

~~UNANNOUNCED~~

REPORT D

AD-A956 318

Form Approved
OMB No. 0704-0188

Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Service, Project (0704-0188), Washington, DC 20503.



is for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Service, Project (0704-0188), Washington, DC 20503.

1. AGENCY USE ONLY (Leave blank) **21 Sept 77** **Memorandum, Sept. 1977**

4. TITLE AND SUBTITLE
CSPAM: A Program For Evaluating Buoy Field Detection Performance

5. FUNDING NUMBERS
C N00014-77-C-0385

6. AUTHOR(S)
McCABE, Bernard J.

7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)
**Daniel H. Wagner, Associates, Inc.
Station Square Two
Paoli, PA 19301**

DTIC ELECTE
MAR 18 1992
S C D

8. PERFORMING ORGANIZATION REPORT NUMBER

9. SPONSORING / MONITORING AGENCY NAME(S) AND ADDRESS(ES)
COMPATWINGSPAC

10. SPONSORING / MONITORING AGENCY REPORT NUMBER

11. SUPPLEMENTARY NOTES

12a. DISTRIBUTION / AVAILABILITY STATEMENT
Unrestricted

12b. DISTRIBUTION CODE

13. ABSTRACT (Maximum 200 words)
The purpose of this memorandum is to describe a revised version of the computer program SPAM, which will be called CSPAM. It incorporates a more detailed model for spatial correlation.

14. SUBJECT TERMS
Detection modelling, spatial correlation, cumulation detection probability

15. NUMBER OF PAGES
47 (incl. Appendix)

16. PRICE CODE

17. SECURITY CLASSIFICATION OF REPORT
Unclassified

18. SECURITY CLASSIFICATION OF THIS PAGE
Unclassified

19. SECURITY CLASSIFICATION OF ABSTRACT
Unclassified

20. LIMITATION OF ABSTRACT
UL

GENERAL INSTRUCTIONS FOR COMPLETING SF 298

The Report Documentation Page (RDP) is used in announcing and cataloging reports. It is important that this information be consistent with the rest of the report, particularly the cover and title page. Instructions for filling in each block of the form follow. It is important to *stay within the lines* to meet *optical scanning requirements*.

Block 1. Agency Use Only (Leave blank).

Block 2. Report Date. Full publication date including day, month, and year, if available (e.g. 1 Jan 88). Must cite at least the year.

Block 3. Type of Report and Dates Covered. State whether report is interim, final, etc. If applicable, enter inclusive report dates (e.g. 10 Jun 87 - 30 Jun 88).

Block 4. Title and Subtitle. A title is taken from the part of the report that provides the most meaningful and complete information. When a report is prepared in more than one volume, repeat the primary title, add volume number, and include subtitle for the specific volume. On classified documents enter the title classification in parentheses.

Block 5. Funding Numbers. To include contract and grant numbers; may include program element number(s), project number(s), task number(s), and work unit number(s). Use the following labels:

C - Contract	PR - Project
G - Grant	TA - Task
PE - Program Element	WU - Work Unit Accession No.

Block 6. Author(s). Name(s) of person(s) responsible for writing the report, performing the research, or credited with the content of the report. If editor or compiler, this should follow the name(s).

Block 7. Performing Organization Name(s) and Address(es). Self-explanatory.

Block 8. Performing Organization Report Number. Enter the unique alphanumeric report number(s) assigned by the organization performing the report.

Block 9. Sponsoring/Monitoring Agency Name(s) and Address(es). Self-explanatory.

Block 10. Sponsoring/Monitoring Agency Report Number. (If known)

Block 11. Supplementary Notes. Enter information not included elsewhere such as: Prepared in cooperation with...; Trans. of...; To be published in... When a report is revised, include a statement whether the new report supersedes or supplements the older report.

Block 12a. Distribution/Availability Statement. Denotes public availability or limitations. Cite any availability to the public. Enter additional limitations or special markings in all capitals (e.g. NOFORN, REL, ITAR).

DOD - See DoDD 5230.24, "Distribution Statements on Technical Documents."

DOE - See authorities.

NASA - See Handbook NHB 2200.2.

NTIS - Leave blank.

Block 12b. Distribution Code.

DOD - Leave blank.

DOE - Enter DOE distribution categories from the Standard Distribution for Unclassified Scientific and Technical Reports.

NASA - Leave blank.

NTIS - Leave blank.

Block 13. Abstract. Include a brief (*Maximum 200 words*) factual summary of the most significant information contained in the report.

Block 14. Subject Terms. Keywords or phrases identifying major subjects in the report.

Block 15. Number of Pages. Enter the total number of pages.

Block 16. Price Code. Enter appropriate price code (*NTIS only*).

Blocks 17. - 19. Security Classifications. Self-explanatory. Enter U.S. Security Classification in accordance with U.S. Security Regulations (i.e., UNCLASSIFIED). If form contains classified information, stamp classification on the top and bottom of the page.

Block 20. Limitation of Abstract. This block must be completed to assign a limitation to the abstract. Enter either UL (unlimited) or SAR (same as report). An entry in this block is necessary if the abstract is to be limited. If blank, the abstract is assumed to be unlimited.

UNANNOUNCED

DANIEL H. WAGNER, PRES.
HENRY R. RICHARDSON, SR. V. PRES.
DAVID C. BOSSARD, V. PRES.
LAWRENCE D. STONE, V. PRES.
BARRY BELKIN, V. PRES.
LESLIE K. ARNOLD, SR. ASSOC.
BERNARD J. McCABE, SR. ASSOC.
THOMAS L. CORWIN, SR. ASSOC.
STANLEY J. BENKOSKI, ASSOC.
WILLIAM J. BROWNING, ASSOC.
BRUCE E. SCRANTON, ASSOC.
WILLIAM H. BARKER, ASSOC.
FRANK P. ENGEL, ASSOC.
SCOTT S. BROWN, ASSOC.
ROBERT P. BUENI, ASSOC.
LARRY K. GRAVES, ASSOC.
JAMES R. WEISINGER, ASSOC.

DANIEL H. WAGNER, ASSOCIATES
CONSULTANTS
OPERATIONS RESEARCH MATHEMATICS
STATION SQUARE ONE
PAOLI, PENNSYLVANIA 19301

NIAGARA 4-3400
AREA CODE 215
(620)

September 21, 1977

MEMORANDUM REPORT

To: COMPATWINGSPAC
Attn: LCDR Philip Harvey
Contract No. N00014-77-C-0385

From: B. J. McCabe

Subject: CSPAM - A Program For Evaluating Buoy Field Detection Performance

The purpose of this memorandum is to describe a revised version of the computer program SPAM, which will be called CSPAM, which attempts to account for the effects of range-dependent buoy to buoy correlation. In SPAM the detection capability of a field of buoys is arrived at by averaging what it would be if the buoys were statistically independent with what it would be if they were completely dependent. The weighting does not depend on the spacing of the buoys. In CSPAM a more elaborate detection model is used so that the correlation between a pair of buoys is monotone decreasing as the range between the two buoys varies from 0 to ∞ . The anticipated use of CSPAM is as a tool to study optimal buoy field patterns and spacing.

In the sections to follow we describe the mathematical model for detection used in CSPAM and compare it to that in SPAM, give some sample runs of

92 3 16 052

92-06769


CSPAM to illustrate the effects of varying the correlation function, give an abbreviated programmer's guide, and provide a listing of CSPAM.

The inputs to CSPAM, as currently configured, are identical in form and import to those for SPAM, with one exception: the parameter which determines the correlation function. Moreover, all of SPAM's subroutines are incorporated in CSPAM. For these reasons no separate user's guide for CSPAM is given - the reader should consult reference [a] for a SPAM user's guide as well as reference [b] for additional background material on SPAM and its detection model.

A comprehensive assessment of the impact of treating correlation by means of this more elaborate model has not yet been made. Such analysis will be forthcoming. Some sample runs are included but they pertain to only one environment and one target scenario.

The abbreviated programmer's guide has a twofold purpose. Firstly, the routines in CSPAM that are different from those in SPAM are explained. Secondly, there are portions of CSPAM that are currently configured in an arbitrary way, awaiting further discussion and deliberation. Attention is directed to these problem areas and the parts of the program where suitable changes can be made are pointed out. This memorandum is partly intended as an impetus for discussion of these provisional aspects of CSPAM.

Underlying Analysis

In this section we discuss the problem of modeling correlated sensors, and how this problem is addressed in CSPAM.



Accession For	
NTR GRAM	
DTIC Tab	
Unannounced	
Justification	
By	
Distribution/	
Availability Code	
Dist	Avail and/or Special
A-1	
UNANNOUNCED	

Correlated sensors. In modeling acoustic detection it is generally assumed that the occurrence of a detection is determined by a function

$$SE(t) + \alpha(t), \quad t \geq 0$$

where

$$SE(t) = FOM - N_w(R(t))$$

is the expected signal excess at time t and α is a stochastic process representing the uncertainties and fluctuations in the various components of figure of merit (FOM) and propagation loss (N_w). $R(t)$ is the distance between the sensor and the target at time t .

Suppose there are n sensors and a single target and n corresponding signal excess histories SE_i and fluctuation processes α_i , $i = 1, \dots, n$. Suppose that cumulative detection probability is given by a threshold crossing* model

$$cdp_i(t) = \Pr \{ SE_i(s) + \alpha_i(s) \geq 0 \quad \text{for some } s \leq t \}.$$

If the processes α_i , $i = 1, \dots, n$, were all mutually independent, then cdp for the field of sensors as a whole would be an easy computation,

$$cdp_I(t) = 1 - \prod_{i=1}^n (1 - cdp_i(t)),$$

or if the fluctuation processes were identical, $\alpha_1 = \dots = \alpha_n = \alpha$, we would have an easy calculation

*The detection model in SPAM and CSPAM is slightly different from this but the gist of this discussion is relevant.

$$\text{cdp}_D(t) = \Pr \left\{ \alpha(s) + \max_{1 \leq i \leq n} \text{SE}_i(s) \geq 0 \quad \text{for some } s \leq t \right\}.$$

However, it is reasonable to believe that the processes α_i , $i = 1, \dots, n$, have correlation between 0 and 1, and that the amount of correlation between two sensors should decrease with the distance between them. The SPAM model recognizes correlation by taking a weighted average of cdp_I and cdp_D but the weighting is independent of the spacing among the n sensors.

Model for range dependent correlation. Suppose that each process α_i is a sum of processes each of which is a model for the fluctuations contributed by the components of the sonar equation: target radiated noise (L_S), background noise (L_E), recognition differential (N_{RD}), and propagation loss (N_W).

We make the following assumptions which are rough approximations and subject to debate.

Fluctuations in L_S are felt equally at all sensors so we assume that the component of α_i due to L_S is identical for each i . This neglects the aspect dependence of radiated noise.

For buoys, background noise is dominated by ambient noise which at most frequencies of interest is due to shipping. Thus we assume that the component of α_i due to L_E is correlated with the corresponding component of α_j , for all $i \neq j$, and the correlation structure is given by a model such as that of reference [c], and, in particular, is range dependent. More about this in a later subsection.

The correlation in N_{RD} from buoy to buoy is determined by the performance of the same operator examining n lofargrams. If the operator is more or less perceptive, diligent or attentive in examining one lofargram then he will tend to perform similarly at each other display. Thus we assume that the component

of α_i due to N_{RD} is positively correlated with the corresponding component of α_j and that this amount of correlation is the same for any pair i, j .

The effects due to propagation loss are more difficult to describe compactly. There is no doubt some correlation between any pair of sensors. The correlation depends not only on the distance between the sensors but also on the position of the target relative to the sensor pair, and thus the amount of correlation is also time dependent since the target is moving. These effects could be addressed but only at the expense of great added complexity and computer time, so we have for the present decided to ignore these effects and hypothesize an independent component for N_W .

To summarize, we have four major contributors to uncertainty in SE. Three of them will be modeled fairly adequately, and it is hoped that the deficiency in the modeling of the other term will not be critical, especially since we only require that the sum of these four terms be reasonably accurate in its portrayal of buoy to buoy correlation.

Our mathematical model for each α_i is then of this form*:

$$\alpha_i = \xi + \xi_i + \eta_i^1 + \eta_i^2, \quad i = 1, \dots, n,$$

where:

ξ is $N(0, \sigma_1)$ and independent of all $\xi_i, \eta_i^1, \eta_i^2$,

ξ_i is $N(0, \sigma_2)$, independent of ξ_j for $j \neq i$, and independent of all η_j^1, η_j^2 ,

η_i^1 is $N(0, \sigma_3)$, independent of all η_j^2 , and has correlation $\rho \geq 0$ with each $\eta_j^1, j \neq i$, and

η_i^2 is $N(0, \sigma_4)$ and has correlation $C(r_{ij})$ with η_j^2 where r_{ij} is the distance between sensors i and j , and C is the ambient noise correlation function to be discussed below.

* $N(\mu, \sigma)$ denotes a random variable with a Gaussian distribution, mean μ and standard deviation σ .

The variance of each α_i is thus $\sigma^2 = \sigma_1^2 + \sigma_2^2 + \sigma_3^2 + \sigma_4^2$.

Note that we have modeled these components as random variables, not as time varying stochastic processes. This is consistent with the methodology of SPAM to which we are adhering. A time varying model is more realistic. It allows for detections past CPA, for example, which are precluded in this kind of model. Unfortunately, for this application it would lead to an unreasonably long running time for the program, and it is therefore a luxury that cannot be afforded.

As a comment on the mathematical model it might be mentioned that if a time varying model were being used and if running time were not a problem, a reasonable parametric model for propagation loss correlation could be easily constructed. For example, one might hypothesize that correlation between two buoys is of the form $\kappa R_1(t) \cos(\theta(t)/2)/R_2(t)$ where R_1 and R_2 are the ranges from the target to the two buoys, R_1 being the smaller, and θ is the angular separation of the two buoys as viewed from the target. It can be checked that this formula gives sensible values in all limiting cases and the parameter κ can be used to tune the results to any available data.

Finally, we note that choices must be made for the parameters $\sigma_1, \sigma_2, \sigma_3, \sigma_4$ and ρ . These choices are difficult because there probably is not any suitable body of data from which to estimate them. For lack of any better information the program is currently configured with $\sigma_1 = \sigma_2 = \sigma_3 = \sigma_4 = 4$ db and $\rho = .5$ and these values were used in the test runs included in the next section. These particular values imply that the correlation between α_i and α_j is between .375

and .625, these limiting values being reached when $r_{ij} = +\infty$ and $r_{ij} = +0$, respectively. This is a fairly narrow window and it will be seen that the result is to make cdp not extremely sensitive to the shape of the correlation function C. If σ_4 were higher, the other σ_i lower and ρ lower, then the window would be larger and the results more sensitive to C. In other words the choices for these parameters are quite important and need to be discussed.

The CTW model. A thorough description of the Cumulative Time Window (CTW) model is in reference [b] but we give a summary account here for purposes of our discussion. In this subsection we discuss the model as applied in SPAM; the next subsection describes the revision in CSPAM.

There are three inputs required in SPAM: t_0 , t_1 , and t_2 . To put it briefly, t_0 is a minimum integration time, t_2 is a maximum integration time (opportunities at a fixed signal excess which are of longer duration than t_2 buy no additional detection probability) and t_1 is the time step used in the simulation.

Since SPAM takes a simple weighted average of independent and completely dependent buoys it suffices to define $cdp_i(j)$, the probability that buoy i makes a detection by time jt_1 .

Let

$$c_{ij} = \Pr \{ SE_1(jt_1) + X \geq 0 \}$$

where X is $N(0, \sigma)$; c_{ij} is called the instantaneous probability of detection (ipd).

Let $A(j) = \{ j - \left\lceil \frac{t_2}{t_1} \right\rceil, \dots, j - 1, j \}$.

Then we define

$$cdp_i(j) = \begin{cases} 1 - \prod_{k \in A(j)} (1 - c_{ik})^{t_1/t_0} & \text{if this quantity is } \geq cdp_i(j-1), \\ cdp_i(j-1) & \text{otherwise.} \end{cases}$$

To initialize, assume $cdp_i(0) = 0$ and $c_{ik} = 0$ for any $k < 0$.

Incorporation of the general model into the framework of SPAM. Just as in SPAM, an initial position for the target, its course, and its speed are drawn from the appropriate distributions, for each replication. SPAM at this point computes cdp_i analytically for each buoy i , and arrives at cdp for the field by combining cdp_i and cdp_D as described above. Each replication produces a cdp curve and these are all averaged to give the final estimated cdp .

In CSPAM we cannot compute cdp for the buoy field analytically because of the complicated correlation structure of the α_i 's. Recalling that

$$\alpha_i = \xi + \xi_i + \eta_i^1 + \eta_i^2$$

we see that one way to proceed would be to simulate values of ξ , η_i^1 , η_i^2 , $i=1, \dots, n$ and compute cdp analytically from this point since the detection events

$SE_i + \alpha_i - N_W(R_i) > 0$ are independent when conditioned on values of ξ , η_i^1 , η_i^2 .

This is basically how CSPAM works.

As it turns out, because of the special nature of the correlation structure of the η_i^1 , it is actually not necessary to simulate them. The following gimmick allows us to simulate two processes instead of three, which saves labor and reduces variance.

Since the correlation of η_i^1 and η_j^1 is ρ for all $i \neq j$, we may represent η_i^1 in the form

$$\eta_i^1 = \sqrt{\rho} \sigma_3 N_0 + \sqrt{1-\rho} \sigma_3 N_i$$

where N_0, N_1, \dots, N_n are $N(0, 1)$ and independent. This is a sort of decomposition of each η_i^1 into identical and independent parts. Now these parts can be grouped with ξ and ξ_i respectively to give the following representation:

$$\begin{aligned} \alpha_i &= \xi + \xi_i + \eta_i^1 + \eta_i^2 \\ &= (\xi + \sqrt{\rho} \sigma_3 N_0) + (\xi_i + \sqrt{1-\rho} \sigma_3 N_i) + \eta_i^2. \end{aligned}$$

Thus there is actually no need to simulate the η_i^1 's. Their role can be subsumed into two other terms if we make the transformations

$$\begin{aligned} \sigma_1 &\rightarrow \sqrt{\sigma_1^2 + \rho \sigma_3^2} \quad \text{and} \\ \sigma_2 &\rightarrow \sqrt{\sigma_2^2 + (1-\rho) \sigma_3^2}. \end{aligned}$$

In addition to saving computer time this reduces the variance of our results since a ratio $(\sigma_2^2 + (1-\rho)^2 \sigma_3^2)/\sigma^2$ of our work on the α_i 's is now being done analytically instead of just σ_2^2/σ^2 .

Let $\bar{\xi}$ denote the adjusted process $\xi + \sqrt{\rho} \sigma_3 N_0$ and $\bar{\xi}_i$ the adjusted process $\xi_i + \sqrt{1-\rho} \sigma_3 N_i$. Then

$$\alpha_i = \bar{\xi} + \bar{\xi}_i + \eta_i^2.$$

In CSPAM we make draws for $\bar{\xi}$ and η_1^2 , $i = 1, \dots, n$, and compute the conditional idp

$$c_{ij}(\bar{\xi}, \eta_1^2) = \Pr \{SE_1(jt_1) + \bar{\xi} + \bar{\xi}_1 + \eta_1^2 \geq 0\}.$$

Then cdp_1 , conditioned on the choices of $\bar{\xi}$, η_1^2 , is computed using the c_{ij} , just as in SPAM, and finally cdp conditioned on $\bar{\xi}$, η_1^2 , $i = 1, \dots, n$, is computed as

$$cdp(j) = 1 - \prod_{i=1}^n (1 - cdp_1(j)).$$

Just as in SPAM, these cdp functions, one for each replication, are then averaged.

The method for generating the η_1^2 's with the correct joint distribution will now be described.

Let D be an arbitrary $n \times n$ covariance matrix. Let η be an n -dimensional vector of independent $N(0, 1)$ random variables. Since D is non-negative definite there exists an $n \times n$ matrix B such that $BB^T = D$. Then $B\eta$ is an n -dimensional vector of Gaussian random variables whose i and j components have as their covariance the (i, j) element of D .

CSPAM uses this technique to generate sample values of η_1^2 , $i = 1, \dots, n$. For the η_1^2 , D is a matrix with $\sigma_4^2 C(r_{ij})$ in the (i, j) position.

CSPAM uses the Cholesky algorithm to compute the matrix B such that $BB^T = D$. This is discussed in reference [c].

The range correlation function. A required input to CSPAM is the function $C(r)$ which gives the correlation in ambient noise received at two sensors

separated by a distance r . In principle any correlation function C can be used whether it is derived from data or a mathematical model such as in reference [c]. The current version of CSPAM, however, assumes the $C(r)$ is of the form $\exp(-\beta r)$. The user inputs a value of the range R^* at which he feels correlation in ambient noise is equal to .5. The program then computes $\beta = (\ln 2)/R^*$.

There are several reasons for using this simple parametric form at this time. The main one is that CSPAM is intended as a research tool which will enable us to decide on optimal patterns and their spacings and these will depend mainly on the rate of decrease of the function C . Having R^* as an input gives us a convenient way to vary this rate of decrease while holding other tactical variables fixed.

A related reason is that if C were to be estimated via the technique of reference [c] which depends on the propagation loss curve, it has been our experience that the shape of C is extremely sensitive to the fairly minor oscillations of N_W . In most tactical problems, however, we do not know N_W well enough to predict all of its oscillations and minor wiggles so that our conclusions may be based on spurious effects.

Eventually a technique such as in reference [c] may be used to characterize the C that pertains to a certain type of environment by averaging the results over several representative propagation losses for that environment but for now we recommend using the exponential correlation function to study the effects of variation in R^* .

Sample Results

Nine sample runs were made, six with a 5-6-5 distributed field and three with a BRUSHTAC. In each case all inputs are fixed except figure of merit and R^* . The fixed inputs are shown in Table 1. Figures 1 to 9 show the resulting cdp functions and Table 2 summarizes the total cdp results. These runs can be used to compare results with SPAM to verify that the two programs are giving compatible answers.

We note from Table 2 that the results as a function of R^* do not vary spectacularly and that this is a result of the relatively narrow (.375, .625) correlation window mentioned earlier. If the values $\sigma_1 = \sigma_2 = \sigma_3 = \sigma_4 = 4$ db, $\rho = .5$, that were used are valid, one begins to suspect, pending more extensive runs, that the effects of range dependent ambient noise correlation are minor. However, these input values must be subjected to scrutiny.

TABLE 1

Fixed Inputs to Nine Sample Runs

ENTER FREQUENCY INDEX (1, 2 OR 3): 2
ENTER SOURCE-RECEIVER GEOMETRY (1=D-I, 2=S-S, 3=I-S) : 1
ENTER .5 CORRELATION RANGE (MILES): 100
ENTER THE FIGURE OF MERIT: 74
ENTER YOUR PATTERN TYPE. THE CHOICES ARE:
 DF44 IF56 IF68 BTAC
 CIRC ARC SPEC
ENTER PATTERN TYPE: IF56
ENTER NUMBER OF BUOYS MONITORED: 16
ENTER MONITORING TIME (MINUTES): 180
ENTER THE TRUE PATTERN BEARING: 90
SPECIFY PATTERN SPACING AS FRACTION OF C2? (Y OR N): N
ENTER THE PATTERN SPACING (MILES): 18
ENTER E/B TO SPECIFY AN ELLIPSE/BEARING BOX: E
ENTER SEMI-MAJOR AXIS LENGTH: 25
ENTER SEMI-MINOR AXIS LENGTH: 15
ENTER TRUE BEARING, RANGE FROM SPA TO PATTERN CENTER: .0,0
ENTER THE TRUE BEARING OF THE TPA: 90
ENTER ON-STATION TIME IN HOURS: 3
ENTER A/C GROUND SPEED IN KNOTS: 250
ENTER THE TIME LATE IN HOURS: 0
SPECIFY TARGET MOTION CATEGORIES (Y OR N): N
ENTER THE TARGET COURSE: 0
ENTER THE COURSE STANDARD DEVIATION: -180
ENTER THE LOWER SOA LIMIT: 3
ENTER THE UPPER SOA LIMIT: 5
OUTPUT BUOY COORDINATES (Y OR N): N
ENTER A COMMENT TO IDENTIFY YOUR RUN:
ENTER THE NUMBER OF REPETITIONS: 100
ENTER THE RF RANGE: 80
PLOT PROLOSS CURVE (Y OR N): N
ENTER RANDOM NUMBER SEED: ".55555
ENTER SONAR EQ. STD. DEV. (1=6 DB, 2=8 DB, 3=10 DB, 4=12 DB): 2

TABLE 2

Summary of cdp Results

R* =	5 nm	18nm	100nm
DF 5-6-5, FOM=74 db	.86	.85	.79
DF 5-6-5, FOM=70 db	.67	.64	.56
BRUSHTAC, FOM=70 db	.74	.70	.66

FIGURE 1

CDP Results for Case 1

5-6-5 Distributed Field

FOM = 74 R_{50} = 5nm

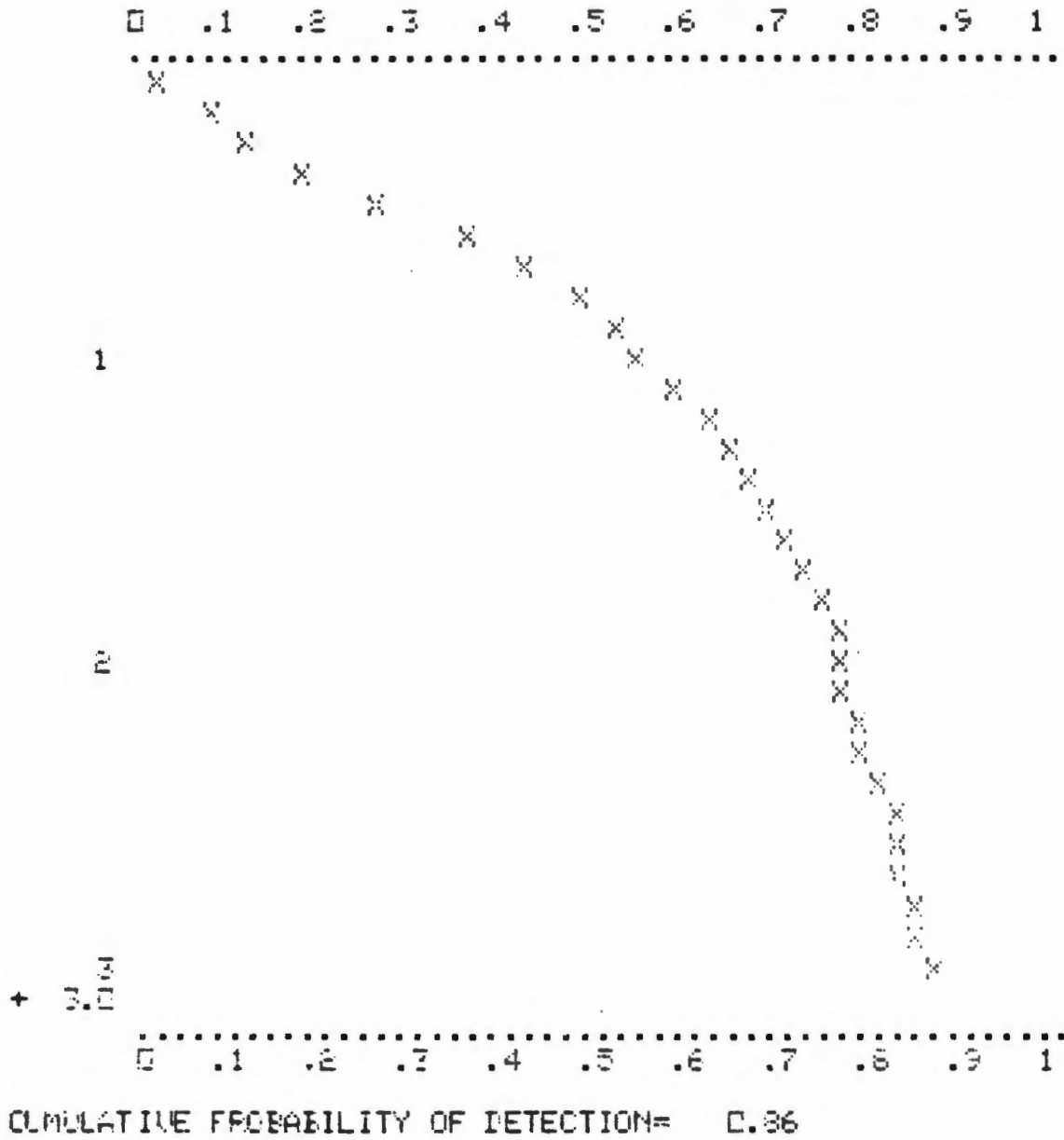


FIGURE 2

CDP Results for Case 2

5-6-5 Distributed Field

FOM = 74 R_{50} = 18nm

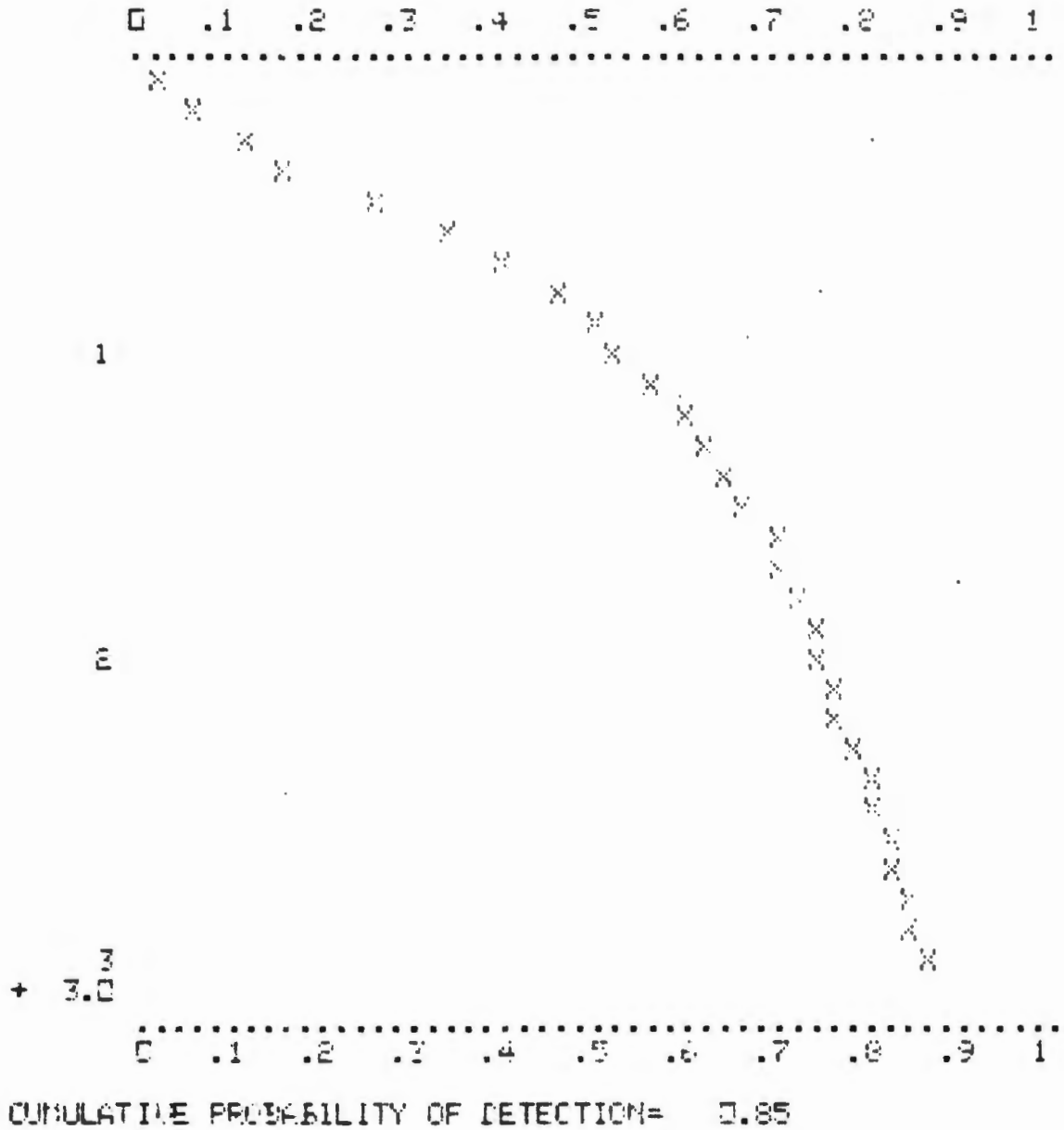


FIGURE 3

CDP Results for Case 3

5-6-5 Distributed Field

FOM = 74 R_{50} = 100 nm

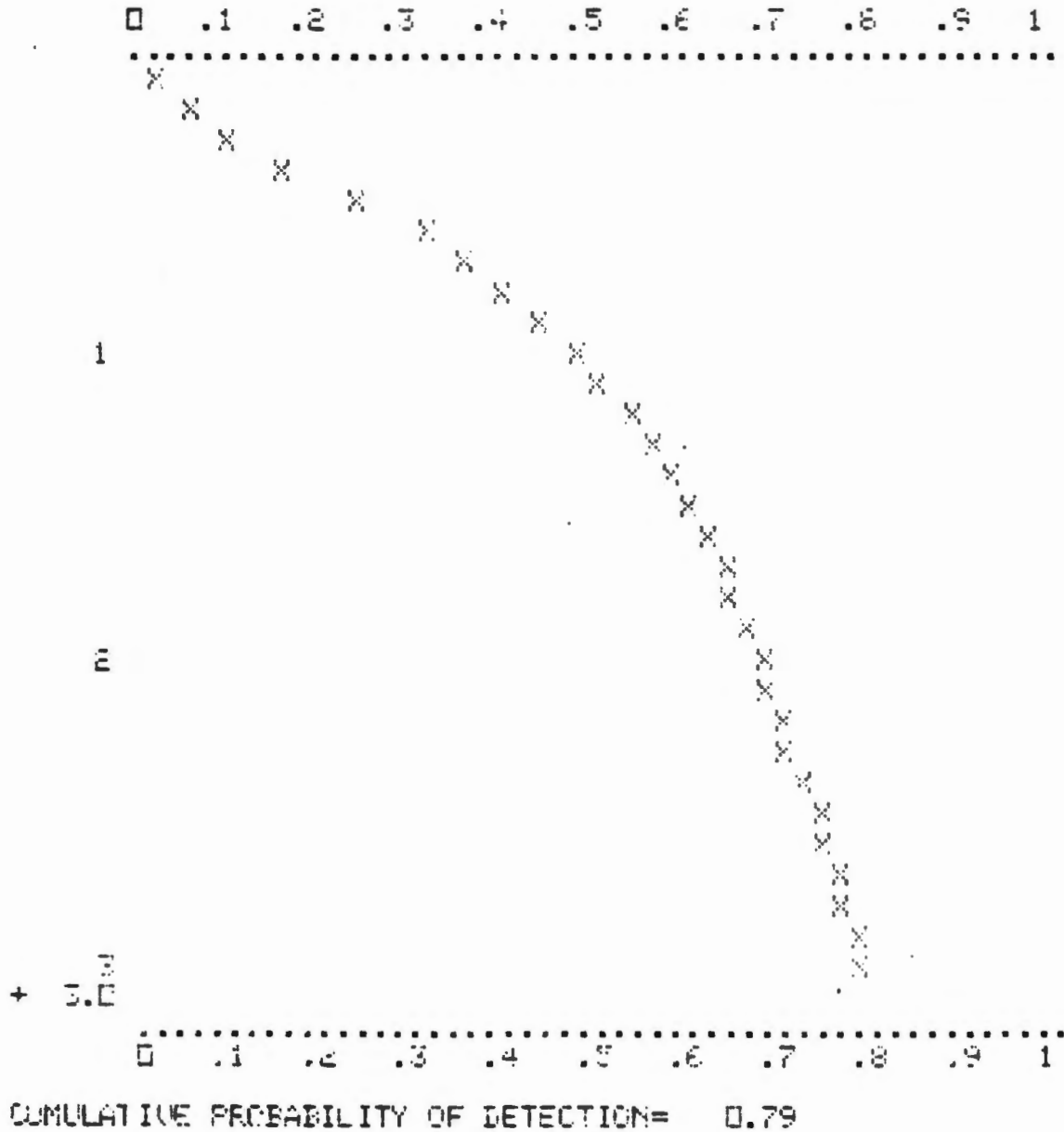


FIGURE 4

CDP Results for Case 4

5-6-5 Distributed Field

FOM = 70 R_{50} = 5nm

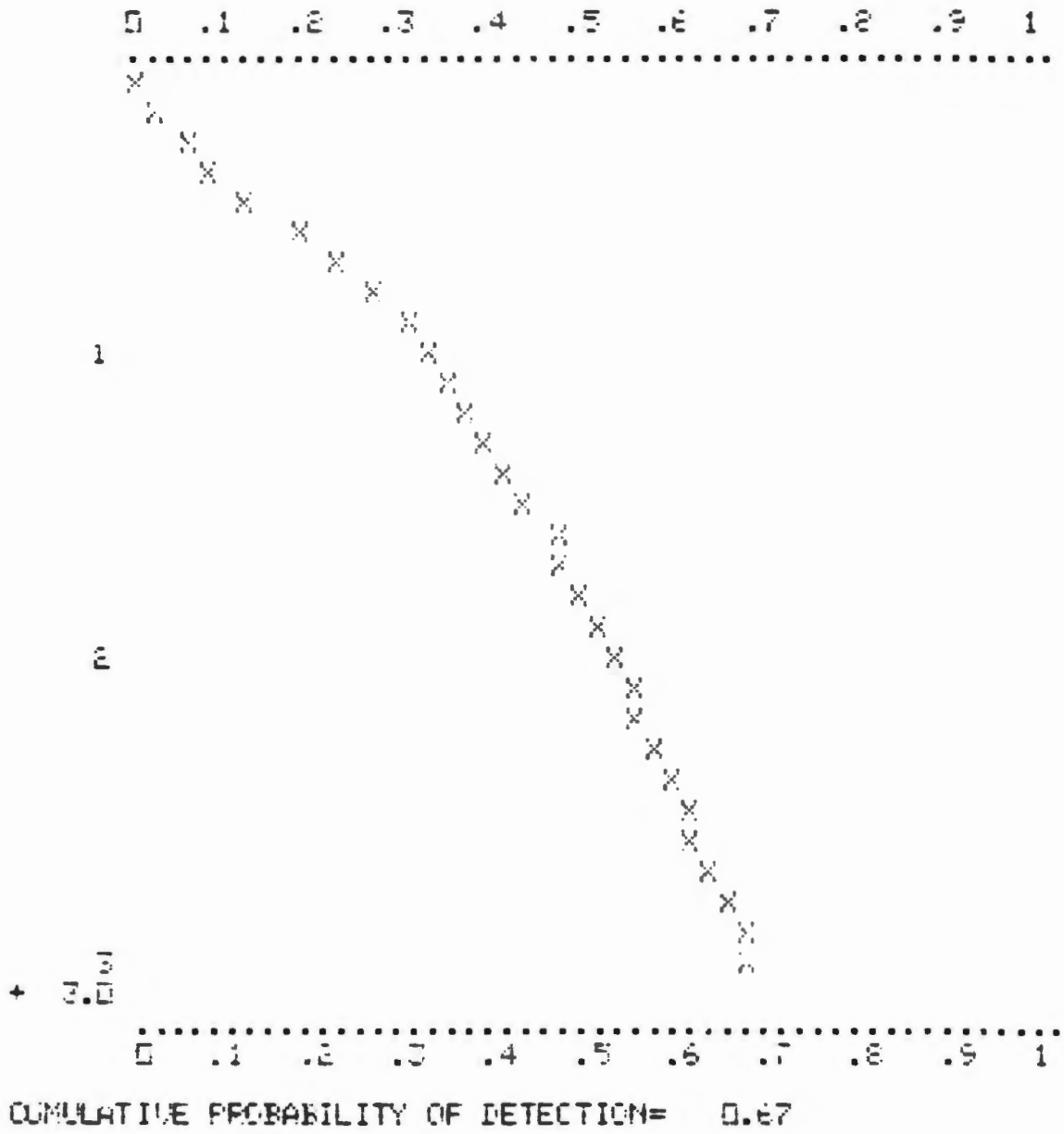


FIGURE 5

CDP Results for Case 5

5-6-5 Distributed Field

FOM = 70 R_{50} = 18nm

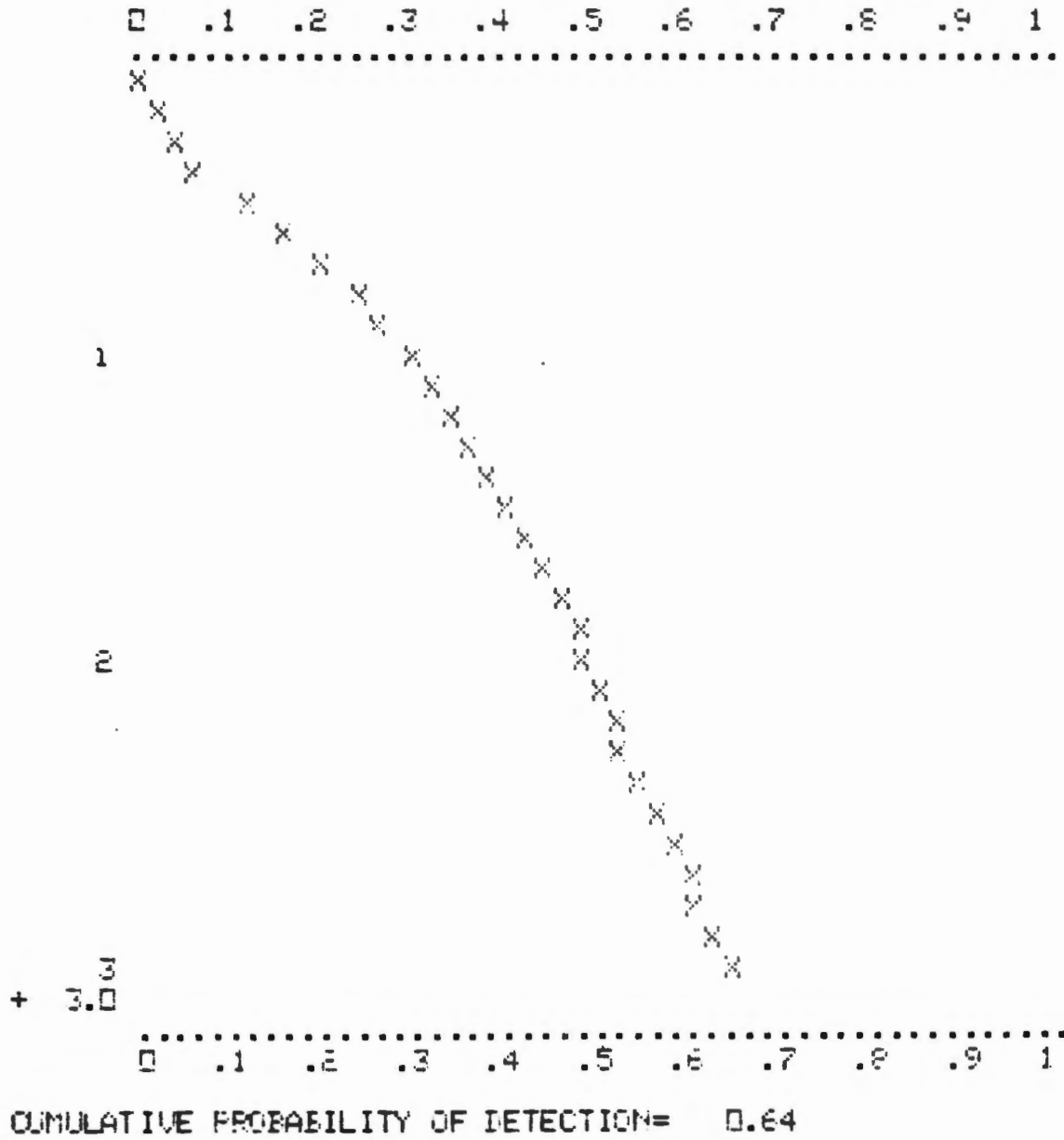


FIGURE 6

CDP Results for Case 6

5-6-5 Distributed Field

FOM = 70 R_{50} = 100nm

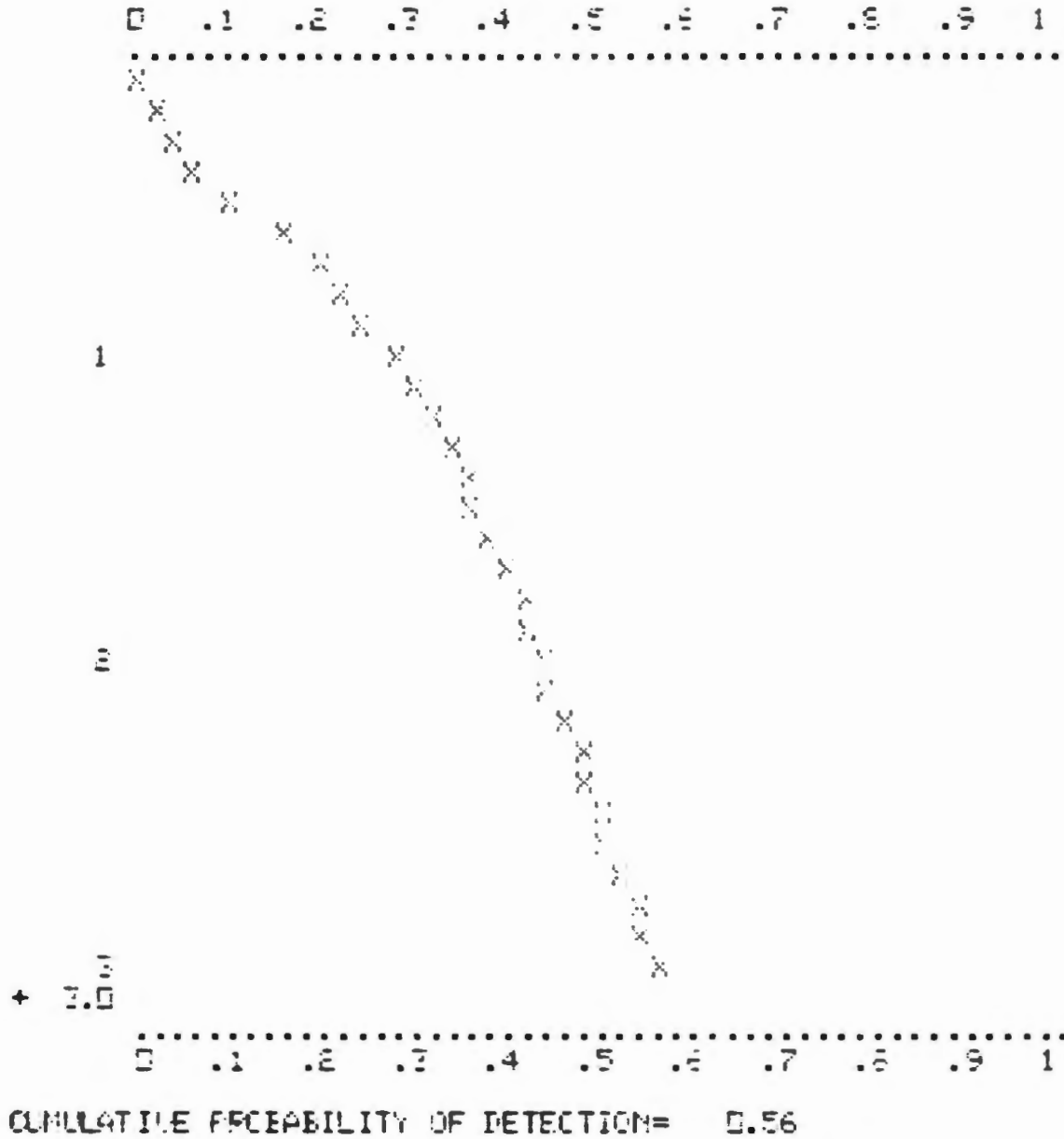


FIGURE 7

CDP Results for Case 7

BRUSHTAC

FOM = 70 R_{50} = 5nm

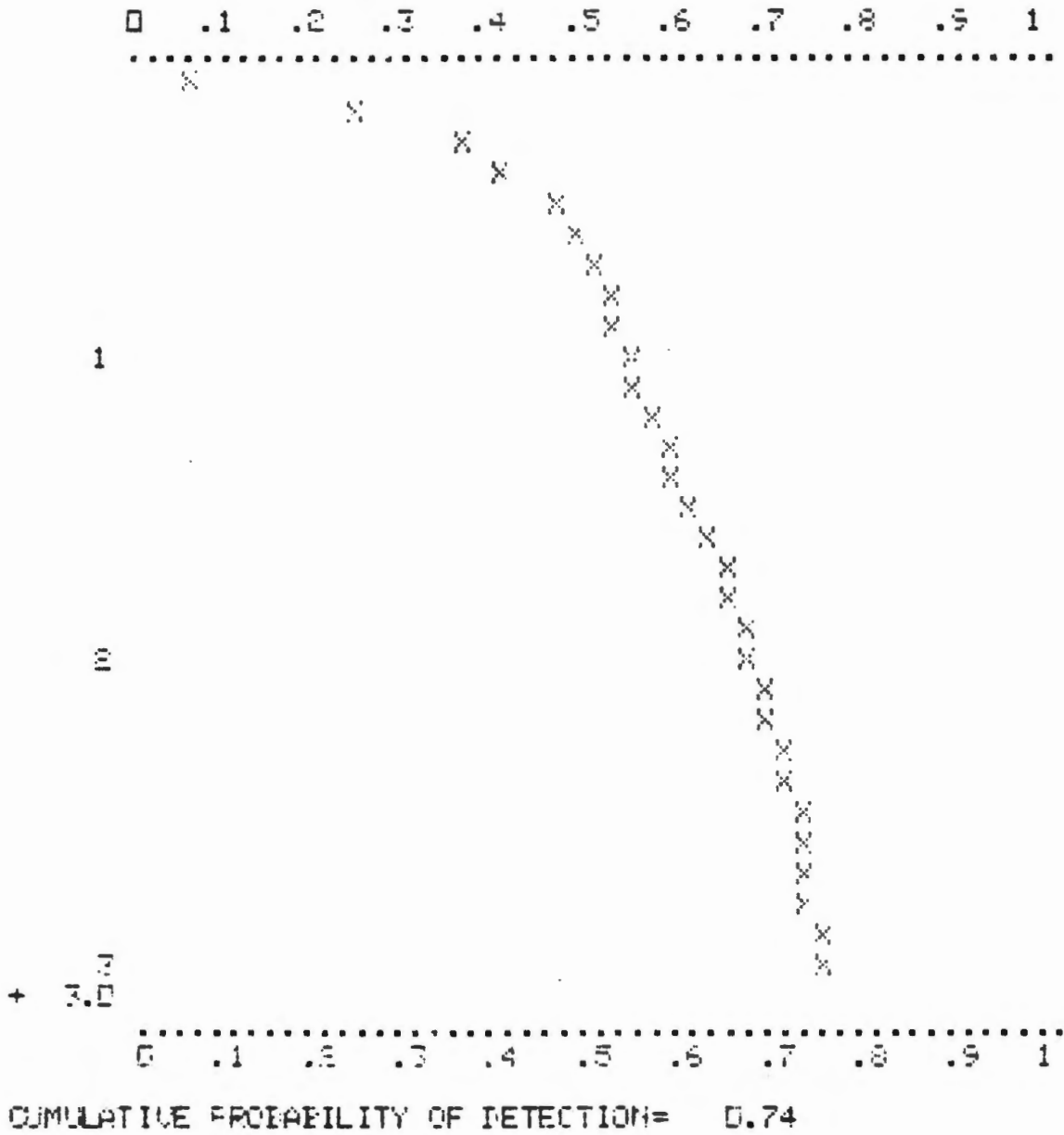


FIGURE 8

CDP Results for Case 8

BRUSHTAC

FOM = 70 R_{50} = 18nm

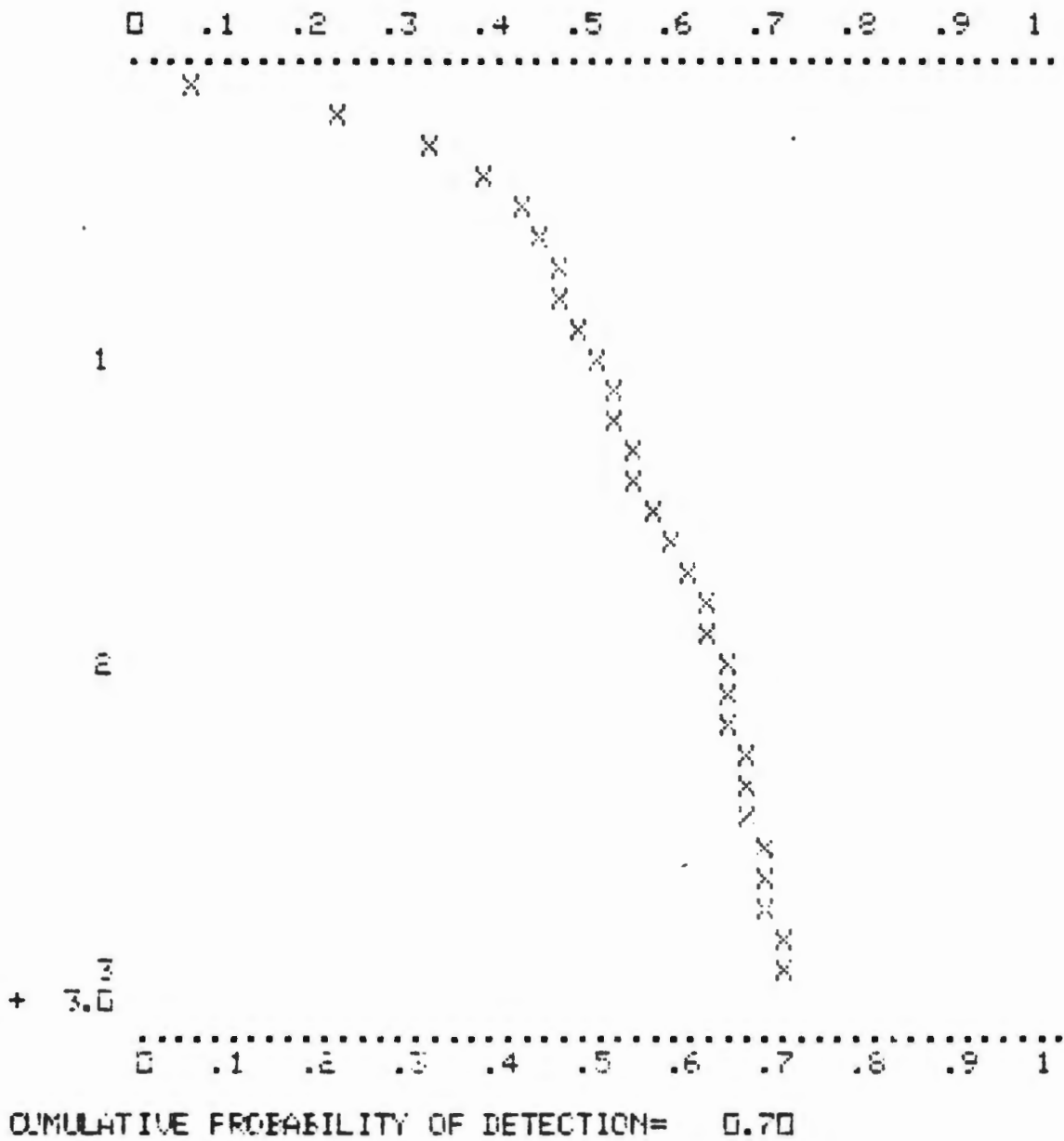
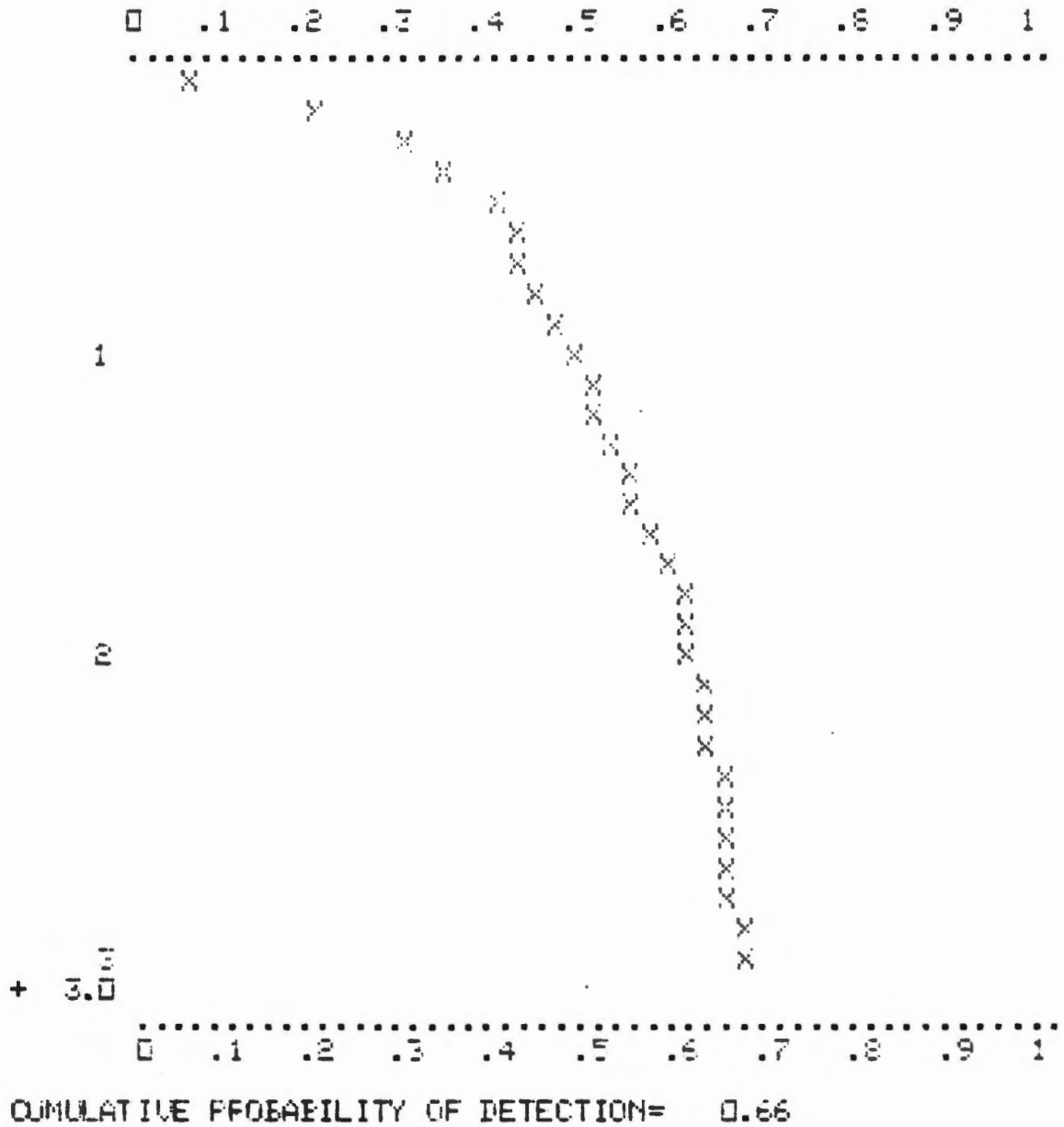


FIGURE 9

CDP Results for Case 9

BRUSHTAC

FOM = 70 R_{50} = 100nm



Programmer's Guide

The variables σ_1 , σ_2 , σ_3 , σ_4 , and ρ are set at the top of the program. They are called, respectively, SIG1, SIG2, SIG3, SIG4, and ALPHA. Currently, the σ_i 's are set equal to $\sigma/2$ where σ is an input standard deviation, and ρ is set equal to .5. As mentioned above we may want to try other values of these variables in which case they may be changed directly in the code or a new set of enter statements may be programmed.

The correlation function is used on only one line in the program, in the CHOLES subroutine at the point where ETA(I, J) is defined. Thus an arbitrary correlation function could be accommodated easily by writing a routine to input it manually and changing this line in CHOLES.

In SPAM idp's are computed using a table that has range as its input. This is not possible in CSPAM because idp depends not only on range but on the conditioning values of $\bar{\xi}$ and η_1^2 . Thus idp, called BW(IBUOY, INDEX), is computed as a function of $FOM + \bar{\xi} + \eta_1^2 - N_W$ using the array TABLE defined at the top of the program. Note that TABLE evaluates the cumulative Gaussian distribution raised to the t_1/t_0 power. This saves doing an exponentiation in the innermost loop.


Bernard J. McCabe

BJM/dd

References

- [a] Search Pattern Assessment Model (SPAM), COMPATWINGSPAC report by G. A. Marin, April 14, 1976, Unclassified.
- [b] ASW Detection Simulation and the Cumulative Time Window Model, forthcoming CNA memorandum, by G. A. Marin, Unclassified.
- [c] Ambient Noise Effects in the Modeling of Detections by a Field of Sensors, Daniel H. Wagner, Associates report by B. J. McCabe, November 5, 1976, Unclassified.

APPENDIX

LISTING OF CSPAM

C*****

C*
C* PROGRAM XSPAM
C* IMPROVED VERSION OF SPAM

C* BJM/BMM/JSR JUNE, 1977

C* DANIEL H. WAGNER, ASSOCIATES
C* PAOLI, PA

C*****

DIMENSION BW(32,100),LM(32),DELTA(32),BS(8),
* ETA1(32,32),ETA2(32,32),PROB(220),PROPLO(220),
* RAN1(32),RAN2(32),JF(8),KG(8),
* BR1(32),BR2(32),PREV(32),TABLE(321),PLMAP(220),
* NCT(100),ICTRY(100),CTMAX(100),PCAT(100),THRSH(100),
* COMENT(15),BX(32),BY(32),BXI(32),BYI(32),DISTAB(32)
NAMELIST/INFO/ISEED,NREPS,IFREQ,IGEO,RF,OSTH,NOPROP,T0,T1,T2,IGO,
* CORR50,BETA,DIMX,DIMY,COURSE,SPD,SDDIMX,SDDIMY,SDCRSE,SDSPD,
* TIMLAT,FOM,NPAT,NCRS,NSOA,SDEV,NB,NM,ACFTGS,TIMMON,PATSPC
DATA YES/3HY /

C
C
C

CALL WPRNOS

READ (10,5002) COMENT
READ (10,5003) ISEED,NREPS,IFREQ,IGEO,RF,OSTH,NOPROP,T0,T1,T2,
* IGO,BETA,CORR50
READ (10,5004) DIMX,DIMY,COURSE,SPD,SDDIMX,SDDIMY,SDCRSE,SDSPD,
* TIMLAT,FOM,NPAT,SDEV
READ (10,5005) NCRS,CRSINT,CRSWND,NSOA,SOAINT,SOAWND
IF (NCAT.EQ.0) GO TO 25
READ (10,5006) (PCAT(I),I=1,NCAT)
READ (10,5006) (THRSH(I),I=1,NCAT)
25 READ (10,5006)
READ (10,5007) NB,NM,ACFTGS,TIMMON,PATSPC
READ (10,5008) (BXI(I),I=1,NB)
READ (10,5008) (BYI(I),I=1,NB)
DO 28 I=1,NB
BX(I)=BXI(I)
BY(I)=BYI(I)
28 CONTINUE

C
C
C
C
C

WRITE (6,5000) (COMENT(I),I=1,15)

LIST BUOY POSITIONS

30 WRITE (6,5019)
DO 40 I=1,NB
40 WRITE (6,5020) I,BX(I),BY(I)
WRITE (6,5001)

C
C
C
C

SET-UP PROGRAM CONSTANTS

DO 50 I=1,220

```
M=34359738367
CALL RANSET(M,ISEED)
WRITE (6,INI
```

C

```
MAXTIM=T2/T1
IF (IGO.NE.7) GO TO 52
DISTAB(1)=0.
DO 51 I=2,NB
  DISTAB(I)=DISTAB(I-1)+SQRT((BY(I)-BY(I-1))**2 +
  * (BX(I)-BX(I-1))**2)
```

```
51 CONTINUE
  DMAX=DISTAB(NB)
  GO TO 53
52 DMAX=(NB-1)*PATSPC
53 TRAT=T1/T0
  NCAT = NCRS * NSOA
  VAR=SDEV/2.
  ISTART=TIMLAT*60.+0.5
  ISTOP=(TIMLAT+OSTH)*60.+0.5
  ISTEP=T1*60.+0.5
  ALPHA=0.5
  MAX=0
  PMAX=0.
```

C

```
DO 55 I = 1,100
  NCT(I) = 0
  ICTRY(I) = 0
  CTMAX(I) = 0.
```

55

```
CONTINUE
```

C

C

C

C

```
SET-UP TABLE CONTAINING (1-NORMAL INTEGRAL) VALUES
WITH LIMITS OF [-15,5]
```

C

```
DO 60 I=1,321
```

```
60 TABLE(I)=ERFC(((I-1.)/16.)-15.):**TRAT
```

C

C

C

C

```
INPUT PROPLOSS DATA
```

C

```
M=0
```

```
100 READ (9,3000,END=110) (IX,JF(I),KG(I),BS(I),I=1,8)
```

```
DO 105 I=1,8
```

```
IF (JF(I).NE.IFREQ.OR.KG(I).NE.IGEO) GO TO 105
```

```
M=M+1
```

```
IF (M.GT.220) GO TO 110
```

```
PROPLO(M)=BS(I)
```

```
105 CONTINUE
```

```
GO TO 100
```

```
110 IF (NOPROP.EQ.0) GO TO 115
```

C

C

C

C

```
OUTPUT PROPLOSS CURVE
```

```
WRITE (6,5022)
```

```
PMAX = 0.0
```

```
DO 113 I = 1,220
```

```
IF (PROPLO(I) .GT. PMAX) PMAX = PROPLO(I)
```

113

```
CONTINUE
```

```
DO 114 I = 1,220
```

```
PLMAP(I) = PROPLO(I) / PMAX
```

114

```
CONTINUE
```

```
WRITE (6,5023) PMAX
```

```
CALL WSHOW(PLMAP,220,4)
```


COMPUTE CORRELATION QUANTITIES - -
PSIC, BR1 AND BR2.

```
DO 150 I=1,NB
  BR1(I)=0.
  BR2(I)=0.
  RAN1(I)=ANRMRN(0.)*VAR
  RAN2(I)=ANRMRN(0.)*VAR
  PREV(I)=0.
  DO 150 J=1,MAXTIM
150  BW(I,J)=1.
  DO 170 I = 1, NB
    DO 160 J = 1, NB
      BR1(I) = BR1(I) + ETA1(I,J) * RAN1(J)
      BR2(I) = BR2(I) + ETA2(I,J) * RAN2(J)
160  CONTINUE
  DELTA(I) = FOM + BR1(I) + BR2(I) + PSIC
170  CONTINUE
```

RESET TIME COUNTERS - -
INDEX, JTIM AND TIMMON.

```
INDEX = 0
JTIM = TIMMON
MON = 0
```

FOR THIS REP, SELECT RANDOM DETECTION PROBABILITY USING
THRESHOLD FOR THE SELECTED CATEGORY.

```
PTRN = URAND(0.0)
IF (NCRS.GT.0) PTRN=URAND(0.0)*(1.-THRSH(ICAT))+THRSH(ICAT)
```

BEGIN THE TIME LOOP

```
DO 400 ITIM=ISTART,ISTOP,ISTEP
```

COMPUTE PRESENT BUOY CONFIGURATION UP UNTIL
RELATIVE ELAPSED TIME, JDEX.

```
JDEX=(ITIM-ISTART)/ISTEP+1
ITMIN=JDEX
IF (MAXTIM .LT. JDEX) ITMIN = MAXTIM
TIME=JDEX*T1
```

```
CALL MONITR(BX,BY,LM,NM,NB,ISTEP,JTIM,TIMMON,TIME,ACFTGS,
* PATSPC,RF,DMAX,MON,IGO,DISTAB)
```

COMPUTE TARGET LOCATION

```
TX=RDIMX+ITIM*DX
TY=RDIMY+ITIM*DY
PROD=1.
```

UPDATE TIME WINDOW INDEX

```
INDEX=INDEX+1
```

```

C      BEGIN BUOY LOOP
C
C      DO 300 IBUOY=1,NB
C
C      IF BUOY IS OUT OF RF RANGE OF AIRCRAFT,
C      OR NOT PRESENTLY BEING MONITORED,
C      USE PREVIOUS DETECTION PROBABILITY FOR THIS BUOY.
C
C      PR=PREV(IBUOY)
C      IF (LM(IBUOY).NE.0) GO TO 180
C      BW(IBUOY,INDEX) = 1.0
C      GO TO 300
C
C      CONVERT RANGE FROM MILES TO KILOYARDS FOR
C      PROPLOSS TABLE LOOK-UP.
C
180      RANGE=SQRT((TX-BX(IBUOY))*(TX-BX(IBUOY))+
*          (TY-BY(IBUOY))*(TY-BY(IBUOY)))
C      IRANGE = RANGE + RANGE
C      IF (IRANGE.GT.220) IRANGE=220
C
C      COMPUTE NEW TIME WINDOW ELEMENT
C
C      DEL=(DELTA(IBUOY)-PROPLO(IRANGE))/VAR
C      IDEL=(DEL+15.)*16.+1.5
C      IF (IDEL.LT.1) IDEL=1
C      IF (IDEL.GT.321) IDEL=321
C      BW(IBUOY,INDEX)=TABLE(IDEL)
C
C      COMPUTE PRODUCT OVER ENTIRE TIME WINDOW
C
C      PR=1.
C      DO 200 I=1,ITMIN
200      PR=PR*BW(IBUOY,I)
C      PR=1.-PR
C      IF (PREV(IBUOY).GT.PR) PR = PREV(IBUOY)
C      PREV(IBUOY)=PR
C
C      300      PROD=PROD*(1.-PR)
C      PROD=1.-PROD
C      IF (NCRS .EQ. 0) GO TO 400
C
C      COUNT REPS WITH SUCCESSFUL DETECTIONS
C
C      CTMAX(ICAT) = AMAX1(CTMAX(ICAT),PROD)
400      PROB(JDEX)=PROB(JDEX)+PROD
C      IF (PROD .LT. PTRN) NCT(ICAT) = NCT(ICAT) + 1
500      CONTINUE
C
C      END OF LOOPS
C      RENORMALIZE PROB OVER TIME
C
C      DO 600 I=1,JDEX
C      PROB(I)=PROB(I)/NREPS
C      IF (PROB(I).LE.PMAX) GO TO 600
C      MAX=I

```

PRODUCE PLOT ; DETECTION PROBABILITY VS. TIME

CALL WSHOW(PROB,MAX,20)
WRITE (6,5021) PMAX

OUTPUT THE CATEGORY RESULTS

IF (NCRS .EQ. 0) GO TO 699
WRITE (6,5030)
IWR = 0

CATEGORY DESCRIPTIONS

HD2 = CRSINT - ABS(CRSWND)
DO 601 IROW = 1,NCRS
HD1 = HD2
HD2 = HD1 + 2.*ABS(CRSWND)
SOA2 = SOAINT - ABS(SOAWND)
DO 601 ICOL = 1,NSOA
IWR = IWR + 1
SOA1 = SOA2
SOA2 = SOA1 + 2.*ABS(SOAWND)
WRITE (6,5031) IWR, HD1, HD2, SOA1, SOA2

601 CONTINUE
NCAT = NCRS * NSOA

RENORMALIZE CATEGORY DETECTION PROBABILITIES

PSTDNM = 0.
DO 602 IWR = 1,NCAT
RMISS = FLOAT(NCT(IWR))
RTRY = FLOAT(ICTRY(IWR))
IF (RTRY .EQ. 0.) GO TO 602
PSTDNM = PSTDNM + (RMISS/RTRY)*PCAT(IWR)

602 CONTINUE

COMPUTE NEW THRESHOLDS AND POSTERIOR DISTRIBUTION
FOR EACH CATEGORY.

WRITE (6,5032)

DO 610 IWR = 1,NCAT
RMISS = FLOAT(NCT(IWR))
RTRY = FLOAT(ICTRY(IWR))
PSTR = 0.
IF(RMISS .EQ. 0.) GO TO 608
CTMAX(IWR) = CTMAX(IWR) / RMISS
CTMAX(IWR) = CTMAX(IWR)*(1.-THRSH(IWR)) + THRSH(IWR)
IF (RTRY .EQ. 0.) GO TO 608
PSTR = ((RMISS/RTRY)*PCAT(IWR))/PSTDNM

608 WRITE (6,5033) IWR,PCAT(IWR),NCT(IWR),ICTRY(IWR),PSTR
610 CONTINUE

WRITE (6,5034) (THRSH(I), I=1,NCAT)
WRITE (6,5035) (CTMAX(I), I=1,NCAT)

INPUT PATTERN MODIFICATION PARAMETERS

```

699 WRITE (6,5001)
    WRITE (6,5010)
    READ (5,5025) ANSWER
    IF (ANSWER .NE. YES ) STOP
700 WRITE (6,5011)
    READ (5,5026,ERR=700) CK
        DO 821 I = 1,NB
            BX(I) = BXI(I) * CK
            BY(I) = BYI(I) * CK
821 CONTINUE
    PATSPC = PATSPC * CK
701 WRITE (6,5012)
    READ (5,5026,ERR=701) ROT
702 WRITE (6,5013)
    READ (5,5027,ERR=702) TRANX, TRANY
    CALL ROTATE (NB, BX, BY, ROT, TRANX, TRANY)
    WRITE (6,5028)
    GO TO 30

```

C
C

```

3000 FORMAT (8(I3,2I1,F5.1))
5000 FORMAT (//20A2//)
5001 FORMAT (//)
5002 FORMAT (1X,15A4)
5003 FORMAT ('X',2I9,2I1,2F8.1,I2,3F8.2,I2,2F10.6)
5004 FORMAT (10F7.1,2I5)
5005 FORMAT (2(I5,2F10.5))
5006 FORMAT (16F5.4)
5007 FORMAT (2I3,2F7.1,F6.2)
5008 FORMAT (16F5.1)
5010 FORMAT (' MODIFY PATTERN AND RE-RUN (Y OR N): ')
5011 FORMAT (' SPACING MULTIPLICATION FACTOR: ')
5012 FORMAT (' PATTERN ROTATION (DEG.): ')
5013 FORMAT (' PATTERN TRANSLATION IN MILES (X,Y): ')
5019 FORMAT (//' BUOY POSITIONS:')
5020 FORMAT (' BUOY',I3,2F10.2)
5021 FORMAT (/' CUMULATIVE PROBABILITY OF DETECTION=',F7.2)
5022 FORMAT (/' PROBABILITY OF DETECTION VS. DISTANCE'//)
5023 FORMAT (' MAXIMUM CORRESPONDS TO PROPLOSS OF',F8.2)
5025 FORMAT (A1)
5026 FORMAT (F10.0)
5027 FORMAT (2F10.0)
5028 FORMAT (//' RE-RUN BEGINS.'//)
5030 FORMAT (//30X,' DESCRIPTION OF CATEGORIES'/1X,'CATEGORY',
1 10X,'HEADING INTERVAL',10X,'SOA INTERVAL')
5031 FORMAT (2X,I4,15X,F5.0,' - ',F5.0,11X,F5.0,' - ',F5.0)
5032 FORMAT (1X,'CATEGORY',10X,'PRIOR',10X,'MISSES',10X,'TRIES',
1 10X,'POSTERIOR')
5033 FORMAT (2X,I4,11X,F7.5,10X,I5,10X,I5,11X,F7.5)
5034 FORMAT (10X,'OLD THRESHOLD VALUES = ',12F10.5)
5035 FORMAT (10X,'NEW THRESHOLD VALUES = ',12F10.5)
END

```

SUBROUTINE WPRNOS

C

```

DIMENSION ICD2(4),CD2(2),CD3(10),ICD3(2),ICD6(2),
1ICD6(2),BX(32),BY(32)
DIMENSION ICD4(2),CD4(4),PCAT(100)
DIMENSION COMENT(15),PNAME(7)
CALL OBEY('EQUATE 10 INPUT',4)
DATA PNAME/4HDF44,4HDF56,4HDF88,4HBTAC,4HCIRC,3HARC,4HSPEC/
DATA YES/1HY/,BEARNG/1HB/
80 CONTINUE
WRITE(6,300)
300 FORMAT(' ENTER THE FREQUENCY INDEX FOR YOUR PROPLOSS. ')
READ(5,*,ERR=80) ICD2(3)
81 CONTINUE
WRITE(6,301)
301 FORMAT(' ENTER THE SOURCE-RECEIVER GEOMETRY INDEX. ')
READ(5,*,ERR=81) ICD2(4)
8133 CONTINUE
WRITE(6,3333)
3333 FORMAT(' ENTER .5 CORRELATION RANGE (MILES). ')
READ(5,*,ERR=8133) CORR50
BETA=ALOG(2.)/CORR50
82 CONTINUE
WRITE(6,302)
302 FORMAT(' ENTER THE FIGURE OF MERIT. ')
READ(5,*,ERR=82) CD3(10)
83 CONTINUE
WRITE(6,303)
303 FORMAT(' ENTER YOUR PATTERN TYPE. YOU HAVE',
1' THE FOLLOWING CHOICES:')
WRITE(6,304) (PNAME(I),I=1,7)
READ(5,200,ERR=83) PATYPE
304 FORMAT(7(20X,A4/))
WRITE(6,888) PATYPE
888 FORMAT(' PATYPE - ',A4)
DO 195 IGO = 1,7
IF (PNAME(IGO).EQ.PATYPE) GO TO 307
195 CONTINUE
WRITE(6,210)
210 FORMAT(' INVALID PATTERN TYPE. ')
GO TO 83
307 CONTINUE
NB=16
ICD6(1)=16
ICD6(2)=16
IF(PATYPE.EQ.PNAME(5))GO TO 126
IF(PATYPE.NE.PNAME(7)) GO TO 60
97 CONTINUE
WRITE(6,305)
305 FORMAT(' ENTER THE NUMBER OF BUOYS TO BE DROPPED',
1' 32 IS THE MAXIMUM ALLOWABLE. ')
READ(5,*,ERR=97) ICD6(1)
NB=ICD6(1)
ICD6(2)=ICD6(1)
DO 151 IBUOY=1,NB
130 CONTINUE
WRITE(6,150) IBUOY
150 FORMAT(' ENTER X,Y COORDINATES OF BUOY',I4)

```

```

151 CONTINUE
    GO TO 61
60 CONTINUE
    ICD6(1)=16
    NB=16
    ICD6(2)=16
103 FORMAT(' ENTER THE TRUE PATTERN BEARING      ')
104 FORMAT(' ENTER PATTERN SPACING              ')
106 FORMAT(' ENTER PATTERN RADIUS.              ')
107 FORMAT(' DO YOU WANT TO SPECIFY PATTERN SPACING AS A ',
1 'FRACTION OF CZ?')
112 FORMAT(' ENTER THE CZ WIDTH.              ')
108 FORMAT(' ENTER THE FRACTION OF CZ.      X.X  ')
111 FORMAT(' ENTER THE CZ RANGE.              ')
200 FORMAT(A4)
    IWRFLG=-1
    ICZFLG=0
    DO 101 ITY=1,3
    IF(PATYPE.EQ.PNAME(ITY)) IWRFLG=1
101 CONTINUE
70 CONTINUE
    WRITE(6,103)
    READ(5,*,ERR=70)PBEAR
    WRITE(6,107)
    READ(5,201)ANSWER
201 FORMAT(A1)
    IF(ANSWER.EQ.YES) ICZFLG=IWRFLG
    IF(ICZFLG)50,20,10
121 CONTINUE
50 WRITE(6,112)
    READ(5,*,ERR=121)CZR
122 CONTINUE
    WRITE(6,108)
    READ(5,*,ERR=122)FRAC
    PATSPC=FRAC*CZR
    GO TO 30
123 CONTINUE
10 WRITE(6,111)
    READ(5,*,ERR=123)CZR
124 CONTINUE
    WRITE(6,108)
    READ(5,*,ERR=124)FRAC
    PATSPC=FRAC*CZR
    GO TO 30
125 CONTINUE
20 WRITE(6,104)
    READ(5,*,ERR=125)PATSPC
30 CONTINUE
    IF(PATYPE.NE.PNAME(5).AND.PATYPE.NE.PNAME(6))GO TO 61
126 CONTINUE
    WRITE(6,106)
    READ(5,*,ERR=126)RADIUS
    PATSPC=.3901806*RADIUS
61 CONTINUE
    WRITE(6,306)
306 FORMAT(' ENTER E/B TO SPECIFY AN ELLIPSE/BEARING BOX. ')
    READ(5,201,ERR=61)TYPE
    IF(TYPE.EQ.BEARNG)GO TO 308
84 CONTINUE
    WRITE(6,309)
309 FORMAT(' ENTER SEMI-MAJOR AXIS LENGTH. ')
    READ(5,*,ERR=84)SMAT,

```

```

310 FORMAT(' ENTER SEMI-MINOR AXIS LENGTH. ')
    READ(5,*,ERR=85)SMIL
    CD3(5)=SMAL/2.0
    CD3(6)=SMIL/2.0
    GO TO 311
86 CONTINUE
308 WRITE(6,312)
312 FORMAT(' ENTER BEARING BOX LENGTH. ')
    READ(5,*,ERR=86)SMAL
    CD3(5)=-SMAL/2.0
87 CONTINUE
    WRITE(6,313)
313 FORMAT(' ENTER BEARING BOX HALF WIDTH. ')
    READ(5,*,ERR=87)CD3(6)
    CD3(6)=CD3(6)/2.0
311 CONTINUE
    IF(PATYPE.EQ.PNAME(7))GO TO 344
    IF(PATYPE.NE.PNAME(5).AND.PATYPE.NE.PNAME(6))GO TO 342
344 BPAT=0.
    RPAT=0.
    TBEAR=90.
    GO TO 89
342 WRITE(6,314)
314 FORMAT(' ENTER TRUE BEARING,RANGE FROM SPA CENTER TO PATTERN',
1 ' CENTER. ')
    READ(5,*,ERR=311)BPAT,RPAT
    BPAT=3.1415927*BPAT/180.
    PATX=RPAT*SIN(BPAT)
    PATY=RPAT*COS(BPAT)
88 CONTINUE
    WRITE(6,315)
315 FORMAT(' ENTER THE TRUE BEARING OF THE SPA. ')
    READ(5,*,ERR=88)TBEAR
89 CONTINUE
    WRITE(6,316)
316 FORMAT(' ENTER ON-STATION TIME IN HOURS. ')
    READ(5,*,ERR=89)CD2(2)
90 CONTINUE
    WRITE(6,317)
317 FORMAT(' ENTER A/C GROUND SPEED IN KNOTS. ')
    READ(5,*,ERR=90)CD6(1)
91 CONTINUE
    WRITE(6,318)
318 FORMAT(' ENTER TIME LATE. ')
    READ(5,*,ERR=91)CD3(9)
92 CONTINUE
    WRITE(6,319)
319 FORMAT(' DO YOU WISH TO SPECIFY TARGET MOTION CATEGORIES? ')
    READ(5,201,ERR=92)ANSWER
    IF(ANSWER.NE.YES)GO TO 93
94 CONTINUE
    WRITE(6,321)
321 FORMAT(' ENTER THE NUMBER OF COURSE CATEGORIES',
1 ' (NO MORE THAN 10). ')
324 FORMAT(' ENTER THE NUMBER OF SOA CATEGORIES',
1 ' (NO MORE THAN 10). ')
    READ(5,*,ERR=94)ICD4(1)
95 CONTINUE
    WRITE(6,322)
322 FORMAT(' ENTER THE CENTER COURSE OF THE FIRST COURSE WINDOW. ')

```

```

96 CONTINUE
WRITE (6,323)
323 FORMAT(' ENTER THE HALF WIDTH OF THE COURSE WINDOWS.')
```

READ(5,*,ERR=96)CD4(2)

```

131 CONTINUE
WRITE (6,324)
READ(5,*,ERR=131)ICD4(2)
132 CONTINUE
WRITE (6,325)
325 FORMAT(' ENTER THE CENTER SOA OF THE FIRST SOA WINDOW.')
```

READ(5,*,ERR=132)CD4(3)

```

133 CONTINUE
WRITE (6,326)
326 FORMAT(' ENTER THE HALF WIDTH OF THE SOA WINDOWS.')
```

READ(5,*,ERR=133)CD4(4)

NCAT=ICD4(1)*ICD4(2)

WRITE(6,331)

```

331 FORMAT(20X,' DESCRIPTION OF CATEGORIES')
```

WRITE(6,332)

```

332 FORMAT(2X,' CATEGORY',10X,'HEADING-INTERVAL',13X,
1'SOA INTERVAL')
```

NCRS=ICD4(1)

NSOA=ICD4(2)

HD2=CD4(1)-CD4(2)

IWR=0

DO 330 IROW=1,NCRS

HD1=HD2

HD2=HD1+2.0*CD4(2)

SOA2=CD4(3)-CD4(4)

DO 431 ICOL=1,NSOA

IWR=IWR+1

SOA1=SOA2

SOA2=SOA1+2.0*CD4(4)

WRITE(6,432)IWR,HD1,HD2,SOA1,SOA2

```

432 FORMAT(4X,I4,15X,F5.0,' - ',F5.0,11X,F5.0,' - ',F5.0)
431 CONTINUE
330 CONTINUE
WRITE (6,328)
328 FORMAT(' ENTER THE CATEGORY PROBABILITIES. THEY',
1' SHOULD TOTAL 1.')
```

DO 329 I=1,NCAT

```

134 CONTINUE
WRITE (6,333)I
333 FORMAT(' CATEGORY ',I3)
READ(5,*,ERR=134) PCAT(I)
329 CONTINUE
GO TO 135
93 CONTINUE
CD3(3)=0.
CD3(7)=-180.
WRITE (6,334)
334 FORMAT(' ENTER THE LOWER SOA LIMIT.')
```

READ(5,*,ERR=93)SLOW

```

136 CONTINUE
WRITE (6,335)
335 FORMAT(' ENTER THE UPPER SOA LIMIT.')
```

READ(5,*,ERR=136)SUP

CD3(8)=(SUP-SLOW)/2.0

CD3(4)=SLOW+CD3(8)

CD3(8)=-CD3(8)

```

135 CONTINUE
```

```

336 FORMAT(' DO YOU WANT OUTPUT OF BUOY COORDINATES?')
    READ(5,201,ERR=135)ANSWER
    CALL PATGEN(PATYPE,PATX,PATY,PBEAR,PATSPC,
1    RADIUS,NB,BX,BY,CD3(9),CD4(3),CZR,TBEAR,CD4(1))
    IF(ANSWER.NE.YES)GO TO 137
    WRITE(6,337) (BX(IWR),IWR=1,NB)
    WRITE(6,338) (BY(IWR),IWR=1,NB)
337 FORMAT('0 BX = '/4(2X,F8.2))
338 FORMAT('0 BY = '/4(2X,F8.2))
137 CONTINUE
    WRITE(6,339)
339 FORMAT(' ENTER A COMENT TO IDENTIFY YOUR RUN. ')
    READ(5,340) (COMENT(I),I=1,15)
340 FORMAT(15A4)
    WRITE(10,341) (COMENT(I),I=1,15)
341 FORMAT(1X,15A4)
140 CONTINUE
    WRITE(6,806)
806 FORMAT(' ENTER THE NUMBER OF REPETITIONS. ')
    READ(5,*,ERR=140)ICD2(2)
    CD2(1)=90.
    CD3(1)=0.
    CD3(2)=0.
    CD6(2)=180.
    NOPROP=0
    T0=.25
    T1H=.05
    T2=.50
    ICD2(1)=1357931
    WRITE(10,800) ICD2,CD2,NOPROP,T0,T1H,T2,IGO,BETA,CORR50
800 FORMAT('X',2I9,2I1,2F8.1,I2,3F8.2,I2,2F10.6)
    ICD3(1)=1
8012 WRITE(6,8010)
8010 FORMAT(' ENTER SONAR EQ. STANDARD DEVIATION. ')
    READ(5,*,ERR=8012) ICD3(2)
    WRITE(10,801) CD3,ICD3
801 FORMAT(10F7.2,2I5)
    WRITE(10,802) ICD4(1),(CD4(IWR),IWR=1,2),ICD4(2),
1(CD4(IWR),IWR=3,4)
802 FORMAT(2(I5,2F10.5))
    IF(ICD4(1).EQ.0)GO TO 138
    WRITE(10,803) (PCAT(I),I=1,NCAT)
803 FORMAT(16F5.3)
    WRITE(10,804)
804 FORMAT(' ')
138 CONTINUE
    WRITE(10,804)
    WRITE(10,805) ICD6,CD6,PATSPC
805 FORMAT(2I3,2F7.1,F6.2)
    WRITE(10,807) (BX(IB),IB=1,NB)
807 FORMAT(16F5.1)
    WRITE(10,807) (BY(IB),IB=1,NB)
    WRITE(6,152)
152 FORMAT(20X,'THE INPUT FILE HAS BEEN CREATED ')
    ENDFILE 10
    REWIND 10
    RETURN
    END

```

```

        SUBROUTINE GENATE (X,Y,Z)
        IF(Y)1,4,2
C   UNIFORM DISTRIBUTION OVER (X+Y,X-Y)

        1 R=URAND(DUMMY)
          Z=X - Y*(2.*R-1.)
          RETURN
C   NORMAL DISTRIBUTION N(X,Y)
        2 Z=ANRMRN(DUMMY)
          Z=X+Z*Y
          RETURN
C   OPERATOR SPECIFIED VALUE
        4 Z=X
          RETURN
        END

```

```

SUBROUTINE RANORM(R)
R=ANRMRN(R)
RETURN
END

```

```

C*****
C*
C*      SHOW:          PRODUCES PLOTTED OUTPUT
C*
C*          ARRAY 'PROB' IS PLOTTED FROM 1 TO 'MAX'
C*
C*****
      SUBROUTINE WSHOW(PROB,MAX,ID)
      DIMENSION PROB(220),LOSS(51)
      DATA IB,IX/1H ,1HX/
      DO 200 I=1,51
200    LOSS(I)=IB
350  WRITE (6,2)
      WRITE (6,5)
      J=0
      DO 120 I=2,MAX,2
      VAL=50.*PROB(I)+.5
      K = INT(VAL) + 1
      LOSS(K)=IX
      J=J+1
      IF (J .NE. 10) GO TO 130
      J=I/ID
      WRITE (6,3) J,LOSS
      J=0
      GO TO 120
130  WRITE (6,4) LOSS
120  LOSS(K)=IB
      Q=MAX
      R=ID
      Q=Q/R
      WRITE (6,6) Q
      WRITE (6,5)
      WRITE (6,2)
      RETURN
2  FORMAT(7X,'0  .1  .2  .3  .4  .5  .6  .7  .8  .9  1')
3  FORMAT(1X,15,1X,51A1)
4  FORMAT(7X,51A1)
5  FORMAT(7X,51('.'))
6  FORMAT('+',F5.1)
      END

```

```

REAL FUNCTION URAND(SAME)
COMMON/MIRNG/RAN(10),GEN(10),NWRD,BASE,MOD,FBASE,FMOD
DIMENSION SUM(10)
INTEGER RAN,GEN,BASE,CARRY,SUM,PROD,HPROD
DO 30 IS=1,NWRD
30 SUM(IS)=0
DO 1 IG=1,NWRD
N2=NWRD-IG+1
DO 1 IR=1,N2
IS=IR+IG-1
PROD=RAN(IR)*GEN(IG)
HPROD=PROD/BASE
LPROD=PROD-HPROD*BASE
SUM(IS)=SUM(IS)+LPROD
IF(IS.LT.NWRD) SUM(IS+1)=SUM(IS+1)+HPROD
1 CONTINUE
N2=NWRD-1
DO 5 IS=1,N2
CARRY=SUM(IS)/BASE
SUM(IS)=SUM(IS)-CARRY*BASE
SUM(IS+1)=SUM(IS+1)+CARRY
5 CONTINUE
SUM(NWRD)=SUM(NWRD)-MOD*(SUM(NWRD)/MOD)
DO 20 IS=1,NWRD
20 RAN(IS)=SUM(IS)
FRAN=SUM(1)
DO 10 IS=2,NWRD
10 FRAN=FRAN/FBASE+SUM(IS)
FRAN=FRAN/FMOD
URAND=FRAN
RETURN
END

```

```

SUBROUTINE ROTATE(NB,BX,BY,ROT,TRANX,TRANY)
C*****
C* ANGLES IN THIS SUBROUTINE ARE MEASURED COUNTER-
C* CLOCKWISE FROM THE POSITIVE X AXIS IN CONTRAST *
C* TO "TRUE" BEARINGS THAT ARE USED IN THE OTHER *
C* SUBROUTINES. *
C*****
      DIMENSION BX(32),BY(32)
      PI=3.1415926
      IF(ROT.EQ.0.0) GO TO 200
      DO 100 I=1,NB
      R=SQRT(BX(I)*BX(I)+BY(I)*BY(I))
      IF(BX(I).NE.0.)GO TO 120
      IF(BY(I).GE.0.)A=PI/2.
      IF(BY(I).LT.0.)A=-PI/2.
      GO TO 110
120 A=ATAN(BY(I)/BX(I))
      IF(BX(I).LT.0.)A=PI+A
110 A=A-(PI*ROT/180.)
      BX(I)=R*COS(A)
      BY(I)=R*SIN(A)
100 CONTINUE
200 DO 300 I=1,NB
      BX(I)=BX(I)+TRANX
      BY(I)=BY(I)+TRANY
300 CONTINUE
      RETURN
      END

```

```

SUBROUTINE RANUMB(U)
COMMON/RANNO/NORAND
%NORAND IS THE COUNT OF RANDOM NUMBER PICKS
NORAND=NORAND+ 1
U=URAND(U)
RETURN
END

```

```

FUNCTION EXPRN(DUMMY)
I=0
100 X=URAND(X)
105 Y=URAND(Y)
      IF(X.LT.Y) GO TO 120
110 X=URAND(X)
      IF(X.LT.Y) GO TO 105
115 I=I+1
      GO TO 100
120 EXPRN=X+I
      RETURN
      END

```

```

SUBROUTINE RANSET (MAXINT,NSTRT)
COMMON/MIRNG/RAN(10),GEN(10),NWRD,BASE,MOD,FBASE,FMOD
INTEGER RAN,GEN,BASE,CARRY,REM
MAXI=MAXINT/4
IB=0
BASE=1
99 IF(BASE.GT.MAXI) GO TO 100
BASE=BASE*4
IB=IB+1
GO TO 99
100 BASE=2**IB
FBASE=BASE
NWRD=47/IB+1
REM=47-IB*(NWRD-1)
MOD=2**REM
FMOD=MOD
DO 101 N=1,10
RAN(N)=0
101 GEN(N)=0
GEN(1)=5
DO 200 I=1,14
CARRY=0
DO 190 N=1,NWRD
GEN(N)=GEN(N)*5+CARRY
CARRY=0
IF(GEN(N).LT.BASE) GO TO 190
CARRY=GEN(N)/BASE
GEN(N)=GEN(N)-BASE*CARRY
190 CONTINUE
200 CONTINUE
NSTART=NSTRT
IF(NSTART.LE.0) NSTART=2001
NSTART=2*(NSTART/2)+1
DO 300 N=1,NWRD
NTEMP=NSTART/BASE
RAN(N)=NSTART-NTEMP*BASE
300 NSTART=NTEMP
RETURN
END

```

C*****

C*

C* ERFC(X) RETURNS 1- (INTEGRAL OF NORMAL DENSITY)

C*

C* OR 1 - PHI(X)

C*

C* POLYNOMIAL APPROX. FROM HANDBOOK OF MATHEMATICAL FUNCTIONS

C* SECTION 26.2.18 (1964 EDITION)

C*

C*****

FUNCTION ERFC(X)

DATA C1,C2,C3,C4/.196854,.115194,.000344,.019527/
X2=ABS(X)

ERFC=.5/(1.0+C1*X2+C2*X2*X2+C3*X2**3+C4*X2**4)**4

IF (X.LT.0.) ERFC=1-ERFC

RETURN

END

FUNCTION ANRMRN(DUMMY)

1 R=URAND(R)

IF(R.GT.0.8638) GO TO 10

ANRMRN=2.*(URAND(X)+URAND(Y)+URAND(Z)-1.5)

RETURN

10 IF(R.GT.0.9745) GO TO 20

ANRMRN=1.5*(URAND(X)+URAND(Y)-1.0)

RETURN

20 IF(R.GT.0.9973020) GO TO 100

25 X=6.*URAND(X)-3.0

Y=0.358*URAND(X)

XSQ=X*X

GX=17.49731*EXP(-XSQ*.5)

AX=ABS(X)

IF(AX.GT.1.0) GO TO 30

IF(Y.GT.(GX-17.44392+4.735703**XSQ+2.157875*AX)) GO TO 25

ANRMRN=X

RETURN

30 AX3=2.367851*(3-AX)**2

IF(AX.GT.1.5) GO TO 40

IF(Y.GT.(GX-AX3-2.157875*(1.5-AX))) GO TO 25

ANRMRN=X

RETURN

40 IF(Y.GT.(GX-AX3)) GO TO 25

ANRMRN=X

RETURN

100 X=SQRT(9+2*EXPRN(X))

IF(URAND(X).GT.3/X) GO TO 100

IF(URAND(X).GT.0.5) X=-X

ANRMRN=X

IF(ABS(X).GT.3.) GO TO 1

RETURN

END

```

C*****
C*
C*   CHOLES:      PERFORMS CHOLESKY DECOMPOSITION
C*                TO GET ETA1 AND ETA2 MATRICES
C*
C*****
SUBROUTINE CHOLES(NB,IFREQ,ALPHA,BETA,BX,BY,ETA1,ETA2)
DIMENSION BX(32),BY(32),ETA(32,32),ETA1(32,32),ETA2(32,32)
  DO 100 I=1,NB
    DO 50 J=1,NB
      ETA(I,J)=ALPHA
      ETA1(I,J)=0.
50    ETA(I,I)=1.
100   ETA1(I,1)=ETA(I,1)
      DO 251 K=2,NB
        K1=K-1
        DO 150 J=1,K1
150   ETA1(K,K)=ETA1(K,K)+ETA1(K,J)*ETA1(K,J)
      ETA1(K,K)=SQRT(ETA(K,K)-ETA1(K,K))
      K2=K+1
      IF (K2 .GT. NB) GO TO 251
      DO 250 I=K2,NB
        DO 200 J=1,K1
200   ETA1(I,K)=ETA1(I,K)+ETA1(I,J)*ETA1(K,J)
250   ETA1(I,K)=(ETA(I,K)-ETA1(I,K))/ETA1(K,K)
251   CONTINUE
      DO 350 I=1,NB
        DO 300 J=1,NB
          RANGE=SQRT((BX(I)-BX(J))*(BX(I)-BX(J))+
          *          (BY(I)-BY(J))*(BY(I)-BY(J)))
          ETA(I,J)=EXP(-BETA*RANGE)
300   ETA2(I,J)=0.
350   ETA2(I,1)=ETA(I,1)
      DO 501 K=2,NB
        K1=K-1
        DO 400 J=1,K1
400   ETA2(K,K)=ETA2(K,K)+ETA2(K,J)*ETA2(K,J)
      ETA2(K,K)=SQRT(ETA(K,K)-ETA2(K,K))
      K2=K+1
      IF (K2 .GT. NB) GO TO 501
      DO 500 I=K2,NB
        DO 450 J=1,K1
450   ETA2(I,K)=ETA2(I,K)+ETA2(I,J)*ETA2(K,J)
500   ETA2(I,K)=(ETA(I,K)-ETA2(I,K))/ETA2(K,K)
501   CONTINUE
      RETURN
      END

```

C*****

C*
C* MONITR ROUTINE: RETURNS LIST OF BUOYS TO BE MONITORED
C*
C* CALCULATES WHICH BUOYS HAVE BEEN DROPPED, AND ARE IN
C* RANGE, OR SELECTS SET OF BUOYS TO MONITOR AFTER ALL
C* HAVE BEEN DROPPED.
C*

C*****

C SUBROUTINE MONITR(BX,BY,LM,NM,NB,ISTEP,JTIM,TIMMON,TIME,ACFTGS,
* PATSPC,RF,DMAX,MON,IGO,DISTAB)
C DIMENSION BX(32),BY(32),LM(32),DISTAB(32)
C DATA NL/1/

C
C CALCULATE DISTANCE TRAVELED BY AIRCRAFT
C DIST=TIME*ACFTGS
C COMPARE WITH TOTAL DISTANCE TO COMPLETE PATTERN
C IF (DIST.GT.DMAX) GO TO 25

C
C SPECIAL CASE FOR USER SPECIFIED PATTERN IN WHICH THE
C PATTERN SPACING MAY NOT BE CONSTANT
C IF (IGO.NE.7) GO TO 15
C DO 5 I=NL,NB

C COMPARE DIST WITH CUMULATIVE DISTANCE TO BUOY I
C IF (DISTAB(I).GT.DIST) GO TO 10
C 5 CONTINUE

10 NL=I-1
GO TO 16

C NORMAL CASE: BUOY SPACING IS CONSTANT (PATSPC APART)

15 NL=DIST/PATSPC+1
16 DIST1=(NL-1)*PATSPC

C DO LINEAR INTERPOLATION FOR POSITION BETWEEN BUOYS
C RATIO=(DIST-DIST1)/PATSPC
C PX=BX(NL)+RATIO*(BX(NL+1)-BX(NL))
C PY=BY(NL)+RATIO*(BY(NL+1)-BY(NL))

C
C BEGIN BUOY LOOP, CHECKING RANGE TO EACH BUOY
C DO 20 I=1,NB
C LM(I)=0
C IF (I.GT.NL) GO TO 20
C DX=PX-BX(I)
C DY=PY-BY(I)
C DIST=SQRT(DX*DX+DY*DY)
C IF (DIST.LE.RF) LM(I)=1
C 20 CONTINUE
C RETURN

C
C CASE 2: ALL BUOYS DROPPED. SELECT A SET TO MONITOR
C

25 JTIM = JTIM + ISTEP
IF (JTIM .LE. TIMMON) RETURN

C SELECT NEW SET
C DO 30 I = 1, NB

30 LM(I) = 0
IF (NM .LE. 0) GO TO 50

DO 40 I = 1, NM
INDEX = MON + I
IF (INDEX .GT. NB) INDEX = INDEX - NB
LM(INDEX) = 1

40 CONTINUE
MON = MON + NM
IF (MON .GT. NB) MON = MON - NB

SUBROUTINE PATGEN(PATYPE,PATX,PATY,PBEAR,PATSPC,RADIUS,
INB,BX,BY,TIMLAT,SPDI,CZR,TBEAR,CUSI)

DIMENSION BX(32),BY(32)

DIMENSION PNAME(7)

DATA PNAME/4HDF44,4HDF56,4HDF88,4HBTAC,4HCIRC,3HARC,4HSPEC/

THIS SUBROUTINE BUILDS A PATTERN OF THE INDICATED TYPE WITH
THE FOLLOWING SPECIFICS:

CENTER: PATX,PATY

PATTERN BEARING: PBEAR

TPA BEARING: TBEAR

SPACING: PATSPC

RADIUS: RADIUS (FOR CIRCULAR OR ARC PATTERNS)

NOTE THAT THE PATTERN IS BUILT SO THAT IT IS PERPENDICULAR
TO THE HEADING PATHD THAT IS CALCULATED BELOW.

IGO=0

DO 72 I=1,7

IF(PATYPE.EQ.PNAME(I)) IGO=I

72 CONTINUE

PI=3.1415927

(XP,YP) = FINAL COORDINATES OF THE PATTERN CENTER

PATHD = FINAL PATTERN HEADING RELATIVE TO STANDARD TPA

TBPC = TRUE BEARING OF THE PATTERN CENTER

THETA = REFERENCE ANGLE TO X-AXIS FOR ANGLE TBPC

TR = TPA ROTATION REQUIRED TO REACH STANDARD POSITION

DIST = DISTANCE BETWEEN PATTERN CENTER AND TPA CENTER

HSPC=PATSPC*SIN(PI/3.)

DIST=SQRT(PATX*PATX+PATY*PATY)

IF(PATX.NE.0.) GO TO 70

IF(PATY.GE.0.) TBPC=0.

IF(PATY.LT.0.) TBPC=180.

GO TO 71

70 THETA = ATAN(PATY/PATX)

IF (PATX.GT.0.) TBPC = (0.5)*PI - THETA

IF (PATX.LT.0.) TBPC = 1.5*PI - THETA

71 IF (TBEAR.LE.180.) TR=90. - TBEAR

IF (TBEAR.GT.180.) TR = 270. - TBEAR

CUSI=CUSI+TR

PATHD = PBEAR - 90. + TR

IF(IGO.EQ.5.OR.IGO.EQ.6) PATHD = PATHD + 90.

TR = (TR*PI)/180.

XP=DIST*SIN(TBPC+TR)

YP=DIST*COS(TBPC+TR)

IF (IGO.LE.0) GO TO 100

GO TO 200

100 WRITE(6,101)

101 FORMAT(' ',10X,'ERROR...UNIDENTIFIABLE PATTERN TYPE.
1A 5-6-5 DISTRIBUTED FIELD PATTERN HAS BEEN ASSUMED.')

IGO=2

200 GO TO (10,20,30,40,50,60,300),IGO

CODE FOR DF44 PATTERN. IGO=1

10 DO 11 I=1,4

BX(I)=-1.75*PATSPC + (I-1)*PATSPC

BX(I+8)=BX(I)

BY(I)=-1.5*HSPC

BY(I+8)=.5*HSPC

```

J=9-I
BX(J)=BX(I)+.5*PATSPC
BX(J+8)=BX(J)
BY(J)= -.5*HSPC
11 BY(J+8) =1.5*HSPC
GO TO 300
C
CODE FOR DF56 PATTERN. IGO=2
20 DO 21 I=1,5
BX(I)= -2.*PATSPC + (I-1)*PATSPC
BX(I+11)=BX(I)
BY(I)= - HSPC
21 BY(I+11) = HSPC
DO 22 I=1,6
BX(12-I)=-2.5*PATSPC + (I-1)*PATSPC
22 BY(12-I)=0.
GO TO 300
C
CODE FOR DF88 PATTERN. IGO=3
30 DO 31 I=1,8
BX(I)= -3.75*PATSPC + (I-1)*PATSPC
BX(17-I)=BX(I) + .5*PATSPC
BY(I)= -.5*HSPC
31 BY(I+8) = .5*HSPC
GO TO 300
C
CODE FOR BTAC PATTERN. IGO=4
40 DO 41 I=1,16
BX(I)= -7.5*PATSPC + (I-1)*PATSPC
41 BY(I)=0.
GO TO 300
C
CODE FOR CIRCULAR PATTERN. IGO=5
50 IF (RADIUS.GT.0) GO TO 51
RADIUS = TIMLAT*SPDI-CZR
IF (RADIUS.LE.0.) RADIUS=TIMLAT*SPDI + CZR
WRITE(6,102) RADIUS
102 FORMAT(' ',10X,'ERROR... CIRCULAR OR ARC PATTERN HAS NON-POSITIVE
1RADIUS. A RADIUS OF ',F10.5,' HAS BEEN USED.')
51 THETA=(2.*PI)/16.
DO 52 I=1,16
ANGLE=(I-8.5)*THETA
BX(I)=RADIUS*COS(ANGLE)
52 BY(I)=RADIUS*SIN(ANGLE)
GO TO 300
C
CODE FOR ARCP. IGO=6
60 IF(RADIUS.GT.0.) GO TO 61
RADIUS=TIMLAT*SPDI-CZR
IF(RADIUS.LE.0.)RADIUS=CZR+TIMLAT*SPDI
WRITE(6,102)RADIUS
61 THETA=2*ARSIN((.5*PATSPC)/RADIUS)
DO 62 I=1,16
ANGLE=(I-8.5)*THETA
BX(I)=RADIUS*SIN(ANGLE)
62 BY(I)=RADIUS*COS(ANGLE)
300 CALL ROTATE(16,BX,BY,PATHD,XP,YP)
RETURN
END

```