



Multi-Objective Path Planning for a Team of Unmanned Aerial Vehicles (UAVs) in a Dynamic and Uncertain Environment

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Outline

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- **Multi-Objective Path Planning for UAVs**
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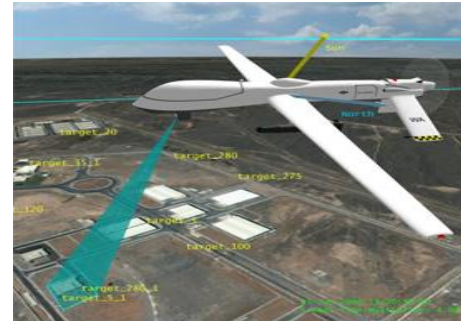
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Introduction: UAV Mission Planning

- UAVs have **ultra long endurance** and can accept **high mission risk**; these attributes make them suitable for *dull, dirty, and dangerous* tasks in complex environments:

- **Military:**

- Intelligence, Surveillance & Reconnaissance (ISR)
- Search and Rescue Operations (SAR)
- Demining Operations



- **Security:**

- Border Patrol
- Surveillance of Smuggling Operations
- Interdiction Operations



- **Civil:**

- Disaster Management
- Forest Fire Detection
- Traffic Monitoring



- In the future, UAVs are expected to operate with a higher level of autonomy to carry out complex tasks, while efficiently coordinating with unmanned ground and unmanned underwater vehicles ⇒ **Need for systematic mission planning processes**

Introduction

Technical Challenges

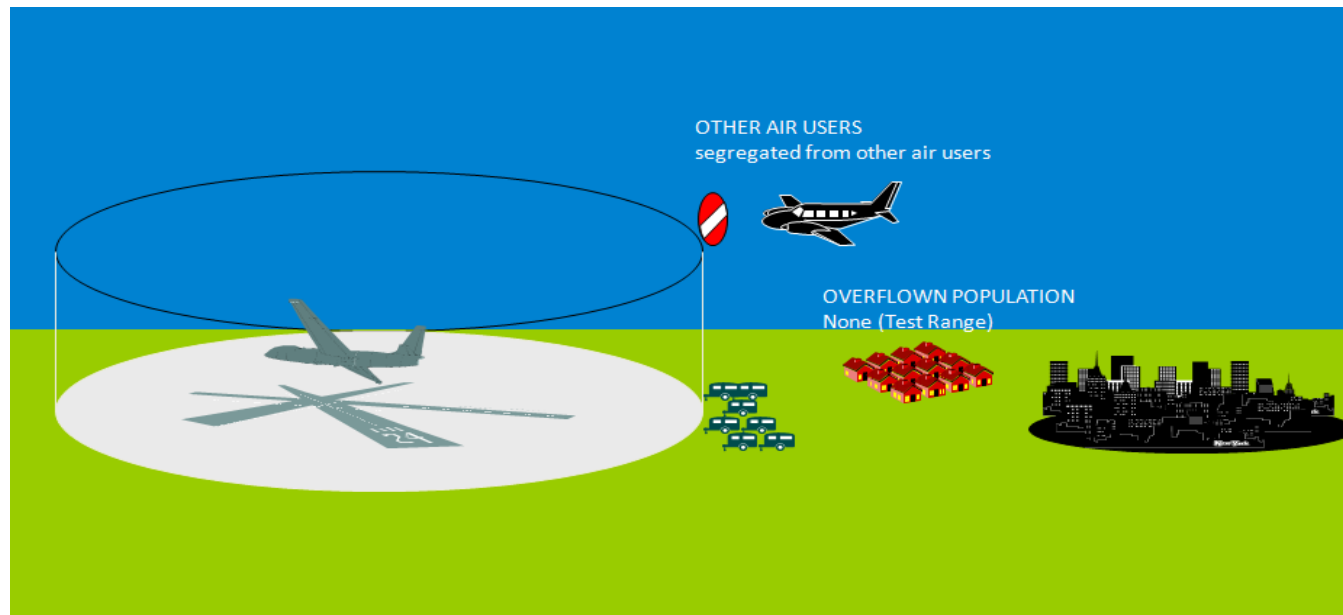
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- Lack of see and avoid capability :
 - May lead to mid-air collisions with manned vehicles
 - Restricts UAVs to operate in segregated regions in the airspace
 - Needs substantial human supervision
 - Limits operational flexibility



Flying UAV within national borders in controlled, segregated airspace over an unpopulated area

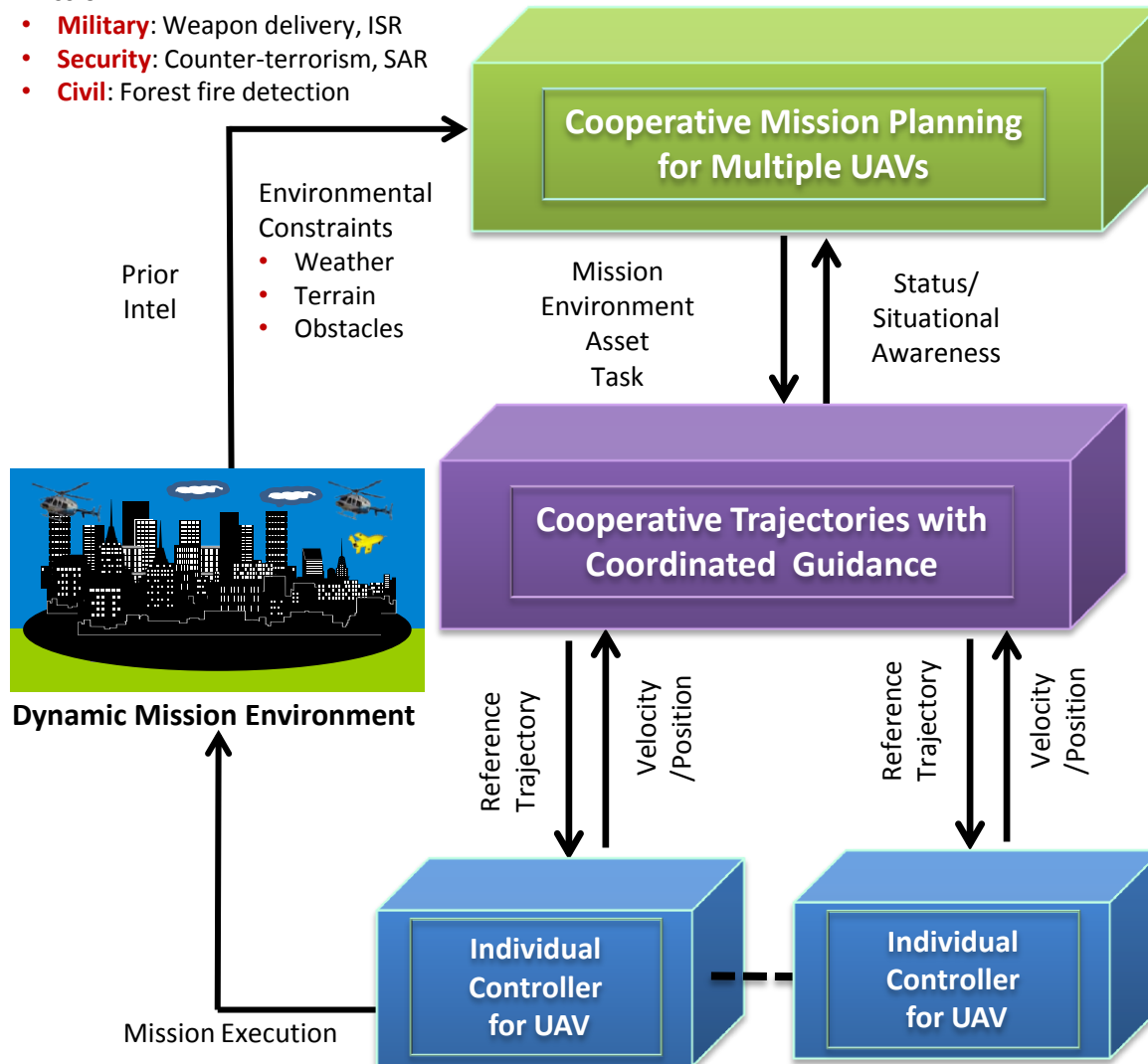
- Limited sensor ranges and payload capacity requires multiple UAVs to:
 - Work cooperatively
 - Expedite the mission execution
 - Reduce the possibility of mission failure

Hierarchical Architecture for UAV Mission Planning

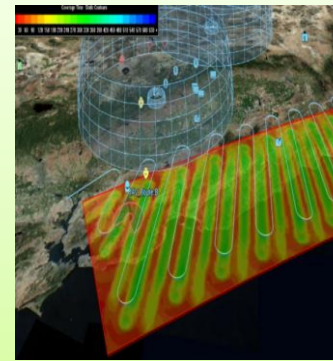
- Systematic mission planning structure for conducting complex tasks involving multiple UAVs

Mission

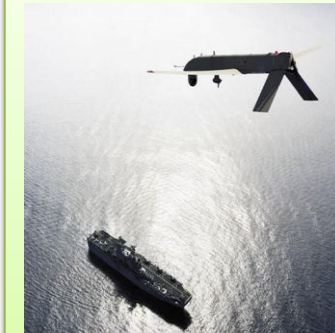
- Military:** Weapon delivery, ISR
- Security:** Counter-terrorism, SAR
- Civil:** Forest fire detection



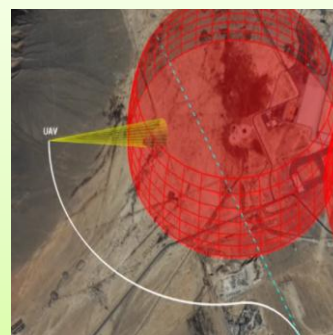
Dynamic Path Planning



Target Search & Tracking



Dynamic Task Assignment



Formation Hold



Ref: <http://www.agi.com/solutions/uav-and-aircraft-mission-software/Default.aspx>

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Multi-Objective Path Planning for UAVs

- **Objective:** *Coordinated* multi-objective path planning for a group of UAVs in a dynamic environment to carry out *time-critical mission tasks*:
 - Minimize mission risk (path cost, e.g., distance of UAV from obstacle)
 - Minimize task latencies

- Dynamic Obstacles
- Static Obstacles
- UAV
- Task Locations

Mission Scenario

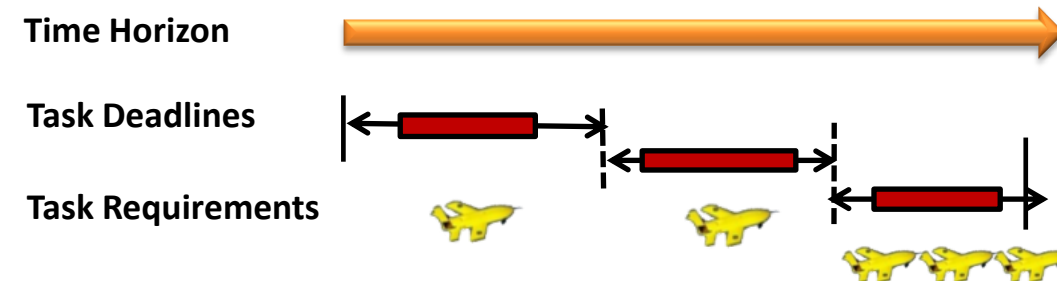
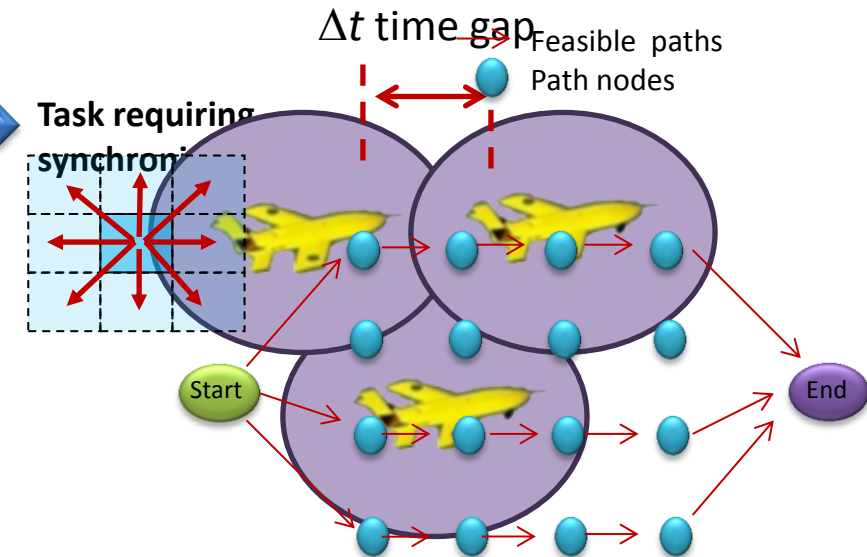


Given:

- Dynamic environment with static and dynamic obstacles, e.g., high rise buildings, manned aircraft
- Task locations, deadlines, task requirements

Constraints:

- Dynamic environment constraint
- Task workflow constraints



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UAV Path Planning Formulation

- Multi-Objective Mixed Integer Linear Programming (MILP) Problem:
 - Objective I: Minimize cumulative path risk* - Time varying travel and usage cost

$$\text{Obj}_1 : \min_{x_{ijkt}} \sum_{t=1}^T \sum_{k=1}^K \sum_{(i,j) \in \Omega} r_{ijkt} x_{ijkt} \quad (1)$$

$$x_{ijkt} = \begin{cases} 1, & \text{if UAV } k \text{ moves from cell } i \text{ to cell } j \text{ at time } t \\ 0, & \text{otherwise} \end{cases}$$

where T is the time horizon, K is the total number of UAVs and Ω is the set of accessible paths

r_{ijkt} is the path risk experienced by UAV k in moving from cell i to cell j at time t

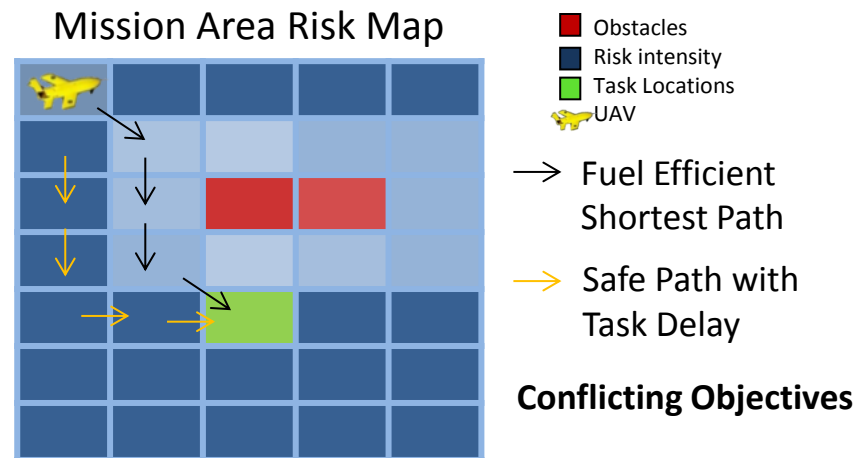
- Objective II: Minimize task latency* - Delay in meeting the task deadline

$$\text{Obj}_2 : \min \sum_{l=1}^L t_l^{\text{latency}}, \quad t_l^{\text{latency}} = \max(0, t_l^{\text{start}} + t_l^{\text{process}} - t_l^{\text{deadline}}) \quad (2)$$

where

$t_l^{\text{start}}, t_l^{\text{process}}, t_l^{\text{deadline}}$ denote the start time, processing time and deadline for task l

L denotes the total number of tasks



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Multi-Objective MILP Problem Constraints



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- Network Flow Constraints:** Time-varying travel and usage cost

$$\sum_{t=1}^T \sum_{i \in Q(1,t)} x_{1ikt} = 1, \forall k \quad 1(a)$$

$$\sum_{t=1}^T \sum_{i \in P(N,t)} x_{iNkt} = 1, \forall k \quad 1(b)$$

$$\sum_{t=1}^T \sum_{j \in Q(i,t)} x_{ijkt} - \sum_{t=1}^T \sum_{j \in P(i,t)} x_{jikt} = 0, \forall k, \forall i \neq 1 \& i \neq N \quad 1(c)$$

$$\sum_{t=1}^{\tilde{T}} \sum_{j \in Q(i,t)} x_{ijkt} \leq \sum_{t=1}^{\tilde{T}} \sum_{j \in P(i,t)} x_{jikt}, \forall k, \forall i \neq 1, \forall \tilde{T} < T \quad 1(d)$$

where

x_{ijkt} : Path risk

k : UAV index

N : Total number of cells

T : Time horizon

$Q(i,t)$: Successor cells of i at time t

$P(i,t)$: Predecessor cells of i at time t

- Task Execution Constraints:** Delay in meeting the task deadline

$$t_{kloc(l)}^{depart} \geq t_l^{start} + t_l^{process}, \forall l, \forall k \in \Psi_l^{asgn} \quad 2(a)$$

$$t_l^{start} = \max_{k \in \Psi_l^{asgn}} t_{kloc(l)}^{arrive}, \forall l \quad 2(b)$$

$$\sum_{j \in P(loc(l),t)} \sum_{k=1}^K x_{jloc(l)kt} \leq q_l, \forall l, \forall t \quad 2(c)$$

where

$t_{kloc(l)}^{depart}$: Departure time of UAV k

$t_{kloc(l)}^{arrive}$: Arrival time of UAV k

Ψ_l^{asgn} : Set of assigned UAVs for task l

q_l : Maximum number of UAVs for task l

$loc(l)$: Location of task l

Multi-Objective MILP Problem Constraints



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- *Collision Avoidance Constraints*: Ensures safe path by avoiding collision with obstacles

$$\begin{aligned}
 t_{k'i}^{arrive} - t_{ki}^{depart} &\geq \Delta t - M \alpha_{kk'i} \quad \forall i, k, k' \neq k & 3(a) \\
 t_{ki}^{arrive} - t_{k'i}^{depart} &\geq \Delta t - M (1 - \alpha_{kk'i}) \quad \forall i, k, k' \neq k & 3(b) \\
 \alpha_{kk'i} &\in \{0, 1\}, \forall i, k, k' \neq k
 \end{aligned}$$

where

M : Large number

$\alpha_{kk'i}$: Binary variable indicating when UAV k arrives after k'

Δt : Time gap

- *Arrival and Departure Constraints*: Tracks the execution status of tasks

$$\begin{aligned}
 t_{k1}^{arrive} &= 0, \forall k & 4(a) \\
 t_{ki}^{depart} + t_k^{travel} x_{ijkt} &\leq t_{kj}^{arrive} + M (1 - x_{ijkt}), \forall k, \forall i, \forall j \neq 1, \forall t & 4(b) \\
 t_{ki}^{depart} &\geq t_{ki}^{arrive}, \quad \forall i \notin \{loc(l)\}, \forall k & 4(c) \\
 t_{ki}^{depart} &\geq t_{ki}^{arrive}, \quad \forall i \in \{loc(l)\}, \forall k \notin \Psi_l^{asgn} & 4(d)
 \end{aligned}$$

where

t_{ki}^{depart} : Departure time of UAV k from cell i

t_k^{travel} : Travel time of UAV k

t_{ki}^{arrive} : Arrival time of UAV k at cell i

Multi-Objective UAV Path Planning Results

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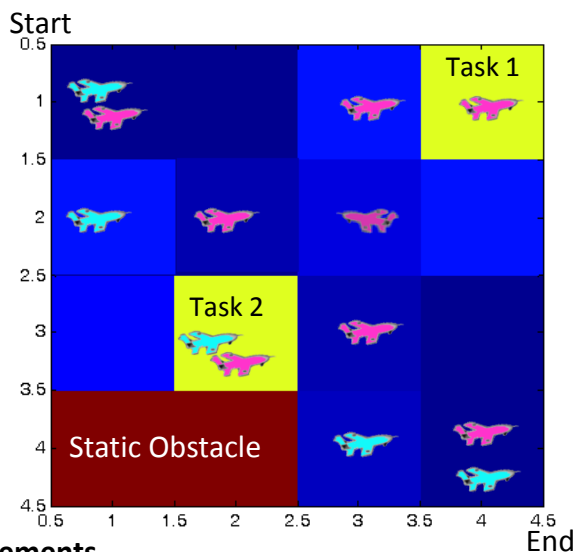
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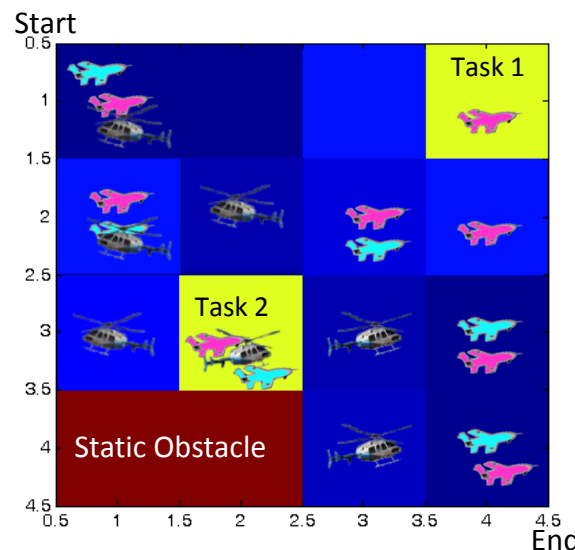
Results

- **Solution:** Decomposed MILP solution approach:
 - **Phase I:** Minimize the path risk of each UAV given the estimated arrival time at each task location
 - **Phase II:** Minimize the task latency with respect to the arrival time of each UAV at each task location given the path in Phase I
- **Scenario I:** Coordinated path planning in different contexts

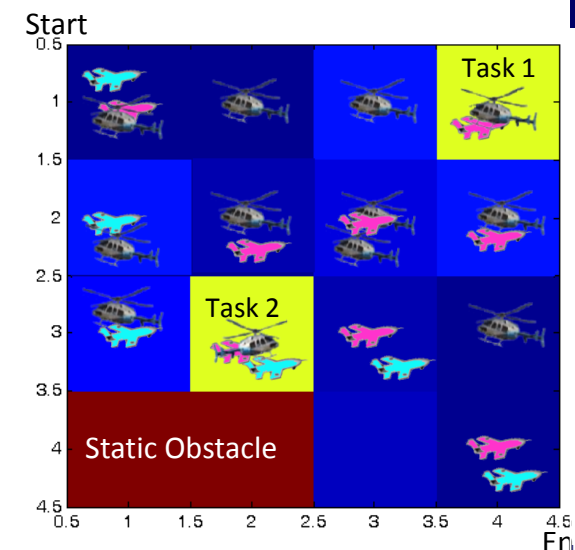
a) No manned aircraft



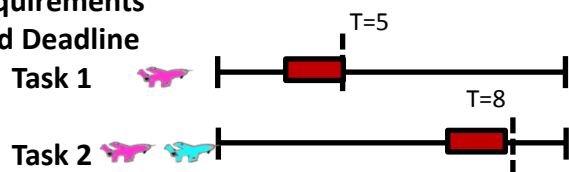
b) One manned aircraft



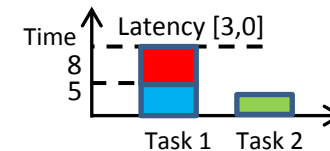
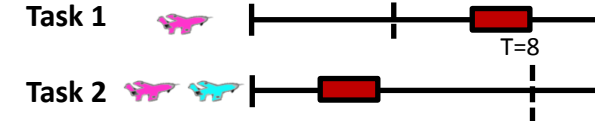
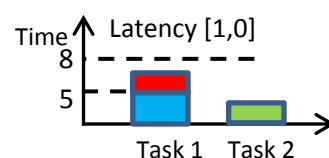
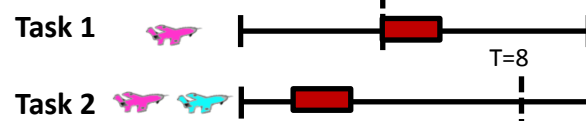
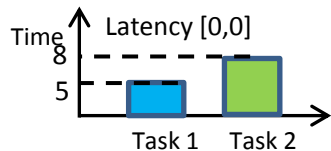
c) Two manned aircraft



Requirements and Deadline



Task Latency



Multi-Objective UAV Path Planning Results

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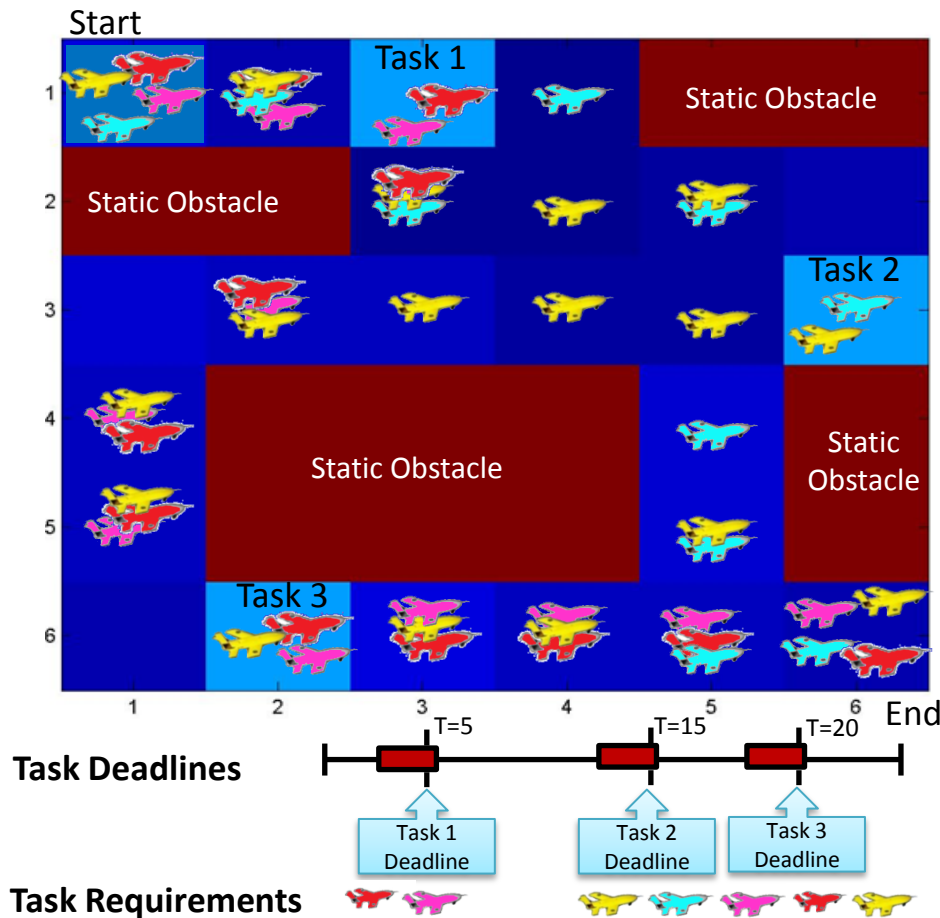
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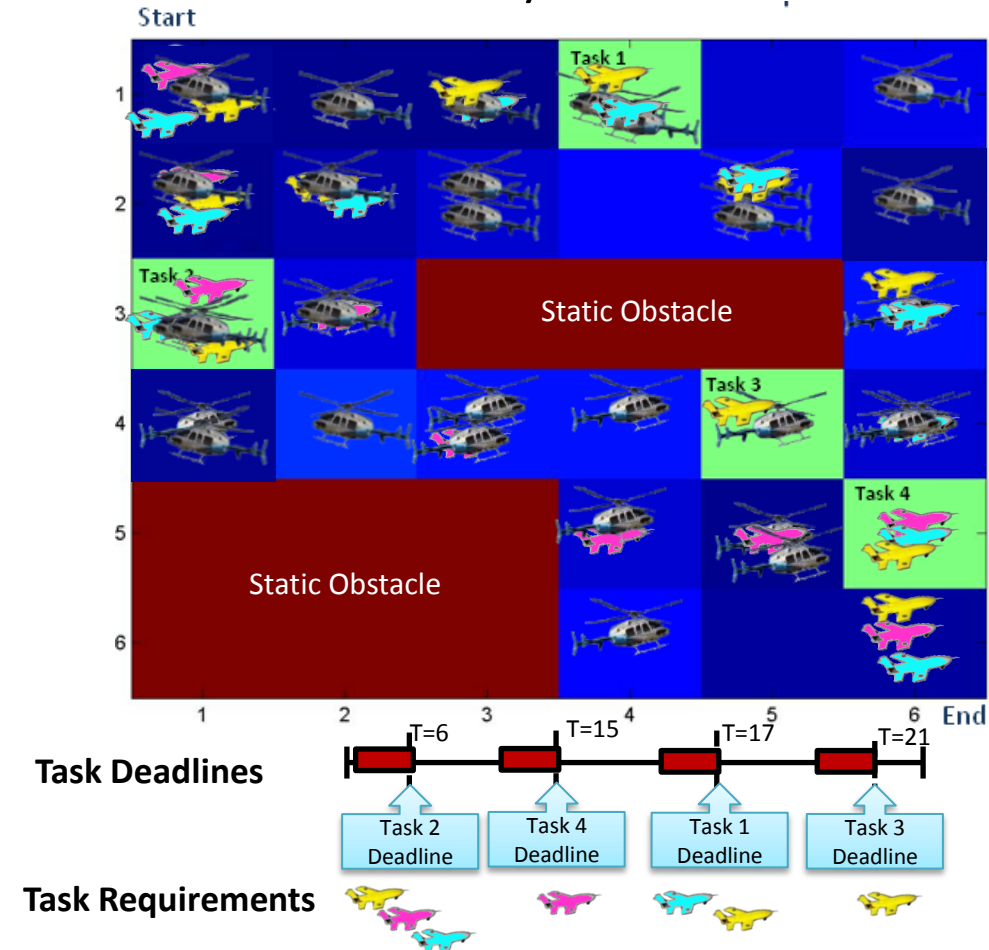
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- **Scenario II:** Coordinated path planning around static obstacles



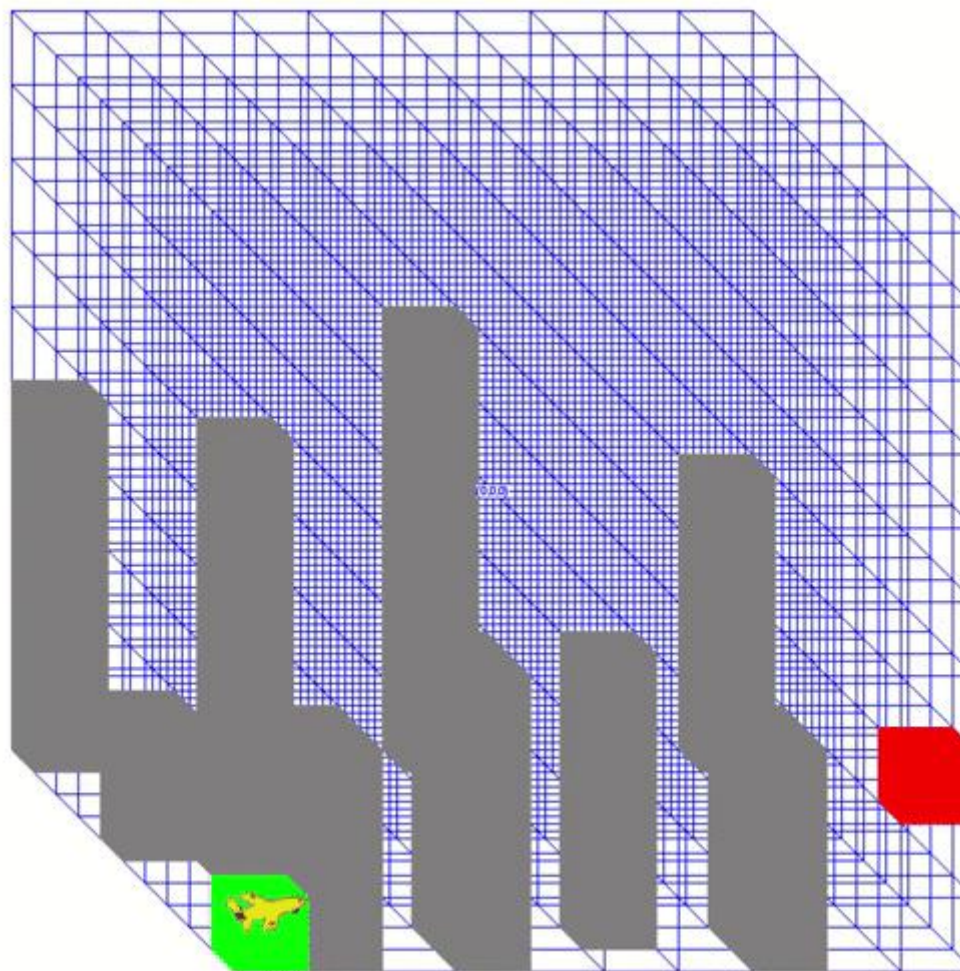
- **Scenario III:** Coordinated path planning around static and dynamic obstacles



- **Scenario I:** An increase in the number of manned aircraft delays the task processing time in order to guarantee safe trajectory planning within a confined mission area
- **Scenario II & III:** Mission tasks are completed on time in a large environment with static and dynamic obstacles

Python Implementation of 3D A* Algorithm

- Given:
 - **Mission:** Path planning
 - **Environment:** 3D mission space
 - **Asset:** UAV
 - **Task:** Plan path from start point to end point while avoiding static obstacles
- **Future Work:** 3D path planning for multiple UAVs within a dynamic environment



-  End Point
-  Start Point
-  Obstacles
-  Path
-  UAV

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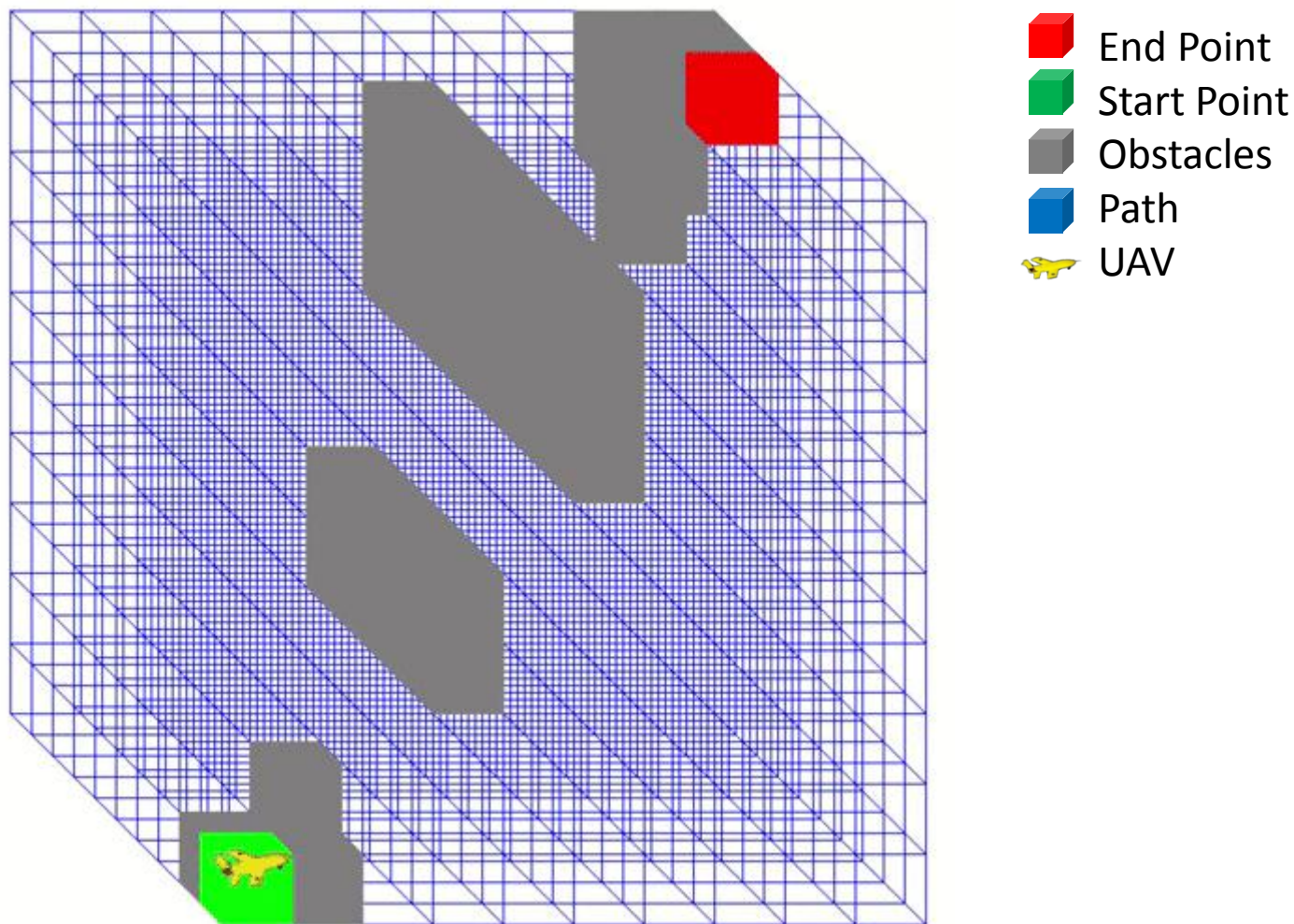
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- Summary

- UAVs are useful for dull, dirty, and dangerous military and civilian operations
- A multi-objective UAV path planning problem was investigated for coordinated task execution in a dynamic environment including:
 - Mathematical formulation of the path planning problem
 - A two-phase algorithm to solve the resulting MILP problem
- 3D A* algorithm was implemented in Python

- Future Work

- Explore approximation techniques, such as ant colony system and genetic algorithms
- Revise the current planning structure to a distributed setting
- Explore 3D path planning and address the vertical collision avoidance problem
- Incorporate pop-up threats and sudden UAV breakdown scenarios



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Future UAV Mission Planning Challenges



Future UAV Mission Planning Challenges

- Provide capabilities more efficiently through *modularity and interoperability*
- Increase in autonomous *multi-platform control*
- More *survivable* with improved and *resilient communications* and security from tampering
- Efficient *manned and unmanned teaming to reduce the number of personnel* required to operate and maintain the systems
- *Consider realistic models* and incorporate/fuse data from different sources

UAV Mission Planning Objectives

- *Dynamic coordination* of multiple unmanned vehicles operating on ground, air, and water
- Develop efficient *algorithms to mimic human-like behavior* in unmanned aerial vehicles for proactive decision support
- Data protection and exploitation using *High Performance Computing (HPC)*
- *Reduce operator workload* by improving autonomy using hierarchical mission planning
- Improve *data flow and standard message architectures* for reliable communication

High Performance Computing Impacts

- Provides a *consolidated plug-and-play* application architecture
- Improves *scalability and feasibility* for unmanned aerial system vendors
- *Improved battle space awareness* via tasking, collection, processing, exploitation, and dissemination (TCPED) processes, required to translate vast quantities of sensor data into a shared understanding of the environment
- HPC enables *cross domain data sharing* of information and adapts rapidly to changing threats
- HPC addresses the challenges in *cloud computing* and *multilayer security*, communications, open standards, data storage, cost, ease of technology insertion, etc.

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