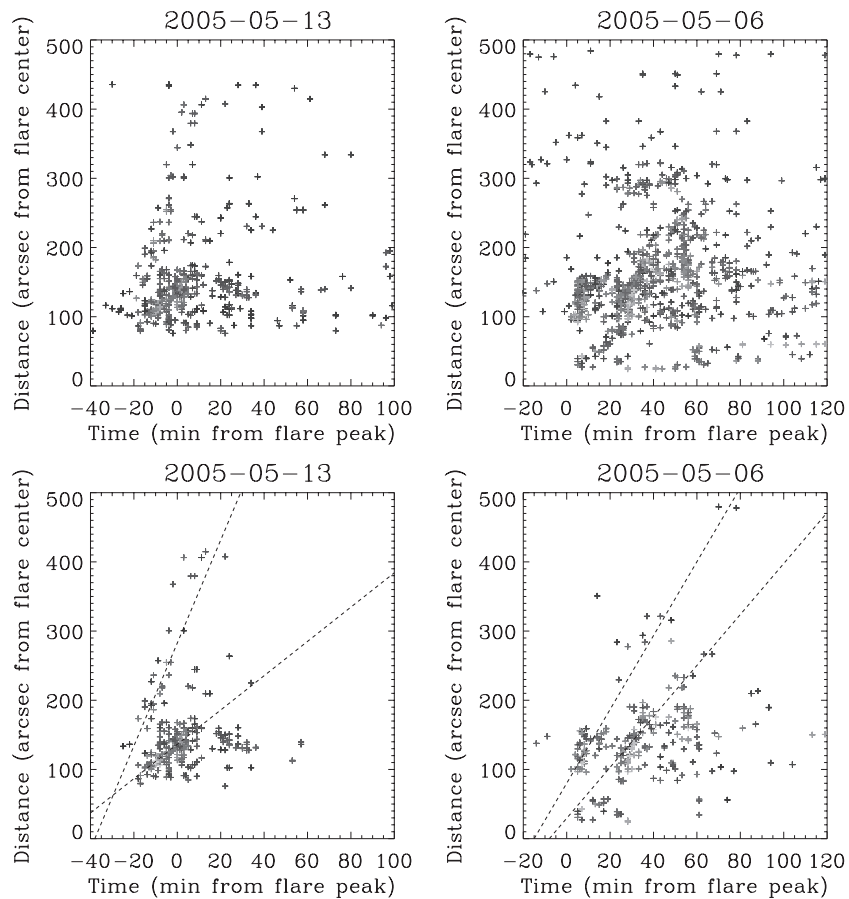


Figure 14. Derived statistics for all SCBs for the 2005 May 6 and 2005 May 13 events. All panels show the distance at which the SCB occurs vs. time from the $H\alpha$ flare peak. The color of each plotted point is representative of its relative intensity; the lighter points are higher intensity detections. Bottom: the same plots as the top two panels except with a Doppler filter applied—each point had to have an SCB Type I Doppler shift associated with the line center brightening. The dashed lines are fit to the two visually distinct groups in each event.

This method requires the user to identify the number of groups to be fitted and the location of each group. The fitting routine then searches all linear combinations of features for the next “best point” to minimize the χ^2 to a regression fit of the candidate group. Repeating this method over all the points in the set produces an ordered set of points that when fit, have an increasing χ^2 value. A threshold is taken where the derivative of the χ^2 curve increases to beyond one standard deviation, which has the effect of identifying where the χ^2 begins to increase dramatically. Running this routine several times minimizes the effect of the user and provides an estimate of the error associated with the fitted line. This method has two caveats. First, this fitting method relies on the detections having Poissonian noise. This is not necessarily correct since the detection process of compact brightenings introduces a selection bias. Second, the fitting method makes the assumption that no acceleration occurs in the propagation of SCBs. This is a reasonable approximation but from studies of Moreton waves in the chromosphere (e.g., Balasubramaniam et al. 2010), a constant velocity propagation is unlikely.

Applying the forward-fitting technique these two data sets yields two propagation speeds: a fast and a slow group. The May 6 event has propagation speeds of $71 \pm 2 \text{ km s}^{-1}$ and $49 \pm 2 \text{ km s}^{-1}$. The May 13 event has propagation speeds of $106 \pm 7 \text{ km s}^{-1}$ and $33 \pm 4 \text{ km s}^{-1}$. Beyond these detections, the May 13 event has a third ambiguous detection with a propagation

speed of $-7 \pm 5 \text{ km s}^{-1}$. The implications of these statistics are discussed in Section 6.

The X-ray intensity measured with *RHESSI* temporally covers a part of the flaring event on 2005 May 13. *RHESSI* data coverage begins at 16:37 UT during the impulsive phase of the flare. Comparing the integrated X-ray intensity curve between 25 and 50 keV to the aggregate of SCB intensities integrated over each minute yields some similarities (Figure 15). The X-ray intensity peaks about a minute after the integrated SCBs reach their maximum intensity. The decay of both the X-ray intensity and SCB integrated curve occurs approximately on the same timescale of ≈ 50 minutes.

5. PHYSICAL INTERPRETATION OF RESULTS

From the results of the tracking method, we can gain insight into the physical processes associated with SCBs and flares. First, the flare ribbons studied are both spatially and temporally clumped into discrete kernels. The relatively smooth ribbon motions observed in $H\alpha$ and the nearly ideal exponential decay characterized in X-ray flux measurements belie the substructure that makes up a two-ribbon flare. This is discussed in Section 5.1. Second, the brightening in the flare ribbons is caused by a distinctly different physical process than the one causing SCBs. In this sense, SCBs are different than micro-flares. Our interpretation of the physical origin of SCBs is addressed in Section 5.2.

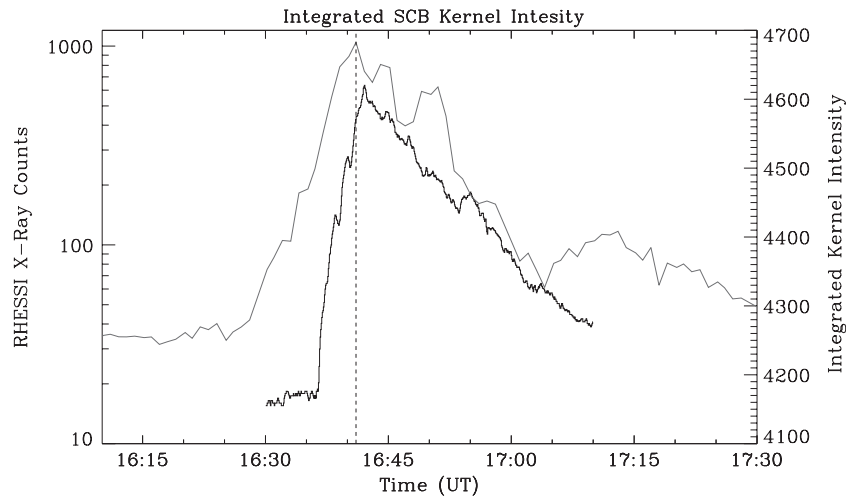


Figure 15. Plot showing the *RHESSI* non-thermal 25–50 keV intensity in black and the $H\alpha$ SCB integrated intensity curve in gray for the 2005 May 13 flare. The vertical dashed line indicates the peak of the integrated SCB curve.

5.1. Two Ribbon Chromospheric Flares

Flare kernels are observed to appear and disappear as the underlying flare ribbons evolve, as discussed in Section 3.1. Examining individual kernel structure suggests that there is substructure within a flare ribbon whose elements impulsively brighten and dim within the brightness that encompasses the intensity curve. These results support the premise that flares are made up of several magnetic field lines reconnecting (e.g., Priest & Forbes 2002). There is no evidence to claim that an individual flare kernel is directly tracking a loop footprint. Within a tracked flare kernel, multiple coronal reconnection events are superimposed to produce the observed asymmetries a single flare kernel’s light curve.

Maurya & Ambastha (2010) tracked subsections of the 2003 October 28 X17 flare as it evolved. They reported peak speeds ranging from ~ 10 to 60 km s^{-1} (depending on the spatially tracked part of the flare) over the observed span of 13 minutes. Maurya & Ambastha (2010) also reported that the total apparent distances the ribbons traveled were $\sim 10^4 \text{ km}$. The October 28 flare is several orders of magnitude greater in *GOES* X-ray intensity than the flares considered for this study. In the present study, despite this difference, peak speeds of flare kernels observed in this work are measured at $\sim 2.3 \text{ km s}^{-1}$ and the mean velocity of all flare kernels is $\sim 0.2 \text{ km s}^{-1}$. The maximum distance flare kernels traversed was $\sim 2 \times 10^4 \text{ km}$ and the average distance traveled was $\sim 5 \times 10^3 \text{ km}$; both of these values are similar to the 2003 October 28 event. Although the velocities of the flare ribbons studied here are at least an order of magnitude less, the two to three orders-of-magnitude difference in the *GOES* peak intensity between the October 28 flare and the flares studied here implies that the apparent velocities and distance traveled by flare ribbons do not scale linearly with the strength of the eruption.

The bulk of the apparent motion and acceleration in the flare ribbons are observed after the peak of the flare intensity. Integrating this into the dynamical model of a two-ribbon flare (Démoulin & Priest 1988) implies that the peak intensity of the flare occurs in the low-lying arcade and loses intensity as the x-point reconnection progresses vertically to higher levels (Baker et al. 2009). The measured divergence of the ribbons dominates the motion but there is significant apparent flow tangential to the flare ribbons. This predicates that there is lateral propagation to the x-point as well as vertical propagation.

5.2. A Physical Model of SCBs

Figure 16 is a proposed phenomenological model of the overlying physical topology. SCBs are hypothesized to be caused by electron beam heating confined by magnetic loop lines overarching flare ribbons. These overarching loops are analogous to the higher lying, unsheared tethers in the breakout model of CMEs (Antiochos et al. 1999). As the flare erupts, magnetic reconnection begins in a coronal x-point. The CME escapes into interplanetary space, the remaining loop arcade produces a two-ribbon flare, and the tethers reconnect to a new equilibrium position. The tether reconnection accelerates trapped plasma which impacts the denser chromosphere causing observed brightening. This description implies that the driver of SCBs is the eruption of an CME. Balasubramaniam et al. (2006) found a strong correlation between CMEs and the presence of SCBs.

A simple loop configuration without localized diffusion or anomalous resistance implies that the length of the loop directly proportional to the travel time of the electron beam. This means that the different propagation groups observed in Figure 14 result from different physical orientations of overarching loops. The time it takes to observe a chromospheric brightening can therefore be described as

$$\tau_{\text{SCB}} = \gamma \frac{L}{v_e}, \quad (9)$$

where τ_{SCB} is the time it takes for accelerated plasma to travel from the coronal x-point, along the magnetic loop lines, impact the chromosphere, and produce a brightening, L is the length of the tether before reconnection, v_e is the electron velocity along the loop line, and γ is a function of changing diffusion and resistance between chromosphere and corona. In physical scenarios, v_e is likely a combination of the Alfvén speed and the electron thermal velocity.

The slopes plotted in Figure 14 show two different propagation speeds for SCBs: $33\text{--}49 \text{ km s}^{-1}$ and $71\text{--}106 \text{ km s}^{-1}$. The sound speed in the chromosphere is approximately $c_s \approx 10 \text{ km s}^{-1}$ (Nagashima et al. 2009), while the Alfvén speed in the upper chromosphere is approximated to be between $v_A \approx 10$ and 100 km s^{-1} (Aschwanden 2005). Both of the SCB propagation speeds are significantly above the approximated sound speed; however, they fall reasonably well into the

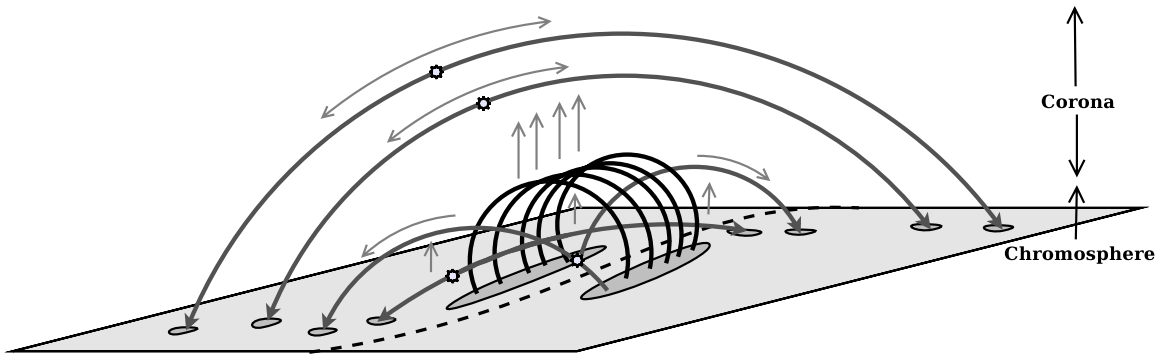


Figure 16. Schematic model of the physical cause of SCBs. A dashed line marks the neutral line in this model. The central loops represent the emerging two-ribbon flare arcade. The arches represent field lines connecting outside of the flare ribbons. The arrows on top of both the loops and arches show the direction trapped plasma flows as the flare begins to erupt and the stars suggest the location where the plasma is disrupted. Once perturbed, the trapped plasma streams down the loop lines and impacts the chromosphere causing the $H\alpha$ intensity brightening. The different orientations of off-flare loops account for the different propagation speeds of SCBs observed.

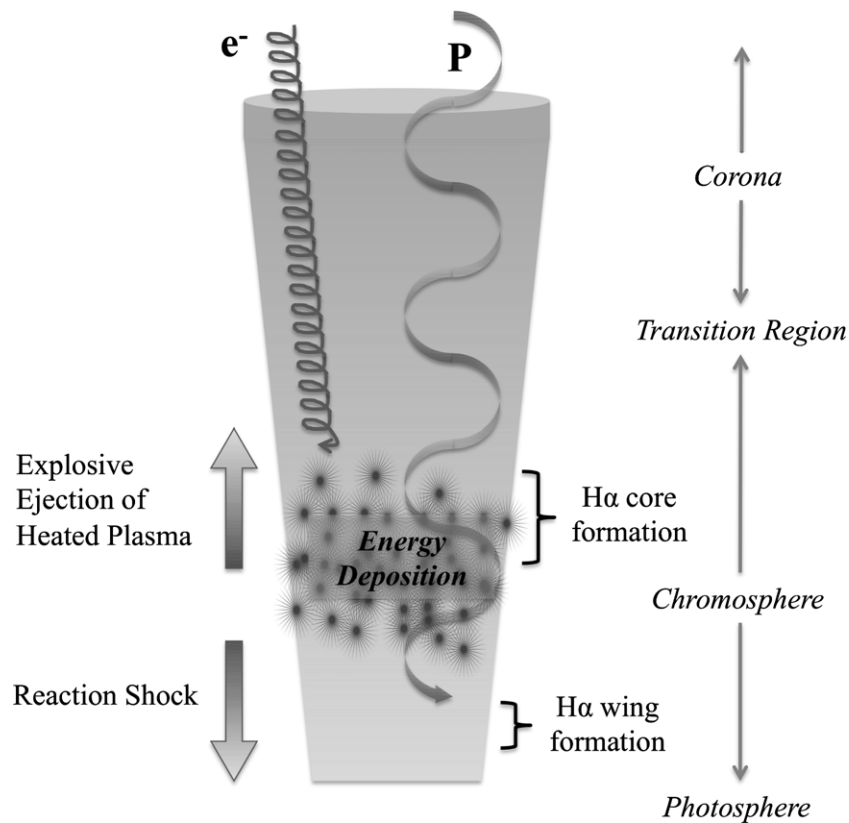


Figure 17. Diagram of the physical dynamics occurring in a single SCB. Electrons and protons accelerated by magnetic reconnection further up in the corona come streaming down the flare loop. Since the mean free path of electrons is significantly less, the electrons deposit energy into the upper chromosphere. Unable to radiate the energy as heat, the chromosphere explosively responds by sending material back up the flux tube (chromospheric evaporation) and a reaction shock propagates toward the photosphere. This reaction shock explains the velocities observed in Type I SCBs.

range of the Alfvén speed. Assuming the propagation speed of non-thermal plasma along the loop line is consistent between flare loops, the different propagation speeds would then imply different populations of loops being heated as the flare erupts.

Examining single SCBs, the coincident Doppler recoil with the $H\alpha$ intensity presents a contradiction. If an SCB is an example of compact chromospheric evaporation (e.g., Dennis & Schwartz 1989), then the only Doppler motion should be outward, the opposite of what is observed. Figure 17 presents a possible solution to this. Since the scattering length of electrons is significantly smaller than that of protons, the

electron beam impacts the mid-chromosphere and deposits energy into the surrounding plasma while the protons penetrate deeper. This deposited heat cannot dissipate effectively through conduction or radiation and thus expands upward into the flux tube. To achieve an expansion with rates of a few km s^{-1} as observed, the chromospheric heating rate must be below $E_H \leq 10^{10} \text{ erg cm}^{-2} \text{ s}^{-1}$ (Fisher et al. 1984). As a reaction to this expansion, a reaction wave propagates toward the solar surface in the opposite direction of the ejected plasma. Since the Doppler measurements are made in the wings of the $H\alpha$ line, the location of the Doppler measurement is physically closer to the photosphere than the $H\alpha$ line center. Thus, the observer sees

the heating of the $H\alpha$ line center and coincidentally observes the recoil in the lower chromosphere.

In type II SCBs an upflow is observed. This is an example of a classic chromospheric evaporation where the heated plasma in the bulk of the chromosphere is heated and ablated back up the flux tube. In contrast, the type III class of SCB shown in Figure 12 presents an interesting anomaly to both the other observed SCBs and the model proposed in Figure 17. Since there is an initial down-flow, the beginning state of type III SCBs are similar to type Is. As the recoil is propagated, a continual bombardment of excited plasma (both protons and electrons) impacts the lower chromosphere, causing ablation and changing the direction of flow.

6. SUMMARY AND CONCLUSIONS

Two conclusions can be made about the flares studied in this work: first, the asymmetrical motions of the flare ribbons imply that the peak flare energy occurs in the low-lying arcade, and second, flare-related SCBs appear at distances on the order of 10^5 km and have properties of sites of compact chromospheric evaporation. Maurya & Ambastha (2010) estimated reconnection rates from a measurement of the photospheric magnetic field and the apparent velocity of chromospheric flare ribbons. Therefore, it would be possible to estimate the reconnection rates using this technique with the addition of photospheric magnetograms. Associating vector magnetograms with this technique and a careful consideration of the observed Doppler motions underneath the ribbons would provide a full three-dimensional method for estimating the Lorentz force for subsections of a flare ribbon.

SCBs originate during the impulsive rise phase of the flare and often precede the $H\alpha$ flare peak. SCBs are found to appear with similar qualities as compact chromospheric ablation confirming the results of Pevtsov et al. (2007). The heuristic model proposed in Figure 17 requires unipolar magnetic field underneath SCBs. The integration of high-resolution magnetograms and a field extrapolation into the chromosphere would confirm this chromospheric evaporation model. One consequence of chromospheric evaporation is that the brightening should also be visible in EUV and X-ray observations due to non-thermal protons interacting with the lower chromosphere or photosphere.

SCBs are a special case of chromospheric compact brightening that occur in conjunction with flares. The distinct nature of SCBs arises from their impulsive brightenings, unique Doppler velocity profiles, and origin in the impulsive phase of flare eruption. These facts combined demonstrate that SCBs have a non-localized area of influence and are indicative of the conditions

of the entire flaring region. They can possibly be understood by a mechanism in which a destabilized overlying magnetic arcade accelerates electrons along magnetic tubes that impact a denser chromosphere to result in an SCB. This distinguishes SCBs from the flare with which they are associated. In a future work, we plan to address physical mechanisms to explain the energetic differences between SCBs and flares to explain the coupled phenomena.

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