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Report Title

Final Report on "Survey of Quantification and Distance FunctionsUsed for Internet-based Weak-link Sociological Phenomena"

ABSTRACT

We summarize our research activities and results in this manuscript. It ends with some conclusions.

Final Report on "Survey of Quantification and Distance Functions Used for Internet-based Weak-link Sociological Phenomena" *

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January 16, 2013

1 Research Activities:

Dr. Ming-Jun Lai, the PI and Dr. Dawn Robinson, the co-PI had a few meetings in the Lai's office and one meeting at the Robinson's office and discussed how to proceed the research during the Aug. and Sept., 2011. They had several emails communications before and after these meeting. Also, later in March 2012, they had another meeting on the distribution of the grant money, one summer month salary for the PI and one summer month salary for the co-PI. The PI used all the fund allocated for travel, a part of the travel fund was used for Mr. George Slavov, one of the PI's graduate students for his summer salary and a part of the travel fund was used for Mr. Leopold Matamba-Messi's travel to UCLA for a conference. Mr. Leopold Matamba Messi is another graduate students of the PI. Mr. Matamba-Messi graduated in the Aug. 2012 and found a post-doc position at the Mathematical Biology Institute at Ohio State University. Since Aug., 2012, the PI has emailed to the co-PI about the final report several times. The PI and co-PI met again on Dec. 5, 2012 during a workshop and discussed how to write this report. They have met again in the Lai's office on Jan. 16, 2013 for submission of the final report.

2 Research Results:

The PI studied all mathematical literature he can find related to the Google search engine, Google matrix, PageRank as well as the Yahoo search engine and a classic SearchKing HIST algorithm. The co-PI immersed herself in the sociology literature for the relevant studies on social network, strong and weak social ties and etc.. which may be useful for the study of search algorithms. Our findings can be summarized as follows.

- 1) A review of the related mathematical literature is given in section 2.2 of Appendix I.
- 2) In addition, the PI presented a new proof of the convergence of Google searching algorithm although there are several proofs available already. See Section 2.3 of Appendix I. This analysis is used for new algorithms based on sociological analysis discussed in 6) below.

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- 3) The PI proposed a local update algorithm which is new. However, its computational efficiency is not compared with other updated algorithms yet. See Section 2.4 of Appendix I.
- 4) Certainly, the PI studied how to improve the efficiency of the computation in hoping to speed up the search. Due to the explosive increase of the webpages and the Internet surfers, such a study is definitely necessary. However, the study does not lead to any meaningful results so far.
- 5) The PI discussed with the co-PI about the web search algorithms in sociological sense which is one of the key points of this project. The PI found that the Bonacich centrality measure is the same as the one used in Google search algorithm if the relation matrix is the adjacency matrix with an appropriate normalization constant. See section 3 of Appendix I.
- 6) The co-PI suggested to use not only the out-linkages, but also the in-linkages in the search algorithm. In addition, the co-PI suggested to use the secondary linkages to further help determine the relevance in PageRank. Based on these ideas, the PI has proposed a new version of searching algorithm which uses both in- and out-linkages, and proved that the modified algorithm is still convergent and the convergence rate is determined by the damping factor. See section 4 of Appendix I.
- 7) The co-PI reviewed a lot of literature in sociology related to the PageRank, the relevant scores for linkages, in particular, for social linkages, as well as the social strong and weak ties, social cohesion, position and distance. See Appendix II.
- 8) The co-PI was willing to write it out a section to explain why one needs to use both in- and out-linkages in sociological terminology. However, the PI has not received such a write-up as Jan. 15, 2013.
- 9) Finally, the PI studied the Yahoo search algorithm based on its patent although the current Yahoo updates its search algorithm and the PI did not find enough time to study it. See Section 5 of Appendix I.

3 Conclusion:

The PI has surveyed all the mathematical literature related to the search engines up to today and the co-PI has summarized all the sociological concepts related to the internet search, not only the relevance among webpages, but also the closeness, betweenness among people, groups, etc.. The goal of this project to understand the PageRank sociologically and how it could be adjusted to be more effective sociologically as well as how to make the algorithms more efficient. This is still a central issue. The PI is not able to complete this goal of the project as the PI and co-PI have managed their time to only do the surveys of the current literatures in mathematical and sociological senses and have not found enough time to discuss their connections. They made a small progress towards the goal as mentioned above. The PI would like to continue this project if the ARO is willing to fund it again. Due to this project, the PI gains an excellent knowledge on the mathematical study of the Google searching algorithm and other search algorithms. He is ready to attack some research problems related to the algorithms such as how to speed up the computation and how to update in parallel the Google matrix, its PageRank vector and etc.. Also, he is now able to work with a sociologist better as he knows many sociological definitions and notations. See Items 5) and 6) above as an evidence.

With more time, this research team could more deeply digest the existing information, and propose some new algorithms, making use of sociological insights to improve mathematically the characterization of relations in large, complex systems. The PI and co-PI plan to continue their joint work toward a better understanding of the searching algorithms and discovering how to better situate them in the larger contexts of existing mathematical and sociological knowledge.

Appendix I

Ming-Jun Lai and Dawn Robinson, A Mathematical and Sociological Analysis of Google Search Algorithm, a manuscript, 2013.

Appendix II

Dawn Robinson, A Summary of Sociological Concepts Related to Social Network and Its Techniques for Quantifying Social Cohesion, Social Position, Social Distance, a manuscript, 2013.