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October 1975

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ATACM:

ACDA Tactical Air Campaign Model

ACDA/PAB-249

Prepared For

**U.S. ARMS CONTROL
AND
DISARMAMENT AGENCY**

Prepared By

KETRON, INC.

1400 Wilson Boulevard
Arlington, Virginia 22209

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ATACM:
ACDA Tactical Air Campaign Model
ACDA/PAB-249

John R. Fish

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ABSTRACT

ATACM is a computer model designed and built for the Arms Control and Disarmament Agency for use in analyzing the impact of various force mixes upon a tactical airwar in Europe between NATO and Warsaw Pact forces. ATACM models an air campaign as a zero-sum staged game and employs dynamic programming to solve this game for approximate, optimal MAXMIN/MINMAX aircraft allocation strategies for the opposing sides at each stage of the campaign. The model permits multiple aircraft types with user-assigned missions, numerical and fractional reinforcements as a function of stage, and user selection of the objective function used to generate the optimal strategies.

Descriptions of the problem formulation and the engagement and optimization methodologies used to solve it are presented along with a user's guide and CDC 6600 FORTRAN listings.

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ACKNOWLEDGEMENT

Many of the ideas presented here are the result of survey work by Drs. Fred Miercort and Robert Galiano and the author gratefully acknowledges their assistance. In addition, Captain Bernard M. Robinson, USAF, and Dr. George Pitman of ACDA provided helpful guidance during both model development and documentation and their suggestions were appreciatively considered in preparation of this report.

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INTRODUCTION

The ACDA Tactical Air Campaign Model (ATACM) is a computer model designed and built for the Arms Control and Disarmament Agency (ACDA) for use in analyzing the impacts of various Mutual Balanced Force Reduction (MBFR) proposals upon a tactical airwar in Europe between NATO and Warsaw Pact forces. The design of ATACM was based upon the findings of a survey (Reference 1) of existing tactical air models conducted by KETRON to assess the applicability of existing models to ACDA's requirements. Results of the survey indicated the need for a new model incorporating the most desirable features of existing models (e.g., TAC CONTENDER, VECTOR, OPTSA, DY GAM) into a rigorous optimization framework allowing more aircraft types and a wider selection of aircraft missions.

As a realization of the survey's recommendations, ATACM models an air campaign as a zero-sum staged game between opposing forces and employs dynamic programming to solve this game for approximate, optimal aircraft allocation strategies for both sides at each stage of the campaign. Because of the economies associated with the optimization methodology used, ATACM offers many features previously not practical in other optimizing models. Specifically, ATACM permits:

- as many as four user-defined aircraft types per side and as many as eight different missions per aircraft type
- automatic generation of approximate, optimal, enforceable aircraft allocation strategies as a function of stage for any subset of the missions for which user-specified fractions are not supplied. The user may specify all, part, or none of the allocation fractions for a given aircraft type and the model generates optimal values for those fractions not specified.
- calculation of firm upper and lower bounds on the objective function value associated with the enforceable strategies employed
- option to use a weighted sum of three different objective functions as the criterion for generating the optimal strategies
- option to individually weight the Blue and Red contributions to these objective functions as a function of stage
- option to specify fractional or numerical reinforcements for any aircraft type as a function of stage

Following sections present a description of how the problem of tactical air warfare is formulated in ATACM, a description of the attrition relationships used to evaluate the outcomes of air-to-air, air-to-ground, and ground-to-air engagements, and an outline of the optimization methodology used to generate optimal enforceable strategies and objective function bounds. Appendix A is a user's guide for ATACM which describes the model's inputs, outputs, and general operation. Appendix B presents programming documentation and FORTRAN listings coded for the CDC6600.

PROBLEM FORMULATION

ATACM formulates a tactical air campaign as a staged game between opposing Blue and Red air and ground forces. It generates for each side, and for each stage of the war, strategies which optimize the utilization of these forces over the length of the campaign. Figure 1 presents a graphical representation of a general staged game which depicts the roles of those essential elements which will be described in detail in following sections.

In Figure 1, for each stage or time period of the campaign, vertical planes represent the state space of possible beginning and ending force levels for the opposing sides. Corresponding to each point in the beginning state space for a given stage, a game matrix can be constructed with m_t and n_t strategies available to Blue and Red respectively. The numbers of strategies, m_t and n_t , are a function of stage, while the one-stage payoffs in the game matrix depend upon the starting resource levels, the objective function chosen as a measure of overall performance, and the strategies selected by both sides.

For a given strategy selection at the beginning of stage 1, assessment relationships determine the value of the payoff and the attrition or losses suffered by both sides as a result of the one-stage battle. The dashed line in Figure 1 from stage 1 to stage 2 depicts the effect of this attrition and shows that the starting force levels for stage 2 will, barring reinforcements, generally be less than those for stage 1. The decision facing both sides at stage 2 is analogous to that at stage 1, the only possible difference being the strategies available to each side and the associated one-stage payoffs. Once again strategies are chosen, the objective function is incremented by the corresponding payoff, attrition relationships map the starting force level for the current stage into a new point in the state space for the next stage, etc. This process is repeated for the number of stages in the game, and the value of the objective function summed over all stages determines the outcome of the campaign.

Within the general framework depicted in Figure 1, the key elements in the formulation of a tactical air war as a staged game are the forces, strategies, and objective functions. The way these elements are defined in ATACM is described in the following paragraphs of this section. The key elements in the solution of a tactical air war include the assessment methodology, used to compute payoffs and attrition, and the optimization methodology used to select optimal strategies at each stage of the campaign. These elements are discussed in following sections.

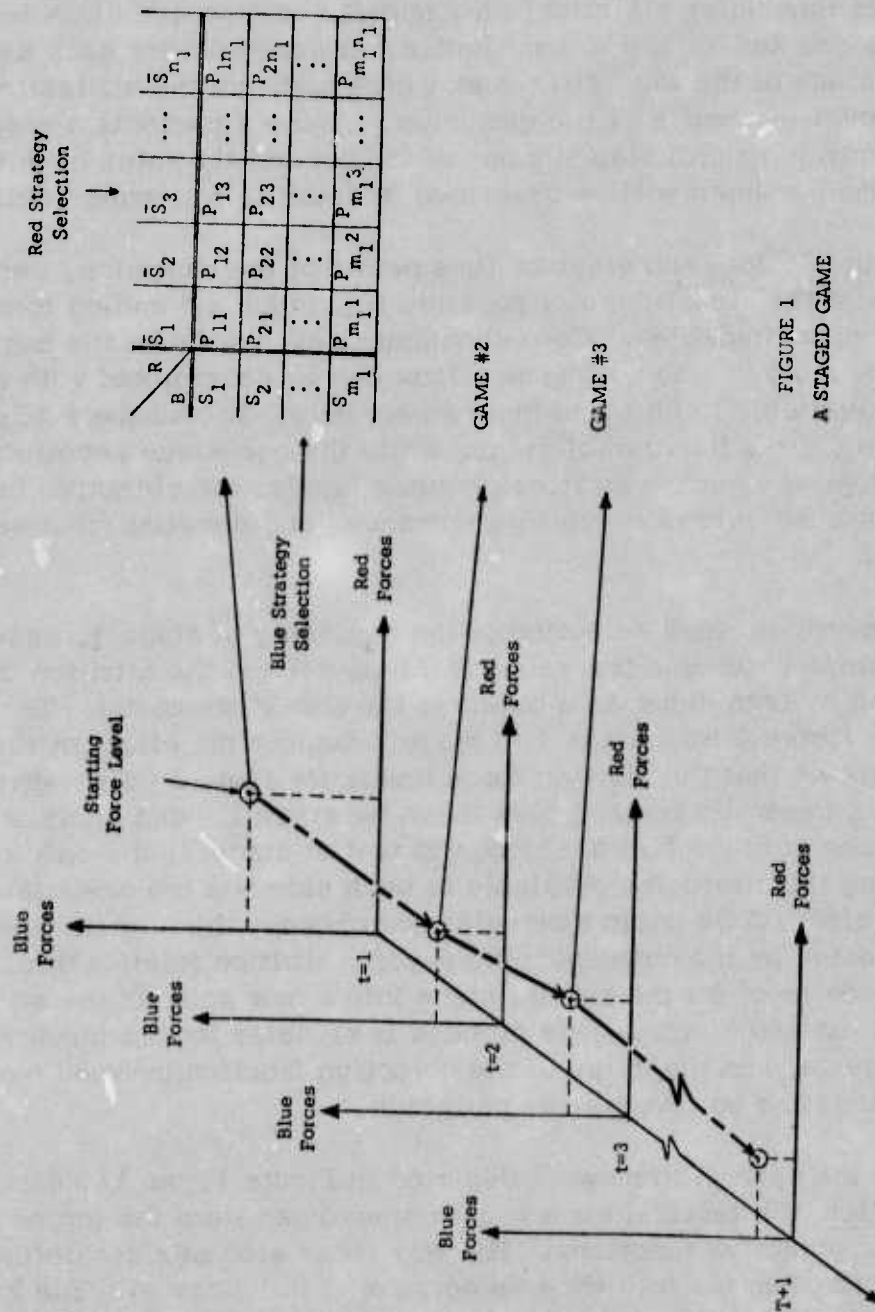


FIGURE 1
A STAGED GAME

OPPOSING FORCES AND MISSIONS

In the ATACM formulation, opposing forces consist of aircraft, SAMs, and ground divisions deployed in the stylized scenario depicted in Figure 2. A single airbase on each side serves as the staging area for all air missions flown against the opponent's SAMs, ground troops, or airbase. SAMs, which may be interpreted as any type of surface-to-air defense weapons, are segregated into forward and rear components corresponding to the location of the area they defend. Ground troops are defined in terms of homogenous divisions fighting on either side of a single-sector front (FEBA).

Aircraft

As many as four aircraft types can be assigned to either side and each of these types may be assigned as many as eight missions chosen from those listed in Table 1. In the course of a battle, forward and rear SAM suppressors (FSS and RSS) deploy before other aircraft and suppress the enemy's SAM sites. Afterward, aircraft assigned to fly close air support (CAS) attack the enemy's ground troops, reduce their total firepower, and directly influence the movement of the FEBA. Airbase attack (ABA) aircraft attack the opponent's airbase, destroy aircraft parked in shelters or on the open airfield, and thus reduce the enemy's effectiveness later in the war. Close air support and airbase attack escorts (CASE and ABAE) accompany the CAS and ABA aircraft on their attack missions and provide them protection from the opponent's battlefield and airbase defenders (BD and ABD). Finally, aircraft assigned to the Nothing mission remain on the ground during the battle because of the strength of opposing forces, maintenance requirements, unpreparedness due to a surprise attack, etc.

SAMs

The mission of the forward and rear SAMs is to defend the ground troops and airbase by attacking and destroying enemy aircraft. In prosecuting this mission, forward SAMs attack FSS, CAS, and CASE aircraft in direct defense of the ground troops, as well as RSS, ABA, and ABAE aircraft which must fly over the forward SAMs to reach their targets in the rear. Rear SAMs attack only those aircraft flying RSS, ABA, and ABAE missions.

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FEBA

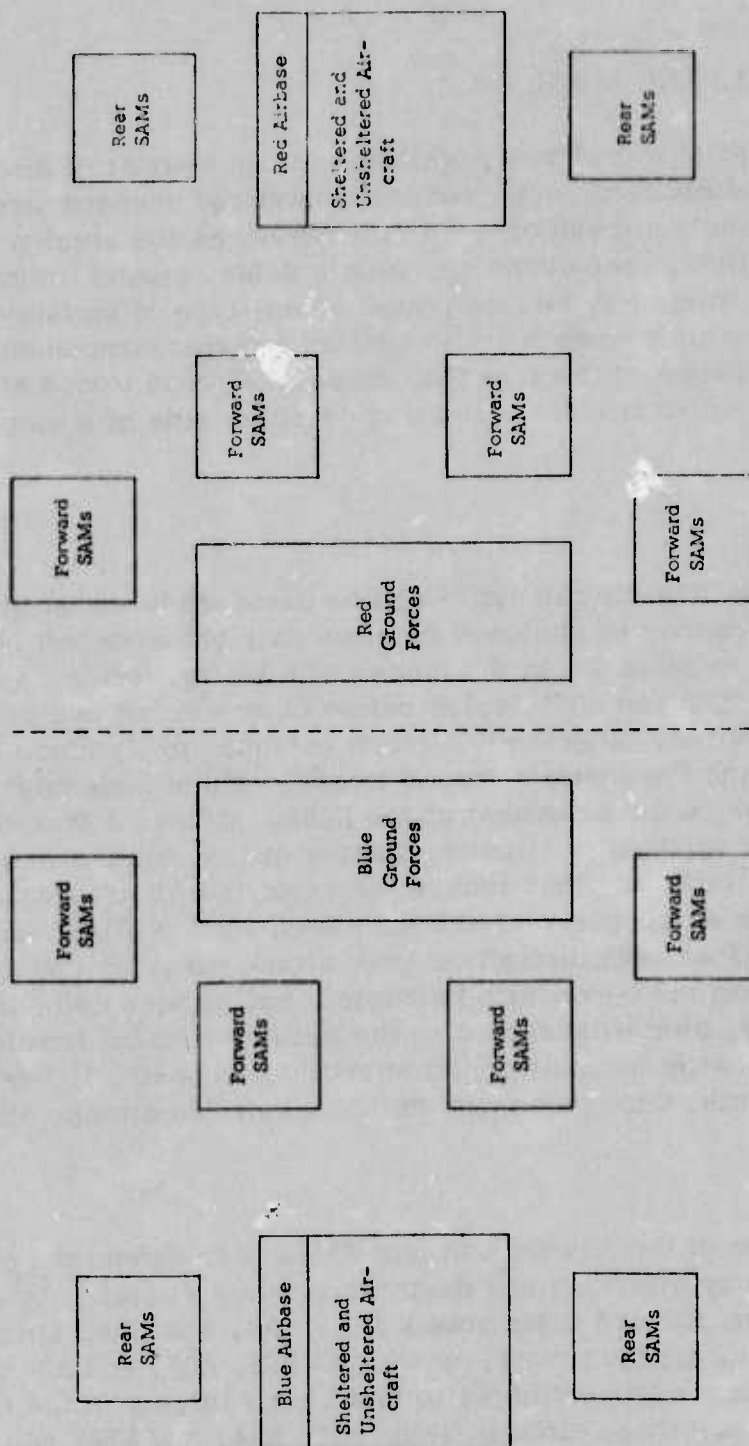


FIGURE 2
ATACM SCENARIO

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TABLE 1

AIRCRAFT MISSIONS PERMITTED IN ATACM

<u>Acronym</u>	<u>Mission</u>
CAS	Close Air Support
ABA	Airbase Attack
BD	Battlefield Defense
ABD	Airbase Defense
CASE	Close Air Support Escort
ABAE	Airbase Attack Escort
FSS	Forward SAM Suppression
RSS	Rear SAM Suppression
Nothing	No assigned mission

Ground Troops

Because ATACM was designed as a tool for studying the effects of different numbers and types of aircraft upon the outcome of an air campaign, the ground representation is simplistic and serves primarily as an input to the figure of merit used in the optimization process. Ground troops are segregated into homogeneous divisions with each division assigned a maximum firepower score. Successful CAS sorties flown against the enemy troops reduce this maximum firepower by a specified amount, and FEBA movement is then calculated as a user-specified function of the ratio of the total net firepowers delivered by Blue and Red respectively.

STRATEGIES

Given the forces and missions described above, the strategy a commander uses during a given time period or stage is a fractional allocation of all aircraft to missions. For example, if only one aircraft type is available to the Blue commander, and this aircraft can prosecute four missions selected from Table 1, the set of possible strategies from which he may choose can be characterized as the set of all 4-tuples whose elements are positive fractions which sum to one. Examples include (.5, 0, .5, 0), (.5, 0, .2, .3), (.25, .25, .25, .25), etc. In the general case of s missions, s-tuples representing possible fractional allocations for one aircraft type are called decision vectors.

If the Blue commander has only one aircraft type, the sets of possible decision vectors and strategies are identical. If two aircraft types are available to the Blue side, the set of possible strategies corresponds to the set of all possible decision vector pairs with the first decision vector representing allocations for aircraft type 1, the second allocations for aircraft type 2. An example of a strategy for two aircraft types, each with four possible missions, would be

$$((.5, 0, .5, 0), (.5, .2, .2, .1))$$

Analogously, possible strategies for a side with three aircraft types can be represented as decision vector triples, etc.

To limit the number of decision vectors (and thus strategies) from which ATACM must choose an optimal allocation, a parameter called a minimum allocation fraction is specified for each aircraft type. The minimum allocation fraction for an aircraft type is the smallest fractional unit which can be assigned to any mission. In the case of an aircraft type with four

assigned missions, a minimum allocation fraction of .5 limits the set of possible decision vectors to the following ten.

(1, 0, 0, 0)	(0, .5, 0, .5)
(.5, 0, 0, .5)	(0, .5, .5, 0)
(.5, 0, .5, 0)	(0, 0, 1, 0)
(.5, .5, 0, 0)	(0, 0, .5, .5)
(0, 1, 0, 0)	(0, 0, 0, 1)

Correspondingly, the number of strategies available to a side with two, three, or four such aircraft types would be 100, 1000, or 10,000 respectively. In general, the number of possible decision vectors V for an aircraft type with s missions and a minimum allocation fraction equal to $1/t$ is given by

$$V = \frac{(s + t - 1)!}{(s - 1)! t!} \quad (1)$$

In addition to aircraft types, missions assigned, and minimum allocation fractions, ATACM permits one other important specification which determines the set of strategies available for a particular stage of the conflict. The user is allowed to specify, for any stage, a fixed assignment of aircraft to mission in terms of a multiple of the minimum allocation fraction. Looking at the previous example, the user can force half of the aircraft to prosecute the first mission assigned by specifying the first element in the corresponding decision vector to always equal .5. In that case, the set of possible decision vectors for the specified stage and aircraft type reduces to the following subset of those shown above:

(.5, 0, 0, .5)
(.5, 0, .5, 0)
(.5, .5, 0, 0)

The set of all strategies generated from these three decision vectors will reflect the specified allocation, and the strategy selected from this set by ATACM will optimize remaining allocations over those missions for which fractions are not specified.

As can be seen from this example, as more and more fractions are specified, the number of possible decision vectors and strategies decreases, and the process of strategy selection optimizes over fewer and fewer missions. In the extreme case, where all fractions in all decision vectors are specified, the set of strategies available at each stage reduces to a single strategy. Strategy selection then becomes a vacuous operation, and the net effect is an evaluation of an air campaign using a user-specified strategy at each

stage. Thus, depending upon the number of mission allocations specified, ATACM can be used as an optimization, sub-optimization, or strategy-specified model.

OBJECTIVE FUNCTIONS

ATACM permits the user to select any linear combination of three objective functions to be used as the overall measure of the opposing forces' performance during an air campaign. Specifically, the overall objective function used as the criterion for strategy selection can be expressed as

$$F = w_1 f_1 + w_2 f_2 + w_3 f_3 \quad (2)$$

where f_1 = difference of total Blue minus total Red CAS firepower

f_2 = difference of total Blue minus total Red (CAS firepower + ground firepower)

f_3 = total FEBA movement computed as a user-specified function of the ratio of Blue's total ground firepower to Red's

and w_j = user specified weight on f_j , $j = 1, 2$, or 3 .

By appropriate choice of the w_j , the user can optimize using any one of the f_j , or he can generate hedging strategies -- those not precisely optimal for any single criterion but instead optimal for several criteria at once -- by specifying F to be a combination of the f_j . Regardless of what F is specified, f_1 , f_2 , and f_3 are also computed and recorded individually making it possible to simultaneously monitor the effects of different optimization criteria on each of the objective functions.

In addition to the weights w_1 , w_2 , and w_3 , ATACM also permits the user to weight the Blue and Red components of f_1 , f_2 , and f_3 by stage. To illustrate, each f_j can be expanded as follows:

$$f_1 = \sum_{t=1}^{T+1} b_t^{\text{CAS}} B_t - r_t^{\text{CAS}} R_t \quad (3)$$

$$f_2 = \sum_{t=1}^{T+1} b_t^{\text{TFP}} B_t - r_t^{\text{TFP}} R_t \quad (4)$$

$$f_3 = \sum_{t=1}^{T+1} \frac{b_t + r_t}{2} \text{FEBA}_t \quad (5)$$

where T = number of stages in the campaign

$\text{CAS}_{kt} = \begin{cases} \text{CAS firepower delivered by side } k \text{ during stage } t & \text{for } t \leq T \\ \text{residual value of undamaged aircraft on side } k \text{ at end of war} & \text{for } t=T+1 \end{cases}$

$\text{TFP}_{kt} = \begin{cases} \text{total firepower (ground + CAS) delivered by side } k \text{ during stage } t & \text{for } t \leq T \\ \text{residual value of undamaged aircraft on side } k \text{ at end of war} & \text{for } t=T+1 \end{cases}$

$\text{FEBA}_t = \begin{cases} \text{FEBA movement during stage } t & \text{for } t \leq T \\ 0 & \text{for } t=T+1 \end{cases}$

b_t = weight on Blue's contribution to the objective function during stage t ($b_{T+1}=1$)

r_t = weight on Red's contribution to the objective function during stage t ($r_{T+1}=1$)

Depending upon the scenario being simulated, the weights b_t and r_t can be used to reflect the various effects of logistics, force readiness, pilot skills, ground terrain, etc., all as a function of stage. For example, in the case of a surprise attack by Red, the amount of firepower Blue can deliver per sortie during early stages of the war might be severely limited by logistics, readiness, etc. To simulate this situation, weights b_t specified for the first few stages of the war would be smaller than those specified for later stages.

ASSESSMENT METHODOLOGY

Returning to the general description of a staged game depicted in Figure 1, the assessment methodology computes the values of the payoffs in each game matrix and the attrition suffered by both sides as a result of each possible one-stage battle. The important considerations in describing this methodology include the types of engagements which may occur between the opposing sides, the sequence in which these engagements occur within each stage, and the relationships used to compute attrition for each type of engagement. An important finding of the survey of existing models was the general lack of agreement concerning the best way to treat each of these facets of the assessment procedure. The assessment methodology described below is a mix of those used in OPTSA and VECTOR (References 2 and 3) and consequently suffers from some of the same limitations cited in Reference 1. In consideration of these limitations, ATACM is purposely structured so that other, alternative assessment methodologies can be implemented with minimal programming effort.

TYPES OF ENGAGEMENTS

In the current version of ATACM the types of engagements permitted can be classified as air-to-air, air-to-ground, and ground-to-air. Air-to-air engagements occur when CAS and CASE aircraft engage battlefield defenders or when ABA and ABAE aircraft engage airbase defenders. Air-to-ground engagements occur when ABA aircraft attack the opponent's airbase, when SAM suppressors attack the opponent's SAMs, or when CAS aircraft deliver ordnance against the opponent's ground troops. Ground-to-air engagements occur between SAMs and opposing aircraft flying SAM suppression, CAS, CASE, ABA, or ABAE missions.

ENGAGEMENT CYCLES

The first event in each stage of the air campaign is the addition of any numerical or fractional aircraft reinforcements specified by the user. Thereafter, attrition and payoffs for each strategy pair are computed and accumulated over a specified number of equal length time periods (e.g. days) called engagement cycles. The first event in each engagement cycle is the assignment of aircraft to missions according to the strategy pair being examined. Then, using specified sortie rates per cycle, these

assignments are converted into sorties which progress en masse through the engagements described below.

FSS and RSS Engagements

FSS and RSS missions depicted in Figure 3 are flown by each side before all other missions in an attempt to clear corridors for subsequent battlefield and airbase attackers. SAMs successfully attacked by suppressors are killed for the duration of the stage in which they are suppressed, but are replaced or restored at the beginning of the next stage. SAM suppressors successfully engaged by SAMs or destroyed by the opponent's airbase attackers are lost for the duration of the campaign.

CAS, CASE, and BD Engagements

The CAS, CASE, and opposing BD missions depicted in Figure 4 are flown after the SAM suppressors. All air-to-air engagements between CAS, CASE, and the opponent's BD sorties are one-on-one encounters. Excess attackers or defenders not engaged in one phase of the engagement cycle proceed unmolested to the next phase. Sorties which are engaged abort their original mission, fight the opposing aircraft, and, if not killed, return to their own airbase. Each successful CAS sortie delivers ordnance on the opponent's ground troops and reduces their total firepower (computed at the beginning of each stage as number of divisions times firepower per division) by a user-specified amount. Thus ground troops, like SAMs, can be thought of as being killed for the duration of the stage in which they are attacked, but replaced at the beginning of the next stage. CAS, CASE, or BD killed in air-to-air engagements or destroyed by the opponent's airbase attackers are lost for the duration of the campaign.

ABA, ABAE, and ABD Engagements

The ABA, ABAE, and opposing ABD missions depicted in Figure 5 are the last missions flown in each engagement cycle. All air-to-air engagements between ABA, ABAE, and the opponent's ABD sorties are one-on-one encounters treated in the same way as those described for CAS, CASE, and BD missions. Each successful ABA sortie delivers ordnance on the opponent's airbase destroying those sheltered and unsheltered aircraft specified as being vulnerable to airbase attack. Shelters are assigned to vulnerable aircraft types in proportion to their relative numbers. Shelters are not destroyed; damaged shelters are

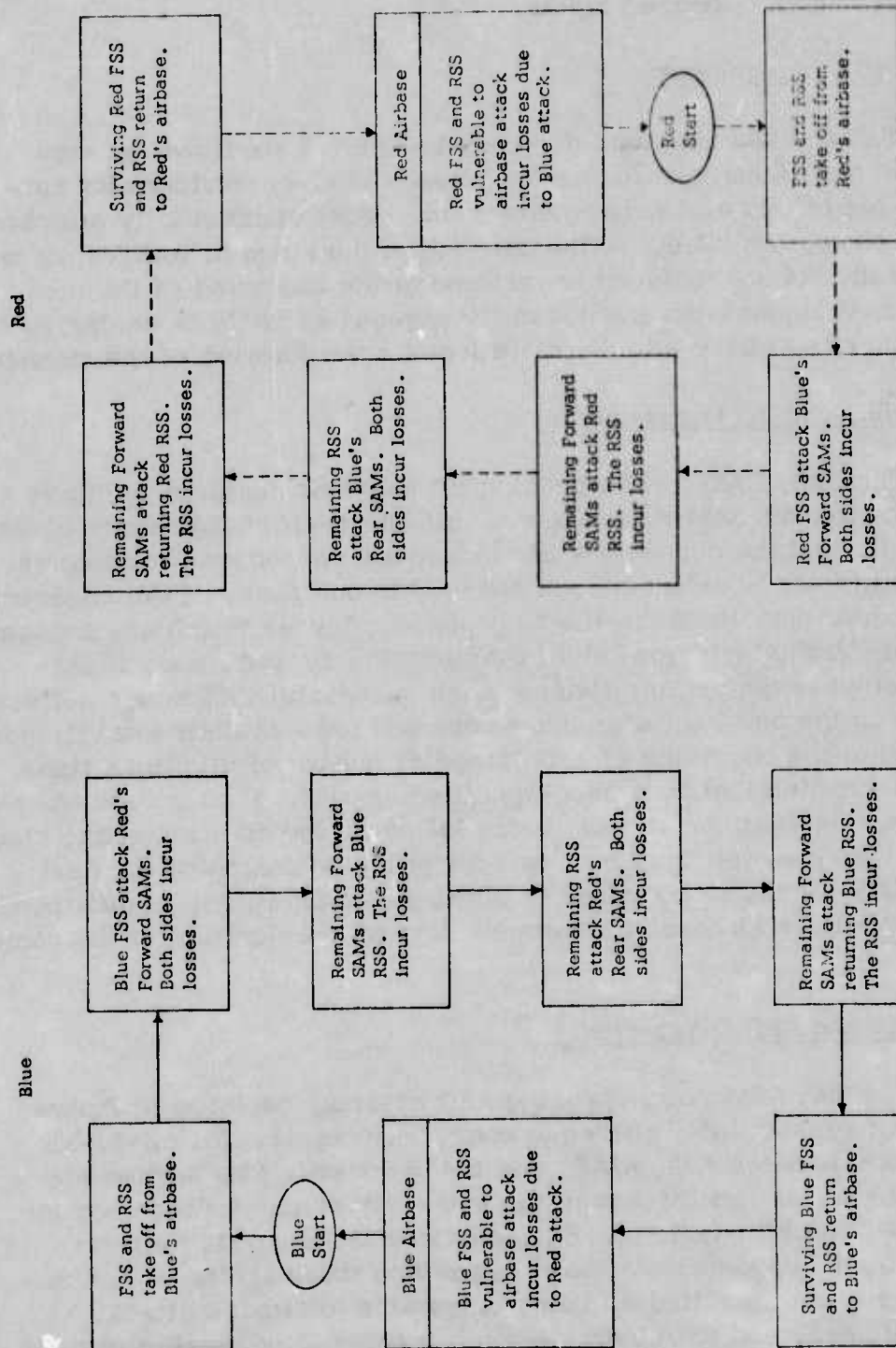


FIGURE 3
FSS AND RSS ENGAGEMENTS DURING AN
ENGAGEMENT CYCLE

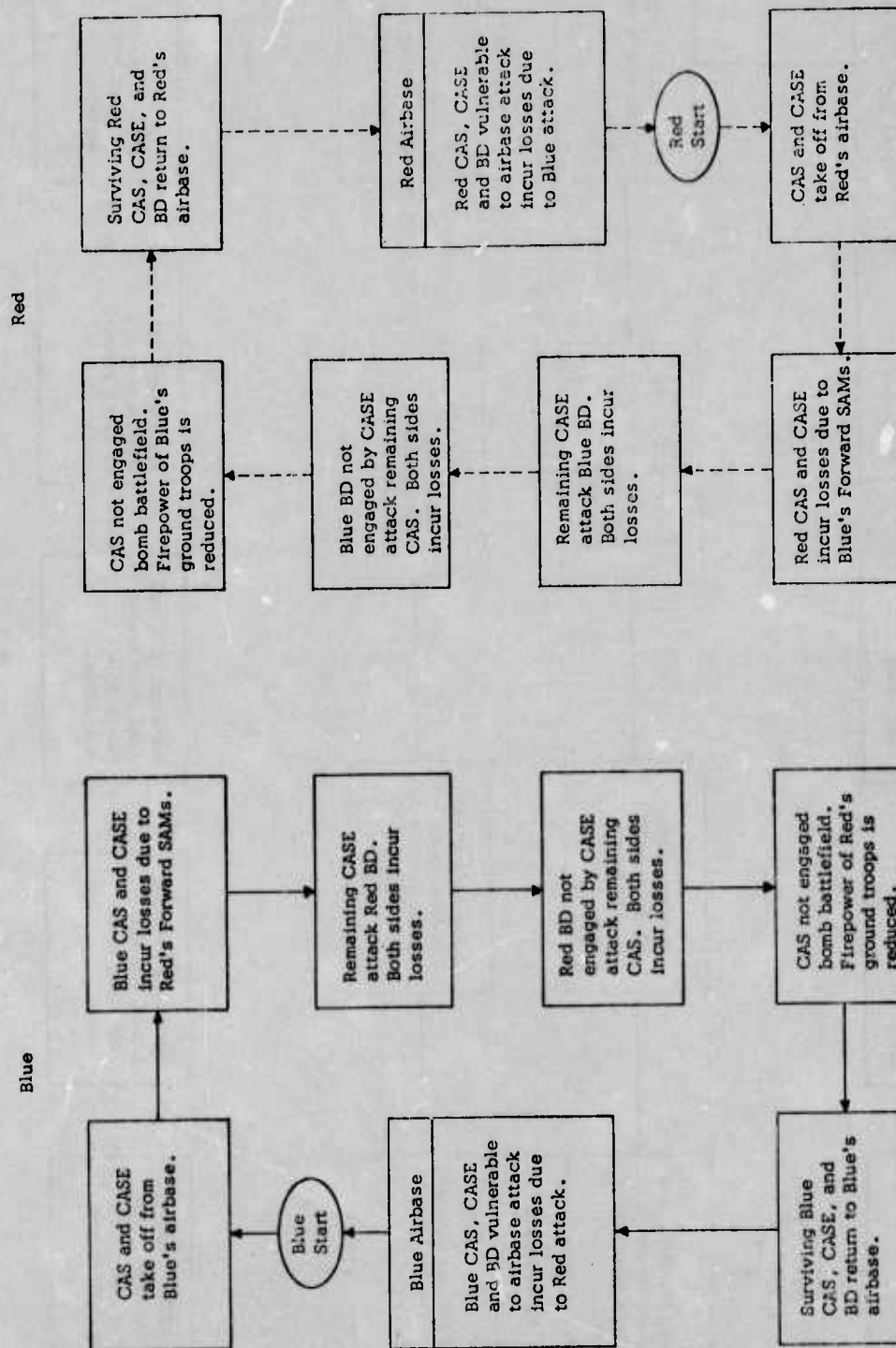


FIGURE 4
CAS, CASE, AND BD ENGAGEMENTS DURING AN
ENGAGEMENT CYCLE

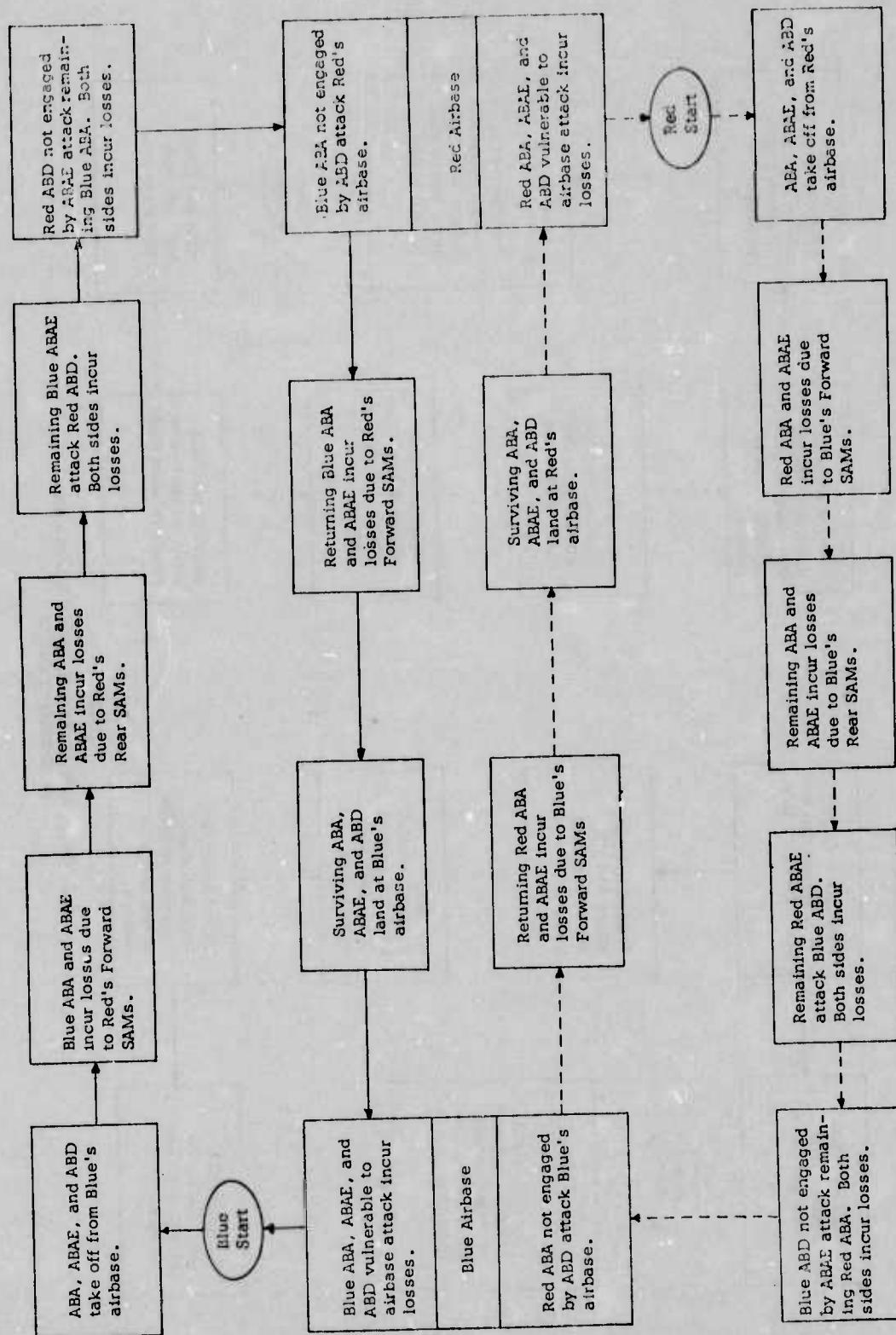


FIGURE 5
ABA, ABAE, AND ABD ENGAGEMENTS DURING AN
ENGAGEMENT CYCLE

assumed to be repaired by the beginning of the next cycle. ABA, ABAB, or ABD killed in air-to-air engagements or destroyed by the opponent's airbase attackers are lost for the duration of the campaign.

ATTRITION RELATIONSHIPS

During the course of the engagement cycles just described, all aircraft casualties due to air-to-air and ground-to-air engagements are computed in terms of sorties lost. Surviving sorties, which successfully return to their airbase at the end of each cycle, are converted to aircraft before they are subjected to airbase attack by dividing numbers of surviving sorties by the sortie rates. The mathematical relationships used to evaluate sortie losses as well as the attrition resulting from air-to-ground engagements are described below.

Air-to-Air Engagements

In general, for each possible air-to-air engagement shown in the blocks of Figures 4 and 5, sorties on one side assigned to a generic attack mission, engage, in one-on-one encounters, sorties on the opposing side assigned to a generic defense mission. Excess attack sorties not engaged in one phase of the air-to-air war proceed to the next phase; sorties that are engaged abort their assigned mission, prosecute the air-to-air engagement and, if not killed, return immediately thereafter to their airbase. To describe how sortie attrition on both sides is computed in such an engagement, let

A_i = number of attack sorties in the current engagement flown by aircraft of type i

D_j = number of defense sorties in the current engagement flown by aircraft of type j

A_i^k = number of the A_i killed in the current engagement

D_j^k = number of the D_j killed in the current engagement

p_{ij} = probability an attack sortie of type i is killed by a defense sortie of type j in a one-on-one encounter

q_{ji} = probability a defense sortie of type j is killed by an attack sortie of type i in a one-on-one encounter

To compute A_i^k and D_j^k , the total numbers of attack and defense sorties are first used to compute E , the number of one-on-one encounters, as

$$E = \min \left(\sum_i A_i, \sum_j D_j \right) \quad (6)$$

The allocation of this total to individual aircraft types is then computed proportionally as

$$E_{ij} = E \left(\frac{A_i}{\sum_i A_i} \right) \left(\frac{D_j}{\sum_j D_j} \right) \quad (7)$$

where E_{ij} represents the number of one-on-one encounters between attackers of type i and defenders of type j .

Finally, expected numbers of killed attack and defense sorties flown by aircraft of types i and j respectively are computed as

$$A_i^k = \sum_j E_{ij} p_{ij} \quad (8)$$

and

$$D_j^k = \sum_i E_{ij} q_{ji} \quad (9)$$

Air-to-Ground Engagements

Of the three types of air-to-ground engagements considered in ATACM, only the SAM suppression and airbase attack missions directly produce losses among the opponent's forces. As described in the discussion of Figure 4, CAS sorties reduce the opponent's ground firepower by a simple subtractive rule which indirectly reflects ground losses. By contrast, SAM and parked aircraft losses are computed using exponential relationships relating the kill probabilities and numbers of attackers (SAM suppressors or ABA) to the number of opponents (SAMs or parked aircraft).

SAM Losses

To derive the expression for SAM losses produced by generic (FSS or RSS) SAM suppression sorties, let

A_i = number of SAM suppression sorties in the current engagement flown by aircraft of type i

D = number of opposing SAMs

D^k = number of D killed in the current engagement

q_i = probability a SAM is killed by a SAM suppressor sortie of type i

To compute D^k , the numbers of SAM suppression sorties flown are used as weights to compute an average probability of kill

$$\bar{q} = \frac{\sum_i A_i q_i}{\sum_i A_i} \quad (10)$$

This probability, along with the numbers of suppression sorties and SAMs, is used to compute D^k as

$$D^k = D \left(1 - \exp \left(- \bar{q} \frac{\sum_i A_i}{D} \right) \right) \quad (11)$$

Losses Due to ABA

The attrition relationship for computing the effect of ABA sorties on parked aircraft is analogous to Equation (11), the only difference being the number of opponent types. Specifically, let

A_i = number of ABA sorties in the current engagement flown by aircraft of type i

D_j = number of parked aircraft of type j vulnerable to airbase attack. Vulnerable aircraft are assigned to shelters in proportion to their relative numbers in the inventory; $j=1$ corresponds to sheltered aircraft, $j=2$ to unsheltered.

D_j^k = number of D_j killed in the current engagement.

q_{ji} = probability a vulnerable aircraft of type j is killed by a sortie flown by an ABA aircraft of type i

To determine D_j^k , first E_{ij} , the number of attack sorties of each type i assumed to attack vulnerable aircraft of type j , is computed pro-

portionally as

$$E_{ij} = A_i \frac{D_j}{\sum_j D_j} \quad (12)$$

Using the E_{ij} as weights, an average probability of killing a parked aircraft of type j is computed as

$$\bar{q}_j = \frac{\sum_i E_{ij} q_{ji}}{\sum_i E_{ij}} \quad (13)$$

Finally, D_j^k is computed using the standard exponential expression

$$D_j^k = D_j \left(1 - \exp \left(- \bar{q}_j \frac{\sum_i E_{ij}}{D_j} \right) \right) \quad (14)$$

Ground-to-Air Engagements

In ground-to-air engagements, SAMs attack opposing sorties in one-on-one encounters analogous to one-sided air-to-air engagements. If the number of opposing sorties exceeds the number of SAMs, excessive sorties are not attacked. If the number of SAMs exceeds the number of sorties, excessive SAMs are not launched. To describe the attrition produced by a generic SAM (forward or rear) attack, let

A = number of SAMs in the current engagement

D_j = number of target sorties in the current engagement flown by aircraft of type j

D_j^k = number of D_j killed in the current engagement

q_j = probability a target sortie flown by an aircraft of type j is killed by a SAM in a one-on-one encounter

To compute D_j^k , the total number of SAMs and opposing aircraft sorties are used to compute E , the number of one-on-one encounters, as

$$E = \min \left(A, \sum_j D_j \right) \quad (15)$$

$$E_j = E \frac{D_j}{\sum_j D_j} \quad (16)$$

where E_j represents the number of one-on-one encounters between SAMs and target sorties of type j .

Finally, the expected number of killed sorties flown by aircraft of type j is computed as

$$D_j^k = E_j q_j \quad (17)$$

OPTIMIZATION METHODOLOGY

The methodology used to select optimal strategies for both sides at each stage of the campaign reflects the recommendations of the survey presented in Reference 1. The basic approach is to select enforceable strategies which individually optimize each side's minimal performance over the length of the campaign. Following paragraphs explain this optimization criterion in detail and describe the dynamic programming methodology used to implement it.

MAXMIN/MINMAX STRATEGIES AND PAYOFFS

In the standard game matrix such as that shown in Figure 1 the possible objective functions used to compute payoffs to Blue are defined such that positive payoffs indicate Blue success. Blue's objective is to choose that strategy which will produce the largest payoff, while Red's objective is to choose that strategy which will produce the smallest payoff. The approach used in ATACM is to assume both Blue and Red act conservatively in choosing their strategies. To illustrate, for a simple case, Figure 6 presents a game matrix for starting force levels in a hypothetical one-stage campaign in which Blue has five possible strategies, Red has four.

One-Stage Game

Since Blue and Red are assumed to be conservative, each chooses that strategy which will produce the most favorable outcome under the worst of circumstances -- i.e. prior knowledge of his selection by his opponent. In the case of Blue, selection of S_1 guarantees a payoff no less than 1 regardless of which strategy Red chooses. Selection of S_2 guarantees a payoff no less than 0, S_3 no less than -1, etc. These minimal payoffs (or row minimums) are shown in Figure 6 for each possible Blue selection. Assuming Red has superior intelligence, Blue would choose that strategy, S_1 , which maximizes over the set of minimal payoffs. Thus S_1 is called Blue's MAXMIN strategy, and 1, the minimal payoff associated with S_1 , is called the MAXMIN payoff or objective function value. The Red strategy $\bar{S}_2$ which would have to be played against S_1 to yield the MAXMIN payoff is called Red's MAXMIN strategy.

		Red MAXMIN		Red MINMAX			
		↓		↓			
		Red Blue	$\bar{s}_1$	$\bar{s}_2$	$\bar{s}_3$	$\bar{s}_4$	Row Min
Blue MAXMIN →	s_1		2	1	4	2	1
	s_2		3	5	0	0	0
Blue MINMAX →	s_3		6	-1	4	3	-1
	s_4		3	1	2	-2	-2
	s_5		0	-3	-5	1	-5
		Col Max	6	5	4	3	

FIGURE 6
ONE-STAGE GAME MATRIX

In the case of Red's selection, choice of $\bar{S}_1$ could result in a payoff as large as 6 if Blue were to play S_3 , selection of $\bar{S}_2$ could result in a payoff as large as 5, $\bar{S}_3$ a payoff as large as 4, and $\bar{S}_4$ a payoff as large as 3. Assuming Blue has superior intelligence, conservative Red would choose that strategy, $\bar{S}_4$, which minimizes over the set of column maximums shown in Figure 6. Strategy $\bar{S}_4$ is called Red's MINMAX strategy, S_3 is called Blue's MINMAX strategy, and 3, the payoff associated with playing $\bar{S}_4$ against S_3 is called the MINMAX payoff.

If Blue were to play its MAXMIN strategy and Red its MINMAX strategy, the payoff which would result is 2. This MAXMIN vs. MINMAX payoff will always be greater than or equal to the MAXMIN payoff (in this case 1) and less than or equal to the MINMAX payoff (in this case 3).

From this example, it should be clear how the optimization criterion used in ATACM would be applied for a one-stage campaign. Given the starting force levels, strategies, and objective function specification, payoffs in the corresponding game matrix would be computed using the assessment methodology described in the previous section. Blue's MAXMIN strategy and payoff would be computed by maximizing over row minimums while Red's MINMAX strategy and payoff would be computed by minimizing over column maximums. Output would consist of the Blue MAXMIN strategy, the Red MINMAX strategy, the lower and upper MAXMIN/MINMAX objective function bounds, and the actual MAXMIN vs. MINMAX payoff which would result if both sides played their conservative strategies.

Multi-Stage Game

To understand how the MAXMIN/MINMAX strategy selection procedures for a one-stage game extend to a multi-stage game, it is helpful to present an alternative representation of a staged game called an extended game as shown in Figure 7. In an extended game representation of a T-stage air campaign, Blue extended strategies are T-tuples whose t^{th} element is a strategy selected from the set of one-stage strategies $S_1, S_2, \dots, S_{m_t}$ available to Blue at the t^{th} stage of the campaign. In other words, the first element in an extended strategy for Blue is the strategy Blue would use for stage 1, the 2nd element is Blue's strategy for stage 2, ..., and the T^{th} element is Blue's strategy for the last stage of the campaign. The number of possible extended

FIGURE 7
EXTENDED GAME REPRESENTATION
OF A T-STAGE GAME

Blue \ Red	$\overline{ES}_1$	$\overline{ES}_2$	...	$\overline{ES}_N$
ES_1	TP_{11}	TP_{12}	...	TP_{1N}
ES_2	TP_{21}	TP_{22}	...	TP_{2N}
$\vdots$	$\vdots$	$\vdots$		$\vdots$
ES_M	TP_{M1}	TP_{M2}	...	TP_{MN}

$$ES_i = \text{Blue Extended Strategy} = (S_{i_1}, S_{i_2}, \dots, S_{i_T})$$

where S_{i_t} = Blue strategy for stage t

$$\overline{ES}_j = \text{Red Extended Strategy} = (\bar{S}_{j_1}, \bar{S}_{j_2}, \dots, \bar{S}_{j_T})$$

where $\bar{S}_{j_t}$ = Red strategy for stage t

$$M = m_1 \cdot m_2 \cdot \dots \cdot m_T \qquad N = n_1 \cdot n_2 \cdot \dots \cdot n_T$$

$$TP_{ij} = \text{Total Payoff produced by playing } ES_i \text{ against } \overline{ES}_j$$

strategies, M , from which Blue may choose is equal to

$$M = m_1 \cdot m_2 \cdot m_3 \cdot \dots \cdot m_T \quad (18)$$

where m_t equals the number of possible Blue strategies available for stage t . Extended strategies for Red are analogous.

Payoffs in an extended game are total payoffs over the length of the campaign which result from playing a Blue extended strategy against a Red extended strategy. Looking back at Figure 1, a total payoff in the extended game depends upon the one-stage payoffs and the attrition represented by the dashed line. Each different combination of Blue-Red extended strategies corresponds to a unique attrition path from the state space at the beginning of stage 1 to the state space at the end of stage T .

Theoretically, selection of MAXMIN/MINMAX strategies in a multi-stage campaign, represented in the context of the extended game, is exactly the same as that described for a one-stage game. Indeed, for a one-stage campaign the extended game representation reduces to a one-stage game. Unfortunately, for air campaigns with reasonable numbers of strategies and stages the extended game representation is valuable only as an abstraction because of its prohibitive size. For example, if Blue and Red each had only 20 possible strategies to choose from at each stage of a three stage campaign, the corresponding extended game would be an 8000 by 8000 matrix requiring 64 million three-stage payoff evaluations. Assuming 10^{-3} seconds of computer time was required for each one-stage assessment, evaluation of the payoffs alone would require over 50 hours. Needless to say, a method other than the straightforward solution of the extended game is required to determine MAXMIN/MINMAX strategies for the general multi-stage campaign.

DYNAMIC PROGRAMMING SOLUTION

The reason the extended game representation of modest sized air campaigns becomes untractable is that it treats the problem of strategy selection for all stages as a single step process. An alternative approach, using dynamic programming, is to decompose the problem into a series of one-stage problems, similar in many respects to the way the problem was originally posed in Figure 1. To illustrate the dynamic programming approach, its necessary to define more precisely many of the

concepts first presented there. For purposes of illustration, we will assume Blue and Red each have one aircraft type -- more types simply increase the dimensionality of the state space. For this case, shown in Figure 8, let

X_t = a point, (B_t, R_t) , in the state space at the beginning of stage t corresponding to B_t and R_t aircraft available to Blue and Red respectively

$S(X_t)$ = Blue's one-stage MAXMIN strategy selection corresponding to X_t

$\bar{S}(X_t)$ = Red's one-stage MINMAX strategy selection corresponding to X_t

$TP(X_t)$ = the total MAXMIN payoff associated with optimal play by Blue from state X_t at the beginning of stage t to the end of the campaign

$\bar{TP}(X_t)$ = the total MINMAX payoff associated with optimal play by Red from state X_t at the beginning of stage t to the end of the campaign

$P_{ij}(X_t)$ = payoff in the one-stage game matrix corresponding to selection of the i^{th} and j^{th} strategies when in state X_t

$Z_{ij}(X_t)$ = state X_{t+1} into which selection of the i^{th} and j^{th} strategies by Blue and Red maps the state X_t

Using these definitions, $TP(X_1)$ and $\bar{TP}(X_1)$ are the desired MAXMIN and MINMAX payoffs associated with the extended strategies

$$ES(X_1) = (S(X_1), S(X_2), S(X_3), \dots, S(X_T)) \quad (19)$$

$$\bar{ES}(X_1) = (\bar{S}(X_1), \bar{S}(X_2), \bar{S}(X_3), \dots, \bar{S}(X_T)) \quad (20)$$

where X_1 represents the starting numbers of aircraft at stage 1 and the X_t and $\bar{X}_t$ are defined recursively by

$$\begin{array}{ll} X_2 = Z_{ij}(X_1) & \bar{X}_2 = Z_{kl}(X_1) \\ X_3 = Z_{ij}(X_2) & \bar{X}_3 = Z_{kl}(\bar{X}_2) \\ \vdots & \vdots \\ X_T = Z_{ij}(X_{T-1}) & \bar{X}_T = Z_{kl}(\bar{X}_{T-1}) \end{array} \quad (21)$$

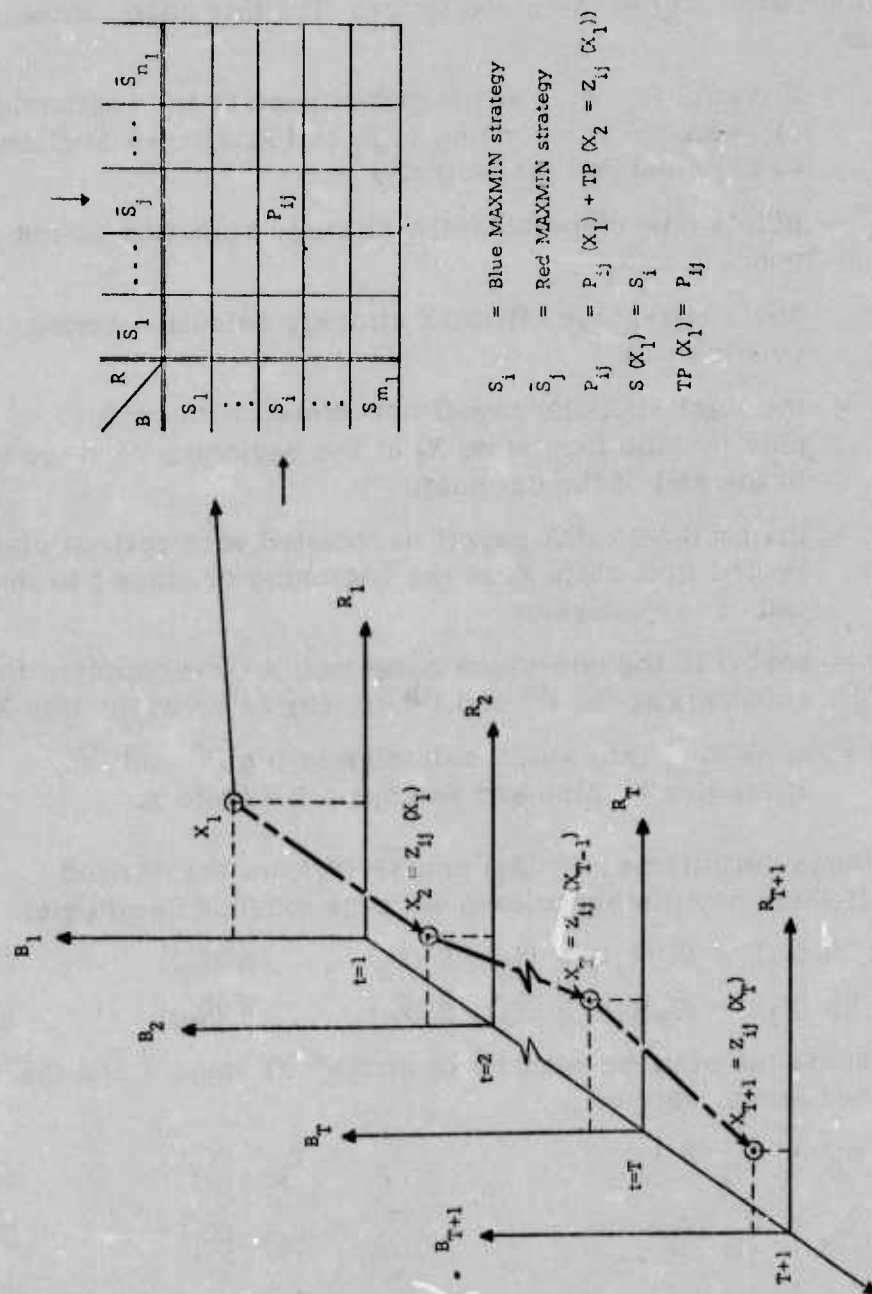


FIGURE 8
DYNAMIC PROGRAMMING SOLUTION FOR
MAXMIN STRATEGIES AND BOUNDS

with i = index of Blue's MAXMIN strategy for the current stage
 j = index of Red's MAXMIN strategy for the current stage
 k = index of Blue's MINMAX strategy for the current stage
 l = index of Red's MINMAX strategy for the current stage

The dynamic programming approach for solving for $TP(X_1)$, $ES(X_1)$, $\overline{TP}(X_1)$, and $\overline{ES}(X_1)$ separates the solution for the MAXMIN total payoff and extended strategy from the MINMAX counterparts. Although all descriptions which follow concentrate on the MAXMIN solution, the MINMAX solution technique is exactly analogous.

Idealized Approach

To compute $TP(X_1)$ and $ES(X_1)$ using a general dynamic programming procedure, one begins at the beginning of the last stage of the campaign and computes one-stage MAXMIN payoffs and strategies, $TP(X_T)$ and $S(X_T)$, for all possible states X_T . The i, j^{th} payoff, P_{ij} , in the MAXMIN game matrix for each state X_T is given by

$$P_{ij} = P_{ij}(X_T) + TP(X_{T+1} = Z_{ij}(X_T)) \quad (22)$$

where $P_{ij}(X_T)$ is the one-stage payoff and $TP(X_{T+1} = Z_{ij}(X_T))$ is the contribution of undamaged aircraft at the end of the war, B_{T+1} and R_{T+1} , to the value of the overall objective function (Equation 2).

After $TP(X_T)$ and $S(X_T)$ have been computed for all states X_T , these values are stored and the process moves backward to the beginning of stage $T-1$. Using the $TP(X_T)$ just computed, the elements in the payoff matrix for each stage X_{T+1} are now given by

$$P_{ij} = P_{ij}(X_{T-1}) + TP(X_T = Z_{ij}(X_{T-1})) \quad (23)$$

where $P_{ij}(X_{T-1})$ is the payoff contribution of the current stage and $TP(X_T = Z_{ij}(X_{T-1}))$ is the MAXMIN payoff associated with optimal play thereafter. Once again, a Blue MAXMIN strategy is computed for each game matrix along with the cumulative MAXMIN payoff $TP(X_{T-1})$ and each is stored for all possible states X_{T-1} . Processing moves backward to the preceding stage in time, game matrices are generated for all states, etc.

Eventually, through this iterative process, strategies and payoffs can be generated for all stages and states from stage T back to the beginning of stage 1. Since X_1 , the hypothesized starting resource level, is

a point in the state space at the beginning of stage 1, the solution is complete. TP (X_1) is available immediately, while the one-stage strategies which compose ES (X_1) can be retrieved from storage by tracing through the states using the attrition map Z_{ij} . Perhaps even more important, as a by-product of the dynamic programming approach, solutions for all other X_t are also available since they have been stored during the processing required to solve for X_1 . By simply retrieving the stored results, solutions for all shorter campaigns less than T stages which begin with any number of aircraft on either side can be easily generated.

Problems

Precise implementation of the general dynamic programming algorithm as described above requires evaluation of one-stage game for every possible state of every possible stage. The number of such states in a reasonable sized game is huge, even for the case in which each side has only one aircraft type. For example, each side might reasonably start with 1000 aircraft, making the number of possible (B_t, R_t) pairs more than one million.

Intuitively, one would suspect states which differ by only a few aircraft would produce approximately the same solution. ATACM exploits this intuitive feel by imposing a discrete grid upon the state space at each stage in a manner analogous to that used in DYGM (Reference 4). If a grid such as that shown in Figure 9 were imposed, a tractable approach would be to explicitly compute one-stage strategies and payoffs for only the discrete grid points using the dynamic programming procedure described above. Unfortunately, as shown in Figure 9, the $Z_{ij}(X_t)$ for a grid point X_t would generally not lie on a grid point in the subsequent stage's state space. Since TP ($Z_{ij}(X_t)$) is necessary to compute the elements in the one-stage game matrix (Equation (22)), an approximation technique is required for computing payoffs associated with points not on the grid.

Possible Approximations

One possible approximation technique for computing TP ($X_{t+1} = Z_{ij}(X_t)$) would be to linearly interpolate using the explicit payoffs for grid points adjacent to X_{t+1} . It can be shown that as the grid becomes finer the strategies which would result from using linear interpolation would approach those produced by the idealized dynamic programming solution. Similarly, the payoffs produced would approach the idealized lower bound TP (X_1), but not necessarily from below. In other words, although the

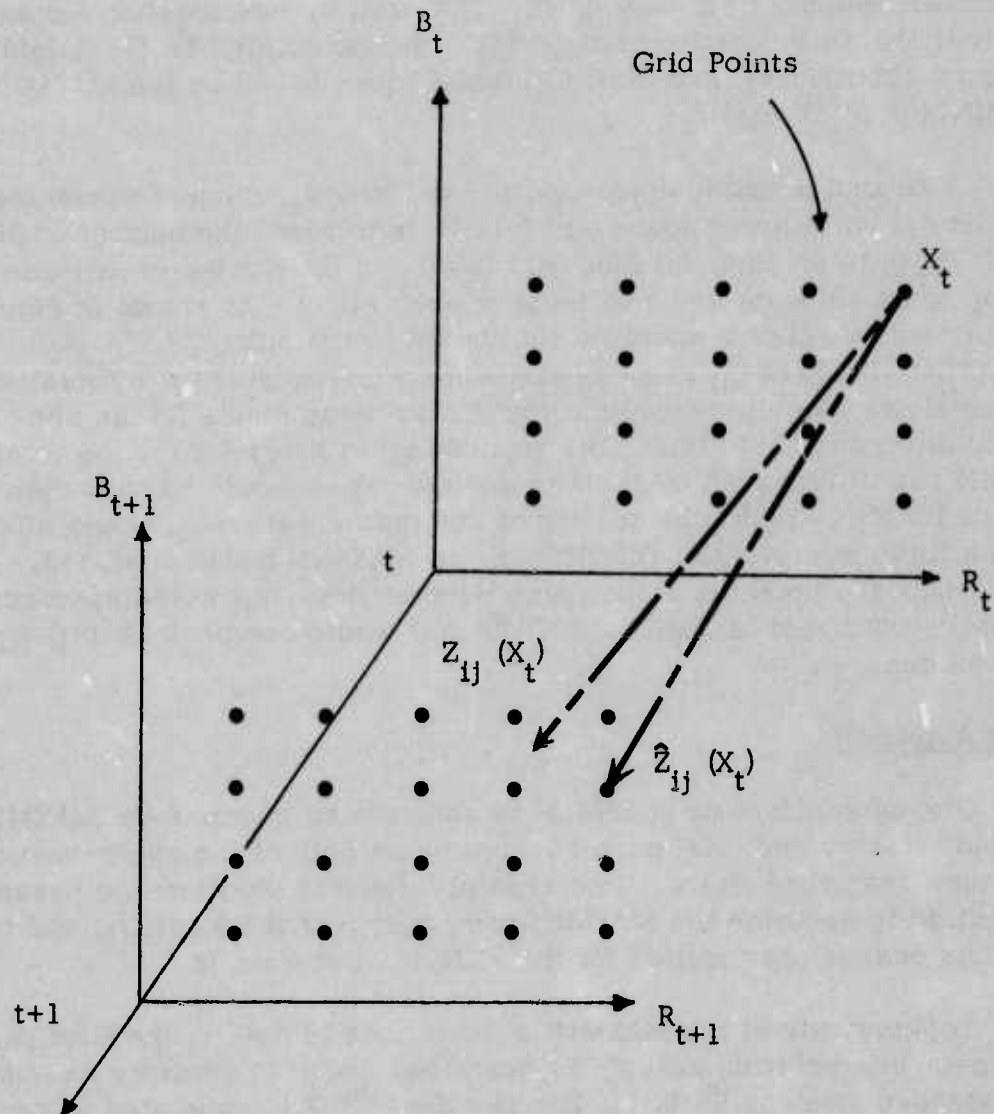


FIGURE 9
DYNAMIC PROGRAMMING
APPROXIMATIONS

approximate extended strategy $\hat{ES}(X_1)$ produced by interpolation would intuitively be a good estimate of $ES(X_1)$, the associated $\hat{TP}(X_1)$ might be greater than $TP(X_1)$ and thus an invalid lower bound on the MAXMIN vs. MINMAX total payoff.

A second possible approximation technique, which is guaranteed to produce a valid lower bound on $TP(X_1)$, is to round the number of Blue aircraft down to an adjacent Blue grid level and the number of Red aircraft up to an adjacent Red grid level at each stage. As shown in Figure 9, such a rounding scheme would be equivalent to replacing $TP(Z_{ij}(X_t))$ by $TP(\hat{Z}_{ij}(X_t))$ where $\hat{Z}_{ij}$ is an approximate mapping which incorporates the Blue-down, Red-up rounding criteria. Because Blue's forces are rounded down and Red's forces are rounded up at every stage, the total MAXMIN payoff produced by such an approximation would be less than or equal to $TP(X_1)$. Thus, the quality of the approximation $\hat{Z}_{ij}$ would affect only the tightness, not the validity, of the MAXMIN bound produced. As the grid imposed upon the state space became finer, $\hat{Z}_{ij}$ would approach Z_{ij} and the computed MAXMIN payoff $\hat{TP}(X_1)$ would approach $TP(X_1)$ from below as desired.

ATACM Approach

The approach used in ATACM to generate an approximate MAXMIN extended strategy and total payoff incorporates both of the approximation techniques described above. Two separate dynamic programming passes are required to generate the MAXMIN components of the solution, and two analogous passes are required for the MINMAX components.

Looking only at the MAXMIN calculations in detail, the first pass uses linear interpolation exactly as described above to generate an approximate extended strategy $\hat{ES}(X_1)$. The payoffs, $\hat{TP}(X_t)$, generated at each stage and state are used only to compute $\hat{ES}(X_1)$ and are discarded after the one-stage strategies are stored.

The second pass, designed to produce a lower bound on the MAXMIN total payoff $TP(X_1)$, uses the $\hat{S}(X_t)$ stored during the first pass as fixed Blue strategies against which Red performs a MINMAX pass using the rounding scheme described above. As shown in Figure 10, in this second pass the game matrix for each stage and state has only one Blue strategy. Column maximums in these one-stage games are the single one-stage payoffs corresponding to each Blue strategy, and the MINMAX pass reduces to the calculation of the minimum payoff Red can achieve against $\hat{ES}(X_1)$.

R B	$\bar{S}_1$	$\bar{S}_2$	$\bar{S}_3$	$\dots$	$\bar{S}_{n_1}$
	P_{i1}	P_{i2}	P_{i3}	$\dots$	P_{in_1}
$\hat{S}(\alpha_1)$					

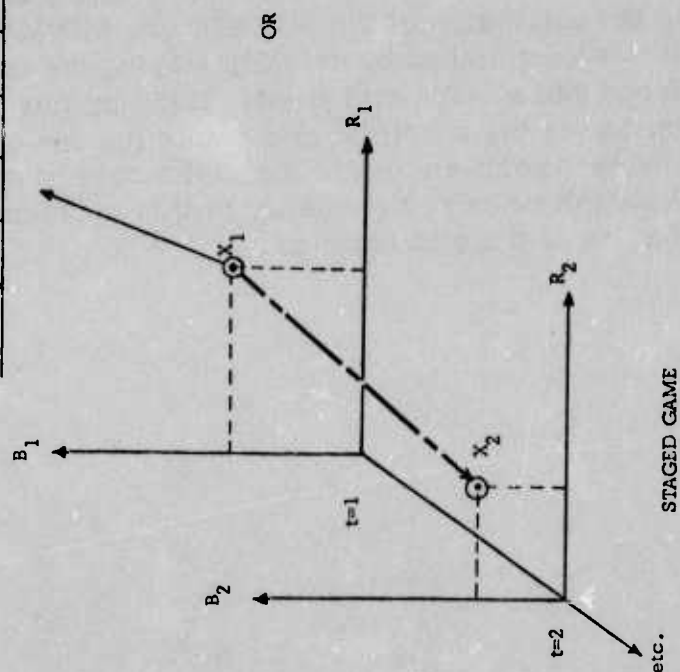


FIGURE 10
ALTERNATIVE REPRESENTATIONS
OF THE SECOND DYNAMIC PROGRAMMING
PASS FOR COMPUTING $TP(\alpha_1)$

	R	$\bar{ES}_1$	$\bar{ES}_2$	$\bar{ES}_3$	$\bar{ES}_N$
		TP_{i1}	TP_{i2}	TP_{i3}	TP_{iN}
B	$\hat{S}(\alpha_1)$				

EXTENDED GAME

To see that this second MINMAX pass produces a lower bound on $TP(X_1)$, consider two cases.

- If $\hat{ES}(X_1)$ is the same as $ES(X_1)$, and no Blue-down/Red-up rounding is required, the best Red can do in the MINMAX pass is to generate Red's MAXMIN extended strategy, which, by definition, produces a total payoff exactly equal to $TP(X_1)$. If rounding is required, the total payoff would clearly be less than or equal to $TP(X_1)$.
- If $\hat{ES}(X_1)$ is not equal to $ES(X_1)$, and rounding is not required, the minimum total payoff Red can achieve in the MINMAX pass is the row minimum corresponding to $\hat{ES}(X_1)$ in the extended game of Figure 10. Since $TP(X_1)$ is defined as the maximum over all row minimums, $TP(X_1)$ must be bounded from below by the MINMAX payoff. As before, if rounding is required the value of the MINMAX payoff can only be reduced.

Finally, after two analogous dynamic programming passes for computing estimates of Red's MINMAX extended strategy $\bar{ES}(X_1)$ and the upper objective function bound $TP(X_1)$, the solution is virtually complete. All that remains is the estimation of the MAXMIN vs. MINMAX payoff for starting state X_1 which is accomplished by actually playing the one-stage strategies stored for Blue and Red at each grid point. If during this calculation a $Z_{ij}(X_t)$ does not fall on one of the specified grid points the one-stage strategies stored for the nearest point are used. As in the case of computing the MAXMIN and MINMAX bounds, the quality of this approximation depends upon the coarseness of the grid imposed.

PAB-249

REFERENCES

1. R. J. Galiano and F. A. Miercort, "Results of a Survey of Tactical Air Campaign Models," Contract No. ACDA/PAB-249, KETRON, Inc., November 1974.
2. Jerome Bracken, "Two Optimal Sortie Allocation Models," Paper P-992, Institute for Defense Analyses, December 1973.
3. S. Bonder, "VECTOR-O, The Battle Model Prototype," WSEG Report 222, Weapons System Evaluation Group, December 1973.
4. Control Analysis Corporation, "Development of an Algorithm to Solve Multi-Stage Games," 24 May 1973.

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APPENDIX A

ATACM USER'S GUIDE

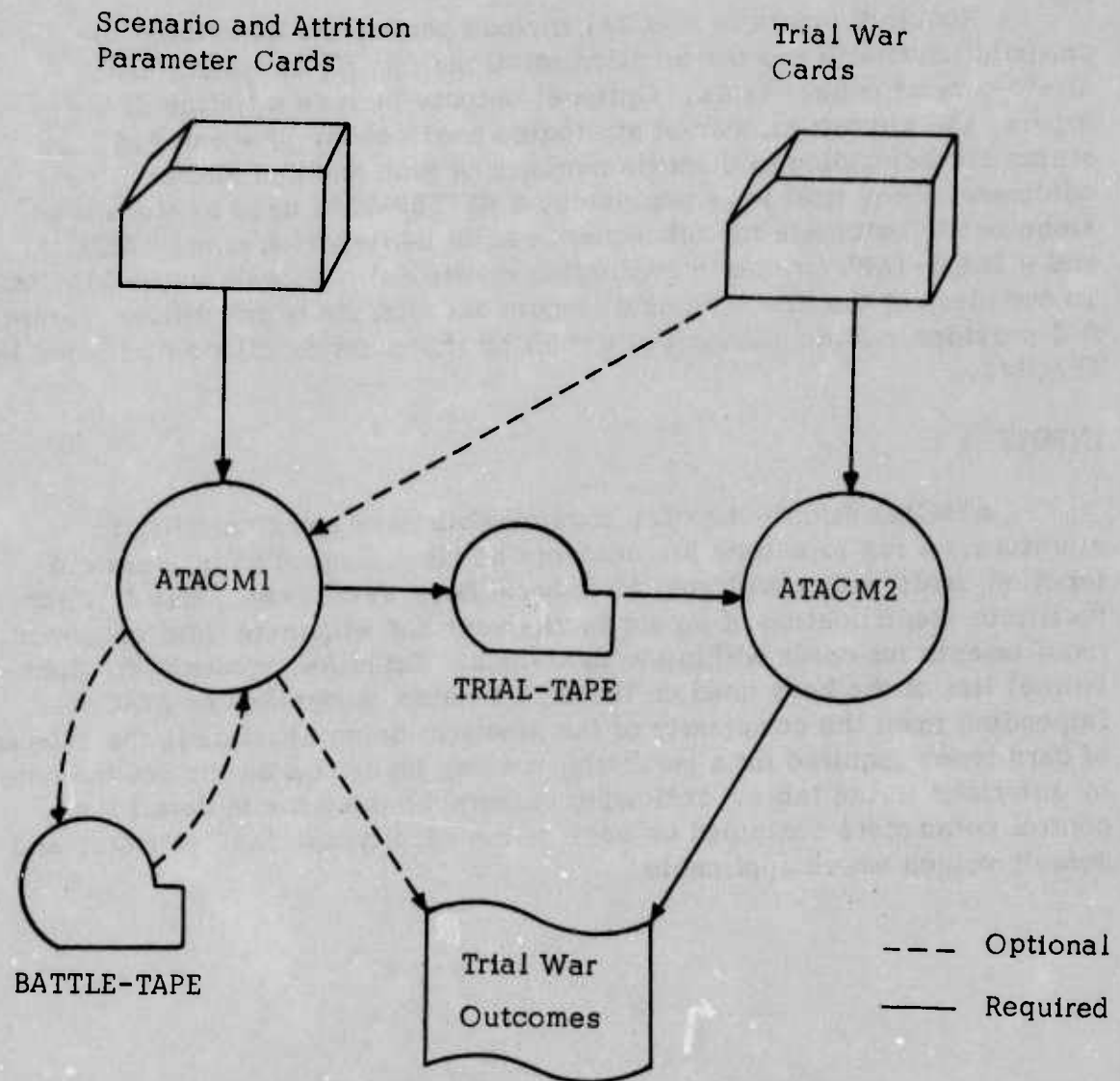
This appendix is a guide to the use of ATACM. Following sections describe the inputs, the operation, and the outputs of the model.

GENERAL OVERVIEW

The computer model ATACM was developed by the Arms Control and Disarmament Agency as a tool for studying the impact of various force postures upon the outcome of a tactical airwar in Europe between NATO and Warsaw Pact forces. ATACM treats an air campaign as a zero-sum staged game between opposing forces, Blue and Red, each consisting of air and ground forces. Most of the emphasis in the current version of ATACM is upon air force interactions although a simplistic representation of the ground war is also included. The model uses dynamic programming to generate for each stage and state of the campaign optimal aircraft allocation strategies and associated MAXMIN/MINMAX bounds on a user-specified objective function.

As currently implemented, ATACM consists of two FORTRAN programs, ATACM1 and ATACM2, designed for use on a CDC 6600 computer. ATACM1 generates optimal strategies and associated objective function bounds for each stage and state and uses these values to evaluate the outcomes of trial wars of specified length which are initiated with user-specified numbers of Blue and Red aircraft. In addition to the outcomes of the trial wars, ATACM1 can output to magnetic tape one-stage battle assessments (BATTLE-TAPE) for use in subsequent runs of ATACM1, and optimal strategies and bounds (TRIAL-TAPE) for use in subsequent trial war evaluations using ATACM2. To evaluate additional trial wars, ATACM2 reads the TRIAL-TAPE and uses the information it contains to process trial war requests and produce outputs identical to those which would have been produced if the requests had been evaluated during the execution of ATACM1. Thus, for a given set of scenario and attrition parameters, only a single execution of ATACM1 is necessary regardless of when or how many trial war evaluations are eventually required.

Figure A-1 presents a schematic representation of how ATACM1, ATACM2, the BATTLE-TAPE, and the TRIAL-TAPE interrelate.



AN OVERVIEW OF ATACM'S OPERATION

FIGURE A-1

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ATACM1

Required inputs to ATACM1 include parameters describing the campaign scenario and the attrition relationships for air-to-air and air-to-ground engagements. Optional outputs include a listing of the inputs, the aircraft allocation strategies available to Blue and Red, the states corresponding to discrete numbers of Blue and Red aircraft, the outcomes of any trial wars requested, a BATTLE-TAPE used to store one-stage battle outcomes for subsequent use in perturbation runs of ATACM1, and a TRIAL-TAPE for use in evaluating additional trial wars using ATACM2. To complement the discussions of inputs and outputs which follow, Figure A-2 provides a logical flowchart depicting the major functions performed by ATACM1.

INPUTS

ATACM1 affords the user considerable ease and flexibility in structuring a run to satisfy his analysis needs. Control parameters are input on cards with identifying alphabetic keys in columns 1 thru 5 which facilitate identification of inputs by the user and eliminate rigid sequence requirements for cards within the data deck. Table A-1 presents an alphabetical list of the keys used on the inputs cards recognized by ATACM1. Depending upon the complexity of the scenario being simulated, the number of card types required for a particular run can be as few as the six indicated by asterisks in the table. Following paragraphs describe in detail the control parameters contained on each of the card types, their formats, and default values where applicable.

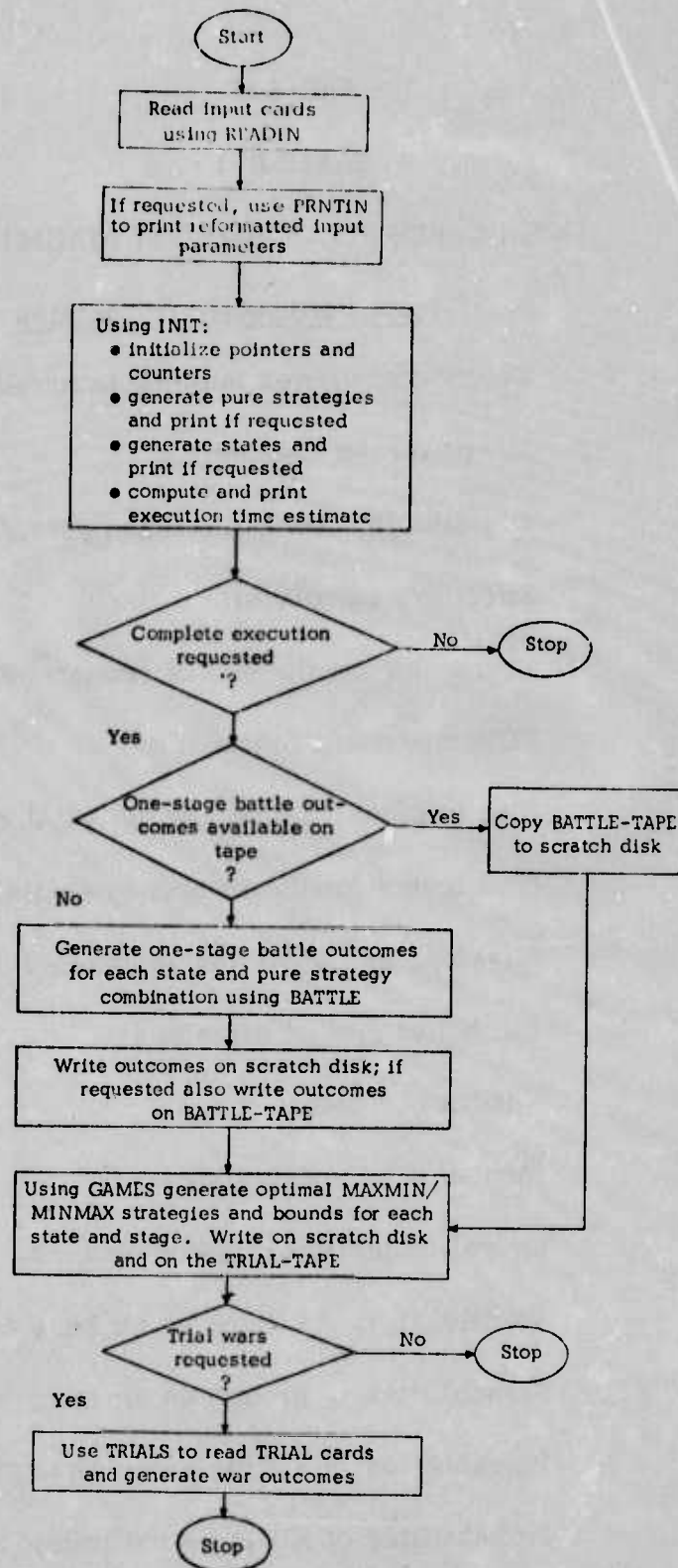


FIGURE A-2
LOGICAL FLOWCHART OF ATACM1

TABLE A-1

INPUT CARDS RECOGNIZED BY ATACM1

<u>Card Key</u>	<u>Input Parameters It Contains</u>
ABAF	Fraction of planes vulnerable to ABA
CASF	Firepower per CAS sortie
DFRC	Division firepower reduction per CAS sortie
DIVF	Firepower per division
END [*]	Flag to signal the end of scenario and attrition inputs
FEBAM	FEBA movement function
FINIS	Flag to signal the end of the TRIAL cards
GRID ^{**}	Grid levels for the number of available planes
MISS ^{**}	Missions assigned and associated sortie rates
NDIV	Number of ground divisions
NSAM	Number of SAMs
NSHL	Number of air base shelters
OWGHT	Overall objective function weights
PKAA	Probabilities of killing an air base attacker
PKAD	Probabilities of killing an air base defender
PKAE	Probabilities of killing an air base attacker escort
PKBA	Probabilities of killing a battlefield attacker
PKBD	Probabilities of killing a battlefield defender

TABLE A-1 (Cont'd)

<u>Card Key</u>	<u>Input Parameters It Contains</u>
PKBE	Probabilities of killing a battlefield attacker escort
PKFA	Probabilities of killing a forward SAM attacker
PKFS	Probabilities of killing a forward SAM
PKNS	Probabilities of killing a non-sheltered plane
PKRA	Probabilities of killing a rear SAM attacker
PKRS	Probabilities of killing a rear SAM
PKSH	Probabilities of killing a sheltered plane
REIN	Plane reinforcements by stage
RUN [*]	Run options and title
STAGE [*]	Number of stages and engagement cycles per stage
STRT ^{**}	Strategy specifications by stage
TRIAL	Initial number of planes and length of a TRIAL war
VALU	Value of an undamaged plane at end of war
WGHT	Objective function weights by stage

* At least one card required for every run.

**At least one card required for each side for every run.

ABAF Card

One ABAF card for each aircraft type is used to specify the fraction of the aircraft assigned to each mission which is vulnerable to airbase attack. By specifying different fractions, aircraft flying selected missions can be made invulnerable or partially vulnerable to the opponent's airbase attack. Generally larger fractions are more applicable for aircraft prosecuting missions close to friendly airbases (e.g., ABD, BD, CAS, and forward SAM suppression) than for aircraft flying missions deep in the opponent's territory (e.g., ABA and rear SAM suppression). Aircraft whose fractions are set equal to zero might include planes housed in impenetrable shelters or long-range bombers flying from a sanctuary base.

The ABAF card is read under

FORMAT (A4, A1, I1, 4X, 8F5.0)

and its fields are assigned as follows:

- A4 - (1-4) - "ABAF"
- A1 - (5) - "B" or "R" to indicate the vulnerability fractions are for either a Blue or Red aircraft type
- I1 - (6) - the number of the aircraft type for which the fractions are applicable
- 8F5.0 - (11-50) - the fraction of the aircraft flying a particular mission which is vulnerable to airbase attack. The fraction specified in columns 11-15 corresponds to the 1st mission assigned on the associated MISS card, columns 16-20 to the 2nd, etc. Default value is 1.

CASF Card

One CASF card for each side is used to specify the firepower delivered per CAS sortie flown. The units used to specify firepower on the CAS card must be consistent with those used on both the DFRC and the DIVF cards. The CASF card is read under

FORMAT (A4, A1, 5X, 4F5.4)

and its fields are defined as follows:

- A4 - (1-4) - "CASF"

- A1 - (5) - "B" or "R" to indicate the firepower rates are for either the Blue or Red side
- 4F5.4 - (11-30) - the firepower delivered per CAS sortie by aircraft of types 1 thru 4 respectively. Default value is 0.

DFRC Card

One DFRC card for each side is used to specify the ground division firepower reduction produced by each CAS sortie flown. The units used to specify firepower reduction on the DFRC card must be consistent with those used on both the CASF and the DIVF cards. The DFRC card is read under

FORMAT (A4, A1, 5X, 4F5.4)

and its fields are defined as follows:

- A4 - (1-4) - "DFRC"
- A1 - (5) - "B" or "R" to indicate the ground division firepower reductions are produced by either a Blue or Red CAS sortie.
- 4F5.4 - (11-30) - the ground division firepower reduction resulting from a CAS sortie flown by aircraft of types 1 thru 4 respectively. Default value is 0.

DIVF Card

One DIVF card for each side is used to specify the firepower per ground division. The units used to specify firepower on the DIVF card must be consistent with those used on both the CASF and the DFRC card. The DIVF card is read under

FORMAT (A4, A1, 5X, F5.0)

and its fields are assigned as follows:

- A4 - (1-4) - "DIVF"
- A1 - (5) - "B" or "R" to indicate the firepower is specified for each Blue or Red ground divisions
- F5.0 - (11-15) - the firepower per ground division. Default value is 0.

END Card

The END card signals the end of the scenario and attrition parameter cards required by ATACM1 and the beginning of the optional TRIAL cards. The END card is read under

FORMAT (A3)

and its only field contains

A3 - (1-3) - "END"

FEBAM Card

As many as four FEBAM cards may be used to specify the rate of FEBA movement per cycle as a function of the ratio of Blue ground firepower to Red ground firepower. Any functional relationship desired can be input by specifying up to 28 points that lie on the graph of the desired function. The model linearly interpolates between these points to yield a piecewise linear approximation. The quality of the approximation depends upon the shape of the desired graph and the number and location of points chosen. The coordinates of the points are read from the FEBAM card under

FORMAT (A5, I1, 4X, 7(2F5.0))

and the fields are assigned as follows:

A5 - (1-5) - "FEBAM"

I1 - (6) - card sequence number. Seven points (smallest firepower ratio to largest) are input on each card to a maximum of four cards or 28 points. The first card has sequence number 1, the second card (if required) has sequence number 2, etc.

7(2F5.0)-(11-80) - x and y coordinates of the ith point on the graph

x = ratio of Blue ground firepower to
Red ground firepower (always positive)

y = FEBA movement per engagement cycle
(positive movement corresponds to
Blue advance)

Default value for (x,y) is (0,0).

FINIS Card

The FINIS card signals the end of the TRIAL cards and consequently the end of the input data. The FINIS card is read under

FORMAT (A5)

and its only field contains

A5 - (1-5) - "FINIS"

GRID Card

One GRID card for each aircraft type is required to indicate the discrete numbers of aircraft for which optimal plays and associated bounds are explicitly computed. The GRID card is read under

FORMAT (A4, A1, I1, 4X, 11I5)

and its fields are assigned as follows:

- A4 - (1-4) - "GRID"
- A1 - (5) - "B" or "R" to indicate the grid levels are for either a Blue or Red aircraft type
- I1 - (6) - the number of aircraft type for which the grid levels are applicable. Aircraft types are numbered in ascending order from 1 to 4.
- 11I5 - (11-65) - the discrete numbers of aircraft of the specified type for which optimal plays and bounds are explicitly generated. The first grid level must be 0 followed by remaining grid levels listed in ascending order. The maximum number of grid levels for an aircraft type is 11. The largest grid level should be the upper bound on the initial number of planes of this type plus the total number of reinforcements which can be added during a trial war.

MISS Card

One MISS card is required for each aircraft type to specify its minimum allocation fraction, the missions it can prosecute, and the asso-

ciated sortie rates. Each MISS card is read under

FORMAT (A4, A1, I1, 4X, I2, 1X, 8(2X,I1), 3X, 8F5.2)

and the fields are assigned as follows:

- A4 - (1-4) - "MISS"
- A1 - (5) - "B" or "R" to indicate the mission information is for either a Blue or Red aircraft type
- I1 - (6) - the number of the aircraft type
- I2 - (11-12) - the denominator of the minimum allocation fraction for this aircraft type. The minimum allocation fraction is the smallest fraction of the total number of planes which can be assigned to any mission. All fractional assignments are integer multiples of the minimum allocation fraction.
- 8(2X,I1)-(14-37) - numerical codes (see Table A-2) corresponding to the missions to which planes of the specified type may be assigned. A maximum of eight missions may be specified for an aircraft type.
- 8F5.2-(41-80) - sortie rates per engagement cycle associated with the missions specified in the preceding columns. The sortie rates must be specified in the same relative order as the mission codes.

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TABLE A-2

AIR MISSION CODES

<u>Code</u>	<u>Mission</u>
1	Close air support (CAS)
2	Airbase attack (ABA)
3	Battlefield defense (BD)
4	Airbase defense (ABD)
5	Close air support escort (CASE)
6	Airbase attack escort (ABAE)
7	Forward SAM suppression (FSS)
8	Rear SAM suppression (RSS)
9	No assigned mission

NDIV Card

One NDIV card for each side is used to specify the number of ground divisions available. The NDIV card is read under

FORMAT (A4, A1, 5X, I5)

and its fields are defined as follows:

A-4 - (1-4) - "NDIV"

A1 - (5) - "B" or "R" to indicate the number of divisions correspond to either the Blue or Red side

I5 - (11-15) - the number of ground divisions. Default value is 0.

NSAM Card

One NSAM card for each side is used to specify the number of for-

ward and rear SAMs available. The NSAM card is read under

FORMAT (A4, A1, 5X, 2I5)

and its fields are defined as follows:

A4 - (1-4) - "NSAM"

A1 - (5) - "B" or "R" to indicate the number of SAMs correspond to either the Blue or Red side

I5 - (11-15) - the number of forward SAMs. Default value is 0.

I5 - (16-20) - the number of rear SAMs. Default value is 0.

NSHL Card

One NSHL card for each side is used to specify the number of aircraft shelters available. The NSHL card is read under

FORMAT (A4, A1, 5X, I5)

and its fields are assigned as follows:

A4 - (1-4) - "NSHL"

A1 - (5) - "B" or "R" to indicate the number of shelters correspond to either the Blue or Red side

I5 - (11-15) - the number of aircraft shelters. Default value is 0.

OWGHT Card

The basic form of the overall function used to generate optimal conservative strategies is given by

$$F = w_1 f_1 + w_2 f_2 + w_3 f_3 \quad (A-1)$$

where f_1 = difference of total Blue minus total Red CAS firepower

f_2 = difference of total Blue minus total Red (CAS firepower + ground firepower)

and f_3 = total FEBA movement (positive movement corresponds to Blue advance).

One OWGHT card is used to specify the values of the weights, w_1 , w_2 , and w_3 to be used in computing F . The OWGHT card is read under

FORMAT (A5, 5X, 3F5.0)

and its fields are defined as follows:

- A5 - (1-5) - "OWGHT"
- F5.0 - (11-15) - the value of w_1 . Default value is 1.
- F5.0 - (16-20) - the value of w_2 . Default value is 0.
- F5.0 - (21-25) - the value of w_3 . Default value is 0.

PKAA Card

For each aircraft type assigned an airbase attack (ABA) mission, one PKAA card is required to specify the probabilities that such an aircraft is killed by an opposing airbase defender or SAM in a one-on-one engagement. The PKAA card is read under

FORMAT (A4, A1, I1, 4X, 4F5.3, 5X, 2F5.3)

and its fields are defined as follows:

- A4 - (1-4) - "PKAA"
- A1 - (5) - "B" or "R" to indicate the ABA aircraft belongs to either the Blue or Red forces
- I1 - (6) - the number of the ABA aircraft type
- 4F5.3-(11-30) - the probability the ABA aircraft is killed by opposing ABD's of types 1 thru 4 respectively. Default value is 0.
- F5.3-(36-40) - the probability the ABA aircraft is killed by an opposing forward SAM. Default value is 0.
- F5.3 - (41-45) - the probability the ABA aircraft is killed by an opposing rear SAM. Default value is 0.

PKAD Card

For each aircraft type assigned an airbase defense (ABD) mission, one PKAD card is required to specify the probabilities that such an aircraft is killed by an opposing airbase attacker or airbase attack escort in a one-on-one engagement. The PKAD card is read under

FORMAT (A4, A1, I1, 4X, 4F5.3, 5X, 4F5.3)

and its fields are assigned as follows:

- A4 - (1-4) - "PKAD"
- A1 - (5) - "B" or "R" to indicate the ABD aircraft belongs to either the Blue or Red forces
- I1 - (6) - the number of the ABD aircraft type
- 4F5.3- (11-30) - the probability the ABD aircraft is killed by opposing ABA's of types 1 thru 4 respectively. Default value is 0.
- 4F5.3- (36-55) - the probability the ABD aircraft is killed by opposing ABA escorts of types 1 thru 4 respectively. Default value is 0.

PKAE Card

For each aircraft type assigned an airbase attack escort (ABAE) mission, one PKAE card is required to specify the probabilities that such an aircraft is killed by an opposing airbase defender or SAM in a one-on-one engagement. The PKAE card is read under

FORMAT (A4, A1, I1, 4X, 4F5.3, 5X, 2F5.3)

and its fields are defined as follows:

- A4 - (1-4) - "PKAE"
- A1 - (5) - "B" or "R" to indicate the ABAE aircraft belongs to either the Blue or Red forces
- I1 - (6) - the number of the ABAE aircraft type
- 4F5.3- (11-30) - the probability the ABAE aircraft is killed by opposing ABD's of types 1 thru 4 respectively. Default value is 0.
- F5.3 - (36-40) - the probability the ABAE aircraft is killed by an opposing forward SAM. Default value is 0.
- F5.3 - (41-45) - the probability the ABAE aircraft is killed by an opposing rear SAM. Default value is 0.

PKBA Card

For each aircraft type assigned a battlefield attack (CAS) mission, one PKBA card is required to specify the probabilities that such an aircraft

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is killed by an opposing battlefield defender or forward SAM in a one-on-one engagement. The PKBA card is read under

FORMAT (A4, A1, I1, 4X, 4F5.3, 5X, F5.3)

and its fields are defined as follows:

- A4 - (1-4) - "PKBA"
- A1 - (5) - "B" or "R" to indicate the CAS aircraft belongs to either the Blue or Red forces
- I1 - (6) - the number of the CAS aircraft type
- 4F5.3- (11-30) - the probability the CAS aircraft is killed by opposing BD's of types 1 thru 4 respectively. Default value is 0.
- F5.3- (36-40) - the probability the CAS aircraft is killed by an opposing forward SAM. Default value is 0.

PKBD Card

For each aircraft type assigned a battlefield defense (BD) mission, one PKBD card is required to specify the probabilities that such an aircraft is killed by an opposing battlefield attacker (CAS) or battlefield attack escort (CASE) in a one-on-one engagement. The PKBD card is read under

FORMAT (A4, A1, I1, 4X, 4F5.3, 5X, 4F5.3)

and its fields are defined as follows:

- A4 - (1-4) - "PKBD"
- A1 - (5) - "B" or "R" to indicate the BD aircraft belongs to either the Blue or Red forces
- I1 - (6) - the number of the BD aircraft type
- 4F5.3- (11-30) - the probability the BD aircraft is killed by opposing CAS's of types 1 thru 4 respectively. Default value is 0.
- 4F5.3- (36-55) - the probability the BD aircraft is killed by opposing CAS escorts of types 1 thru 4 respectively. Default value is 0.

PKBE Card

For each aircraft type assigned a battlefield attack escort (CASE) mission, one PKBE card is required to specify the probabilities that such an aircraft is killed by an opposing battlefield defender or forward SAM in a one-on-one engagement. The PKBE card is read under

FORMAT (A4, A1, I1, 4X, 4F5.3, 5X, F5.3)

and its fields are defined as follows:

- A4 - (1-4) - "PKBE"
- A1 - (5) - "B" or "R" to indicate the CASE aircraft belongs to either the Blue or Red forces
- I1 - (6) - the number of the CASE aircraft type
- 4F5.3- (11-30) - the probability the CASE aircraft is killed by opposing BD's of types 1 thru 4 respectively. Default value is 0.
- F5.3- (36-40) - the probability the CASE aircraft is killed by an opposing forward SAM. Default value is 0.

PKFA Card

For each aircraft type assigned a forward SAM suppression (FSS) mission, one PKFA card is required to specify the probability that such an aircraft is killed by an opposing forward SAM in a one-on-one engagement. The PKFA card is read under

FORMAT (A4, A1, I1, 4X, F5.3)

and its fields are defined as follows:

- A4 - (1-4) - "PKFA"
- A1 - (5) - "B" or "R" to indicate the FSS aircraft belongs to either the Blue or Red forces
- I1 - (6) - the number of the FSS aircraft type
- F5.3- (11-15) - the probability the FSS aircraft is killed by an opposing forward SAM. Default value is 0.

PKFS Card

One PKFS card for each side is used to specify the probabilities that a forward SAM is killed by forward SAM suppressors. The PKFS card is read under

FORMAT (A4, A1, 5X, 4F5.3)

and its fields are defined as follows:

- A4 - (1-4) - "PKFS"
- A1 - (5) - "B" or "R" to indicate the SAM being attacked belongs to either the Blue or Red forces
- 4F5.3 - (11-30) - the probability the SAM is killed by opposing FSS's of types 1 thru 4 respectively. Default value is 0.

PKNS Card

One PKNS card for each side is used to specify the probabilities that a non-sheltered aircraft on the airbase is killed by airbase attackers. These kill probabilities are only applicable to the fraction specified as vulnerable to airbase attack on the ABAF card. The PKNS card is read under

FORMAT (A4, A1, 5X, 4F5.3)

and its fields are assigned as follows:

- A4 - (1-4) - "PKNS"
- A1 - (5) - "B" or "R" to indicate the airbase being attacked is either Blue or Red
- 4F5.3 - (11-30) - the probability a non-sheltered, vulnerable aircraft on the airbase is killed by opposing ABA's of types 1 thru 4 respectively. Default value is 0.

PKRA Card

For each aircraft type assigned a rear SAM Suppression (RSS) mission, one PKRA card is required to specify the probabilities that such an aircraft is killed by an opposing SAM in a one-on-one engagement. The PKRA card is read under

FORMAT (A4, A1, I1, 4X, 2F5.3)

and its fields are defined as follows:

- A4 - (1-4) - "PKRA"
- A1 - (5) - "B" or "R" to indicate the RSS aircraft belongs to either the Blue or Red forces
- I1 - (6) - the number of the RSS aircraft type
- F5.3- (11-15) - the probability the RSS aircraft is killed by an opposing forward SAM. Default value is 0.
- F5.3- (16-20) - the probability the RSS aircraft is killed by an opposing rear SAM. Default value is 0.

PKRS Card

One PKRS card for each side is used to specify the probabilities that a rear SAM is killed by rear SAM suppressors. The PKRS card is read under

FORMAT (A4, A1, 5X, 4F5.3)

and its fields are assigned as follows:

- A4 - (1-4) - "PKRS"
- A1 - (5) - "B" or "R" to indicate the SAM being attacked belongs to either the Blue or Red forces
- 4F5.3- (11-30) - the probability the SAM is killed by opposing RSS's of types 1 thru 4 respectively. Default value is 0.

PKSH Card

One PKSH card for each side is used to specify the probabilities that a sheltered aircraft on the airbase is killed by airbase attackers.

PKSH card is read under

FORMAT (A4, A1, 5X, 4F5.3)

and its fields are assigned as follows:

- A4 - (1-4) - "PKSH"
- A1 - (5) - "B" or "R" to indicate the airbase being attacked is either Blue or Red
- 4F5.3- (11-30) - the probability a sheltered, vulnerable aircraft on the airbase is killed by opposing ABA's of types 1 thru 4 respectively. Default value is 0.

REIN Card

The REIN card is used to specify numerical and/or fractional aircraft reinforcements as a function of stage. The REIN card is read under

FORMAT (A4, A1, 1X, I2, 4F5.0, 5X, 4F5.0)

and its fields are assigned as follows:

- A4 - (1-4) - "REIN"
- A1 - (5) - "B" or "R" to indicate the specified reinforcements are for either the Blue or Red side
- I2 - (7-8) - the number of the stage when the reinforcements arrive. In every case reinforcement occurs at the beginning of the stage before attrition is computed.
- 4F5.0- (11-30) - the number of aircraft of types 1 thru 4 respectively added (or subtracted if entry is negative) at the beginning of the specified stage. Default value is 0.
- 4F5.0- (36-55) - the fractional increase (or decrease if entry is negative) in the number of aircraft of types 1 thru 4 respectively at the beginning of the specified stage. If both a fractional and a numerical change are specified for the same stage, the fractional change is applied before the numerical change. Default value for the fractional change is 0.

RUN Card

The RUN card, which must precede all other input cards, contains parameters to control input, execution, and output options. The RUN card is read under

FORMAT (A3, 7X, 8I1, 2X, 6A10)

and its fields are assigned as follows:

- A3 - (1-3) - "RUN"
- I1 - (11) - print option
 - if 0 or blank input parameters are printed
 - if 1 output is suppressed
- I1 - (12) - print option
 - if 0 or blank the sets of pure strategies available to Blue and Red are printed
 - if 1 output is suppressed
- I1 - (13) - print option
 - if 0 or blank the set of discrete states corresponding to the number of Blue and Red planes available is printed
 - if 1 output is suppressed
- I1 - (14) - abort option
 - if 0 or blank execution proceeds to normal termination
 - if 1 execution is terminated immediately after run-time estimates are printed
- I1 - (15) - BATTLE-TAPE option
 - if 0 or blank one-stage battle outcomes for each state and pure strategy combination are not available on tape and must be computed. The computed battle outcomes are not written and stored on the BATTLE-TAPE
 - if 1 one-stage battle outcomes for each state and pure strategy combination are not available on tape and must be computed. The computed battle outcomes are

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written and stored on the BATTLE-TAPE

if 2 one-stage battle outcomes for each state and pure strategy combination are read from the BATTLE-TAPE

- I1 - (16) - debug option
 - if 0 or blank debug output is suppressed
 - if 1 one-stage battle outcomes for each state and pure strategy combination are printed
 - I1 - (17) - debug option
 - if 0 or blank debug output is suppressed
 - if 1 MAXMIN/MINMAX plays and corresponding bounds are printed for each stage and state
 - I1 - (18) - debug option
 - if 0 or blank debug output is suppressed
 - if 1 beta weights used for linear interpolation are printed each time subroutine BETAS is called
- 6A10-(21-80) - optional run title

STAGE Card

The STAGE card is used to specify the number of stages in the campaign and the number of engagement cycles per stage. It is read under

FORMAT (A5, 5X, I2, 2X, I2)

and contains the following values:

- A5 - (1-5) - "STAGE"
- I2 - (11-12) - the number of stages in the campaign for which plays and associated bounds are generated (≤ 99). Trial wars of longer duration than the number of stages specified can not be evaluated.
- I2 - (15-16) - the number of engagement cycles per stage (≤ 99).

STRT Card

The STRT card is used to specify any, all, or none of the fractional allocations of aircraft to missions as a function of stage. One STRT card is required to specify each time the allocation fractions change for either Blue or Red aircraft types. If no mission allocation fractions are specified for a given stage, ATACM1 optimizes strategy selection from the complete set of possible pure strategies; if the mission allocation fractions are specified for a subset of the missions, the model optimizes strategy selection from the associated subset of possible pure strategies; if allocation fractions are specified for all missions, the set of possible pure strategies consists of a single strategy and optimal selection reduces to the selection of this single specified strategy. Thus by using different combinations of STRT cards, ATACM1 can be used to evaluate the effects of Blue, Red, or both sides using optimal, sub-optimal, or user-specified strategies against its opponent.

The STRT card is read under

FORMAT (A4, A1, 1X, I2, 4 (2X, 8I2))

with the fields defined as follows:

- A4 - (1-4) - "STRT"
- A1 - (5) - "B" or "R" to indicate the specified allocations are for either the Blue or Red side
- I2 - (7-8) - the upper bound on the range of stages over which the allocations specified are in effect. The lower bound is 1 plus the upper bound specified on the preceding STRT card for the same side. The lower bound for the first STRT card for either side is assumed to be 1. The upper bound for the last STRT card for either side must be greater than or equal to the number of stages specified on the STAGE card.
- 4(2X,8I2)-(9-80) - the fractional assignments of the i th aircraft type ($1 \leq i \leq 4$) to its missions, specified as integer multiples of the corresponding minimum allocation fraction. Columns 9-26 correspond to aircraft type 1, 27-44 to type 2, 45-62 to type 3, 63-80 to type 4. The

integer multiples for the i th aircraft type must be specified in the same order as the missions are assigned on the MISS card. To indicate that the allocation fraction for a mission is unspecified, the corresponding 2 character field must be punched with a right-justified asterisk (" *").

TRIAL Card

One TRIAL card is required for each trial war evaluation desired. If input to ATACM1, the first TRIAL card must follow the END card and the last must be followed by a FINIS card. Each TRIAL card is read under

FORMAT (A5, 5X, I2, 2X, 3I1, 3X, 4F5.0, 5X, 4F5.0)

and its fields are assigned as follows:

- | | |
|---------------|---|
| A5 - (1-5) | - "TRIAL" |
| I2 - (11-12) | - the number of stages in the trial war |
| I1 - (15) | - print option
if 0 or blank the number of planes available and the objective function value are printed for every stage
if 1 output is suppressed |
| I1 - (16) | - print option
if 0 or blank the optimal aircraft allocation strategies for Blue and Red are printed for every stage
if 1 output is suppressed |
| I1 - (17) | - print option
if 0 or blank the values of each of the three objective functions (f_1 , f_2 , and f_3 as described under the OWGHT card) are printed for every stage
if 1 output is suppressed |
| 4F5.0-(21-40) | - the number of Blue aircraft of types 1 thru 4 respectively available at the beginning of the trial war |

4F5.0-(46-65) - the number of Red aircraft of types 1 thru 4 respectively available at the beginning of the trial war

VALU Card

One VALU card for each side is used to specify the residual value of an undamaged plane at the end of the war. The units used to specify this residual value should be consistent with those used on the CASF card. The VALU card is read under

FORMAT (A4, A1, 5X, 4F5.0)

and its fields are defined as follows:

A4 - (1-4) - "VALU"

A1 - (5) - "B" or "R" to indicate the values specified apply to either Blue or Red aircraft

4F5.0-(11-30) - the residual value of an undamaged aircraft of types 1 thru 4 respectively. Default value is 0.

WGHT Card

Each component, f_j , of the overall objective function described under the OWGHT card (Equation A-1) can be expanded as

$$f_j = \sum_{t=1}^{T+1} f_{jt} \quad \text{for } j = 1, 2, 3 \quad (\text{A-2})$$

where

$$f_{1t} = \begin{cases} \text{weighted difference of Blue minus Red CAS firepower delivered during stage } t \\ b_t \text{ CAS}_{Bt} - r_t \text{ CAS}_{Rt} \end{cases} \quad (\text{A-3})$$

$$f_{2t} = \begin{cases} \text{weighted difference of Blue minus Red total firepower delivered during stage } t \\ b_t \text{ TFP}_{Bt} - r_t \text{ TFP}_{Rt} \end{cases} \quad (\text{A-4})$$

$$f_{3t} = \begin{cases} \text{weighted FEBA movement during stage } t \\ \frac{b_t + r_t}{2} \quad (\text{FEBA movement during stage } t) \end{cases} \quad (\text{A-5})$$

WGHT cards are used to specify the values of the weights b_t and r_t as a function of stage. Each WGHT card is read under

FORMAT (A4, A1, IX, I2, 2X, F5.0)

and its fields are assigned as follows:

- A4 - (1-4) - "WGHT"
- A1 - (5) - "B" or "R" to indicate whether the value specified is a Blue or Red weight (b_t or r_t)
- I2 - (7-8) - the number of the stage t for which the specified weight is applicable
- F5.0 - (11-15) - the value of the weight. Default value is 1.

As an aid to the user, Figure A-3 summarizes the formats of all the input cards described above and the default values used if a card is not supplied. With the exception of the TRIAL card, all cards for which default values are not specified are required for every run.

DATA DECK STRUCTURE

As alluded to in the descriptions of the individual cards, ATACM1 permits considerable freedom in the ordering of cards within a run deck. Table A-3 summarizes the order constraints for those card types subject to special restrictions. The only sequence requirement applicable to cards not listed in the table is that they follow the RUN card and precede the END card. Figure A-4 presents a sample run deck with the input cards in an acceptable order.

OUTPUTS

The possible outputs of ATACM1 include the printed output which details the results of the run, the TRIAL-TAPE which can be used by ATACM2 to evaluate additional trial wars, and a BATTLE-TAPE containing one-stage battle outcomes which can be used to speed the execution of certain subsequent runs of ATACM1. Each of these outputs are described below.

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TABLE A-3

SEQUENCE RESTRICTIONS ON INPUT CARDS
TO ATACM1

<u>Card Type</u>	<u>Restriction</u>
RUN	First card in the data deck
STRT	In ascending time sequence (e.g., a STRTB card for stage i must precede a STRTB card for stage j if $i < j$)
END	Follow scenario and attrition cards/precede the optional TRIAL and FINIS cards
TRIAL	Follow the END card/precede the FINIS card (optional)
FINIS	Follow TRIAL cards/last card in the data deck (optional)

Printed Output

Unless explicitly suppressed by the print options listed in Table A-4, every run of ATACM1 prints:

- both the input deck and the input parameters reformatted for readability
- the numbers of pure strategies available to Blue and Red
- lists of the pure strategies available to Blue and Red
- the number of possible states
- a list of the possible states
- run-time estimates

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FIGURE A-4

SAMPLE RUN DECK FOR ATACM1

 RUN SAMPLE RUN -- 2 BLUE AIRCRAFT TYPES, 1 RED AIRCRAFT TYPE
 STAGE 2 1
 NDIVB 10
 NDIVR 15
 DIVFB 9.
 DIVFR 7.
 GRIDB1 0 333 667 1000
 GRIDB2 0 200 400
 GRIDB1 0 400 800 1200
 MISSB1 2 1 2 7 8 2.0 1.0 2.0 1.0
 MISSB2 3 3 4 5 6 2.0 2.0 2.0 1.0
 MISSR1 2 1 2 3 4 2.0 1.0 2.0 2.0
 STRTB 2 1 * * * * * 1 *
 STRTR 1 0 2 0 0
 STRTR 2 * * * *
 REINB 2 100 .2
 REINR 2 200
 VALUB 8. 0.
 VALUR 3.
 CASFB 2.
 CASFR 3.
 OWGHT 0. 1.0 0.
 NSMLB 100
 NSMLR 300
 NSAMB 30 50
 NSAMR 20 40
 ABABF1 1.0 .5 1.0 .5
 ABABF2 1.0 1.0 1.0 .5
 ABABF1 .5 .5 .5 .5
 WGHTR 1 .5
 PKSHB .20
 PKSHR .25
 PKNSB .35
 PKNSR .50
 PKRSR .06
 PKFSR .08
 DFRCB .5
 DFRCR .8
 FEBAM1 0. -1. .99 -1. 1.01 1. 200. 1.
 PKBAB1 .10 .16
 PKBAR1 .12 .17
 PKAAB1 .09 .15 .20
 PKAAR1 .11 .14 .21
 PKBDB2 .05 .12
 PKBDR1 .04 .03
 PKADB2 .03 .03
 PKADR1 .02 .01 .02
 PKBEB2 .05 .03
 PKAEB2 .07 .01 .02
 PKFAB1 .01
 PKRAB1 .01 .03
 END
 TRIAL 2 400 100 500
 TRIAL 1 11 600 200 600
 TRIAL 2 1 800 300 800
 FINIS

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TABLE A-4

RUN CARD
PRINT OPTION CONTROLS

<u>To suppress the print of:</u>	<u>Punch a 1 in RUN card column</u>
Input parameters	11
All possible strategies for Blue and Red	12
All possible states	13

If trial war evaluations are requested during the execution of ATACM1, additional outputs are printed under the control of the print option parameters on the TRIAL card. Specifically, unless explicitly suppressed by the print options listed in Table A-5, every trial war evaluation prints:

- the TRIAL card parameters, the MAXMIN and MINMAX bounds on the objective function, and the value of the objective function produced by playing Blue's MAXMIN strategy against Red's MINMAX strategy
- the number of planes available on both sides and the value of the objective function as a function of stage
- the optimal aircraft allocation strategies as a function of stage
- the individual values of the three objective functions (i.e., Blue-Red CAS Firepower, Blue-Red Total Firepower, and FEBA movement) listed as a function of stage

Figures A-5 and A-6, which were produced by the sample input deck of Figure A-4, illustrate the outputs printed under the control of the RUN and TRIAL cards respectively.

TABLE A-5
TRIAL CARD
PRINT OPTION CONTROLS

<u>To suppress the print (by stage) of:</u>	<u>Punch a 1 in TRIAL card column</u>
Number of planes/objective function value	15
Optimal strategies for Blue and Red	16
All three objective function values	17

BATTLE-TAPE

The BATTLE-TAPE is an optional output of ATACM1 which contains the one-stage battle assessments computed in the initialization phase of the run (see Figure A-2). The BATTLE-TAPE has two potential applications:

- it provides a partial backup/restart capability should an ATACM1 job be terminated abnormally after the battle assessments are computed, and
- it can be used to input rather than recompute battle assessments for perturbation runs of ATACM1 in which those parameters affecting one-stage battle outcomes are unchanged.

The advisability of specifying a BATTLE-TAPE as an output of a long-running ATACM1 job should be obvious. If such a job aborts abnormally after the BATTLE-TAPE is written, a rerun can be made by simply assigning the BATTLE-TAPE as an input, punching a "2" in column 15 of the RUN card, and resubmitting the job. The resubmitted job reads the battle assessments directly from the BATTLE-TAPE, thus saving the time required for their calculation.

In the case of a shorter run, the decision whether to create a BATTLE-TAPE depends upon how applicable the computed battle assessments will be to other related runs of ATACM1. Table A-6 lists those input parameters which can be changed without affecting one-stage battle outcomes and thus defines the set of related runs which may share the

SAMPLE OUTPUT PRINTED UNDER CONTROL OF RUN CARD

SAMPLE RUN -- 2 BLUE AIRCRAFT TYPES, 1 RED AIRCRAFT TYPE

NUMBER OF STAGES = 2
 NUMBER OF CYCLES PLN STAGE = 1
 NUMBER OF BLUE PLANE TYPES = 2
 NUMBER OF RED PLANE TYPES = 1
 NUMBER OF BLUE DIVISIONS = 10
 NUMBER OF RED DIVISIONS = 15
 FIREPOWER PER BLUE DIVISION = 9.0000
 FIREPOWER PER RED DIVISION = 7.0000
 NUMBER OF BLUE SHELTERS = 100
 NUMBER OF RED SHELTERS = 100
 NUMBER OF BLUE FORWARD SAMS = 30
 NUMBER OF RED FORWARD SAMS = 20
 NUMBER OF BLUE REAR SAMS = 50
 NUMBER OF RED REAR SAMS = 40
 OBJECTIVE FUNCTION WEIGHTS = CAS WMD - 0.00 TOTL FP - 1.00 FENA - 0.00

CAS FIREPOWER PER SORTIE

BLUE PLANE TYPE	RED PLANE TYPE	RED PLANE TYPE
1 2	3	4
2.0000	-0.0000	-0.0000
3.0000	-0.0000	-0.0000
4.0000	-0.0000	-0.0000

DIVISION FIREPOWER REDUCTION PER CAS SORTIE

BLUE PLANE TYPE	RED PLANE TYPE	RED PLANE TYPE
1 2	3	4
0.5000	-0.0000	-0.0000
0.5000	-0.0000	-0.0000
0.5000	-0.0000	-0.0000

PLSUAL VALUE OF AN UNARMED PLANE AT END OF THE WMD

BLUE PLANE TYPE	RED PLANE TYPE	RED PLANE TYPE
1 2	3	4
0.0000	0.0000	-0.0000
0.0000	0.0000	-0.0000
0.0000	0.0000	-0.0000

FRACTION VULNERABLE TO WMD BY MISSION

BLUE PLANE TYPE	RED PLANE TYPE	RED PLANE TYPE
1 2	3	4
1-1.000 3-1.000 0-1.000 0-1.000	1-1.000 3-1.000 0-1.000 0-1.000	1-1.000 3-1.000 0-1.000 0-1.000
2-1.000 4-1.000 0-1.000 0-1.000	2-1.000 4-1.000 0-1.000 0-1.000	2-1.000 4-1.000 0-1.000 0-1.000
3-1.000 5-1.000 0-1.000 0-1.000	3-1.000 5-1.000 0-1.000 0-1.000	3-1.000 5-1.000 0-1.000 0-1.000
4-1.000 6-1.000 0-1.000 0-1.000	4-1.000 6-1.000 0-1.000 0-1.000	4-1.000 6-1.000 0-1.000 0-1.000

MINIMUM ALLOCATION FRACTIONS

BLUE PLANE TYPE	RED PLANE TYPE	RED PLANE TYPE
1 2	3	4
0.50 0.50 0.00 0.00	0.50 0.00 0.00 0.00	0.00 0.00 0.00 0.00

GRID POINTS

BLUE PLANE TYPE	RED PLANE TYPE	RED PLANE TYPE
1 2	3	4
0 0 0 0	0 0 0 0	0 0 0 0
100 200 400 600	100 200 400 600	100 200 400 600
1000 1200 1400 1600	1000 1200 1400 1600	1000 1200 1400 1600

FENA FUNCTION

F RATIO	MOVEMENT	0.000	1.000	200.000	400.000	600.000	800.000	1000.000
0.000	-1.000	0.000	1.000	200.000	400.000	600.000	800.000	1000.000

FIGURE A-5 (cont'd)

STAGE	OBJECTIVE WEIGHTS		REINFORCEMENTS				REINFORCEMENTS			
			BLUE PLANE TYPE		RED PLANE TYPE		BLUE PLANE TYPE		RED PLANE TYPE	
	BLUE	RED	1	2	3	4	1	2	3	4
1	.500	1.00	0	0	0	0	0.00	0.00	0.00	0.00
2	1.00	1.00	100	0	0	0	0.00	.20	0.00	0.00

KILL PROBABILITIES

ABA AGAINST NON-SHELTERED AIRCRAFT

BLUE KILLS RED		RED KILLS BLUE	
1	2	1	2
.500	-.000	.350	.350
.500	-.000	-.000	-.000
.500	-.000	-.000	-.000
.500	-.000	-.000	-.000

ABA AGAINST SHELTERED AIRCRAFT

BLUE KILLS RED		RED KILLS BLUE	
1	2	1	2
.250	-.000	.200	.200
.250	-.000	-.000	-.000
.250	-.000	-.000	-.000
.250	-.000	-.000	-.000

FIGURE A-5 (cont'd)

KILL PROBABILITIES

KILL PROBABILITIES

CAS ESCORT AGAINST MID

AWA ESCORT AGAINST AWB

BLUE KILLS RED				RED KILLS BLUE			
RED TYPE				RED TYPE			
1	2	3	4	1	2	3	4
1	0.000	0.000	0.000	0.000	0.000	0.000	0.000
2	0.000	0.000	0.000	0.000	0.000	0.000	0.000
3	0.000	0.000	0.000	0.000	0.000	0.000	0.000
4	0.000	0.000	0.000	0.000	0.000	0.000	0.000

AWB AGAINST CAS ESCORT

AWB AGAINST AWA ESCORT

BLUE KILLS RED				RED KILLS BLUE			
RED TYPE				RED TYPE			
1	2	3	4	1	2	3	4
1	0.000	0.000	0.000	0.000	0.000	0.000	0.000
2	0.000	0.000	0.000	0.000	0.000	0.000	0.000
3	0.000	0.000	0.000	0.000	0.000	0.000	0.000
4	0.000	0.000	0.000	0.000	0.000	0.000	0.000

CAS AGAINST AWB

AWA AGAINST AWB

BLUE KILLS RED				RED KILLS BLUE			
RED TYPE				RED TYPE			
1	2	3	4	1	2	3	4
1	0.000	0.000	0.000	0.000	0.000	0.000	0.000
2	0.000	0.000	0.000	0.000	0.000	0.000	0.000
3	0.000	0.000	0.000	0.000	0.000	0.000	0.000
4	0.000	0.000	0.000	0.000	0.000	0.000	0.000

AWB AGAINST CAS

AWB AGAINST AWA

BLUE KILLS RED				RED KILLS BLUE			
RED TYPE				RED TYPE			
1	2	3	4	1	2	3	4
1	0.000	0.000	0.000	0.000	0.000	0.000	0.000
2	0.000	0.000	0.000	0.000	0.000	0.000	0.000
3	0.000	0.000	0.000	0.000	0.000	0.000	0.000
4	0.000	0.000	0.000	0.000	0.000	0.000	0.000

KILL PROBABILITIES

SAM AGAINST CAS										
BLUE KILLS RED			RED KILLS BLUE			FURWARD SAM SUPPRESSOR AGAINST SAM				
RED TYPE			BLUE TYPE			BLUE KILLS RED		RED KILLS BLUE		
1	2	3	1	2	3	1	2	3	1	2
.170	0.000	0.000	.160	0.000	0.000	.000	-0.000	-0.000	0.000	0.000
FURWARD						FURWARD		FURWARD		
SAM AGAINST AWA ESCORT										
BLUE KILLS RED			RED KILLS BLUE			SAM AGAINST FURWARD SAM SUPPRESSOR				
RED TYPE			BLUE TYPE			BLUE KILLS RED		RED KILLS BLUE		
1	2	3	1	2	3	1	2	3	1	2
0.000	0.000	0.000	0.000	.030	0.000	0.000	0.000	0.000	0.000	0.000
FURWARD						FURWARD		FURWARD		
SAM AGAINST AWA										
BLUE KILLS RED			RED KILLS BLUE			SAM AGAINST NEAR SAM SUPPRESSOR				
RED TYPE			BLUE TYPE			BLUE KILLS RED		RED KILLS BLUE		
1	2	3	1	2	3	1	2	3	1	2
.140	0.000	0.000	.150	0.000	0.000	.000	-0.000	-0.000	0.000	0.000
FURWARD						FURWARD		FURWARD		
SAM AGAINST AWA ESCORT										
BLUE KILLS RED			RED KILLS BLUE			SAM AGAINST FURWARD SAM SUPPRESSOR				
RED TYPE			BLUE TYPE			BLUE KILLS RED		RED KILLS BLUE		
1	2	3	1	2	3	1	2	3	1	2
0.000	0.000	0.000	0.000	.010	0.000	0.000	0.000	0.000	0.000	0.000
FURWARD						FURWARD		FURWARD		
SAM AGAINST AWA ESCORT										
BLUE KILLS RED			RED KILLS BLUE			SAM AGAINST FURWARD SAM SUPPRESSOR				
RED TYPE			BLUE TYPE			BLUE KILLS RED		RED KILLS BLUE		
1	2	3	1	2	3	1	2	3	1	2
0.000	0.000	0.000	0.000	.010	0.000	0.000	0.000	0.000	0.000	0.000
FURWARD						FURWARD		FURWARD		

FIGURE A-5 (cont'd)

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FIGURE A-5 (cont'd)

CDC 6600 TIME ESTIMATES FOR CURRENT RUN (SECONDS)

FUNCTION	CPU TIME	I/O TIME
SETUP	2.0	2.0
BATTLES	19.0	5.8
GAMES	7.4	11.5
TOTAL	28.4	19.3

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FIGURE A-6

SAMPLE OUTPUT PRINTED
UNDER CONTROL OF TRIAL CARDS

TRIAL CARD #1

TRIAL NUMBER	NUMBER OF STAGES	NUMBER OF PLANES AVAILABLE								BLUE MAXMIN	RED MINMAX	MAXMIN VS MINMAX
		BLUE				RED						
		1	2	3	4	1	2	3	4			
1	2	400	100	0	0	500	0	0	0	-10515	9735	-2837

TRIAL NUMBER 1

STAGE NUMBER	NUMBER OF BLUE PLANES AVAILABLE				NUMBER OF RED PLANES AVAILABLE				MAXMIN VS MINMAX	TOTAL
	1	2	3	4	1	2	3	4		
1	297	77	0	0	481	0	0	0	442	442
2	396	91	0	0	679	0	0	0	-3279	-2837

TRIAL NUMBER 1

PLANE ALLOCATION FRACTIONS FOR BLUE

STAGE NUMBER	PLANE TYPE/MISSION							
	1/1	1/2	1/7	1/8	2/3	2/4	2/5	2/6
1	.50	0.00	0.00	.50	0.00	0.00	.33	.67
2	.50	0.00	.50	0.00	0.00	0.00	.33	.67

TRIAL NUMBER 1

PLANE ALLOCATION FRACTIONS FOR RED

STAGE NUMBER	PLANE TYPE/MISSION			
	1/1	1/2	1/3	1/4
1	0.00	1.00	0.00	0.00
2	1.00	0.00	0.00	0.00

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FIGURE A-6 (cont'd)

TRIAL CARD #1 (cont'd)

TRIAL NUMBER 1						
STAGE NUMBER	BLUE-RED CAS FIREPOWER	TOTAL	BLUE-RED GRND-AIR FIREPOWER	TOTAL	FEMA MOVEMENT	TOTAL
1	397	397	442	442	1	1
2	-3279	-2882	-3279	-2837	0	1

TRIAL CARD #2

TRIAL NUMBER	NUMBER OF STAGES	NUMBER OF PLANES AVAILABLE								BLUE MAXMIN	RED MINMAX	MAXMIN VS MINMAX
		BLUE				RED						
		1	2	3	4	1	2	3	4			
2	1	600	200	0	0	600	0	0	0	-5721	5321	-15

TRIAL NUMBER 2						
STAGE NUMBER	BLUE-RED CAS FIREPOWER	TOTAL	BLUE-RED GRND-AIR FIREPOWER	TOTAL	FEMA MOVEMENT	TOTAL
1	0	0	-15	-15	-1	-1

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FIGURE A-6 (cont'd)

TRIAL CARD #3

TRIAL NUMBER	NUMBER OF STAGES	NUMBER OF PLANES AVAILABLE								BLUE MAXMIN	RED MINMAX	MAXMIN VS MINMAX
		BLUE				RED						
		1	2	3	4	1	2	3	4			
3	2	800	300	0	0	800	0	0	0	-9412	6660	-1909

TRIAL NUMBER 3

STAGE NUMBER	NUMBER OF BLUE PLANES AVAILABLE				NUMBER OF RED PLANES AVAILABLE				MAXMIN VS MINMAX	TOTAL
	1	2	3	4	1	2	3	4		
1	717	254	0	0	737	0	0	0	842	842
2	816	295	0	0	910	0	0	0	-2751	-1909

TRIAL NUMBER 3

PLANE ALLOCATION FRACTIONS FOR BLUE

STAGE NUMBER	PLANE TYPE/MISSION							
	1/1	1/2	1/7	1/8	2/3	2/4	2/5	2/6
1	.50	0.00	0.00	.50	0.00	.67	.33	0.00
2	.50	0.00	.50	0.00	.67	0.00	.33	0.00

TRIAL NUMBER 3

PLANE ALLOCATION FRACTIONS FOR RED

STAGE NUMBER	PLANE TYPE/MISSION			
	1/1	1/2	1/3	1/4
1	0.00	1.00	0.00	0.00
2	1.00	0.00	0.00	0.00

same BATTLE-TAPE. For example, to study the sensitivity of war outcomes to reinforcement policies, numerous runs of ATACM1 would be required in which only the reinforcement parameters on the REIN cards would change. In such a case, since reinforcement parameters are listed in Table A-6, the BATTLE-TAPE produced by the first run of ATACM1 could be used to input, rather than recompute, the one-stage battle outcomes required by the remaining runs. The only changes required in the data deck for one of these perturbation runs would be the changed REIN cards and a modified RUN card with a "2" punched in column 15.

In the CDC 6600 version of ATACM1, the BATTLE-TAPE is assigned the logical file name "TAPE10".

TABLE A-6
INPUT PARAMETERS WHICH DO NOT AFFECT
ONE-STAGE BATTLE ASSESSMENTS

<u>Card Type</u>	<u>Parameters</u>	<u>Columns</u>
REIN	Reinforcements	11-30, 36-55
STAGE	Number of stages	11-12
VALU	Residual value of undamaged plane	11-30
WGHT	Objective function weights by stage	11-15

TRIAL-TAPE

The TRIAL-TAPE produced by ATACM1 contains the values of the major COMMON areas assigned during the execution of ATACM1 as well as the optimal strategies and associated bounds generated for each state and stage of the campaign. The tape is used exclusively by ATACM2 to input those parameters required to evaluate trial wars of varying length initiated with differing numbers of aircraft available to the opposing forces.

In the CDC 6600 version of ATACM1, the TRIAL-TAPE is assigned the logical file name "TAPE4".

EXECUTION TIME

One of the most important considerations in the use of ATACM1 is the execution time required to generate the results written on the TRIAL-TAPE. There are three phases of calculation necessary for the generation of this tape:

- SETUP - the generation of strategies and states
- BATTLES - the calculation and output to scratch disk (and BATTLE-TAPE if requested) of one-stage battle assessments for each Blue-Red strategy combination
- GAMES - the calculation of the MAXMIN/MINMAX objective function bounds and plays for each stage and state

The time required for SETUP is usually insignificant (2 seconds) compared to the times for BATTLES and GAMES. Run times for these last two phases can range from a few seconds for a simple scenario to several minutes or even hours for the most ambitious requests.

Time Estimates

The run time associated with BATTLES and GAMES is a relatively complex function of the total number of aircraft types on both sides, the number of Blue and Red pure strategies, the size of the state space, and the number of stages and cycles-per-stage in the air campaign being simulated. To provide the user with estimates of the CPU and IO times required for BATTLES and GAMES, all of these variables were incorporated into empirical formulas derived from numerous test runs made on the CDC 6600. The formulas were coded into the subroutine TIMER which prints time estimates for BATTLE and GAMES before the calculations are performed.

To use the time estimates produced by TIMER to assess the reasonableness of a particular run before it is submitted for complete execution, a preliminary run using the candidate data deck should be submitted with a 1 punched in column 14 of the RUN card. All outputs shown in Figure A-5 through the printing of the time estimates are generated in their normal manner. However, execution is terminated just before the BATTLES and GAMES phases of computation begin. The output which is generated permits verification of the accuracy of the input data and provides a basis

for determining whether the length of time required for a complete run is acceptable. Because of the minimal effort and cost associated with such a data-and-time check, its use is strongly recommended for all but the simplest runs.

Use of the BATTLE-TAPE

Another consideration related to the execution time of ATACM1 is the use of the BATTLE-TAPE. As described under the outputs of ATACM1, use of the BATTLE-TAPE permits the one-stage battle assessments produced during the BATTLES phase of calculation to be written and stored on magnetic tape for use in subsequent related runs of ATACM1. Since the time required for the calculation of these battle assessments is typically a significant fraction of the total execution time, judicious job sequencing which permits the use of a single BATTLE-TAPE for numerous runs of ATACM1 will produce substantial savings in the total computer time used.

DIAGNOSTIC MESSAGES

Diagnostic messages generated by ATACM1 are classified in order of increasing severity as

- INFO: Information only -- anomaly is ignored.
- ERROR: Processing error -- job is aborted at the end of the current subroutine.
- ABORT: Abort -- job is aborted immediately.

Messages which may be produced by ATACM1 are listed and interpreted in Table A-7 in approximately the same order they are encountered during program execution.

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TABLE A-7

DIAGNOSTIC MESSAGES GENERATED BY ATACM1

<u>Message</u>	<u>Severity</u>	<u>Interpretation</u>
DATA CARD KEY NOT RECOGNIZED	ERROR	Input card key does not match any of those listed in Table A-1, or a TRIAL or FINIS card precedes the END card.
SMALLEST GRID LEVEL MUST BE ZERO	ERROR	One of the GRID cards does not have a 0 punched in columns 11-15.
SUM OF SPECIFIED ALLOCATIONS EXCEEDS 1.0	ABORT	The sum of the allocations of an aircraft type to its missions, as specified on a STRT card, exceeds the denominator of the minimum allocation fraction for the corresponding aircraft type.
IF ALL ALLOCATIONS ARE SPECIFIED THEY MUST SUM TO 1.0	ABORT	If all the allocations of an aircraft type to its missions are specified on a STRT card, they must sum to the denominator of the minimum allocation fraction for the corresponding aircraft type.
STRATEGIES NOT SPECIFIED THRU THE LAST STAGE OF CAMPAIGN	ABORT	The number in columns 7-8 of last STRT card read for either Blue or Red was less than the total number of stages specified on the STAGE card.

TABLE A-7 (Cont'd)

<u>Message</u>	<u>Severity</u>	<u>Interpretation</u>
TOO MANY PURE STRATEGIES TO BE STORED IN CORE	ABORT	Either the number of pure strategies for one side exceeds 500, the number of decision vectors for a single aircraft type exceeds 200, or the total area required to store the pure strategies for both sides exceeds 25,000 words. Possible remedies include specification of fewer missions, fewer aircraft types, or a larger minimum allocation fraction.
TOO MANY STATES TO STORE VALUES AND PLAYS	ABORT	The total number of states multiplied by 10 plus the dimensioned area used to store the pure strategies exceeds 25,000 words. Either the number of states or the total number of pure strategies must be reduced.
NOT ENOUGH COMMON AREA TO STORE GAME MATRIX	ABORT	Two times the number of elements in the one-stage game matrix, plus 10 times the number of states, plus the dimensioned area used to store the pure strategies exceeds 25,000 words. Either the number of states or the number of pure strategies must be reduced.
BUFFER OUT ERROR TO TAPE9 IN SUBROUTINE READIN	ABORT	System write failure was encountered while writing STRT parameters on scratch disk (TAPE9). Rerun job or consult systems analyst.

TABLE A-7 (Cont'd)

<u>Message</u>	<u>Severity</u>	<u>Interpretation</u>
BUFFER IN ERROR FROM TAPE9 IN SUBROUTINE INIT	ABORT	Either a parity error or system read failure was encountered while reading STRT parameters from scratch disk (TAPE9). Rerun job or consult systems analyst.
USER REQUESTED ONLY A DATA CHECK AND TIME ESTIMATE	ABORT	A 1 was punched in column 14 of the RUN card. Execution is terminated immediately after run-time estimates are printed.
I/O ERROR ON TAPE10 IN SUBROUTINE INIT	ABORT	Either a read parity error or a system I/O failure was encountered on the BATTLE-TAPE (TAPE10). Rerun job or consult systems analyst.
BUFFER OUT ERROR TO TAPE1 IN SUBROUTINE INIT	ABORT	System write failure was encountered while writing battle assessments on scratch disk (TAPE1). Rerun job or consult systems analyst.
BUFFER IN ERROR FROM TAPE1 IN SUBROUTINE GAMES	ABORT	Either a parity error or system read failure was encountered while reading battle assessments from scratch disk (TAPE1). Rerun job or consult systems analyst.
BUFFER OUT ERROR TO TAPE4 IN MAIN PROGRAM	ABORT	System write failure was encountered while writing TRIAL-TAPE (TAPE4). Rerun job or consult systems analyst.

TABLE A-7 (Cont'd)

<u>Message</u>	<u>Severity</u>	<u>Interpretation</u>
BUFFER OUT ERROR TO TAPE7 IN MAIN PROGRAM	ABORT	System write failure was encountered while writing MAXMIN/MINMAX objective function values on scratch disk (TAPE7). Rerun job or consult systems analyst.
BUFFER IN ERROR FROM TAPE7 IN SUBROUTINE TRIALS	ABORT	Parity error or system read failure was encountered while reading MAXMIN/MINMAX objective function values from scratch disk (TAPE7). Rerun job or consult systems analyst.
BUFFER OUT ERROR TO TAPE8 IN MAIN PROGRAM	ABORT	System write failure was encountered while writing MAXMIN/MINMAX plays on scratch disk (TAPE8). Rerun job or consult systems analyst.
BUFFER IN ERROR FROM TAPE8 IN SUBROUTINE TRIALS	ABORT	Parity error or system read failure was encountered while reading MAXMIN/MINMAX plays from scratch disk (TAPE8). Rerun job or consult systems analyst.
DISK I/O ERROR ON TAPE9 IN SUBROUTINE TRIALS	ABORT	A system I/O failure was encountered on scratch disk (TAPE9) used to store available planes and objective function values as a function of stage. Rerun job or consult systems analyst.

TABLE A-7 (Cont'd)

<u>Message</u>	<u>Severity</u>	<u>Interpretation</u>
TRIAL CARD IGNORED -- INCORRECT FORMAT	INFO	The key on one of the TRIAL cards is mis- punched. Columns 1-5 should contain "TRIAL".
TRIAL CARD IGNORED -- TOO MANY STAGES REQUESTED	INFO	The number of stages requested for a trial war exceeds the number of stages specified in the original run of ATACM1.
TRIAL CARD IGNORED -- TOO MANY PLANES OF ONE TYPE SPECIFIED	INFO	The initial number of planes specified on a TRIAL card for one of the aircraft types exceeds the maximum grid level specified for that aircraft type in the original run of ATACM1.
RUN ABORTED DUE TO FATAL ERRORS	ABORT	Indicates previously diagnosed ERRORS necessitate job abortion.

ATACM2

As depicted in the logical flowchart of Figure A-7, the required inputs to ATACM2 are a TRIAL-TAPE written by a previous run of ATACM1 and the TRIAL cards requesting war evaluations. In addition to the outcomes of the requested trial wars, ATACM2 can print the inputs, the strategies, and the states used in the original run of ATACM1 to generate the TRIAL-TAPE being read.

INPUTS

The TRIAL-TAPE is the primary input to ATACM2 and is assigned the logical file name "TAPE4". The input deck to ATACM2 consists of three card types described previously under the discussion of ATACM1's inputs. The first card in the input deck must be a RUN card, the last card must be a FINIS card, and the remaining cards must be TRIAL cards. The formats of all three cards are identical to those shown in Figure A-3 with the exception that RUN card parameters in columns 14-80 are ignored by ATACM2. Figure A-8 presents a sample input deck for ATACM2.

OUTPUTS

The outputs produced by ATACM2 are a subset of those produced by ATACM1. By specifying the print parameters described in Table A-3, the user can elect to print any or all of the following outputs under control of the RUN card:

- the input parameters to the original run of ATACM1 which generated the TRIAL-TAPE
- lists of the pure strategies available to Blue and Red in the original run of ATACM1
- a list of the possible states generated in the original run of ATACM1

In addition, for each trial war evaluation requested, ATACM2 produces outputs identical to those described under the outputs of ATACM1 which are controlled by the print options of Table A-4 and displayed in the sample output of Figure A-6.

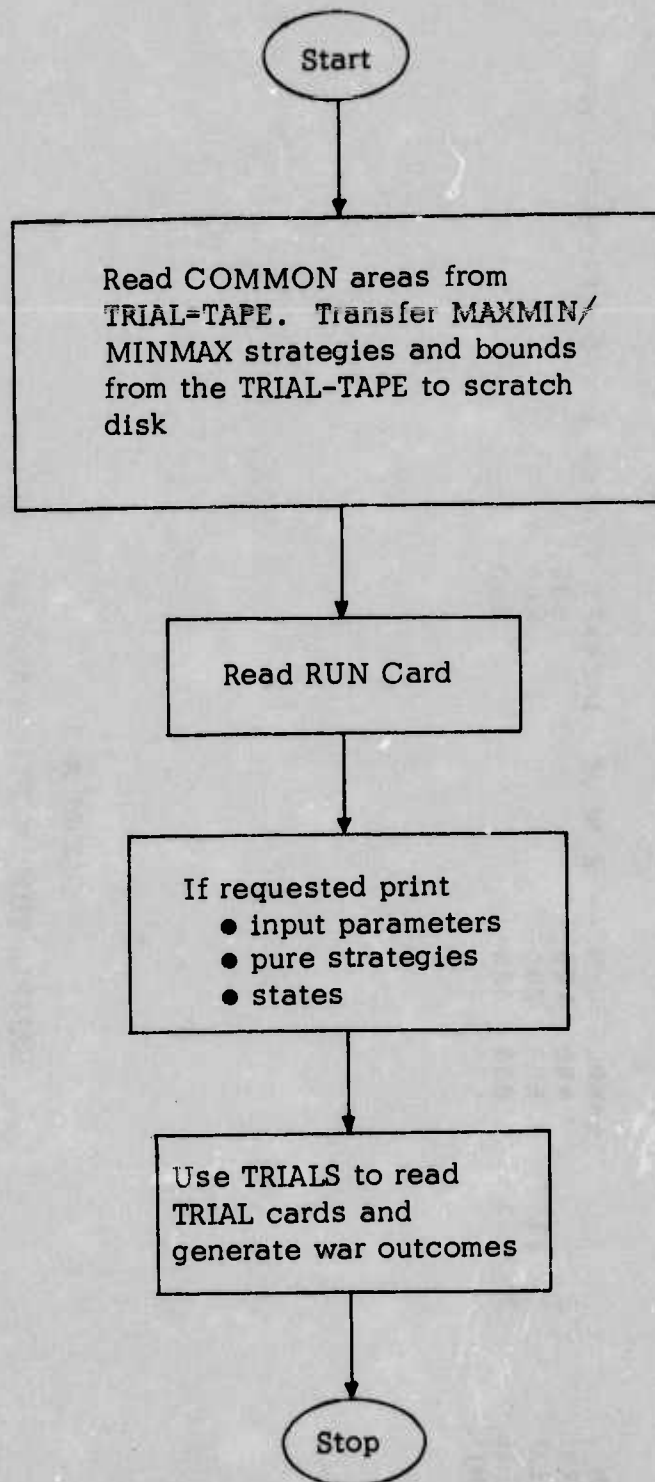


FIGURE A-7
LOGICAL FLOWCHART OF ATACM2

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RUN	2	1	2	SAMPLE RUN	--	2	BLUE	AIRCRAFT	TYPES,	1	RED	AIRCRAFT	TYPE
TRIAL	2	1	2	400	100								
TRIAL				600	200								
TRIAL				800	300								
FINIS													

FIGURE A-8
SAMPLE RUN DECK FOR ATACM2

EXECUTION TIME

The execution time required for ATACM2 is insignificant relative to that required for ATACM1. A typical run requesting the evaluation of 10 trial wars of 10 stages each will generally take less than one minute.

DIAGNOSTIC MESSAGES

Diagnostic messages generated by ATACM2 are classified according to the same scheme described under ATACM1. Table A-8 lists and interprets those messages applicable to ATACM2.

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TABLE A-8

DIAGNOSTIC MESSAGES GENERATED BY ATACM2

<u>Message</u>	<u>Severity</u>	<u>Interpretation</u>
RUN CARD MUST PRECEDE TRIAL CARDS	ABORT	The first card in the input deck was not a RUN card.
BUFFER IN ERROR FROM TAPE4 IN MAIN PROGRAM	ABORT	Parity error or system read failure was encountered while reading the TRIAL-TAPE (TAPE4). Rerun job or consult systems analyst.
BUFFER OUT ERROR TO TAPE7 IN MAIN PROGRAM	ABORT	System write failure was encountered while writing MAXMIN/MINMAX objective function values on scratch disk (TAPE7). Rerun job or consult systems analyst.
BUFFER IN ERROR FROM TAPE7 IN SUBROUTINE TRIALS	ABORT	Parity error or system read failure was encountered while reading MAXMIN/MINMAX objective function values from scratch disk (TAPE7). Rerun job or consult systems analyst.
BUFFER OUT ERROR TO TAPE8 IN MAIN PROGRAM	ABORT	System write failure was encountered while writing MAXMIN/MINMAX plays on scratch disk (TAPE8). Rerun job or consult systems analyst.
BUFFER IN ERROR FROM TAPE8 IN MAIN PROGRAM	ABORT	Parity error or system read failure was encountered while reading MAXMIN/MINMAX plays on scratch disk (TAPE8). Rerun job or consult systems analyst.

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TABLE A-8 (Cont'd)

<u>Message</u>	<u>Severity</u>	<u>Interpretation</u>
DISK I/O ERROR ON TAPE9 IN SUBROUTINE TRIALS	ABORT	A system I/O failure was encountered on scratch disk (TAPE9) used to store available planes and objective function values as a function of stage. Rerun job or consult systems analyst.
TRIAL CARD IGNORED -- INCORRECT FORMAT	INFO	The key on one of the TRIAL cards is mis-punched. Columns 1-5 should contain "TRIAL".
TRIAL CARD IGNORED -- TOO MANY STAGES REQUESTED	INFO	The number of stages requested for a trial war exceeds the number of stages specified in the original run of ATACM1.
TRIAL CARD IGNORED -- TOO MANY PLANES OF ONE TYPE SPECIFIED	INFO	The initial number of planes specified on a TRIAL card for one of the aircraft types exceeds the maximum grid level specified for that aircraft type in the original run of ATACM1.

APPENDIX B

PROGRAMMING DOCUMENTATION

This appendix presents programming documentation for ATACM1 and ATACM2. Following sections describe the storage requirements for the two programs and potential problems associated with converting them to a computer system different from the current CDC6600. In addition, FORTRAN listings and definitions of the most frequently used variable names are provided.

STORAGE REQUIREMENTS

In its current form ATACM1 requires approximately 54,000 words of core storage, of which about 14,000 are used for program instructions and 40,000 are used for array storage. In addition, approximately 2,000,000 words of scratch disk storage, as described in Table B-1, are required for a representative run of the model.

ATACM2 requires approximately 40,000 words of core storage, of which about 8,000 are used for program instructions and 32,000 are used for array storage. Scratch disk requirements for ATACM2 include those shown for files TAPE7, TAPE8, and TAPE9 in Table B-1 -- approximately 16,000 words for a representative run.

CONVERSION TO A DIFFERENT COMPUTER

Both ATACM1 and ATACM2 are coded in CDC 6600 FORTRAN EXTENDED which is generally compatible with FORTRAN compilers available on other major computer systems. Use of those capabilities of the CDC FORTRAN which are unique or less standard was purposely avoided to minimize the problem of program conversions. Subroutine and variable names are limited to six characters, the standard H specification is used in FORMAT statements for the output of Hollerith strings, multiple assignment statements are not used, etc. ENCODE and DECODE statements are used extensively in the subroutine READIN but, if required, they could be eliminated by imposing more strict rules upon the order of the cards in the input deck.

Assuming the problem of FORTRAN compatibility can be resolved, the only remaining obstacles to conversion are the core and disk storage

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TABLE B-1

SCRATCH DISK STORAGE REQUIREMENTS FOR ATACM1

Logical File Name	Access Mode	Number of Records	Number of Words per Record	Total Number of Words Required**
TAPE1	Sequential	NSTATE*	2·NRST·NRST	2,000,000
TAPE2	Random	NSTATE	2·NSTATE	8,000
TAPE3	Random	NSTATE	2·NSTATE	8,000
TAPE7	Sequential	NSTATE	2·NSTATE	8,000
TAPE8	Sequential	NSTATE	2·NSTATE	8,000
TAPE9	Sequential	NSTATE	10	100

* Mnemonic variables are defined below:

NSTATE = number of stages
 NSTATE = number of states
 NBST = number of Blue strategies
 NRST = number of Red strategies

** Representative value computed with:

NSTATE = 10
 NSTATE = 400
 NBST = 50
 NRST = 50

requirements described above. Unfortunately, these requirements will probably increase rather than decrease in a conversion to another machine because of the large 60-bit word used in the CDC6600. The number of words required for program instructions after conversion to a 32 or 36-bit word machine (e.g. IBM or UNIVAC) could be as many as twice (60/32 or 60/36) the number currently required. Most array and disk storage requirements would be unaffected by a smaller word, the one notable exception being the storage used for battle assessments. In the current versions of ATACM1 and ATACM2 ten integer values are required to characterize the results of each one-stage battle assessment and these are packed into two words. Eight unsigned integer values are stored in one word (7 bits each), and the remaining two signed values are stored in the other word (30 bits each). The most natural allocation of these values on machines with 32 or 36-bit words would require four words -- two for the eight values and one word each for the other two. In a representative run such as that described in Table B-1, the one-stage battle assessments for a single state which currently occupy 5,000 words would require 10,000 words in the converted programs. Analogously, the total amount of scratch disk required to store the one-stage battle assessments for all states on TAPE1 (see Table B-1) would increase from 2 to 4 million words. To illustrate the impact of smaller words, Table B-2 summarizes current and estimated storage requirements for both ATACM1 and ATACM2 before and after conversion.

One final consideration in the conversion problem is the possibility of reducing the size or complexity of the air campaign which can be simulated in order to fit the model to the storage available. The major array used for variable storage in both ATACM1 and ATACM2 is a singly dimensioned vector called XARRAY. The location of values in XARRAY are assigned dynamically depending upon the number of strategies, number of missions, and number of states addressed in the scenario being simulated. The total number of words in XARRAY which are required for a particular run is generated by

$$\begin{array}{lcl} \text{Total Words Required} & = & \text{NBST} \cdot \text{NBM} + \text{NRST} \cdot \text{NRM} + \\ \text{in XARRAY} & & 2 \cdot \text{NBST} \cdot \text{NRST} + 10 \cdot \text{NSTATE} \end{array} \quad (\text{B-1})$$

where

- NBST = number of Blue strategies
- NRST = number of Red strategies
- NBM = number of Blue missions per strategy
- NRM = number of Red missions per strategy
- NSTATE = number of states

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TABLE B-2

CURRENT VS. ESTIMATED STORAGE
REQUIREMENTS AFTER CONVERSION TO A 32-BIT WORD COMPUTER *

	ATACM1		ATACM2	
	Before	After	Before	After
Core Storage				
Instructions	14K	28K	8K	16K
Data Arrays	40K	45K	32K	37K
Total	54K	73K	40K	53K
Scratch Disk				
TAPE1	2,000K	4,000K	**	**
TAPE2	8K	8K	**	**
TAPE3	8K	8K	**	**
TAPE7	8K	8K	8K	8K
TAPE8	8K	8K	8K	8K
TAPE9	.1K	.1K	.1K	.1K
Total	2,032K	4,032K	16K	16K

* Based upon the same representative run used in Table B-1.

** Not used by ATACM2.

In the current versions XARRAY is dimensioned to be 25,000 words long, the value of NWORK. If calculations using Equation B-1 indicate fewer than 25,000 words are adequate for the type of runs which will be made on a different computer, both NWORK and the size of XARRAY can be reduced to a more compatible value*. The result would be a commensurate reduction in the data array storage requirements shown in Table B-2. Although additional reductions beyond those possible by changing NWORK can be achieved by reducing other array dimensions, such changes require a more detailed understanding of the program structure and would yield considerably smaller savings relative to the effort required.

FORTRAN LISTINGS

Figures B-1 and B-2 present FORTRAN listings of ATACM1 and ATACM2 as written for the CDC6600 system. Comment cards in the listings describe the functions of the various subroutine while Table B-3 lists and defines the variable names used most frequently in the two programs.

*The only restriction is that NWORK can not be reduced below 6600 -- the length of NALOCs in READIN.

```
PROGRAM ATACH1 (OUTPUT,TAPE1=65,TAPE2,TAPE3,TAPE4=65,  
1 TAPE5,TAPE6=OUTPUT,TAPE7=65,TAPE8=65,TAPE9=65,TAPE10=65)
```

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FIGURE B-1 (cont'd)

WRITE(LUNO,100) T,NAMES(3)	00700
T=TIOCALL(X)	00710
WRITE(LUNO,110) T,NAMES(3)	00720
CALL INIT	00730
CALL SECOND(T)	00740
WRITE(LUNO,100) T,NAMES(4)	00750
T=TIOCALL(X)	00760
WRITE(LUNO,110) T,NAMES(4)	00770
IF(IERR.EQ.1) CALL ERR(1)	00780
CALL GAMES	00790
CALL SECOND(T)	00800
WRITE(LUNO,100) T,NAMES(5)	00810
T=TIOCALL(X)	00820
WRITE(LUNO,110) T,NAMES(5)	00830
IF(IERR.EQ.1) CALL ERR(1)	00840
C	00850
C WRITE COMMON BLOCKS TO THE TRIAL-TAPE TO BE USED FOR	00860
C SUBSEQUENT SENSITIVITY ANALYSES	00870
C	00880
BUFFER OUT (4,1) (INPUTZ,INPUTZ(2680))	00890
IF(UNIT(4)) 200,150,150	00900
150 CALL ERR(11)	00910
200 BUFFER OUT (4,1) (WORKNZ,WORKNZ(1640))	00920
IF(UNIT(4)) 300,150,150	00930
300 BUFFER OUT (4,1) (WORKLZ,WORKLZ(1024))	00940
IF(UNIT(4)) 400,150,150	00950
400 BUFFER OUT (4,1) (WORKZ,WORKZ(NWORK))	00960
IF(UNIT(4)) 500,150,150	00970
C	00980
C WRITE VALUE AND PLAY OUTCOMES FOR EACH STAGE AND	00990
C STATE ON THE TRIAL-TAPE AND ON SCRATCH DISK	01000
C	01010
500 DO 600 I=1,NSTAGE	01020
CALL READMS(2,IARRAY(LOCBV8),NSTAT2,1)	01030
BUFFER OUT (4,1) (IARRAY(LOCBV8),IARRAY(LOCEVR))	01040
IF(UNIT(4)) 520,150,150	01050
520 CALL READMS(3,IARRAY(LOCBPB),NSTAT2,1)	01060
BUFFER OUT (4,1) (IARRAY(LOCBPB),IARRAY(LOCEPR))	01070
IF(UNIT(4)) 530,150,150	01080
530 BUFFER OUT (7,1) (IARRAY(LOCBV8),IARRAY(LOCEVR))	01090
IF(UNIT(7)) 550,540,540	01100
540 CALL ERR(12)	01110
550 BUFFER OUT (8,1) (IARRAY(LOCBPB),IARRAY(LOCEPR))	01120
IF(UNIT(8)) 600,560,560	01130
560 CALL ERR(13)	01140
600 CONTINUE	01150
CALL TRIALS	01160
CALL SECOND(T)	01170
WRITE(LUNO,100) T,NAMES(6)	01180
T=TIOCALL(X)	01190
WRITE(LUNO,110) T,NAMES(6)	01200
END	01210

FIGURE B-1 (cont'd)

	SUBROUTINE BATTLE	00110
C		00120
C	/BATTLE/ COMPUTES THE RESULTS OF A ONE-STAGE ENGAGEMENT	00130
C	BETWEEN SPECIFIED NUMBERS OF BLUE AND RED GROUND AND AIR	00140
C	FORCES ALLOCATED TO MISSIONS ACCORDING TO SPECIFIED	00150
C	STRATEGIES.	00160
C		00170
	COMMON /INPUT/ IMISS(8,4,2), IGRID(11,4,2), LASTP, NALOC(8,4),	00180
	INFRAC(4,2), NSHL(2), NSTAGE, NDAPST, CASF(4,2), IPRINT(8),	00190
	ITITLE(6), VALU(4,2), PKBD(4,4,2), PKBDES(4,4,2), XGRID(11,4,2),	00200
	PKAD(4,4,2), PKADES(4,4,2), PKHA(4,4,2), PKAA(4,4,2),	00210
	PKESBD(4,4,2), PKESAD(4,4,2), PKSH(4,2), PKNS(4,2), REIN(4,2,100),	00220
	WGHT(100,2), XSORT(8,4,2), NDIV(2), OWGHT(5), NRSAM(2),	00230
	PKRS(4,2), PKFS(4,2), ABAF(8,4,2), DIVFP(2), PKSAFS(4,2),	00240
	PKAARS(4,2), PKAARS(4,2), PKAEFS(4,2), PKAERS(4,2), PKREFS(4,2),	00250
	PKFAFS(4,2), PKRAFS(4,2), PKRARS(4,2), DFPRED(4,2), FEWA(2,28),	00260
	REINF(4,2,100)	00270
	COMMON /WORKN/ NTYPE(2), NMISS(4,2), NMISST(2), NGRID(4,2),	00280
	IBLURD(2), NSTRAT(4,2), NFULST(2), NSTAT, NINGAM, IMPNT(32,2),	00290
	ITPNT(32,2), IDEM(8), NSTRTC(2), IRA(100), JRA(100), LUN1, LUNO,	00300
	INWORK, NSTAT2, ISINT(500,2), IDINT(100,2), INPNT(32,2)	00310
	COMMON /WORKL/ LOCST(500,2), LOCBG, LOCEG, KOCBG, KOCEG, LOCBVR,	00320
	LOCBVB, LOCEVR, LOCEVB, LOCBPR, LOCBPB, LOCEPR, LOCEPB,	00330
	KOCBVB, KOCEVB, KOCBVR, KOCEVR, JOCBVB, JOCEVB, JOCBVR, JOCEVR,	00340
	IOCBVB, IOCEVB, IOCBVR, IOCEVR	00350
C		00360
C		00370
C	CODES FOR AIR MISSIONS	00380
C		00390
C	1 - CAS	00400
C	2 - ABA	00410
C	3 - BD	00420
C	4 - ABD	00430
C	5 - CAS ESCORT	00440
C	6 - ABA ESCORT	00450
C	7 - FORWARD DEFENSE SUPPRESSION	00460
C	8 - REAR DEFENSE SUPPRESSION	00470
C	9 - NOTHING	00480
C		00490
C		00500
	COMMON /WORK/ XARRAY(25000)	00510
	DIMENSION IARRAY(1)	00520
	EQUIVALENCE (XARRAY, IARRAY)	00530
	COMMON /BPARM/ CNP(4,2), IBR(2), XNP(9,4,2), OBJEC(2,5)	00540
	DIMENSION TNP(9,2), REMP(4,2), TCASO(2), TOTFP(2), RFSAM(2), HRSAM(2)	00550
	DIMENSION YNP(9,4,2), TFIRE(2), CASO(2), CNPV(4)	00560
	DATA(XNP=72(0.)), (YNP=72(0.))	00570
	TMOVE=0.	00580
	DO 50 K=1,2	00590
	TCASO(K)=0.	00600
	TOTFP(K)=0.	00610
	RFSAM(K)=NFSAM(K)	00620
	RRSAM(K)=NRSAM(K)	00630
50	CONTINUE	00640
	DO 900 N=1, NDAPST	00650
	XMOVE=0.	00660
	DO 100 M=1,9	00670
	DO 100 K=1,2	00680
	TNP(M,K)=0.	00690

FIGURE B-1 (cont'd)

100	CONTINUE	00700
C		00710
C	DETERMINE NUMBER OF SORTIES ALLOCATED TO EACH MISSION	00720
C		00730
	DO 110 K=1,2	00740
	CASO(K)=0.	00750
	Tfire(K)=NDIV(K)*DIVFP(K)	00760
	IUP=NMISS(K)	00770
	IST=IBR(K)	00780
	IST=LOCST(IST,K)-1	00790
	DO 110 I=1,IUP	00800
	IST=IST+1	00810
	L=INPNT(I,K)	00820
	M=IMPNT(I,K)	00830
	J=ITPNT(I,K)	00840
	XNP(M,J,K)=XARRAY(IST)*CNP(J,K)*XSORT(L,J,K)	00850
	YNP(M,J,K)=XNP(M,J,K)	00860
	TNP(M,K)=TNP(M,K)+XNP(M,J,K)	00870
110	CONTINUE	00880
C		00890
C		00900
C	BATTLE ASSESSMENT	00910
C		00920
C		00930
C		00940
	DO 200 K=1,2	00950
	L=3-K	00960
	XFSAM=RFSAM(L)	00970
	XRSAM=RRSAM(L)	00980
	IHL1=NTYPE(K)	00990
C		01000
C	FORWARD SAM SUPPRESSORS VS FORWARD SAMS	01010
C		01020
	IF(XFSAM.EQ. 0.) GO TO 125	01030
	SUMS=0.	01040
	DO 115 I=1,IHL1	01050
	SUMS=SUMS+XNP(7,I,K)*PKFS(1,L)	01060
115	CONTINUE	01070
	RFSAM(L)=XFSAM*EXP(-SUMS/XFSAM)	01080
C		01090
C	FORWARD SAMS VS FORWARD SAM SUPPRESSORS	01100
C		01110
	XOPP=TNP(7,K)	01120
	IF(XOPP.EQ. 0.) GO TO 125	01130
	XNENG=AMINI(XOPP,XFSAM)	01140
	RO=XNENG/XOPP	01150
	DO 120 I=1,IHL1	01160
	XNPS=XNP(7,I,K)	01170
	XN=RO*XNPS*PKFAFS(I,K)	01180
	XNP(7,I,K)=XNP(7,I,K)-XN	01190
120	CONTINUE	01200
C		01210
C	REMAINING FORWARD SAMS VS REAR SAM SUPPRESSORS	01220
C		01230
125	XOPP=TNP(8,K)	01240
	IF(XOPP.EQ. 0.) GO TO 200	01250
	XFSAM=RFSAM(L)	01260
	IF(XFSAM.EQ. 0.) GO TO 140	01270
	XNENG=AMINI(XOPP,XFSAM)	01280
	RO=XNENG/XOPP	

FIGURE B-1 (cont'd)

DO 130 I=1,IH11	01290
XNPS=XNP(8,I,K)	01300
XN=RO*XNPS*PKRAFS(I,K)	01310
XNP(8,I,K)=XNPS-XN	01320
XOPP=XOPP-XN	01330
130 CONTINUE	01340
C	01350
C REMAINING REAR SAM SUPPRESSORS VS REAR SAMS	01360
C	01370
IF(XOPP.LE. 0.) GO TO 200	01380
140 IF(XRSAM.EQ. 0.) GO TO 155	01390
SUMS=0.	01400
DO 145 I=1,IH11	01410
SUMS=SUMS+XNP(8,I,K)*PKRS(I,L)	01420
145 CONTINUE	01430
RRSAM(L)=XRSAM*EXP(-SUMS/XRSAM)	01440
C	01450
C REAR SAMS VS REMAINING REAR SAM SUPPRESSORS	01460
C	01470
C	01480
XNENG=AMIN1(XOPP,XRSAM)	01490
RO=XNENG/XOPP	01500
DO 150 I=1,IH11	01510
XNPS=XNP(8,I,K)	01520
XN=RO*XNPS*PKRARS(I,K)	01530
XNP(8,I,K)=XNPS-XN	01540
XOPP=XOPP-XN	01550
150 CONTINUE	01560
C	01570
C FORWARD SAMS VS RETURNING REAR SAM SUPPRESSORS	01580
C	01590
IF(XOPP.LE. 0.) GO TO 200	01600
155 IF(XFSAM.EQ. 0.) GO TO 200	01610
XNENG=AMIN1(XOPP,XFSAM)	01620
RO=XNENG/XOPP	01630
DO 160 I=1,IH11	01640
XNPS=XNP(8,I,K)	01650
XN=RO*XNPS*PKRAFS(I,K)	01660
XNP(8,I,K)=XNPS-XN	01670
160 CONTINUE	01680
200 CONTINUE	01690
C	01700
DO 700 K=1,2	01710
L=3-K	01720
IH11=NTYPE(K)	01730
IH12=NTYPE(L)	01740
XFSAM=RFSAM(L)	01750
XRSAM=RRSAM(L)	01760
C	01770
C FORWARD SAMS VS CAS ESCORTS	01780
C	01790
C	01800
ROI=1.	01810
XATT=TNP(5,K)	01820
XOPP=TNP(3,L)	01830
IF(XATT.EQ. 0.) GO TO 310	01840
IF(XFSAM.EQ. 0.) GO TO 250	01850
XNENG=AMIN1(XATT,XFSAM)	01860
RO=XNENG/XATT	01870
DO 225 I=1,IH11	
XNPS=XNP(5,I,K)	

FIGURE B-1 (cont'd)

	XN=RO*XNPS*PKBEFS(I,K)	01880
	XNP(5,I,K)=XNPS-XN	01890
	XATT=XATT-XN	01900
225	CONTINUE	01910
C		01920
C	CAS ESCORTS VS BD	01930
C		01940
	IF(XATT.LE.0.) GO TO 310	01950
250	IF(XOPP.EQ.0.) GO TO 310	01960
	XNENG=AMINI(XATT,XOPP)	01970
	RO=XNENG/XOPP	01980
	ROA=RO/XATT	01990
	ROI=1.-RO	02000
	DO 300 I=1,IHI1	02010
	DO 300 J=1,IHI2	02020
	XNPSH=XNP(5,I,K)	02030
	XNPSR=XNP(3,J,L)	02040
	XN=XNPSH*XNPSR*ROA	02050
	XNP(5,I,K)=XNPSH-PKESB(J,I,K)*XN	02060
	XNP(3,J,L)=XNPSR-PKBOES(I,J,L)*XN	02070
300	CONTINUE	02080
310	DO 350 J=1,IHI2	02090
	REMP(J,L)=YNP(3,J,L)*ROI	02100
350	CONTINUE	02110
C		02120
C	FORWARD SAMS VS CAS	02130
C		02140
	XATT=XOPP*ROI	02150
	XOPP=XNP(1,K)	02160
	ROI=1.	02170
	IF(XOPP.EQ.0.) GO TO 410	02180
	IF(XFSAM.EQ.0.) GO TO 370	02190
	XNENG=AMINI(XOPP,XFSAM)	02200
	RO=XNENG/XOPP	02210
	DO 360 I=1,IHI1	02220
	XNPS=XNP(1,I,K)	02230
	XN=RO*XNPS*PKBAFS(I,K)	02240
	XNP(1,I,K)=XNPS-XN	02250
	YNP(1,I,K)=XNP(1,I,K)	02260
	XOPP=XOPP-XN	02270
360	CONTINUE	02280
C		02290
C	BD NOT ENGAGED VS CAS	02300
C		02310
	IF(XOPP.LE.0.) GO TO 410	02320
370	IF(XATT.EQ.0.) GO TO 410	02330
	XNENG=AMINI(XATT,XOPP)	02340
	RO=XNENG/XOPP	02350
	ROA=RO/XATT	02360
	ROI=1.-RO	02370
	DO 400 I=1,IHI1	02380
	DO 400 J=1,IHI2	02390
	XNPS=XNP(1,I,K)	02400
	XN=REMP(J,L)*XNPS*ROA	02410
	XNP(3,J,L)=XNP(3,J,L)-PKBD(I,J,L)*XN	02420
	XNP(1,I,K)=XNPS-PKBA(J,I,K)*XN	02430
400	CONTINUE	02440
C		02450
C	ACCUMULATE CAS ORONANCE DELIVERED BY CAS NOT ENGAGED	02460

FIGURE B-1 (cont'd)

C		02470
410	DO 420 I=1,IH11	02480
	XNPC=YNP(1,I,K)*R01	02490
	CASO(K)=CASO(K)+XNPC*CASF(I,K)	02500
	TFIRE(L)=TFIRE(L)-XNPC*DFPRED(I,K)	02510
420	CONTINUE	02520
C		02530
C	FORWARD SAMS VS ABA ESCORTS	02540
C		02550
	R01=1.	02560
	XATT=TNP(6,K)	02570
	XOPP=TNP(4,L)	02580
	IF(XATT.EQ. 0.) GO TO 540	02590
	IF(XFSAM.EQ. 0.) GO TO 470	02600
	XNENG=AMIN1(XATT,XFSAM)	02610
	RO=XNENG/XATT	02620
	DO 460 I=1,IH11	02630
	XNPS=XNP(6,I,K)	02640
	XN=RO*XNPS*PKAEFS(I,K)	02650
	XNP(6,I,K)=XNPS-XN	02660
	XATT=XATT-XN	02670
460	CONTINUE	02680
C		02690
C	REAR SAMS VS ABA ESCORTS	02700
C		02710
470	IF(XATT.LE. 0.) GO TO 540	02720
	IF(XRSAM.EQ. 0.) GO TO 490	02730
	XNENG=AMIN1(XATT,XRSAM)	02740
	RO=XNENG/XATT	02750
	DO 480 I=1,IH11	02760
	XNPS=XNP(6,I,K)	02770
	XN=RO*XNPS*PKAERS(I,K)	02780
	XNP(6,I,K)=XNPS-XN	02790
	XATT=XATT-XN	02800
480	CONTINUE	02810
C		02820
C	ABA ESCORTS VS ABD	02830
C		02840
	IF(XATT.LE. 0.) GO TO 540	02850
490	IF(XOPP.EQ. 0.) GO TO 510	02860
	XNENG=AMIN1(XATT,XOPP)	02870
	RO=XNENG/XOPP	02880
	ROA=RO/XATT	02890
	R01=1.-RO	02900
	DO 500 I=1,IH11	02910
	DO 500 J=1,IH12	02920
	XNPSB=XNP(6,I,K)	02930
	XNPSR=XNP(4,J,L)	02940
	XN=XNPSB*XNPSR*ROA	02950
	XNN=PKESAD(J,I,K)*XN	02960
	XNP(6,I,K)=XNPSB-XNN	02970
	XATT=XATT-XNN	02980
	XNP(4,J,L)=XNPSR-PKADES(I,J,L)*XN	02990
500	CONTINUE	03000
C		03010
C	FORWARD SAMS VS RETURNING ABA ESCORTS	03020
C		03030
510	IF(XATT.LE. 0.) GO TO 540	03040
	IF(XFSAM.EQ. 0.) GO TO 540	03050

FIGURE B-1 (cont'd)

	XNENG=AMINI(XATT,XFSAM)	03060
	RO=XNENG/XATT	03070
	DO 520 I=1,IH11	03080
	XNPS=XNP(6,I,K)	03090
	XNP(6,I,K)=XNPS-XNPS*RO*PKAEFS(I,K)	03100
520	CONTINUE	03110
540	DO 550 J=1,IH12	03120
	REMP(J,L)=YNP(4,J,L)*ROI	03130
550	CONTINUE	03140
C		03150
C	FORWARD SAMS VS ABA	03160
C		03170
	XATT=XOPP*ROI	03180
	XOPP=TNP(2,K)	03190
	ROI=1.	03200
	IF(XOPP.EQ. 0.) GO TO 640	03210
	IF(XFSAM.EQ. 0.) GO TO 570	03220
	XNENG=AMINI(XOPP,XFSAM)	03230
	RO=XNENG/XOPP	03240
	DO 560 I=1,IH11	03250
	XNPS=XNP(2,I,K)	03260
	XN=RO*XNPS*PKAAFS(I,K)	03270
	XNP(2,I,K)=XNPS-XN	03280
	YNP(2,I,K)=XNP(2,I,K)	03290
	XOPP=XOPP-XN	03300
560	CONTINUE	03310
C		03320
C	REAR SAMS VS ABA	03330
C		03340
	IF(XOPP.LE. 0.) GO TO 640	03350
570	IF(XRSAM.EQ. 0.) GO TO 590	03360
	XNENG=AMINI(XOPP,XRSAM)	03370
	RO=XNENG/XOPP	03380
	DO 580 I=1,IH11	03390
	XNPS=XNP(2,I,K)	03400
	XN=RO*XNPS*PKAARS(I,K)	03410
	XNP(2,I,K)=XNPS-XN	03420
	YNP(2,I,K)=XNP(2,I,K)	03430
	XOPP=XOPP-XN	03440
580	CONTINUE	03450
C		03460
C	ABD NOT ENGAGED VS ABA	03470
C		03480
	IF(XOPP.LE. 0.) GO TO 640	03490
590	IF(XATT.EQ. 0.) GO TO 610	03500
	XNENG=AMINI(XATT,XOPP)	03510
	RO=XNENG/XOPP	03520
	ROA=RO/XATT	03530
	ROI=1.-RO	03540
	DO 600 I=1,IH11	03550
	DO 600 J=1,IH12	03560
	XNPS=XNP(2,I,K)	03570
	XN=REMP(J,L)*XNPS*ROA	03580
	XNN=PKAA(J,I,K)*XN	03590
	XNP(2,I,K)=XNPS-XNN	03600
	XNP(4,J,L)=XNP(4,J,L)-PKAD(I,J,L)*XN	03610
	XOPP=XOPP-XNN	03620
600	CONTINUE	03630
C		03640

FIGURE B-1 (cont'd)

C	FORWARD SAMS VS RETURNING ABA	03650
C		03660
610	IF(XOPP .LE. 0.) GO TO 640	03670
	IF(XFSAM .LE. 0.) GO TO 640	03680
	XNENG=AMINI(XOPP,XFSAM)	03690
	RO=XNENG/XOPP	03700
	DO 620 I=1,IH1	03710
	XNPS=XNP(2,I,K)	03720
	XNP(2,I,K)=XNPS-XNPS*RO*PKAIFS(I,K)	03730
620	CONTINUE	03740
640	DO 650 I=1,IH1	03750
	REMP(I,K)=YNP(2,I,K)*RO	03760
650	CONTINUE	03770
700	CONTINUE	03780
C		03790
C	COMPUTE AIRCRAFT ON GROUND KILLED BY ABA NOT ENGAGED	03800
C		03810
	DO 800 K=1,2	03820
	L=3-K	03830
	IHI1=NTYPE(K)	03840
	IHI2=NTYPE(L)	03850
	ATTK=0.	03860
	TARG=0.	03870
	SUMS=0.	03880
	SUMN=0.	03890
	DO 715 J=1,IHI2	03900
	IUP=NMISS(J,L)	03910
	CNP(J,L)=0.	03920
	CNPV(J)=0.	03930
	DO 710 M=1,IUP	03940
	IM=IMISS(M,J,L)	03950
	CP=XNP(IM,J,L)/XSORT(M,J,L)	03960
	CNP(J,L)=CNP(J,L)+CP	03970
	CNPV(J)=CNPV(J)+CP*ABAF(M,J,L)	03980
710	CONTINUE	03990
	TARG=TARG+CNPV(J)	04000
715	CONTINUE	04010
	IF(TARG .EQ. 0.) GO TO 800	04020
	NTARG=TARG	04030
	TARGS=AMINO(NSHL(L),NTARG)	04040
	TARGN=NTARG-TARGS	04050
	RS=TARGS/TARG	04060
	RN=1.-RS	04070
	DO 720 I=1,IHI1	04080
	CP=REMP(I,K)	04090
	ATTK=ATTK+CP	04100
	SUMS=SUMS+CP*RS*PKSH(I,L)	04110
	SUMN=SUMN+CP*RN*PKNS(I,L)	04120
720	CONTINUE	04130
	IF(ATTK .EQ. 0.) GO TO 800	04140
	TSNK=0.	04150
	IF(TARGS .EQ. 0.) GO TO 730	04160
	TSNK=TARGS*EXP(-SUMS/TARGS)	04170
730	TNNK=0.	04180
	IF(TARGN .EQ. 0.) GO TO 740	04190
	TNNK=TARGN*EXP(-SUMN/TARGN)	04200
740	FR=1.-(TSNK+TNNK)/TARG	04210
	DO 750 J=1,IHI2	04220
	CNP(J,L)=CNP(J,L)-CNPV(J)*FR	04230
750	CONTINUE	04240

FIGURE B-1 (cont'd)

```

800  CONTINUE                                04250
      DO 805 K=1,2                          04260
      TCASO(K)=TCA50(K)*CASO(K)             04270
805  CONTINUE                                04280
      BTFP=AMAX1(0.,TFIRE(1))               04290
      RTFP=AMAX1(0.,TFIRE(2))               04300
      TOTFP(1)=TOTFP(1)+BTFP*CASO(1)        04310
      TOTFP(2)=TOTFP(2)+RTFP*CASO(2)        04320
      IF(FEBA(1,1).EQ.-1.) GO TO 900        04330
      FRATIO=100.                           04340
      IF(RTFP.EQ.0.) GO TO 810              04350
      FRATIO=BTFP/RTFP                      04360
      IF(FRATIO.GT.100.) FRATIO=100.        04370
      GO TO 815                             04380
810  IF(BTFP.EQ.0.) FRATIO=1.0              04390
815  DO 820 I=2,28                          04400
      IF(FRATIO.LE.FEBA(1,I)) GO TO 830    04410
820  CONTINUE                                04420
      GO TO 850                             04430
830  XMOVE=FEBA(2,I-1)+(FRATIO-FEBA(1,I-1))*(FEBA(2,I)-FEBA(2,I-1))/ 04440
      1*(FEBA(1,I)-FEBA(1,I-1))            04450
850  TMOVE=TMOVE+XMOVE                      04460
900  CONTINUE                                04470
C                                           04480
C      ASSIGN OBJECTIVE FUNCTION VALUES    04490
C                                           04500
      DO 920 K=1,2                          04510
      OBJEC(K,1)=TCASO(K)                  04520
      OBJEC(K,2)=TOTFP(K)                  04530
920  CONTINUE                                04540
      OBJEC(1,3)=TMOVE/2.                  04550
      OBJEC(2,3)=-OBJEC(1,3)               04560
      RETURN                                04570
      END                                  04580

```

```

SUBROUTINE BETAS                                00110
C                                           00120
C      /BETAS/ COMPUTES THE WEIGHTS USED FOR LINEAR INTERPOLATION 00130
C      BETWEEN GRID POINTS IN THE STATE SPACE. 00140
C                                           00150
COMMON /INPUT/ IMISS(8,4,2), IGRID(11,4,2), LASTP, NALOC(8,4), 00160
INFRAC(4,2), NSHL(2), NSTAGE, NDAPST, CASF(4,2), IPRINT(8), 00170
IITITLE(6), VALU(4,2), PKBD(4,4,2), PKBDES(4,4,2), XGRID(11,4,2), 00180
IPKAD(4,4,2), PKADES(4,4,2), PKBA(4,4,2), PKAA(4,4,2), 00190
IPKESBD(4,4,2), PKESAD(4,4,2), PKSH(4,2), PKNS(4,2), REIN(4,2,100), 00200
IWGHT(100,2), XSORT(8,4,2), NDIV(2), OWGHT(5), NRSAM(2), NFSAM(2), 00210
IPKRS(4,2), PKFS(4,2), ABAF(8,4,2), DIVFP(2), PKBAFS(4,2), 00220
IPKAIFS(4,2), PKAHS(4,2), PKAEFS(4,2), PKAERS(4,2), PKBEFS(4,2), 00230
IPKFAFS(4,2), PKRAFS(4,2), PKRAFS(4,2), DFPRED(4,2), FEBA(2,28), 00240
IREINF(4,2,100) 00250
COMMON /WORKN/ NTYPE(2), NMIS(4,2), NMISST(2), NGRID(4,2), 00260
IBLURD(2), NSTRAT(4,2), NFULST(2), NSTAT, NINGAM, IMPNT(32,2), 00270
IITPNT(32,2), IDEH(8), NSTRTC(2), IRA(100), JRA(100), LUNI, LUNO, 00280
INWORK, NSTAT2, ISINT(500,2), IDINT(100,2), INPNT(32,2) 00290

```

FIGURE B-1 (cont'd)

```

COMMON /WORKL/ LOCST(500,2),LOCBG,LOCEG,KUCBG,KOCEG,LOCBVR,
1LOCBVB,LOCEVR,LOCEVB,LOCBPR,LOCBPR,LOCEPR,LOCEPB,
1KOCBVB,KOCEVR,KOCEVB,JOCEVR,JOCEVB,JOCEVR,JOCEVR,
1IOCBVB,IOCEVR,IOCBVR,IOCEVR
COMMON /BPARM/ CNP(8),IB,IR,XNP(9,4,2),OBJEC(2,5)
COMMON /INTERP/ BETA(2,8),IBETA(2,8),NDEX(8),IMI(8)
DIMENSION YGRID(11,8)
EQUIVALENCE (XGRID,YGRID)
DO 200 K=1,8
DO 100 M=2,11
IF(CNP(K)-YGRID(M,K)) 150,150,100
100 CONTINUE
M=11
150 N=M-1
IBETA(1,K)=N-1
IBETA(2,K)=M-1
DIF=YGRID(M,K)-YGRID(N,K)
IF(DIF.EQ. 0.) GO TO 175
BETA(1,K)=(YGRID(M,K)-CNP(K))/DIF
GO TO 190
175 BETA(1,K)=1.
IBETA(2,K)=0
190 BETA(2,K)=1.-BETA(1,K)
200 CONTINUE
IF(IPRINT(8).EQ. 0) RETURN
WRITE(LUNO,900) IBETA
900 FORMAT(/,8H IBETAS=,2(8I5/8X))
WRITE(LUNO,910) BETA
910 FORMAT(7H BETAS=,2(8F5,2/7X))
RETURN
END

```

```

SUBROUTINE ERR(K)
C
C /ERR/ IS CALLED TO PRINT A DIAGNOSTIC OR ERROR MESSAGE.
C
COMMON /INPUT/ IMISS(8,4,2),IGRID(11,4,2),LASTP,NALOC(8,4),
1NFRAC(4,2),NSHL(2),NSTAGE,NDAPST,CASF(4,2),IPRINT(8),
1ITITLE(6),VALU(4,2),PKBD(4,4,2),PKBDES(4,4,2),XGRID(11,4,2),
1PKAD(4,4,2),PKADES(4,4,2),PKBA(4,4,2),PKAA(4,4,2),
1PKESBD(4,4,2),PKESAD(4,4,2),PKSH(4,2),PKNS(4,2),REIN(4,2,100),
1WGHT(100,2),XSORT(8,4,2),NDIV(2),OWGHT(5),NRSAM(2),NFSAM(2),
1PKRS(4,2),PKFS(4,2),ABAF(8,4,2),DIVFP(2),PKBAFS(4,2),
1PKAAFS(4,2),PKAARS(4,2),PKAEFS(4,2),PKAERS(4,2),PKBEFS(4,2),
1PKFAFS(4,2),PKRAFS(4,2),PKRARS(4,2),OFFRED(4,2),FEBA(2,28),
1REINF(4,2,100)
COMMON /WORKN/ NTYPE(2),NMISS(4,2),NMISST(2),NGRID(4,2),
1IBLURD(2),NSTRAT(4,2),NFULST(2),NSTAT,NINGAM,IMPNT(32,2),
1ITPNT(32,2),IDEM(8),NSTRTC(2),IRA(100),JRA(100),LUNI,LUNO,
1NWORK,NSTAT2,ISINT(500,2),IDINT(100,2),INPNT(32,2)
COMMON /WORKL/ LOCST(500,2),LOCBG,LOCEG,KUCBG,KOCEG,LOCBVR,
1LOCBVB,LOCEVR,LOCEVB,LOCBPR,LOCBPR,LOCEPR,LOCEPB,
1KOCBVB,KOCEVR,KOCEVB,JOCEVR,JOCEVB,JOCEVR,JOCEVR,
1IOCBVB,IOCEVR,IOCBVR,IOCEVR
COMMON /ERROR/ IERR

```

FIGURE B-1 (cont'd)

```

DIMENSION IMESSG(6,30), IERRDR(3), IETYPE(30)                                00340
DATA(IMESSG=180(1H ))                                                         00350
DATA(IERRDR=10H***INFO***,10H***ERROR**,10H***ABORT**)                       00360
DATA(IMESSG(1,1)=31HRUN ABORTED DUE TO FATAL ERRORS)                         00370
DATA(IMESSG(1,2)=28HDATA CARD KEY NOT RECOGNIZED)                           00380
DATA(IMESSG(1,3)=45HTOD MANY PURE STRATEGIES TO BE STORED IN CORE)           00390
DATA(IMESSG(1,4)=41HTOO MANY STATES TO STORE VALUES AND PLAYS)             00400
DATA(IMESSG(1,5)=43HNOT ENOUGH COMMON AREA TO STORE GAME MATRIX)            00410
DATA(IMESSG(1,6)=44HBUFFER OUT ERROR TO TAPE1 IN SUBROUTINE INIT)           00420
DATA(IMESSG(1,7)=40HUSER REQUESTED ONLY A DATA CHECK AND TIM)              00430
DATA(IMESSG(5,7)=10HE ESTIMATE)                                               00440
DATA(IMESSG(1,8)=40HSUM OF SPECIFIED ALLOCATIONS EXCEEDS 1.0)               00450
DATA(IMESSG(1,9)=32HSMALLEST GRID LEVEL MUST BE ZERO)                      00460
DATA(IMESSG(1,10)=40HBUFFER IN ERROR FROM TAPE1 IN SUBROUTINE)              00470
DATA(IMESSG(5,10)=6H GAMES)                                                    00480
DATA(IMESSG(1,11)=41HBUFFER OUT ERROR TO TAPE4 IN MAIN PROGRAM)              00490
DATA(IMESSG(1,12)=41HBUFFER OUT ERROR TO TAPE7 IN MAIN PROGRAM)             00500
DATA(IMESSG(1,13)=41HBUFFER OUT ERROR TO TAPE8 IN MAIN PROGRAM)             00510
DATA(IMESSG(1,14)=40HBUFFER IN ERROR FROM TAPE7 IN SUBROUTINE)              00520
DATA(IMESSG(5,14)=7H TRIALS)                                                  00530
DATA(IMESSG(1,15)=40HBUFFER IN ERROR FROM TAPE8 IN SUBROUTINE)              00540
DATA(IMESSG(5,15)=7H TRIALS)                                                  00550
DATA(IMESSG(1,16)=33HRUN CARD MUST PRECEDE TRIAL CARDS)                    00560
DATA(IMESSG(1,17)=38HTRIAL CARD IGNORED -- INCORRECT FORMAT)                00570
DATA(IMESSG(1,18)=40HTRIAL CARD IGNORED -- TOO MANY STAGES RE)              00580
DATA(IMESSG(5,18)=7HREQUESTED)                                                00590
DATA(IMESSG(1,19)=40HTRIAL CARD IGNORED -- TOO MANY PLANES OF)              00600
DATA(IMESSG(5,19)=19H ONE TYPE SPECIFIED)                                    00610
DATA(IMESSG(1,20)=40HDISK I/O ERROR ON TAPE9 IN SUBROUTINE TR)              00620
DATA(IMESSG(5,20)=4HIALS)                                                      00630
DATA(IMESSG(1,21)=40HBUFFER OUT ERROR ON TAPE9 IN SUBROUTINE )              00640
DATA(IMESSG(5,21)=6HREADIN)                                                    00650
DATA(IMESSG(1,22)=42HBUFFER IN ERROR FROM TAPE4 IN MAIN PROGRAM)            00660
DATA(IMESSG(1,23)=40HIF ALL ALLOCATIONS ARE SPECIFIED THEY MU)              00670
DATA(IMESSG(5,23)=13HST SUM TO 1.0)                                           00680
DATA(IMESSG(1,24)=38HI/O ERROR ON TAPE10 IN SUBROUTINE INIT)                00690
DATA(IMESSG(1,25)=40HSTRATEGIES NOT SPECIFIED THRU THE LAST S)              00700
DATA(IMESSG(5,25)=16HTAGE OF CAMPAIGN)                                         00710
DATA(IMESSG(1,26)=40HBUFFER IN ERROR ON TAPE9 IN SUBROUTINE 1)              00720
DATA(IMESSG(5,26)=3HINIT)                                                      00730
DATA(IETYPE=3,2,6(3),2,7(3),3(1),4(3),7(3))                                00740
IDERR=IETYPE(K)                                                                00750
WRITE(LUN0,100) IERRDR(IDERR), (IMESSG(I,K),I=1,6)                          00760
100 FORMAT(/,1X,A10,1X,6A10,/)                                               00770
IF(IDERR .EQ. 3) STOP                                                         00780
IF(IDERR .EQ. 1) RETURN                                                       00790
IERR=1                                                                          00800
RETURN                                                                          00810
END                                                                              00820

SUBROUTINE GAMES                                                                00110
C                                                                              00120
C /GAMES/ PERFORMS A DYNAMIC PROGRAMMING BACKWARD PASS                      00130
C COMPUTING FOR EACH STAGE AND STATE THE MAXMIN AND MINMAX                 00140
C STRATEGIES AND ASSOCIATED OBJECTIVE FUNCTION VALUES FOR                00150
C BOTH BLUE AND RED.                                                         00160

```

FIGURE B-1 (cont'd)

```

C      COMMON /INPUT/ IMISS(8,4,2), IGRID(11,4,2), LASTP, NALOC(8,4),
      INFRAC(4,2), NSHL(2), NSTAGE, NDAPST, CASF(4,2), IPRINT(8),
      ITITLE(6), VALU(4,2), PKBD(4,4,2), PKBDES(4,4,2), XGRID(11,4,2),
      1PKAU(4,4,2), PKADES(4,4,2), PKBA(4,4,2), PKAA(4,4,2),
      1PKESBD(4,4,2), PKESAD(4,4,2), PKSH(4,2), PKNS(4,2), REIN(4,2,100),
      1WGHT(100,2), XSORT(8,4,2), NDIV(2), OWGHT(5), NKSAM(2), NFSAM(2),
      1PKRS(4,2), PKFS(4,2), ABAF(8,4,2), DIVFP(2), PKWAFS(4,2),
      1PKAAFS(4,2), PKAARS(4,2), PKAEFS(4,2), PKAERS(4,2), PKBEFS(4,2),
      1PKFAFS(4,2), PKRAFS(4,2), PKRAHS(4,2), DFPRED(4,2), FEBA(2,28),
      1REINF(4,2,100)
      COMMON /WORKN/ NTYPE(2), NMISS(4,2), NMISST(2), NGRID(4,2),
      11BLURD(2), NSTRAT(4,2), NFULST(2), NSTAT, NINGAM, IMPNT(32,2),
      11TPNT(32,2), IDEM(8), NSTRIC(2), IRA(100), JRA(100), LUNI, LUNO,
      1NWORK, NSTAT2, ISINT(500,2), IDINT(100,2), INPNT(32,2)
      COMMON /WORKL/ LOCST(500,2), LOCHG, LOCEG, KOCHG, KOCEG, LOCBVR,
      1LOCBVB, LOCEVR, LOCEVB, LOCBPR, LOCBPB, LOCEPR, LOCEPB,
      1KOCBVB, KOCEVB, KOCHVR, KOCEVR, JOCBVB, JOCEVB, JOCBVR, JOCEVR,
      1IOCBVB, IOCEVB, IOCHVR, IOCEVR
      COMMON /INTERP/ BETA(2,8), 1BETA(2,8), J1, J2, J3, J4, J5, J6, J7, J8,
      1JH11, JH12, JH13, JH14, JH15, JH16, JH17, JH18
      COMMON /IPARM/ DELTA(8), JBETA(2,8,128), XBETA(2,8,128), IBIT(8)
      COMMON /ROUND/ JDEX(4,2,2)
      DIMENSION MVEC(8), NVEC(8)
      EQUIVALENCE(MVEC, JDEX(1,1,1)), (NVEC, JDEX(1,1,2))
      COMMON /WORK/ XARRAY(25000)
      DIMENSION JHI(8), JVEC(8), NDEX(8), BMIN(500), RMAX(500), IARRAY(1)
      DIMENSION IVERT(8,256), IRSINT(500), IRSINT(500)
      EQUIVALENCE(IRSINT(1,1), IRSINT), (IRSINT(1,2), IRSINT)
      EQUIVALENCE(XARRAY, IARRAY), (NDEX, J1), (JH1, JH11)
      DIMENSION SEIN(8,100), SEINF(8,100)
      EQUIVALENCE(REIN, SEIN), (REINF, SEINF)
      COMMON /TEMP/ IPPNT(8), TEIN(8), TEINF(8), NPTT
      DATA(JDEX=16(0)), (JVEC=8(0)), (JH1=8(1)), (IVERT=2048(1))
      NPTT=NTYPE(1)*NTYPE(2)
      MPTT=NPTT
      M=4-NTYPE(1)
      DO 25 NN=1, NPTT
      JHI(NN)=2
      N=NN
      IF(N.GT. NTYPE(1)) N=N*M
      IPPNT(NN)=N
      25  CONTINUE
      IF(1PPNT(NPTT).EQ. 8) MPTT=MPTT-1
      ICNT=0
      DO 50 J8=1, JH18
      DO 50 J7=1, JH17
      DO 50 J6=1, JH16
      DO 50 J5=1, JH15
      DO 50 J4=1, JH14
      DO 50 J3=1, JH13
      DO 50 J2=1, JH12
      DO 50 J1=1, JH11
      ICNT=ICNT+1
      DO 50 NN=1, NPTT
      IVERT(NN, ICNT)=NDEX(NN)
      50  CONTINUE
      LPTT=ICNT
      IH11=NFULST(2)

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00170
00180
00190
00200
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00750

```

FIGURE B-1 (cont'd)

	IHI2=IHI1-1	00760
	IHI3=NFULST(1)	00770
	LVB=LOCBVB-1	00780
	LVR=LOCBVR-1	00790
	LPB=LOCBPB-1	00800
	LPR=LOCBPR-1	00810
	KVB=KOCBVB-1	00820
	KVR=KOCBVR-1	00830
	JVB=JOCBVB-1	00840
	JVR=JOCBVR-1	00850
	IVB=IOCBVB-1	00860
	IVR=IOCBVR-1	00870
	DO 900 I=1,NSTAGE	00880
	MSLOC=NSTAGE-I+1	00890
	NSLOC=MSLOC+1	00900
	IDINTB=IDINT(MSLOC,1)	00910
	IDINTR=IDINT(MSLOC,2)	00920
	WGHTB=WGHT(MSLOC,1)	00930
	WGHTR=WGHT(MSLOC,2)	00940
	DO 75 NN=1,NPTT	00950
	N=IPPNT(NN)	00960
	TEINF(N)=SEINF(N,NSLOC)	00970
	TEIN(N)=SEIN(N,NSLOC)/DELTA(N)+1.5	00980
75	CONTINUE	00990
	REWIND 1	01000
	DO 800 J=1,NSTAT	01010
	IF(IPRINT(7) .NE. 0) WRITE(LUNO,80) MSLOC,J	01020
80	FORMAT(/,7H STAGE=,I3,3X,6HSTATE=,I3)	01030
	BUFFER IN (1,1) (IARRAY(LOCBG),IARRAY(KOCEG))	01040
	IF(UNIT(1)) 200,100,100	01050
100	CALL ERR(10)	01060
C		01070
C	COMPUTE INTERPOLATED VALUES AND PLAYS FOR EACH STATE	01080
C		01090
200	DO 210 K=1,IHI3	01100
	BMIN(K)=1.E10	01110
210	CONTINUE	01120
	DO 220 K=1,IHI1	01130
	RMAX(K)=-1.E10	01140
220	CONTINUE	01150
	ICNT=0	01160
	DO 400 K=LOCBG,LOCEG,IHI1	01170
	ICNT=ICNT+1	01180
	IF(IRSINT(ICNT) .EQ. IDINTB) GO TO 300	01190
	BMIN(ICNT)=-1.E10	01200
	GO TO 400	01210
300	IHI=K+IHI2	01220
	JCNT=0	01230
	DO 390 L=K,IHI	01240
	JCNT=JCNT+1	01250
	IF(IRSINT(JCNT) .EQ. IDINTR) GO TO 305	01260
	RMAX(JCNT)=1.E10	01270
	GO TO 390	01280
305	IWORD=IARRAY(L)	01290
	JWORD=IARRAY(L+NINGAM)	01300
	DO 310 NN=1,NPTT	01310
	N=IPPNT(NN)	01320
	LEVEL=LBYT(IBIT(N),7,JWORD)	01330

FIGURE B-1 (cont'd)

	LEVEL=TEINF(N)*LEVEL+TEIN(N)	01340
	IF(LEVEL.LT. 1) LEVEL=1	01350
	IF(LEVEL.GT. 128) LEVEL=128	01360
	DO 310 M=1,2	01370
	1BETA(M,N)=JBETA(M,N,LEVEL)	01380
	BETA(M,N)=XBETA(M,N,LEVEL)	01390
310	CONTINUE	01400
	IOBJ=LBYT(31,29,IWORD)	01410
	JOBJ=LBYT(1,29,IWORD)	01420
	IF(LBYT(60,1,IWORD).EQ. 1) IOBJ=-IOBJ	01430
	IF(LBYT(30,1,IWORD).EQ. 1) JOBJ=-JOBJ	01440
	CHECKB=IOBJ*WGHTB-JOBJ*WGHTR	01450
	CHECKR=CHECKB	01460
	DO 340 LL=1,LPTT	01470
	ALPHA=1.	01480
	DO 320 NN=1,NPTT	01490
	N=1PPNT(NN)	01500
	M=1VERT(NN,LL)	01510
	JVEC(N)=IBETA(M,N)	01520
	ALPHA=ALPHA*BETA(M,N)	01530
320	CONTINUE	01540
	IF(ALPHA.EQ. 0.) GO TO 340	01550
	1STAT=JVEC(8)+1	01560
	DO 330 NN=1,MPTT	01570
	N=1PPNT(NN)	01580
	1STAT=1STAT+JVEC(N)*IDEM(N)	01590
330	CONTINUE	01600
	CHECKB=CHECKB+ALPHA*XARRAY(LVB+1STAT)	01610
	CHECKR=CHECKR+ALPHA*XARRAY(LVR+1STAT)	01620
340	CONTINUE	01630
	IF(CHECKB.GE. BMIN(1CNT)) GO TO 350	01640
	BMIN(1CNT)=CHECKB	01650
350	IF(CHECKR.LE. RMAX(1CNT)) GO TO 390	01660
	RMAX(1CNT)=CHECKR	01670
390	CONTINUE	01680
400	CONTINUE	01690
C		01700
C	STORE BLUES MAXMIN PLAY	01710
C		01720
	XMAX=-1.E10	01730
	DO 410 N=1,1H13	01740
	IF(XMAX.GE. BMIN(N)) GO TO 410	01750
	XMAX=BMIN(N)	01760
	1BPLAY=N	01770
410	CONTINUE	01780
	XARRAY(KVB+J)=XMAX	01790
	1ARRAY(LPB+J)=1BPLAY	01800
C		01810
C	STORE REDS MINMAX PLAY	01820
C		01830
	XMIN=1.E10	01840
	DO 420 N=1,1H11	01850
	IF(XMIN.LE. RMAX(N)) GO TO 420	01860
	XMIN=RMAX(N)	01870
	1RPLAY=N	01880
420	CONTINUE	01890
	XARRAY(KVR+J)=XMIN	01900
	1ARRAY(LPR+J)=1RPLAY	01910
C		01920

FIGURE B-1 (cont'd)

C	COMPUTE AND STORE MAXMIN FOR BLUE	01930
C		01940
	ILO=LOCBG+IHII*(IBPLAY-1)	01950
	IHI=ILO+IHII-1	01960
	JCNT=0	01970
	XMIN=1.E10	01980
	DO 600 K=ILO,IHI	01990
	JCNT=JCNT+1	02000
	IF(IRSINT(JCNT) .NE. IDINTR) GO TO 600	02010
	IWORD=IARRAY(K)	02020
	JWORD=IARRAY(K+NINGAM)	02030
	IOBJ=LBYT(31,29,IWORD)	02040
	JOBJ=LBYT(1,29,IWORD)	02050
	IF(LBYT(60,1,IWORD) .EQ. 1) IOBJ=-IOBJ	02060
	IF(LBYT(30,1,IWORD) .EQ. 1) JOBJ=-JOBJ	02070
	DO 510 NN=1,NPTT	02080
	N=IPPNT(NN)	02090
	M=(N-1)/4+1	02100
	LEVEL=LBYT(1BIT(N),7,JWORD)	02110
	LEVEL=TEINF(N)*LEVEL+TEIN(N)	02120
	IF(LEVEL .LT. 1) LEVEL=1	02130
	IF(LEVEL .GT. 128) LEVEL=128	02140
	MVEC(N)=JBETA(M,N,LEVEL)	02150
510	CONTINUE	02160
	IS=ISTATE(MVEC)	02170
	CHECK=IOBJ*WGHTB-JOBJ*WGHTR+XARRAY(JVB-IS)	02180
	IF(CHECK .GE. XMIN) GO TO 600	02190
	XMIN=CHECK	02200
600	CONTINUE	02210
	XARRAY(IVB+J)=XMIN	02220
	IF(IPRINT(7) .NE. 0) WRITE(LUNO,605) XMIN,IBPLAY	02230
605	FORMAT(8H MAXMIN=,F10.0,2X,5HPLAY=,I3)	02240
C		02250
C	COMPUTE AND STORE MINMAX FOR RED	02260
C		02270
	ILO=LOCBG+IRPLAY-1	02280
	IHI=ILO+(IHII3-1)*IHII	02290
	ICNT=0	02300
	XMAX=-1.E10	02310
	DO 700 K=ILO,IHI,IHI	02320
	ICNT=ICNT+1	02330
	IF(IRSINT(ICNT) .NE. IDINTB) GO TO 700	02340
	IWORD=IARRAY(K)	02350
	JWORD=IARRAY(K+NINGAM)	02360
	IOBJ=LBYT(31,29,IWORD)	02370
	JOBJ=LBYT(1,29,IWORD)	02380
	IF(LBYT(60,1,IWORD) .EQ. 1) IOBJ=-IOBJ	02390
	IF(LBYT(30,1,IWORD) .EQ. 1) JOBJ=-JOBJ	02400
	DO 610 NN=1,NPTT	02410
	N=IPPNT(NN)	02420
	MM=2-(N-1)/4	02430
	LEVEL=LBYT(1BIT(N),7,JWORD)	02440
	LEVEL=TEINF(N)*LEVEL+TEIN(N)	02450
	IF(LEVEL .LT. 1) LEVEL=1	02460
	IF(LEVEL .GT. 128) LEVEL=128	02470
	NVEC(N)=JBETA(MM,N,LEVEL)	02480
610	CONTINUE	02490
	IS=ISTATE(NVEC)	02500
	CHECK=IOBJ*WGHTB-JOBJ*WGHTR+XARRAY(JVR-IS)	02510

FIGURE B-1 (cont'd)

	IF(CHECK .LE. XMAX) GO TO 700	02520
	XMAX=CHECK	02530
700	CONTINUE	02540
	XARRAY(IVR+J)=XMAX	02550
	IF(IPRINT(7) .NE. 0) WRITE(LUNO,705) XMAX,IRPLAY	02560
705	FORMAT(8H MINMAX=,F10.0,2X,5HPLAY=,I3)	02570
800	CONTINUE	02580
C		02590
C	WRITE PLAYS AND VALUES ON RA MASS STORAGE	02600
C		02610
	CALL WRITMS(3,IARRAY(LOCBPB),NSTAT2,MSLOC)	02620
	CALL WRITMS(2,IARRAY(IOCBBB),NSTAT2,MSLOC)	02630
	DO 850 J=1,NSTAT2	02640
	IARRAY(LVB+J)=IARRAY(KVB+J)	02650
	IARRAY(JVB+J)=IARRAY(IVB+J)	02660
850	CONTINUE	02670
900	CONTINUE	02680
	RETURN	02690
	END	02700
	SUBROUTINE INIT	00110
C		00120
C	/INIT/ ASSIGNS COUNTERS AND POINTERS, COMPUTES THE PURE	00130
C	STRATEGIES AND THE NUMBER OF STATES, AND COMPUTES AND STORES	00140
C	ON MASS STORAGE THE BATTLE ASSESSMENTS FOR EACH STATE AND	00150
C	PURE STRATEGY COMBINATION.	00160
C		00170
	COMMON /INPUT/ IMISS(8,4,2),IGRID(11,4,2),LASTP,NALOC(8,4),	00180
	INFRAC(4,2),NSHL(2),NSTAGE,NDAPST,CASF(4,2),IPRINT(8),	00190
	IITITLE(6),VALU(4,2),PKBD(4,4,2),PKBDES(4,4,2),XGRID(11,4,2),	00200
	IPKAD(4,4,2),PKADES(4,4,2),PKBA(4,4,2),PKAA(4,4,2),	00210
	IPKESBD(4,4,2),PKESAD(4,4,2),PKSH(4,2),PKNS(4,2),KEIN(4,2,100),	00220
	WGHT(100,2),XSORT(8,4,2),NDIV(2),OWGHT(5),NRSAM(2),NFSAM(2),	00230
	IPKRS(4,2),PKFS(4,2),ABAF(8,4,2),DIVFP(2),PKBAFS(4,2),	00240
	IPKAIFS(4,2),PKAARS(4,2),PKAEFS(4,2),PKAERS(4,2),PKBEFS(4,2),	00250
	IPKFAFS(4,2),PKRAFS(4,2),PKRARS(4,2),DFPREU(4,2),FEDA(2,28),	00260
	IREINF(4,2,100)	00270
	COMMON /WORKN/ NTYPE(2),NMISS(4,2),NMISST(2),NGRID(4,2),	00280
	IIBLURD(2),NSTRT(4,2),NFULST(2),NSTAT,NINGAM,IMPNT(32,2),	00290
	IITPNT(32,2),IDEM(8),NSTRIC(2),IRA(100),JRA(100),LUNI,LUNO,	00300
	INWORK,NSTAT2,ISINT(500,2),IDINT(100,2),INPNT(32,2)	00310
	COMMON /WORKL/ LOCST(500,2),LOCBG,LOCEG,KUCBG,KOCEG,LOCBVR,	00320
	ILOCBVB,LOCEVR,LOCEVB,LOCBPR,LOCBPB,LOCEPR,LOCEPB,	00330
	IKOCBVB,KOCEVB,KOCBVR,KOCEVR,JOCBVB,JOCEVB,JOCBVR,JOCEVR,	00340
	IIOCBBVB,IOCEVB,IOCBVR,IOCEVR	00350
	COMMON /WORK/ XARRAY(25000)	00360
	DIMENSION IARRAY(1)	00370
	DIMENSION KEVL(8)	00380
	EQUIVALENCE (XARRAY,IARRAY)	00390
	DIMENSION STRATS(8,200,4),JGRID(11,8),YGRID(11,8)	00400
	EQUIVALENCE (XARRAY(18601),STRATS)	00410
	EQUIVALENCE (IGRID,JGRID),(XGRID,YGRID)	00420
	COMMON /SPARM/ MFRAC,HMISS,IBR,ITYPE,NSTOR(8),IPNT(8)	00430
	COMMON /BPARM/ CNP(4,2),IB,IR,XNP(9,4,2),OBJEC(2,5)	00440
	COMMON /IPARM/ DEL1A(4,2),JBETA(2,8,128),XWETA(2,8,128),IBIT(8)	00450

FIGURE B-1 (cont'd)

COMMON /INTERP/ BETA(2,8),IBETA(2,8),NDEX(8),IH1(8)	00460
COMMON /SINTVL/ IRL0(500),IRH1(500)	00470
DIMENSION ISTR(4)	00480
DATA(NWORK=25000)	00490
DATA(IBIT=50,43,36,29,22,15,8,1)	00500
DATA(NSTRAT=8(0)),(NMISS=8(0)),(XNP=72(0.))	00510
C	00520
DO 100 I=1,NWORK	00530
IARRAY(I)=0	00540
100 CONTINUE	00550
DO 110 K=1,2	00560
DO 110 J=1,4	00570
DO 110 I=1,11	00580
XGRID(I,J,K)=IGRID(I,J,K)	00590
110 CONTINUE	00600
C	00610
C	00620
C	00630
ASSIGN COUNTERS AND POINTERS	00640
DO 140 K=1,2	00650
L=0	00660
DO 135 J=1,4	00670
DO 115 I=1,8	00680
IF(I MISS(I,J,K) .EQ. 0) GO TO 120	00690
L=L+1	00700
INPNT(L,K)=1	00710
IMPNT(L,K)=I MISS(I,J,K)	00720
ITPNT(L,K)=J	00730
115 CONTINUE	00740
120 NMISS(J,K)=I-1	00750
DO 125 I=2,11	00760
IF(IGRID(I,J,K) .EQ. 0) GO TO 130	00770
125 CONTINUE	00780
130 NGRID(J,K)=I-1	00790
DELTA(J,K)=XGRID(I-1,J,K)/127.	00800
135 CONTINUE	00810
NMISST(K)=L	00820
140 CONTINUE	00830
C	00840
C	00850
C	00860
COMPUTE INTERPOLATION PARAMETERS	00870
DO 160 I=1,128	00880
L=I-1	00890
DO 150 K=1,2	00900
DO 150 J=1,4	00910
CNP(J,K)=L*DELTA(J,K)	00920
150 CONTINUE	00930
CALL BETAS	00940
DO 160 K=1,2	00950
DO 160 J=1,8	00960
JBETA(K,J,1)=IBETA(K,J)	00970
XBETA(K,J,1)=BETA(K,J)	00980
160 CONTINUE	00990
DO 165 K=1,2	01000
DO 165 J=1,4	01010
IF(DELTA(J,K) .EQ. 0.) DELTA(J,K)=1.	01020
165 CONTINUE	01030
CALL OPENMS(2,IRA,100,0)	01040
CALL OPENMS(3,JRA,100,0)	
C	

FIGURE B-1 (cont'd)

C	GENERATE PURE STRATEGIES FOR BLUE AND RED	01050
C		01060
	ILOC=1	01070
	REWIND 9	01080
	DO 400 K=1,2	01090
	IBR=K	01100
	IUP1=NTYPE(K)	01110
	IUP3=NSTRIC(K)	01120
	JCNT=0	01130
	KASTP=1	01140
	DO 360 II=1,IUP3	01150
	BUFFER IN (9,1) (LASTP,NALOC(8,4))	01160
	IF (UNIT(9)) 175,170,170	01170
170	CALL ERR(26)	01180
175	DO 180 J=KASTP, LASTP	01190
	IDINT(J,K)=LASTP	01200
180	CONTINUE	01210
	KASTP=LASTP+1	01220
	DO 300 J=1,IUP1	01230
	ITYPE=J	01240
	MMISS=NMISS(J,K)	01250
	MFRAC=MFRAC(J,K)	01260
	IHI2=MMISS	01270
	ICNT=0	01280
	DO 200 I=1,IHI2	01290
	IPNT(I)=0	01300
	IF (NALOC(I,J) .EQ. -1) GO TO 190	01310
	MMISS=MMISS-1	01320
	MFRAC=MFRAC-NALOC(I,J)	01330
	IF (MFRAC .LT. 0) CALL ERR(8)	01340
	NSTR(I)=NALOC(I,J)	01350
	GO TO 200	01360
190	ICNT=ICNT+1	01370
	IPNT(ICNT)=1	01380
200	CONTINUE	01390
	IF (MMISS .EQ. 0 .AND. MFRAC .GT. 0) CALL ERR(23)	01400
	CALL STRAT	01410
300	CONTINUE	01420
	IHI1=NSTRAT(1,K)	01430
	IHI2=NSTRAT(2,K)	01440
	IHI3=NSTRAT(3,K)	01450
	IHI4=NSTRAT(4,K)	01460
	IF (IHI1 .EQ. 0) IHI1=1	01470
	IF (IHI2 .EQ. 0) IHI2=1	01480
	IF (IHI3 .EQ. 0) IHI3=1	01490
	IF (IHI4 .EQ. 0) IHI4=1	01500
	DO 360 I=1,IHI1	01510
	DO 360 J=1,IHI2	01520
	DO 360 L=1,IHI3	01530
	DO 360 M=1,IHI4	01540
	JCNT=JCNT+1	01550
	LOCST(JCNT,K)=ILOC	01560
	ISINT(JCNT,K)=LASTP	01570
	ISTOR(1)=1	01580
	ISTOR(2)=J	01590
	ISTOR(3)=L	01600
	ISTOR(4)=M	01610
	DO 360 II=1,IUP1	01620
	IDEX=ISTOR(1)	01630

FIGURE B-1 (cont'd)

	IUP2=NMISS(11,K)	01640
	DO 360 N=1,IUP2	01650
	XARRAY(ILOC)=STRATS(N,INDEX,11)	01660
	ILOC=ILOC+1	01670
360	CONTINUE	01680
	NFULST(K)=JCNT	01690
	IF(JCNT.GT.500) CALL ERR(3)	01700
	IF(K.EQ.1.AND. ILOC.GT. NWORK-6400) CALL ERR(3)	01710
	IF(LASTP.LT. NSTAGE) CALL ERR(25)	01720
400	CONTINUE	01730
	WRITE(LUNO,410)	01740
410	FORMAT(1H1)	01750
	WRITE(LUNO,420) (IBLURD(K),NFULST(K),K=1,2)	01760
420	FORMAT(//11H NUMBER OF, A4,24H PURE STRATEGIES EQUALS,15)	01770
	IF(ILOC.GT. NWORK) CALL ERR(3)	01780
		01790
C	SET POINTERS FOR EACH BLUE STRATEGY TO INDICATE THE RED	01800
C	STRATEGIES WHICH CAN BE PLAYED AGAINST IT	01810
C		01820
C		01830
	IH11=NFULST(1)	01840
	IH12=NFULST(2)	01850
	ILOB=0	01860
	DO 428 I=1,IH11	01870
	IF(ISINT(1,I).EQ. ILOB) GO TO 426	01880
	IRL=0	01890
	IBL=ILOB+1	01900
	IBH=ISINT(1,I)	01910
	DO 424 K=IBL,IBH	01920
	DO 422 J=1,IH12	01930
	IF(ISINT(J,2).NE. IDINT(K,2)) GO TO 422	01940
	IF(IRL.EQ. 0) IRL=J	01950
	IRH=J	01960
422	CONTINUE	01970
424	CONTINUE	01980
	ILOB=IBH	01990
426	IRLO(I)=IRL	02000
	IRHI(I)=IRH	02010
428	CONTINUE	02020
C		02030
C	PRINT STRATEGIES UNLESS SUPPRESSED	02040
C		02050
	IF(IPRINT(2).NE. 0) GO TO 500	02060
	DO 460 K=1,2	02070
	IH13=NMISS(K)	02080
	IH11=NFULST(K)	02090
	DO 460 I=1,IH11	02100
	ILO2=LOCST(1,K)	02110
	IH12=ILO2+NMISS(K)-1	02120
	IF((I-I)/50*50.NE. 1-1) GO TO 438	02130
	WRITE(LUNO,430) IBLURD(K), (ITPNT(J,K),IMPNT(J,K),J=1,IH13)	02140
430	FORMAT(1H1//,17X,A5,15HPURE STRATEGIES//,6H STRAT,4X,4H LAST,	02150
	112X,18HPLANE TYPE/MISSION/,7H NUMBER,3X,5HSTAGE,5X,	02160
	14(10(11,1H/,11,2X)/20X))	02170
	WRITE(LUNO,435)	02180
435	FORMAT(1H1)	02190
438	WRITE(LUNO,440) 1,ISINT(1,K),(XARRAY(J),J=ILO2,IH12)	02200
440	FORMAT(1X,15,5X,13,4X,4(10F5,2/,18X))	02210
460	CONTINUE	02220
C		

FIGURE B-1 (cont'd)

C	COMPUTE TOTAL NUMBER OF STATES	02230
C		02240
500	NSTAT=1	02250
	ICNT=9	02260
	DO 510 K=1,2	02270
	DO 510 J=1,4	02280
	L=3-K	02290
	M=5-J	02300
	ICNT=ICNT-1	02310
	IDEM(ICNT)=NSTAT	02320
	NSTAT=NSTAT*NGRID(M,L)	02330
510	CONTINUE	02340
	NSTAT2=2*NSTAT	02350
	WRITE(LUNO,520) NSTAT	02360
520	FORMAT(1H1,/,25H NUMBER OF STATES EQUALS ,17)	02370
	IF(1LOC+5*NSTAT2 .GT. NWORK) CALL ERR(4)	02380
	NG1=NGRID(1,1)	02390
	NG2=NGRID(2,1)	02400
	NG3=NGRID(3,1)	02410
	NG4=NGRID(4,1)	02420
	NG5=NGRID(1,2)	02430
	NG6=NGRID(2,2)	02440
	NG7=NGRID(3,2)	02450
	NG8=NGRID(4,2)	02460
C		02470
C	PRINT STATES UNLESS SUPPRESSED	02480
C		02490
	IF(IPRINT(3) .NE. 0) GO TO 635	02500
	ICNT=0	02510
	DO 630 I1=1,NG1	02520
	DO 630 I2=1,NG2	02530
	DO 630 I3=1,NG3	02540
	DO 630 I4=1,NG4	02550
	DO 630 I5=1,NG5	02560
	DO 630 I6=1,NG6	02570
	DO 630 I7=1,NG7	02580
	DO 630 I8=1,NG8	02590
	ICNT=ICNT+1	02600
	IF((ICNT-1)/50*50 .EQ. ICNT-1) WRITE(LUNO,610)	02610
610	FORMAT(1H1,/,18X,27H LIST OF ALL POSSIBLE STATES,/,6H STATE,	02620
	115X,4H BLUE,27X,3H RED,/,7H NUMBER,7X,2(19H1 2 3 4,	02630
	111X)/)	02640
	WRITE(LUNO,620) ICNT,JGRID(11,1),JGRID(12,2),JGRID(13,3),	02650
	1JGRID(14,4),JGRID(15,5),JGRID(16,6),JGRID(17,7),JGRID(18,8)	02660
620	FORMAT(1X,15,4X,2(416,6X))	02670
630	CONTINUE	02680
635	CALL TIMER	02690
C		02700
C	TERMINATE EXECUTION IF ABORT OPTION IS SPECIFIED	02710
C		02720
	IF(IPRINT(4) .EQ. -1) CALL ERR(7)	02730
	JLOC=1LOC	02740
C		02750
C	COMPUTE FINAL PAYOFFS FOR EACH STATE AND STORE IN	02760
C	NEXT-STAGE-ARRAYS	02770
C		02780
	DO 645 I1=1,NG1	02790
	DO 645 I2=1,NG2	02800
	DO 645 I3=1,NG3	02810

FIGURE B-1 (cont'd)

	DO 645 I4=1,NG4	02820
	DO 645 I5=1,NG5	02830
	DO 645 I6=1,NG6	02840
	DO 645 I7=1,NG7	02850
	DO 645 I8=1,NG8	02860
	XARRAY(ILOC)=YGRID(11,1)*VALU(1,1)+YGRID(12,2)*VALU(2,1)+	02870
	YGRID(13,3)*VALU(3,1)+YGRID(14,4)*VALU(4,1)+	02880
	YGRID(15,5)*VALU(1,2)+YGRID(16,6)*VALU(2,2)+	02890
	YGRID(17,7)*VALU(3,2)+YGRID(18,8)*VALU(4,2)	02900
	XARRAY(ILOC)=XARRAY(ILOC)*(OWGHT(1)+OWGHT(2))	02910
	ILOC=ILOC+1	02920
645	CONTINUE	02930
	JLOC2=ILOC-1	02940
	LOCBVB=JLOC1	02950
	LOCEVB=JLOC2	02960
	DO 648 I=JLOC1,JLOC2	02970
	XARRAY(ILOC)=XARRAY(I)	02980
	ILOC=ILOC+1	02990
648	CONTINUE	03000
	LOCBVR=JLOC2+1	03010
	LOCEVR=ILOC-1	03020
	KOCBVB=LOCEVR+1	03030
	KOCEVB=LOCEVR+NSTAT	03040
	KOCBVR=KOCEVB+1	03050
	KOCEVR=KOCEVB+NSTAT	03060
	JOCBVB=KOCEVR+1	03070
	JOCEVB=KOCEVR+NSTAT	03080
	JOCBVR=JOCEVB+1	03090
	JOCEVR=JOCEVB+NSTAT	03100
	IOCBVB=JOCEVR+1	03110
	IOCEVB=JOCEVR+NSTAT	03120
	IOCBVR=IOCEVB+1	03130
	IOCEVR=IOCEVB+NSTAT	03140
	LOCBPR=IOCEVR+1	03150
	LOCEPR=IOCEVR+NSTAT	03160
	LOCBPR=LOCEPR+1	03170
	LOCEPR=LOCEPR+NSTAT	03180
	DO 650 I=1,NSTAT2	03190
	J=I-1	03200
	XARRAY(JOCBVR+J)=XARRAY(LOCBVB+J)	03210
650	CONTINUE	03220
C		03230
C	READ OR COMPUTE BATTLE ASSESSMENTS FOR EACH STATE AND	03240
C	PURE STRATEGY COMBINATION AND STORE ON SCRATCH DISK	03250
C		03260
	IHI1=NFULST(1)	03270
	IHI2=NFULST(2)	03280
	NINGAM=IHI1*IHI2	03290
	LOCBG=LOCEPR+1	03300
	LOCEG=LOCEPR+NINGAM	03310
	KOCBG=LOCEG+1	03320
	KOCEG=LOCEG+NINGAM	03330
	IF(KOCEG.GT.NWORK) CALL ERR(5)	03340
	CALL SECOND(T)	03350
	WRITE(LUN0,651) T	03360
651	FORMAT(/////1X,F9.3,25H CPU SECONDS USED IN INIT/)	03370
	IF(IPRINT(5).LT.2) GO TO 665	03380
C		03390
C	IF AVAILABLE READ BATTLE ASSESSMENTS FROM BATTLE-TAPE	03400
C		03410

FIGURE B-1 (cont'd)

	DO 660 I=I, NSTAT	03420
	BUFFER IN (I,1) (IARRAY(LOCBG), IARRAY(KOCEG))	03430
	IF (UNIT(I)) 655, 653, 653	03440
653	CALL ERR(24)	03450
655	BUFFER OUT (I,1) (IARRAY(LOCBG), IARRAY(KOCEG))	03460
	IF (UNIT(I)) 660, 658, 658	03470
658	CALL ERR(6)	03480
660	CONTINUE	03490
	RETURN	03500
C		03510
C	IF BATTLE-TAPE IS NOT AVAILABLE, COMPUTE ASSESSMENTS	03520
C	USING SUBROUTINE /BATTLE/	03530
C		03540
665	DO 900 I1=I, NG1	03550
	DO 900 I2=I, NG2	03560
	DO 900 I3=I, NG3	03570
	DO 900 I4=I, NG4	03580
	DO 900 I5=I, NG5	03590
	DO 900 I6=I, NG6	03600
	DO 900 I7=I, NG7	03610
	DO 900 I8=I, NG8	03620
	LOCWD=LOCBG-1	03630
	DO 800 I8=I, IH1	03640
	DO 800 IR=I, IH2	03650
	IWORD=0	03660
	JWORD=0	03670
	IF (IR .LT. IRLO(I8) .OR. IR .GT. IRHI(I8)) GO TO 780	03680
	CNP(1,1)=YGRID(I1,1)	03690
	CNP(2,1)=YGRID(I2,2)	03700
	CNP(3,1)=YGRID(I3,3)	03710
	CNP(4,1)=YGRID(I4,4)	03720
	CNP(1,2)=YGRID(I5,5)	03730
	CNP(2,2)=YGRID(I6,6)	03740
	CNP(3,2)=YGRID(I7,7)	03750
	CNP(4,2)=YGRID(I8,8)	03760
	IF (IPRINT(6) .EQ. 0) GO TO 680	03770
	WRITE(LUNO, 670) I8, IR	03780
670	FORMAT(/, 4H I8=, I3, 2X, 3HIR=, I3)	03790
	WRITE(LUNO, 675) CNP	03800
675	FORMAT(/, 4H CNP, 6F9.2)	03810
680	CALL BATTLE	03820
	LOCLEV=0	03830
	DO 700 K=1, 2	03840
	DO 700 J=1, 4	03850
	LEVEL=CNP(J,K)/DELTA(J,K)+.5	03860
	LOCLEV=LOCLEV+1	03870
	KEVEL(LOCLEV)=LEVEL	03880
	CALL SBYT(IBIT(LOCLEV), 7, JWORD, LEVEL)	03890
700	CONTINUE	03900
	BOBJ=0.	03910
	ROBJ=0.	03920
	DO 720 J=1, 3	03930
	BOBJ=BOBJ+OBJEC(I,J)*OWGHT(J)	03940
	ROBJ=ROBJ+OBJEC(2,J)*OWGHT(J)	03950
720	CONTINUE	03960
	IOBJ=BOBJ+SIGN(.5, BOBJ)	03970
	JOBJ=ROBJ+SIGN(.5, ROBJ)	03980
	IF (IPRINT(6) .EQ. 0) GO TO 780	03990
	WRITE(LUNO, 775) CNP, IOBJ, JOBJ, KEVEL	04000

FIGURE B-1 (cont'd)

775	FORMAT(4H CNP,8F9.2/6H IOBJ=,110,5X,5HJOB=,110,5X,7HLEVELS=,814)	04010
780	IF(IOBJ.GE. 0) GO TO 785	04020
	IOBJ=-IOBJ	04030
	CALL SBYT(60,1,IWORD,1)	04040
785	CALL SBYT(31,29,IWORD,IOBJ)	04050
	IF(JOBJ.GE. 0) GO TO 790	04060
	JOBJ=-JOB	04070
	CALL SBYT(30,1,IWORD,1)	04080
790	CALL SBYT(1,29,IWORD,JOBJ)	04090
	LOCWD=LOCWO+1	04100
	IARRAY(LOCWD)=IWORD	04110
	IARRAY(LOCWO+NINGAM)=JWORD	04120
800	CONTINUE	04130
	BUFFER OUT (1,1) (IARRAY(LOCBG),IARRAY(KOCEG))	04140
	IF(UNIT(1)) 875,850,850	04150
850	CALL ERR(6)	04160
875	IF(IPRINT(5).EQ. 0) GO TO 900	04170
C		04180
C	WRITE BATTLE ASSESSMENTS ON BATTLE-TAPE IF REQUESTED	04190
C		04200
	BUFFER OUT (10,1) (IARRAY(LOCBG),IARRAY(KOCEG))	04210
	IF(UNIT(10)) 900,880,880	04220
880	CALL ERR(24)	04230
900	CONTINUE	04240
	RETURN	04250
	END	04260
	FUNCTION ISTATE(IV)	00110
C		00120
C	/ISTATE/ COMPUTES THE INDEX OF THE STATE CORRESPONDING	00130
C	TO A SPECIFIED COMBINATION OF GRID POINTS.	00140
C		00150
	COMMON /INPUT/ IMISS(8,4,2),IGRID(11,4,2),LASTP,NALOC(8,4),	00160
	INFRAC(4,2),NSHL(2),NSTAGE,NDAPST,CASF(4,2),IPRINT(8),	00170
	ITITLE(6),VALU(4,2),PKBO(4,4,2),PKBDES(4,4,2),XGRID(11,4,2),	00180
	IPKAU(4,4,2),PKADES(4,4,2),PKBA(4,4,2),PKAA(4,4,2),	00190
	IPKESB(4,4,2),PKESAD(4,4,2),PKSH(4,2),PKNS(4,2),REIN(4,2,100),	00200
	OWGHT(100,2),XSORT(8,4,2),NDIV(2),OWGHT(5),NHSAM(2),NFSAM(2),	00210
	IPKRS(4,2),PKFS(4,2),ABAF(8,4,2),OIVFP(2),PKWAFS(4,2),	00220
	IPKAIFS(4,2),PKAARS(4,2),PKAEFS(4,2),PKAERS(4,2),PKBEFS(4,2),	00230
	IPKFAFS(4,2),PKRAFS(4,2),PKRARS(4,2),OPPREU(4,2),FEBA(2,28),	00240
	IREINF(4,2,100)	00250
	COMMON /WORKN/ NTYPE(2),NMISS(4,2),NMISST(2),NGRID(4,2),	00260
	IIBLUR(2),NSTRAT(4,2),NFULST(2),NSTAT,NINGAM,IMPNT(32,2),	00270
	IITPNT(32,2),IDEM(8),NSTRTC(2),IRA(100),JRA(100),LUNI,LUNO,	00280
	INWORK,NSTAT2,ISINT(500,2),IDINT(100,2),INPNT(32,2)	00290
	COMMON /WORKL/ LOCST(500,2),LOCBG,LOCEG,KUCBG,KOCEG,LOCBVR,	00300
	LOCBVB,LOCEVR,LOCEVB,LOCBPR,LOCBPR,LOCEPR,LOCEPB,	00310
	LOCBVB,KOCEVB,KOCEVR,KOCEVR,JOCBVB,JOCVEB,JOCBVR,JOCVEVR,	00320
	LOCBVB,IOCEVB,IOCBVR,IOCEVR	00330
	DIMENSION IV(1)	00340
	ISTATE=IV(8)+1	00350
	DO 100 I=1,7	00360
	ISTATE=ISTATE+IV(I)*IDEM(I)	00370
100	CONTINUE	00380
	RETURN	00390
	END	00400

FIGURE B-1 (cont'd)

```

SUBROUTINE PRNTIN
C
C /PRNTIN/ PRINTS THE INPUT PARAMETERS.
C
COMMON /INPUT/ IMISS(8,4,2), IGRID(11,4,2), LASTP, NALOC(8,4),
INFRAC(4,2), NSHL(2), NSTAGE, NDAPST, CASF(4,2), IPRINT(8),
IITITLE(6), VALU(4,2), PKBD(4,4,2), PKBDES(4,4,2), XGRID(11,4,2),
IPKAD(4,4,2), PKADES(4,4,2), PKBA(4,4,2), PKAA(4,4,2),
IPKESBD(4,4,2), PKESAD(4,4,2), PKSH(4,2), PKNS(4,2), KEIN(4,2,100),
IWGHT(100,2), XSORT(8,4,2), NDIV(2), OWGHT(5), NRSAM(2), NFSAM(2),
IPKRS(4,2), PKFS(4,2), ABAF(8,4,2), DIVFP(2), PKWAFS(4,2),
IPKAFS(4,2), PKAARS(4,2), PKAEFS(4,2), PKAERS(4,2), PKBEFS(4,2),
IPKFAFS(4,2), PKRAFS(4,2), PKRAERS(4,2), OFPRED(4,2), FEBA(2,28),
IREINF(4,2,100)
COMMON /WORKN/ NTYPE(2), NMISS(4,2), NMISST(2), NGRID(4,2),
IBLURD(2), NSTRAT(4,2), NFULST(2), NSTAT, NINGAM, IMPNT(32,2),
IITPNT(32,2), IDEM(8), NSTRTC(2), IRA(100), JRA(100), LUN1, LUNO,
INWORK, NSTAT2, ISINT(500,2), IDINT(100,2), INPNT(32,2)
COMMON /WORKL/ LDCST(500,2), LOCBG, LOCEG, KUCBG, KOCEG, LOCBVR,
LOCBVB, LOCEVR, LOCEVB, LOCBPR, LOCBPB, LOCEPR, LOCEPB,
IKOCBVB, KOCEVB, KOCEVR, KOCEPR, JOCBVB, JOCEVB, JOCBVR, JOCEVR,
IOCBVB, IOCEVB, IOCBVR, IOCEVR
DIMENSION IHEAD(4,25), IM(4,2), XF(4,2), PKS(4,4,2)
DATA(IHEAD(1, 1))=40H CAS ESCORT AGAINST BD )
DATA(IHEAD(1, 2))=40H BD AGAINST CAS ESCORT )
DATA(IHEAD(1, 3))=40H CAS AGAINST BD )
DATA(IHEAD(1, 4))=40H BD AGAINST CAS )
DATA(IHEAD(1, 5))=40H ABA ESCORT AGAINST ABD )
DATA(IHEAD(1, 6))=40H ABD AGAINST ABA ESCORT )
DATA(IHEAD(1, 7))=40H ABA AGAINST ABD )
DATA(IHEAD(1, 8))=40H ABD AGAINST ABA )
DATA(IHEAD(1, 9))=40H ABA AGAINST NON-SHELTERED AIRCRAFT )
DATA(IHEAD(1,10))=40H ABA AGAINST SHELTERED AIRCRAFT )
DATA(IHEAD(1,11))=40H FORWARD SAM SUPPRESSOR AGAINST SAM )
DATA(IHEAD(1,12))=40H SAM AGAINST FORWARD SAM SUPPRESSOR )
DATA(IHEAD(1,13))=40H REAR SAM SUPPRESSOR AGAINST SAM )
DATA(IHEAD(1,14))=40H SAM AGAINST REAR SAM SUPPRESSOR )
DATA(IHEAD(1,15))=40H SAM AGAINST CAS )
DATA(IHEAD(1,16))=40H SAM AGAINST CAS ESCORT )
DATA(IHEAD(1,17))=40H SAM AGAINST ABA )
DATA(IHEAD(1,18))=40H SAM AGAINST ABA ESCORT )
WRITE(LUNO,100) (ITITLE(1),I=1,6)
100 FORMAT(1H1,1X,6A10/)
WRITE(LUNO,102) NSTAGE
102 FORMAT(1X,18HNUMBER OF STAGES =,I3)
WRITE(LUNO,104) NDAPST
104 FORMAT(1X,28HNUMBER OF CYCLES PER STAGE =,I3)
WRITE(LUNO,110) (IBLURD(K),NTYPE(K),K=1,2)
110 FORMAT(1X,10HNUMBER OF ,A4,14H PLANE TYPES =,I2)
WRITE(LUNO,120) (IBLURD(K),NDIV(K),K=1,2)
120 FORMAT(1X,10HNUMBER OF ,A4,12H DIVISIONS =,I6)
WRITE(LUNO,125) (IBLURD(K),DIVFP(K),K=1,2)
125 FORMAT(1X,14HFIREFPOWER PER ,A4,11H DIVISION =,F10.4)
WRITE(LUNO,130) (IBLURD(K),NSHL(K),K=1,2)
130 FORMAT(1X,10HNUMBER OF ,A4,11H SHELTERS =,I6)
WRITE(LUNO,140) (IBLURD(K),NFSAM(K),K=1,2)
140 FORMAT(1X,10HNUMBER OF ,A4,15H FORWARD SAMS =,I6)
WRITE(LUNO,150) (IBLURD(K),NRSAM(K),K=1,2)
150 FORMAT(1X,10HNUMBER OF ,A4,12H REAR SAMS =,I6)

```

FIGURE B-1 (cont'd)

	WRITE(LUNO,160) (OWGHT(1),1=1,3)	00700
160	FORMAT(1X,29HOBJECTIVE FUNCTION WEIGHTS = ,9HCAS ORD -,F6.2,	00710
	13X,9HTOTL FP -,F6.2,3X,6HFEBA -,F6.2)	00720
	WRITE(LUNO,200)	00730
200	FORMAT(/// ,29X,21HMISSIONS ASSIGNED AND/,28X,	00740
	123HASSOCIATED SORTIE RATES//)	00750
	WRITE(LUNO,210)	00760
210	FORMAT(15X,15HBLUE PLANE TYPE,21X,14HRED PLANE TYPE/	00770
	12(10X,25H1 2 3 4//)	00780
	DO 300 I=1,8	00790
	DO 240 K=1,2	00800
	DO 240 J=1,4	00810
	IF(IMISS(1,J,K) .NE. 0) GO TO 250	00820
240	CONTINUE	00830
	GO TO 310	00840
250	DO 260 K=1,2	00850
	DO 260 J=1,4	00860
	IM(J,K)=0	00870
	XF(J,K)=0.	00880
	IF(IMISS(1,J,K) .NE. 0) IM(J,K)=IMISS(1,J,K)	00890
	IF(XSORT(1,J,K) .NE. 0.) XF(J,K)=XSORT(1,J,K)	00900
260	CONTINUE	00910
	WRITE(LUNO,280) ((IM(J,K),XF(J,K),J=1,4),K=1,2)	00920
280	FORMAT(4X,2(3X,4(11,1H-,F5.2,1X)))	00930
300	CONTINUE	00940
310	WRITE(LUNO,312)	00950
312	FORMAT(/// ,26X,28HMINIMUM ALLOCATION FRACTIONS//)	00960
	WRITE(LUNO,210)	00970
	DO 315 K=1,2	00980
	DO 315 J=1,4	00990
	XF(J,K)=0.	01000
	IF(NFRAC(J,K) .EQ. 0) GO TO 315	01010
	XF(J,K)=1./NFRAC(J,K)	01020
315	CONTINUE	01030
	WRITE(LUNO,318) ((XF(J,K),J=1,4),K=1,2)	01040
318	FORMAT(2X,2(3X,4(F7.2,1X)))	01050
	WRITE(LUNO,320)	01060
320	FORMAT(/// ,35X,11HGRID POINTS//)	01070
	WRITE(LUNO,210)	01080
	DO 370 I=1,11	01090
	DO 330 K=1,2	01100
	DO 330 J=1,4	01110
	IF(IGRID(1,J,K) .NE. 0 .OR. 1 .EQ. 1) GO TO 340	01120
330	CONTINUE	01130
	GO TO 400	01140
340	WRITE(LUNO,360) ((IGRID(1,J,K),J=1,4),K=1,2)	01150
360	FORMAT(3X,2(3X,4(16,2X)))	01160
370	CONTINUE	01170
400	WRITE(LUNO,410)	01180
410	FORMAT(1H1//,28X,24HCAS FIREPOWER PER SORTIE//)	01190
	WRITE(LUNO,210)	01200
	WRITE(LUNO,420) ((CASE(J,K),J=1,4),K=1,2)	01210
420	FORMAT(3X,2(3X,4(F7.4,1X)))	01220
	WRITE(LUNO,422)	01230
422	FORMAT(/// ,26X,28HDIVISION FIREPOWER REDUCTION,/	01240
	134X,14HPER CAS SORTIE//)	01250
	WRITE(LUNO,210)	01260
	WRITE(LUNO,420) ((DFPRED(J,K),J=1,4),K=1,2)	01270
	WRITE(LUNO,423)	01280

FIGURE B-1 (cont'd)

423	FORMAT(///,30X,20HRESIDUAL VALUE OF AN/ 123X,33HUNDAMAGED PLANE AT END OF THE WAR//)	01290
	WRITE(LUNO,210)	01300
	WRITE(LUNO,420) ((VALU(J,K),J=1,4),K=1,2)	01310
	WRITE(LUNO,424)	01320
424	FORMAT(///,27X,26HFRACTION VULNERABLE TO ABA/,35X, 110HBY MISSION//)	01330
	WRITE(LUNO,210)	01340
	DO 430 I=1,8	01350
	DO 425 K=1,2	01360
	DO 425 J=1,4	01370
	IF(1MISS(I,J,K) .NE. 0) GO TO 426	01380
425	CONTINUE	01390
	GO TO 431	01400
426	DO 427 K=1,2	01410
	DO 427 J=1,4	01420
	1M(J,K)=0	01430
	XF(J,K)=0.	01440
	IF(1MISS(I,J,K) .NE. 0) 1M(J,K)=1MISS(I,J,K)	01450
	IF(ABAF(I,J,K) .NE. 0.) XF(J,K)=ABAF(I,J,K)	01460
427	CONTINUE	01470
	WRITE(LUNO,428) ((1M(J,K),XF(J,K),J=1,4),K=1,2)	01480
428	FORMAT(4X,2(3X,4(11,1H-,F5.3,1X)))	01490
430	CONTINUE	01500
431	IF(FEBA(1,1) .EQ. -1.) GO TO 439	01510
	WRITE(LUNO,433)	01520
433	FORMAT(1H1///,33X,13HFEBA FUNCTION//)	01530
	DO 434 I=2,28	01540
	IF(FEBA(1,1) .EQ. 0.) GO TO 435	01550
434	CONTINUE	01560
435	I=I-1	01570
	DO 438 K=1,1,7	01580
	L=K*6	01590
	WRITE(LUNO,436) (FEBA(1,J),J=K,L)	01600
436	FORMAT(/1X,7HF RATIO,6X,7F9.3)	01610
	WRITE(LUNO,437) (FEBA(2,J),J=K,L)	01620
437	FORMAT(1X,8HMOVEMENT,5X,7F9.3)	01630
438	CONTINUE	01640
439	DO 470 I=1,NSTAGE	01650
	IF((I-1)/50*50 .NE. 1-1) GO TO 445	01660
	WRITE(LUNO,440)	01670
440	FORMAT(1H1//12X,9HOBJECTIVE,2(24X,14HREINFORCEMENTS,17X)/13X, 17HWEIGHTS,29X,6HNUMBER,48X,8HFRACTION/18X, 12(13X,15HBLUE PLANE TYPE,12X,14HRED PLANE TYPE,1X)/1X,5HSTAGE, 14X,4HBLUE,5X,3HRED,2(7X,19H1 2 3 4,1X),1X, 12(7X,19H1 2 3 4,1X)/)	01680
	DO 450 K=1,2	01690
	DO 450 J=1,4	01700
	1M(J,K)=REIN(J,K,1)	01710
	XF(J,K)=REINF(J,K,1)-1.	01720
450	CONTINUE	01730
	WRITE(LUNO,460) 1.(WGHT(1,K),K=1,2),((1M(J,K),J=1,4),K=1,2), 1((XF(J,K),J=1,4),K=1,2)	01740
460	FORMAT(3X,12,1X,2F8.2,2(3X,4I6),1X,2(3X,4F6.2))	01750
470	CONTINUE	01760
	WRITE(LUNO,500)	01770
500	FORMAT(1H1//31X,18HKILL PROBABILITIES/)	01780
	CALL PKILLS(1HEAD(1,1),PKBDES,0.,0.)	01790
	CALL PKILLS(1HEAD(1,2),PKESBU,0.,0.)	01800
		01810
		01820
		01830
		01840
		01850
		01860
		01870

FIGURE B-1 (cont'd)

	CALL PKILLS(IHEAD(1,3),PKBD,0.,0.)	01880
	CALL PKILLS(IHEAD(1,4),PKBA,0.,0.)	01890
	WRITE(LUNO,500)	01900
	CALL PKILLS(IHEAD(1,5),PKADES,0.,0.)	01910
	CALL PKILLS(IHEAD(1,6),PKESAD,0.,0.)	01920
	CALL PKILLS(IHEAD(1,7),PKAD,0.,0.)	01930
	CALL PKILLS(IHEAD(1,8),PKAA,0.,0.)	01940
	WRITE(LUNO,500)	01950
	DO 600 I=1,4	01960
	DO 600 J=1,4	01970
	DO 600 K=1,2	01980
	PKS(I,J,K)=PKNS(J,K)	01990
600	CONTINUE	02000
	CALL PKILLS(IHEAD(1,9),PKS,0.,0.)	02010
	DO 700 I=1,4	02020
	DO 700 J=1,4	02030
	DO 700 K=1,2	02040
	PKS(I,J,K)=PKSH(J,K)	02050
700	CONTINUE	02060
	CALL PKILLS(IHEAD(1,10),PKS,0.,0.)	02070
	WRITE(LUNO,500)	02080
	CALL SAMS(IHEAD(1,11),1.,PKFS,-2.)	02090
	CALL SAMS(IHEAD(1,12),1.,PKFAFS,-1.)	02100
	CALL SAMS(IHEAD(1,13),1.,-2.,PKRS)	02110
	CALL SAMS(IHEAD(1,14),1.,PKNAFS,PKRARS)	02120
	WRITE(LUNO,500)	02130
	CALL SAMS(IHEAD(1,15),1.,PKBAFS,-1.)	02140
	CALL SAMS(IHEAD(1,16),1.,PKBEFS,-1.)	02150
	CALL SAMS(IHEAD(1,17),1.,PKAAFS,PKAARS)	02160
	CALL SAMS(IHEAD(1,18),1.,PKAEFS,PKAERS)	02170
	END	02180
	SUBROUTINE PKILLS (LABL,PK,PKF,PKR)	02190
C		02200
C	/PKILLS/ AND /SAMS/ ARE PRINT SUBROUTINES USED IN	02210
C	CONJUNCTION WITH /PRNTIN/.	02220
C		02230
	COMMON /WORKN/ NTYPE(2),NMISS(4,2),NMISST(2),NGRID(4,2),	02240
	IIBLURO(2),NSTRAT(4,2),NFULST(2),NSTAT,NINGAM,IMPNT(32,2),	02250
	IITPNT(32,2),IDEM(8),NSTRTC(2),IRA(100),JRA(100),LUNI,LUNO,	02260
	INWORK,NSTAT2,ISINT(500,2),IDINT(100,2),INPNT(32,2)	02270
	DIMENSION LABL(1),PK(4,4,2),PKF(4,2),PKR(4,2)	02280
	WRITE(LUNO,100) (LABL(I),I=1,4)	02290
100	FORMAT(3(/,20X,4A10,///,16X,14HBLUE KILLS RED,20X,	02300
	114HRED KILLS BLUE,/,19X,8HRED TYPE,26X,8HRED TYPE/	02310
	12(12X,22H1 2 3 4))	02320
	WRITE(LUNO,200) (PK(1,I,2),I=1,4),(PK(I,1,1),I=1,4)	02330
200	FORMAT(7X,1H1,4(2X,F5.3),6X,4(2X,F5.3))	02340
	WRITE(LUNO,300) (PK(2,I,2),I=1,4),(PK(I,2,1),I=1,4)	02350
300	FORMAT(7X,1H2,4(2X,F5.3),6X,4(2X,F5.3))	02360
	WRITE(LUNO,400) (PK(3,I,2),I=1,4),(PK(I,3,1),I=1,4)	02370
400	FORMAT(7X,1H3,4(2X,F5.3),6X,4(2X,F5.3))	02380
	WRITE(LUNO,500) (PK(4,I,2),I=1,4),(PK(I,4,1),I=1,4)	02390
500	FORMAT(7X,1H4,4(2X,F5.3),6X,4(2X,F5.3))	02400
	RETURN	02410

FIGURE B-1 (cont'd)

	ENTRY SAMS	02420
	WRITE(LUNO,600) (LABL(1),I=1,4)	02430
600	FORMAT(3(//),20X,4A10,///,16X,14HBLUE KILLS RED,20X, 114HRED KILLS BLUE/)	02440
	IF(PKF(1,1) .EQ. -2. .OR. PKR(1,1) .EQ. -2.) GO TO 650	02450
	WRITE(LUNO,610)	02460
610	FORMAT(19X,8HRED TYPE,25X,9HBLUE TYPE)	02470
	GO TO 670	02480
650	WRITE(LUNO,660)	02490
660	FORMAT(18X,9HBLUE TYPE,26X,8HRED TYPE)	02500
670	WRITE(LUNO,680)	02510
680	FORMAT(2(12X,22HI 2 3 4))	02520
	IF(PKF(1,1) .LT. 0.) GO TO 750	02530
	WRITE(LUNO,700) (PKF(J,2),J=1,4), (PKF(J,1),J=1,4)	02540
700	FORMAT(1X,7HFORWARD,4(2X,F5.3),6X,4(2X,F5.3))	02550
	IF(PKR(1,1) .LT. 0.) RETURN	02560
750	WRITE(LUNO,800) (PKR(J,2),J=1,4), (PKR(J,1),J=1,4)	02570
800	FORMAT(2X,4HREAR,2X,4(2X,F5.3),6X,4(2X,F5.3))	02580
	RETURN	02590
	END	02600
		02610

	SUBROUTINE READIN	00110
C		00120
C	/READIN/ READS THE INPUT PARAMETER CARDS.	00130
C		00140
	COMMON /INPUT/ IMISS(8,4,2), IGRID(11,4,2), LASTP, NALOC(8,4),	00150
	INFRAC(4,2), NSHL(2), NSTAGE, NDAPST, CASF(4,2), IPRINT(8),	00160
	11TITLE(6), VALU(4,2), PKBD(4,4,2), PKBDES(4,4,2), XGRID(11,4,2),	00170
	IPKAD(4,4,2), PKADES(4,4,2), PKBA(4,4,2), PKAA(4,4,2),	00180
	IPKESBD(4,4,2), PKESAD(4,4,2), PKSH(4,2), PKNS(4,2), REIN(4,2,100),	00190
	1WGHT(100,2), XSORT(8,4,2), NDIV(2), OWGHT(5), NRSAM(2), NFSAM(2),	00200
	IPKRS(4,2), PKFS(4,2), ABAF(8,4,2), DIVFP(2), PKBAFS(4,2),	00210
	IPKAFS(4,2), PKAARS(4,2), PKAEFS(4,2), PKAERS(4,2), PKBEFS(4,2),	00220
	IPKFAFS(4,2), PKRAFS(4,2), PKRAKS(4,2), OFPRED(4,2), FEA(2,28),	00230
	IREINF(4,2,100)	00240
	COMMON /WORKN/ NTYPE(2), NMISS(4,2), NMISST(2), NGRID(4,2),	00250
	11BLURD(2), NSTRAT(4,2), NFULST(2), NSTAT, NINGAM, IMPNT(32,2),	00260
	11TPNT(32,2), IDEN(8), NSTRTC(2), IRA(100), JRA(100), LUN1, LUNO,	00270
	INWORK, NSTAT2, ISINT(500,2), IDINT(100,2), INPNT(32,2)	00280
	COMMON /WORKL/ LOCST(500,2), LOCBG, LOCEG, KOCBG, KOCEG, LOCBVR,	00290
	1LOCBVB, LOCEVR, LOCEVB, LOCBPR, LOCBPB, LOCEPR, LOCEPB,	00300
	1KOCBVB, KOCEVB, KOCBVR, KOCEVR, JOCBVB, JOCEVB, JOCBVR, JOCEVR,	00310
	1IOCBVB, IOCEVB, IOCBVR, IOCEVR	00320
	COMMON /WORK/ IARRAY(25000)	00330
	DIMENSION IDUMMY(8), KEY(35), NALOC(33,100,2), MALOC(33)	00340
	EQUIVALENCE (IARRAY, NALOC), (MALOC, LASTP)	00350
	DATA (NKEYS=30)	00360
	DATA (1BLURD=4HBLUE, 3HRED)	00370
	DATA (LUN1=5), (LUNO=6)	00380
	DATA (KEY=3HRED, 4HMISS, 4HGRID, 4HPKBD, 4HPKAD, 4HPKBA,	00390
	14HPKAA, 4HCASF, 4HVALU, 4HSTAG, 4HPKBE, 4HPKAE, 4HNSHL, 4HPKSH,	00400
	14HPKNS, 4HSTRT, 4HWGHT, 4HREIN, 4HCWGH, 4HNDIV, 4HDIVF, 4HDFRC,	00410
	14HNSAM, 4HPKFS, 4HPKRS, 4HFEB, 4HABAF, 4HPKFA, 4HPKRA, 3HEND, 5(1H))	00420
	DATA (REIN=800(0.)), (IREINF=800(1.)), (WGHT=200(1.))	00430
	DATA (PKBD=32(0.)), (PKBDES=32(0.)), (PKAD=32(0.)), (PKADES=32(0.))	00440

FIGURE B-1 (cont'd)

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DATA(PKBA=32(0.)),(PKAA=32(0.)),(PKESBD=32(0.)),(PKESAD=32(0.)) 00450
DATA(PKSH=8(0.)),(PKNS=8(0.)) 00460
DATA(CASF=8(0.)),(VALU=8(0.)),(NSHL=2(0.)),(NFRAC=8(0.)) 00470
DATA(NTYPE=2(0.)),(NSTRTC=2(0.)),(IGRID=88(0.)),(IMISS=64(0.)) 00480
DATA(XSORT=64(0.)),(OWGHT=1.4(0.)),(NDIV=2(0.)),(NRSAM=2(0.)) 00490
DATA(NFSAM=2(0.)),(PKRS=8(0.)),(PKFS=8(0.)),(ABAF=64(1.)) 00500
DATA(DIVFP=2(0.)),(PKBAFS=8(0.)),(PKAAPS=8(0.)),(PKAARS=8(0.)) 00510
DATA(PKAAPS=8(0.)),(PKAERS=8(0.)),(PKBEFS=8(0.)),(DFPRED=8(0.)) 00520
DATA(FEBA=-1.55(0.)),(PKFAFS=8(0.)),(PKRAFS=8(0.)),(PKRARS=8(0.)) 00530
DATA(IPRINT(1)=0) 00540
WRITE(LUNO,70) 00550
70 FORMAT(IH1) 00560
C 00570
C READ DATA CARD 00580
C 00590
100 READ(LUN1,I10) 1KEY,JBR,JTP,(IDUMMY(I),I=1,8) 00600
110 FORMAT(A4,2A1,7A10,A4) 00610
IF(IPRINT(1) .EQ. 0) WRITE(LUNO,120) 1KEY,JBR,JTP, 00620
1(IDUMMY(I),I=1,8) 00630
120 FORMAT(IX,A4,2A1,7A10,A4) 00640
DO 150 I=1,NKEYS 00650
IF(1KEY .EQ. KEY(I)) GO TO 200 00660
150 CONTINUE 00670
CALL ERR(2) 00680
GO TO 100 00690
200 IBR=1 00700
IF(JBR .EQ. 1HR) IBR=2 00710
DECODE(I,210,JTP) ITP 00720
210 FORMAT(I1) 00730
GO TO (300,320,340,360,380,400,420,440,460,480,500,510, 00740
1520,540,560,580,600,620,630,640,650,660,670,680,690,700, 00750
1710,720,730,800) I 00760
C 00770
C RUN CARD 00780
C 00790
300 DECODE(74,301,IDUMMY) (IPRINT(I),I=1,8),(ITITLE(I),I=1,6) 00800
301 FORMAT(4X,8I1,2X,6A10) 00810
GO TO 100 00820
C 00830
C MISS CARD 00840
C 00850
320 DECODE(74,321,IDUMMY) NFRAC(ITP,IBR),(IMISS(I,ITP,IBR), 00860
1I=1,8),(XSORT(I,ITP,IBR),I=1,8) 00870
321 FORMAT(4X,I2,1X,8(1X,I2),3X,8F5.2) 00880
GO TO 100 00890
C 00900
C GRID CARD 00910
C 00920
340 DECODE(59,341,IDUMMY) (IGRID(I,ITP,IBR),I=1,11) 00930
341 FORMAT(4X,11I5) 00940
IF(IGRID(1,ITP,IBR) .NE. 0) CALL ERR(9) 00950
IF(NTYPE(IBR) .LT. ITP) NTYPE(IBR)=ITP 00960
GO TO 100 00970
C 00980
C PKBD CARD 00990
C 01000
360 DECODE(49,361,IDUMMY) (PKBD(I,ITP,IBR),I=1,4), 01010
1(PKBDDES(I,ITP,IBR),I=1,4) 01020
361 FORMAT(4X,4F5.3,5X,4F5.3) 01030

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FIGURE B-1 (cont'd)

GO TO 100	01040
C	01050
C PKAD CARD	01060
C	01070
380 DECODE(49,361,1DUMMY) (PKAD(I,1TP,1BR),I=1,4),	01080
1(PKADES(1,1TP,1BR),I=1,4)	01090
GO TO 100	01100
C	01110
C PKBA CARD	01120
C	01130
400 DECODE(34,401,1DUMMY) (PKBA(1,1TP,1BR),I=1,4),PKBAFS(1TP,1BR)	01140
401 FORMAT(4X,4F5.3,5X,F5.3)	01150
GO TO 100	01160
C	01170
C PKAA CARD	01180
C	01190
420 DECODE(39,421,1DUMMY) (PKAA(1,1TP,1BR),I=1,4),PKAAFS(1TP,1BR),	01200
1PKAARS(1TP,1BR)	01210
421 FORMAT(4X,4F5.3,5X,4F5.3)	01220
GO TO 100	01230
C	01240
C CASF CARD	01250
C	01260
440 DECODE(24,441,1DUMMY) (CASF(1,1BR),I=1,4)	01270
441 FORMAT(4X,4F5.4)	01280
GO TO 100	01290
C	01300
C VALU CARD	01310
C	01320
460 DECODE(24,461,1DUMMY) (VALU(1,1BR),I=1,4)	01330
461 FORMAT(4X,4F5.0)	01340
GO TO 100	01350
C	01360
C STAG CARD	01370
C	01380
480 DECODE(10,481,1DUMMY) NSTAGE,NDAPST	01390
481 FORMAT(2X,2(2X,12))	01400
GO TO 100	01410
C	01420
C PKBE CARD	01430
C	01440
500 DECODE(34,401,1DUMMY) (PKESBD(1,1TP,1BR),I=1,4),PKBEFS(1TP,1BR)	01450
GO TO 100	01460
C	01470
C PKAE CARD	01480
C	01490
510 DECODE(39,421,1DUMMY) (PKESAO(1,1TP,1BR),I=1,4),PKAEFS(1TP,1BR),	01500
1PKAERS(1TP,1BR)	01510
GO TO 100	01520
C	01530
C NSHL CARD	01540
C	01550
520 DECODE(9,521,1DUMMY) NSHL(1BR)	01560
521 FORMAT(4X,15)	01570
GO TO 100	01580
C	01590
C PKSH CARD	01600
C	01610
540 DECODE(24,541,1DUMMY) (PKSH(1,1BR),I=1,4)	01620
541 FORMAT(4X,4F5.3)	01630

FIGURE B-1 (cont'd)

	GO TO 100	01640
C		01650
C	PKNS CARD	01660
C		01670
560	DECODE(24,541,IDUMMY) (PKNS(I,IBR),I=1,4)	01680
	GO TO 100	01690
C		01700
C	STRT CARD	01710
C		01720
580	DECODE(74,581,IDUMMY) (MALOC(I),I=1,33)	01730
581	FORMAT(I2,4(2X,8A2))	01740
	NSTRTC(IBR)=NSTRTC(IBR)+1	01750
	DO 583 I=2,33	01760
	IF(MALOC(I).EQ.2H*.OR.MALOC(I).EQ.2H**) MALOC(I)=2H-1	01770
	DECODE(2,582,MALOC(I)) IHOLD	01780
582	FORMAT(I2)	01790
	MALOC(I)=IHOLD	01800
583	CONTINUE	01810
	J=NSTRTC(IBR)	01820
	DO 584 I=1,33	01830
	NALOC(I,J,IBR)=MALOC(I)	01840
584	CONTINUE	01850
	GO TO 100	01860
C		01870
C	WGHT CARD	01880
C		01890
600	DECODE(9,601,IDUMMY) J,WGHT(J,IBR)	01900
601	FORMAT(I2,2X,F5.0)	01910
	GO TO 100	01920
C		01930
C	REIN CARD	01940
C		01950
620	DECODE(49,621,IDUMMY) J,(REIN(I,IBR,J),I=1,4),	01960
	1(REINF(I,IBR,J),I=1,4)	01970
621	FORMAT(I2,2X,4F5.0,5X,4F5.0)	01980
	DO 625 I=1,4	01990
	REINF(I,IBR,J)=REINF(I,IBR,J)+1.	02000
625	CONTINUE	02010
	GO TO 100	02020
C		02030
C	OWGHT CARD	02040
C		02050
630	DECODE(29,631,IDUMMY) (OWGHT(I),I=1,5)	02060
631	FORMAT(4X,5F5.0)	02070
	GO TO 100	02080
C		02090
C	NDIV CARD	02100
C		02110
640	DECODE(9,521,IDUMMY) NDIV(IBR)	02120
	GO TO 100	02130
C		02140
C	DIVF CARD	02150
C		02160
650	DECODE(9,651,IDUMMY) DIVFP(IBR)	02170
651	FORMAT(4X,F5.0)	02180
	GO TO 100	02190
C		02200
C	DFRC CARD	02210
C		02220

FIGURE B-1 (cont'd)

660	DECODE(24,44I,IOUMMY) (DFPRED(I,IBR),I=1,4)	02230
	GD TO 100	02240
C		02250
C	NSAM CARD	02260
C		02270
670	DECODE(14,67I,IOUMMY) NFSAM(IBR),NRSAM(IBR)	02280
671	FORMAT(4X,2IS)	02290
	GO TO 100	02300
C		02310
C	PKFS CARD	02320
C		02330
680	DECODE(24,54I,IOUMMY) (PKFS(I,IBR),I=1,4)	02340
	GD TO 100	02350
C		02360
C	PKRS CARD	02370
C		02380
690	DECODE(24,54I,IOUMMY) (PKRS(I,IBR),I=1,4)	02390
	GD TO 100	02400
C		02410
C	FEBAM CARD	02420
C		02430
700	ILO=(ITP-1)*7+1	02440
	IHI=ILO+6	02450
	DECODE(74,70I,IOUMMY) ((FEBA(I,J),I=1,2),J=ILO,IHI)	02460
701	FORMAT(4X,14F5.0)	02470
	GO TO 100	02480
C		02490
C	ABAF CARD	02500
C		02510
710	DECODE(44,71I,IOUMMY) (ABAF(I,ITP,IBR),I=1,8)	02520
711	FORMAT(4X,8F5.0)	02530
	GO TO 100	02540
C		02550
C	PKFA CARD	02560
C		02570
720	DECODE(9,72I,IOUMMY) PKFAFS(ITP,IBR)	02580
721	FORMAT(4X,F5.3)	02590
	GO TO 100	02600
C		02610
C	PKRA CARD	02620
C		02630
730	DECODE(14,73I,IOUMMY) PKRAFS(ITP,IBR),PKRARS(ITP,IBR)	02640
731	FORMAT(4X,2F5.3)	02650
	GO TO 100	02660
C		02670
C	ENO CARD	02680
C		02690
800	DO 810 K=1,2	02700
	J=NSTRC(K)	02710
	DO 810 I=1,J	02720
	BUFFER OUT (9,1) (NALDCS(1,I,K),NALOCS(33,I,K))	02730
	IF(UNIT(9)) 810,807,807	02740
807	CALL ERR(21)	02750
810	CONTINUE	02760
	RETURN	02770
	ENO	02780

FIGURE B-1 (cont'd)

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SUBROUTINE STRAT
C
C   /STRAT/ GENERATES THE PURE STRATEGIES FOR A PARTICULAR PLANE
C   TYPE RESULTING FROM A SPECIFIED ALLOCATION OF A MINIMUM
C   ALLOCATION FRACTION TO MISSIONS.
C
COMMON /INPUT/ IMISS(8,4,2), IGR10(11,4,2), LASTP, NALOC(8,4),
INFRAC(4,2), INSHL(2), NSTAGE, NDAPST, CASF(4,2), IPRINT(8),
11TITLE(6), VALU(4,2), PKBD(4,4,2), PKBDES(4,4,2), XGRID(11,4,2),
1PKAD(4,4,2), PKAES(4,4,2), PKBA(4,4,2), PKAA(4,4,2),
1PKESAD(4,4,2), PKESAD(4,4,2), PKSH(4,2), PKNS(4,2), REIN(4,2,100),
1WGHT(100,2), XSORT(8,4,2), NDIV(2), UWGHT(5), NRSAM(2), NFSAM(2),
1PKRS(4,2), PKFS(4,2), ABAF(8,4,2), DIVFP(2), PKWAFS(4,2),
1PKAAFS(4,2), PKAARS(4,2), PKAEFS(4,2), PKAEHS(4,2), PKBEFS(4,2),
1PKFAFS(4,2), PKRAFS(4,2), PKRARS(4,2), DFPRED(4,2), FEWA(2,28),
1REINF(4,2,100),
COMMON /WORKN/ NTYPE(2), NMISS(4,2), NMISST(2), NGR10(4,2),
1IBLURD(2), NSTRAT(4,2), NFULST(2), NSTAT, NINGAM, IMPNT(32,2),
11TPNT(32,2), IDEN(8), NSTRIC(2), IRA(100), JRA(100), LUNI, LUNO,
1NWORK, NSTAT2, ISINT(500,2), IDINT(100,2), INPNT(32,2),
COMMON /WORKL/ LOCST(500,2), LOCBG, LOCEG, KOCWG, KOCEG, LOCBVR,
1LOCBVB, LOCEVR, LOCEVB, LOCBPR, LOCBPB, LOCEPR, LOCEPB,
1KOCBVB, KOCEVB, KOCBVR, KOCEVR, JOCBVB, JOCEVB, JOCBVR, JOCEVR,
1IOCBVB, IOCEVB, IOCBVR, IOCEVR
COMMON /WORK/ SPACER(18600), STRATS(8,200,4)
C
C   IF NWORK IS CHANGED IN INIT, THE LENGTH OF SPACER MUST
C   BE SET EQUAL TO NWORK-6400.
C
COMMON /SPARM/ MFRAC, NMISS, IBR, ITYPE, NSTOR(8), IPNT(8)
DIMENSION MSTOR(8)
NSTRAT(ITYPE, IBR)=0
MISSN=NMISS(ITYPE, IBR)
FRACN=MFRAC(ITYPE, IBR)
IF(MMISS .NE. 0) GO TO 200
DO 100 I=1, MISSN
STRATS(I,1, ITYPE)=NSTOR(I)/FRACN
100 CONTINUE
NSTRAT(ITYPE, IBR)=1
RETURN
200 IH1=MFRAC*I
ILO1=1
IF(MMISS .EQ. 1) ILO1=IH1
DO 400 I1=ILO1, IH1
MSTOR(I1)=I1-I
IH12=IH1-MSTOR(1)
ILO2=I
IF(MMISS .EQ. 2) ILO2=IH12
DO 400 I2=ILO2, IH12
MSTOR(I2)=I2-I
IH13=IH12-MSTOR(2)
ILO3=I
IF(MMISS .EQ. 3) ILO3=IH13
DO 400 I3=ILO3, IH13
MSTOR(I3)=I3-I
IH14=IH13-MSTOR(3)
ILO4=I
IF(MMISS .EQ. 4) ILO4=IH14
DO 400 I4=ILO4, IH14

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FIGURE B-1 (cont'd)

	MSTOR(4)=14-1	00700
	IHI5=IHI4-MSTOR(4)	00710
	IL05=1	00720
	IF(MMISS.EQ. 5) IL05=IHI5	00730
	DO 400 I5=IL05,IHI5	00740
	MSTOR(5)=I5-1	00750
	IHI6=IHI5-MSTOR(5)	00760
	IL06=1	00770
	IF(MMISS.EQ. 6) IL06=IHI6	00780
	DO 400 I6=IL06,IHI6	00790
	MSTOR(6)=I6-1	00800
	IHI7=IHI6-MSTOR(6)	00810
	IL07=1	00820
	IF(MMISS.EQ. 7) IL07=IHI7	00830
	DO 400 I7=IL07,IHI7	00840
	MSTOR(7)=I7-1	00850
	IHI8=IHI7-MSTOR(7)	00860
	IL08=1	00870
	IF(MMISS.EQ. 8) IL08=IHI8	00880
	DO 400 I8=IL08,IHI8	00890
	MSTOR(8)=I8-1	00900
	NSTRAT(ITYPE,IBR)=NSTRAT(ITYPE,IBR)+1	00910
	DO 300 I=1,MMISS	00920
	J=IPNT(I)	00930
	NSTOR(J)=MSTOR(I)	00940
300	CONTINUE	00950
	J=NSTRAT(ITYPE,IBR)	00960
	DO 350 I=1,MISSN	00970
	STRATS(I,J,ITYPE)=NSTOR(I)/FRACN	00980
350	CONTINUE	00990
400	CONTINUE	01000
	IF(NSTRAT(ITYPE,IBR).GT. 200) CALL ERR(3)	01010
	RETURN	01020
	END	01030

	SUBROUTINE TIMER	00110
C		00120
C	/TIMER/ USES AN EMPIRICAL FORMULA TO ESTIMATE THE	00130
C	EXECUTION TIME REQUIRED FOR THE CURRENT RUN.	00140
C		00150
	COMMON /INPUT/ IMISS(8,4,2), IGRID(11,4,2), LASTP, NALOC(8,4),	00160
	INFRAC(4,2), NSHL(2), NSTAGE, NDAPST, CASF(4,2), IPRINT(8),	00170
	ITITLE(6), VALU(4,2), PKBD(4,4,2), PKBDES(4,4,2), XGRID(11,4,2),	00180
	IPKAD(4,4,2), PKADES(4,4,2), PKBA(4,4,2), PKAA(4,4,2),	00190
	IPKESBD(4,4,2), PKESAD(4,4,2), PKSH(4,2), PKNS(4,2), REIN(4,2,100),	00200
	IWGHT(100,2), XSORT(8,4,2), NDIV(2), OWGHT(5), NRSAM(2), NFSAM(2),	00210
	IPKRS(4,2), PKFS(4,2), ABAF(8,4,2), DIVFP(2), PKBAFS(4,2),	00220
	IPKAARS(4,2), PKAARS(4,2), PKAEFS(4,2), PKAERS(4,2), PKWEFS(4,2),	00230
	IPKFAFS(4,2), PKRAFS(4,2), PKRARS(4,2), DFPRED(4,2), FEWA(2,28),	00240
	IREINF(4,2,100)	00250
	COMMON /WORKN/ NTYPE(2), NMISS(4,2), NMISST(2), NGRID(4,2),	00260
	IBLURD(2), NSTRAT(4,2), NFULST(2), NSTAT, NINGAM, IMPNT(32,2),	00270
	ITPNT(32,2), IDEM(8), NSTRTC(2), IRA(100), JRA(100), LUN1, LUN0,	00280
	INWORK, NSTAT2, ISINT(500,2), IOINT(100,2), INPNT(32,2)	00290

FIGURE B-1 (cont'd)

	COMMON /WORKL/ LOCST(500,2),LOCB6,LOCEG,KOCB6,KOCEG,LOCBVR,	00300
	ILOCBVB,LOCEVR,LOCEVB,LOCBPR,LOCBPB,LOCEPR,LOCEPB,	00310
	IKOCBVB,KOCEVB,KOCBVR,KOCEVR,JOCBVB,JOCEVB,JOCBVR,JOCEVR,	00320
	IIOCBVB,IOCEVB,IOCBVR,IOCEVR	00330
	COMMON /SINTVL/ IRLO(500),IRHI(500)	00340
	DIMENSION IFUNC(4),TIMEC(4),TIMEI(4)	00350
	DATA(V=.12),(W=2.0E-3),(X=1.2E-5),(Y=4.4E-4),(Z=2.0E-4)	00360
	DATA(IFUNC=5HSETUP,7HBATTLES,5HGGAMES,5HTOTAL)	00370
	IHI1=NFULST(1)	00380
	IHI2=NFULST(2)	00390
	TIMEC(1)=2.0	00400
	TIMEI(1)=2.0	00410
	NTP=NTYPE(1)*NTYPE(2)	00420
	NPNTS=1	00430
	DO 100 I=1,NTP	00440
	NPNTS=NPNTS*2	00450
100	CONTINUE	00460
	NBATLS=0	00470
	TIMEC(3)=0.	00480
	DO 200 I=1,IHI1	00490
	NBATLS=NBATLS+IRHI(1)-IRLO(1)+1	00500
200	CONTINUE	00510
	TIMEC(2)=NSTAT*NDAPST*NBATLS*W	00520
	TIMEI(2)=NSTAT*V	00530
	DO 500 I=1,NSTAGE	00540
	ICNT=0	00550
	DO 300 J=1,IHI1	00560
	IF(ISINT(J,1).NE.IDINT(1,1)) GO TO 300	00570
	ICNT=ICNT+1	00580
300	CONTINUE	00590
	JCNT=0	00600
	DO 400 J=1,IHI2	00610
	IF(ISINT(J,2).NE.IDINT(1,2)) GO TO 400	00620
	JCNT=JCNT+1	00630
400	CONTINUE	00640
	TIMEC(3)=TIMEC(3)+ICNT*JCNT*(Y+NTP*X*NPNTS)+Z*(ICNT+JCNT)	00650
500	CONTINUE	00660
	TIMEC(3)=NSTAT*TIMEC(3)	00670
	TIMEI(3)=NSTAGE*NSTAT*V	00680
	IF(IPRINT(4).EQ.1) TIMEI(2)=2.*TIMEI(2)	00690
	IF(IPRINT(4).EQ.2) TIMEC(2)=0.	00700
	TIMEC(4)=TIMEC(1)+TIMEC(2)+TIMEC(3)	00710
	TIMEI(4)=TIMEI(1)+TIMEI(2)+TIMEI(3)	00720
	WRITE(LUNO,600)	00730
600	FORMAT(IHI1///10X,40HCDC 6600 TIME ESTIMATES FOR CURRENT RUN ,	00740
	19H(SECONDS)//16X,8HFUNCTION,8X,8HCPU TIME,3X,8H170 TIME//)	00750
	DO 700 I=1,3	00760
	WRITE(LUNO,650) IFUNC(I),TIMEC(I),TIMEI(I)	00770
650	FORMAT(16X,A7,9X,F8.1,3X,F8.1)	00780
700	CONTINUE	00790
	WRITE(LUNO,750) IFUNC(4),TIMEC(4),TIMEI(4)	00800
750	FORMAT(/16X,A7,9X,F8.1,3X,F8.1///)	00810
	RETURN	00820
	END	00830

FIGURE B-1 (cont'd)

```

SUBROUTINE TRIALS
C
C      /TRIALS/ COMPUTES THE MAXMIN AND MINMAX BOUNDS AND PERFORMS
C      THE FORWARD EVALUATION FOR A TRIAL AIRWAR OF SPECIFIED
C      LENGTH BEGINNING WITH A SPECIFIED NUMBER OF BLUE AND RED
C      PLANES. /TRIALS/ COMPUTES THESE VALUES USING THE OPTIMAL
C      STRATEGIES AND VALUES PREVIOUSLY DETERMINED BY /GAMES/.
C
COMMON /INPUT/ IMISS(8,4,2), IGRID(11,4,2), LASTP, NALOC(8,4),
INFRAC(4,2), NSHL(2), NSTAGE, NDAFST, CASF(4,2), IPRINT(8),
IITITLE(6), VALU(4,2), PKBO(4,4,2), PKBOES(4,4,2), XGRID(11,4,2),
IPKAD(4,4,2), PKAOES(4,4,2), PKBA(4,4,2), PKAA(4,4,2),
IPKESBD(4,4,2), PKESAO(4,4,2), PKSH(4,2), PKNS(4,2), KEIN(4,2,100),
IWGHT(100,2), XSORT(8,4,2), NOIV(2), OWGHT(5), NRSAM(2), NFSAM(2),
IPKRS(4,2), PKFS(4,2), ABAF(8,4,2), DIVFP(2), PKWAFS(4,2),
IPKAAS(4,2), PKAARS(4,2), PKAFS(4,2), PKAERS(4,2), PKBEFS(4,2),
IPKFAFS(4,2), PKRAFS(4,2), PKRARS(4,2), DFPRED(4,2), FEBA(2,28),
IREINF(4,2,100)
COMMON /WORKN/ NTYPE(2), NMISS(4,2), NMISST(2), NGRID(4,2),
IIBLUR(2), NSTRAT(4,2), NFULST(2), NSTAT, NINGAM, IMPNT(32,2),
IITPNT(32,2), IDEM(8), NSTRIC(2), IRA(100), JRA(100), LUNI, LUNO,
INWORK, NSTAT2, ISINT(500,2), IJINT(100,2), INPNT(32,2)
COMMON /WORKL/ LOCST(500,2), LOCBG, LOCEG, KOCBG, KOCEG, LOCBVR,
ILOCBVB, LOCEVR, LOCEVB, LOCBPR, LOCBPB, LOCEPR, LOCEPB,
IKOCBVB, KOCEVB, KOCEVR, KOCEVR, JOCBVB, JOCEVB, JOCBVR, JOCEVR,
IIOCBVB, IOCEVB, IOCEVR, IOCEVR
COMMON /BPAR/ CNP(4,2), IB, IR, XNP(9,4,2), OJBEC(2,5)
COMMON /INTERP/ BETA(2,8), IBETA(2,8), I1, I2, I3, I4, I5, I6, I7, I8,
I1I1, I1I2, I1I3, I1I4, I1I5, I1I6, I1I7, I1I8
COMMON /WORK/ XARRAY(25000)
DIMENSION IOPTN(5), IOUT(10), JOUT(4,2), JOPTN(5), IARRAY(1)
DIMENSION IPLAL(100,2), XOBJF(3,100), TXOBJF(3)
EQUIVALENCE (XARRAY, IARRAY)
COMMON /ROUND/ JDEX(4,2,2)
DIMENSION MVEC(1), NVEC(1)
EQUIVALENCE (MVEC, JDEX(1,1,1)), (NVEC, JOEX(1,1,2))
DATA (JOPTN=5(0))
NTRIAL=0
100 READ(LUNI,110) KEY, MSTAGE, ((IOPTN(I), I=1,5), ((CNP(I,K), I=1,4),
1K=1,2)
110 FORMAT(A5,5X,I2,2X,5I1,1X,2(4F5.0,5X))
IF(EOF(LUNI)) 990,120
120 IF(KEY.EQ.5HTRIAL) GO TO 200
IF(KEY.EQ.5HFINIS) GO TO 990
CALL ERR(17)
GO TO 100
200 IF(MSTAGE.LE.NSTAGE) GO TO 240
CALL ERR(18)
GO TO 100
240 DO 250 K=1,2
DO 250 I=1,4
IUP=NGRID(I,K)
IF(CNP(I,K).GT.XGRID(IUP,I,K)) GO TO 270
250 CONTINUE
GO TO 300
270 CALL ERR(19)
GO TO 100
300 REWIND 7

```

FIGURE B-1 (cont'd)

	REWIND 8	00690
	REWIND 9	00700
	TOBJF=0.	00710
	DO 305 K=1,2	00720
	DO 305 I=1,4	00730
	JOUT(I,K)=CNP(I,K)+.5	00740
305	CONTINUE	00750
	NTRIAL=NTRIAL+1	00760
	NSKIP=NSTAGE-MSTAGE	00770
	IF(NSKIP.EQ. 0) GO TO 400	00780
	DO 350 I=1,NSKIP	00790
	BUFFER IN (7,1) (IARRAY(LOCVB),IARRAY(LOCVB))	00800
	IF(UNIT(7)) 320,310,310	00810
310	CALL ERR(14)	00820
320	BUFFER IN (8,1) (IARRAY(LOCBPB),IARRAY(LOCBPB))	00830
	IF(UNIT(8)) 350,340,340	00840
340	CALL ERR(15)	00850
350	CONTINUE	00860
400	BUFFER IN (7,1) (IARRAY(LOCVB),IARRAY(LOCVR))	00870
	IF(UNIT(7)) 410,405,405	00880
405	CALL ERR(14)	00890
C		00900
C	COMPUTE MAXMIN AND MINMAX	00910
C		00920
410	DO 420 K=1,16	00930
	MVEC(K)=0	00940
420	CONTINUE	00950
	DO 460 K=1,2	00960
	L=3-K	00970
	IUP=NTYPE(L)	00980
	DO 460 J=1,IUP	00990
	N=1	01000
	DO 440 M=1,11	01010
	IF(CNP(J,L)-XGRID(M,J,L)) 450,445,440	01020
440	CONTINUE	01030
	M=11	01040
445	N=0	01050
450	M=M-1	01060
	JDEX(J,L,K)=M	01070
	JDEX(J,L,L)=M-N	01080
460	CONTINUE	01090
	IBS=1STATE(MVEC)-1	01100
	IRS=1STATE(NVEC)-1	01110
	XMIN=XARRAY(LOCVB+IBS)	01120
	XMAX=XARRAY(LOCVR+IRS)	01130
		01140
C		01150
C	PERFORM FORWARD EVALUATION FOR SPECIFIED TRIAL	01160
C		01170
	DO 700 M=1,MSTAGE	01180
	MSLOC=M+NSKIP	01190
	NSLOC=MSLOC+1	01200
	BUFFER IN (8,1) (IARRAY(LOCBPB),IARRAY(LOCVR))	01210
	IF(UNIT(8)) 510,505,505	01220
505	CALL ERR(15)	01230
510	CALL BETAS	01240
	DO 600 N=1,8	01250
	MVEC(N)=1BETA(1,N)	01260
	IF(BETA(1,N).LT. BETA(2,N)) MVEC(N)=1BETA(2,N)	01270
600	CONTINUE	

FIGURE B-1 (cont'd)

IS=ISTATE(MVEC)-1	01280
IB=1ARRAY(LOCBPB+IS)	01290
IR=1ARRAY(LOCBPR+IS)	01300
IPLAL(M,1)=LOCST(1B,1)	01310
IPLAL(M,2)=LOCST(1R,2)	01320
CALL BATTLE	01330
BOBJ=0.	01340
ROBJ=0.	01350
DO 605 I=1,3	01360
BOBJ=BOBJ+OBJEC(1,I)*OWGHT(I)	01370
ROBJ=ROBJ+OBJEC(2,I)*OWGHT(I)	01380
605 CONTINUE	01390
OBJF=BOBJ*WGHT(MSLOC,1)-ROBJ*WGHT(MSLOC,2)	01400
TOBJF=TOBJF+OBJF	01410
IF(1OPTN(1).NE.0) GO TO 630	01420
ICNT=0	01430
DO 610 K=1,2	01440
DO 610 I=1,4	01450
ICNT=ICNT+1	01460
IOUT(ICNT)=CNP(1,K)*.5	01470
CNP(1,K)=REINF(1,K,NSLOC)*CNP(1,K)+REIN(1,K,NSLOC)	01480
610 CONTINUE	01490
IOUT(9)=OBJF+SIGN(.5,OBJF)	01500
IOUT(10)=TOBJF+SIGN(.5,TOBJF)	01510
BUFFER OUT (9,1) (IOUT,IOUT(10))	01520
IF(UNIT(9)) 630,620,620	01530
620 CALL ERR(20)	01540
630 IF(1OPTN(3).NE.0) GO TO 700	01550
DO 640 I=1,3	01560
XOBJF(1,M)=OBJEC(1,I)*WGHT(MSLOC,1)-OBJEC(2,I)*WGHT(MSLOC,2)	01570
640 CONTINUE	01580
700 CONTINUE	01590
C	01600
C WRITE DESIGNATED OUTPUT FOR CURRENT TRIAL	01610
C	01620
IF((NTRIAL-1)/25*25.EQ.NTRIAL-1) GO TO 720	01630
DO 710 I=1,3	01640
IF(JOPTN(I).EQ.0) GO TO 720	01650
710 CONTINUE	01660
GO TO 730	01670
720 WRITE(LUNO,725)	01680
725 FORMAT(1H1,/,8X,6HNUMBER,7X,26HNUMBER OF PLANES AVAILABLE,27X	01690
1,6HMAXMIN/,1X,5HTRIAL,4X,2HOF,5X,16H-----BLUE-----,4X,	01700
116H-----RED-----,4X,4HBLUE,5X,3HRED,7X,2HVS,/,1X,	01710
113HNUMBER STAGES,3X,16H1 2 3 4,4X,	01720
116H1 2 3 4,3X,6HMAXMIN,3X,6HMINMAX,3X,6HMINMAX)	01730
730 IMIN=XMIN+SIGN(.5,XMIN)	01740
IMAX=XMAX+SIGN(.5,XMAX)	01750
IOBJF=TOBJF+SIGN(.5,TOBJF)	01760
DO 735 I=1,5	01770
JOPIN(I)=1OPTN(I)	01780
735 CONTINUE	01790
WRITE(LUNO,740) NTRIAL,MSTAGE,((JOUT(I,K),I=1,4),K=1,2),IMIN,	01800
1IMAX,IOBJF	01810
740 FORMAT(/2X,13,5X,12,2X,815,2(18,1X),18)	01820
IF(1OPTN(1).NE.0) GO TO 850	01830
REWIND 9	01840
DO 840 I=1,MSTAGE	01850
IF((I-1)/50*50.EQ.I-1) WRITE(LUNO,800) NTRIAL	01860

FIGURE B-1 (cont'd)

800	FORMAT(1H1, //21X, 12HTRIAL NUMBER, 15//12X, 14HNUMBER OF BLUE, 7X,	01870
	113HNUMBER OF RED, 8X, 6HMAXMIN, //, 1X, 5HSTAGE, 5X,	01880
	12(16HPLANES AVAILABLE, 5X), 3X, 2HVS, //, 1X, 6HNUMBER, 4X,	01890
	12(16H1 2 3 4, 5X), 1X, 6HMINMAX, 4X, 5HTOTAL//	01900
	BUFFER IN (9,1) (IOUT, IOUT(10))	01910
	IF(UNIT(9)) 810, 805, 805	01920
805	CALL ERR(20)	01930
810	WRITE(LUNO, 820) 1, (IOUT(J), J=1, 10)	01940
820	FORMAT(1X, 14, 2X, 2(1X, 415), 2X, 219)	01950
840	CONTINUE	01960
850	IF(10PTN(2) .NE. 0) GO TO 900	01970
	DO 890 K=1, 2	01980
	IUP=NMISS(K)	01990
	DO 890 I=1, MSTAGE	02000
	IF((I-1)/50*50 .NE. I-1) GO TO 865	02010
	WRITE(LUNO, 860) NTRIAL, IBLURD(K),	02020
	I(ITPNT(J, K), IMPNT(J, K), J=1, IUP)	02030
860	FORMAT(1H1, //21X, 12HTRIAL NUMBER, 15, //13X,	02040
	13HPLANE ALLOCATION FRACTIONS FOR, 4, //, 1X, 5HSTAGE, 16X,	02050
	11HPLANE TYPE/MISSION, //, 1X, 6HNUMBER, 5X,	02060
	13(12(11, 1H, //11, 2X)/12X))	02070
	WRITE(LUNO, 862)	02080
862	FORMAT(1H)	02090
865	ILO=IPLAL(I, K)	02100
	ITP=ILO+IUP-1	02110
	WRITE(LUNO, 880) 1, (XARRAY(J), J=ILO, ITP)	02120
880	FORMAT(1X, 14, 5X, 3(12F5, 2, //, 10X))	02130
890	CONTINUE	02140
900	IF(10PTN(3) .NE. 0) GO TO 100	02150
	DO 905 I=1, 3	02160
	TXOBJF(I)=0.	02170
905	CONTINUE	02180
	DO 930 I=1, MSTAGE	02190
	IF((I-1)/50*50 .EQ. I-1) WRITE(LUNO, 910) NTRIAL	02200
910	FORMAT(1H1, //21X, 12HTRIAL NUMBER, 15, //12X, 8HBLUE-RED, 15X,	02210
	13HBLUE-RED/1X, 5HSTAGE, 8X, 3HCAS, 18X, 8HGRND+AIR, 17X, 4HFEB/	02220
	11X, 6HNUMBER, 5X, 9HFIREPOWER, 4X, 5HTOTAL, 5X, 9HFIREPOWER, 4X,	02230
	15HTOTAL, 5X, 8HMOVEMENT, 5X, 5HTOTAL//	02240
	DO 915 J=1, 3	02250
	TXOBJF(J)=TXOBJF(J)+XOBJF(J, I)	02260
	K=2*J	02270
	IOUT(K-1)=XOBJF(J, I)+SIGN(.5, XOBJF(J, I))	02280
	IOUT(K)=TXOBJF(J)+SIGN(.5, TXOBJF(J))	02290
915	CONTINUE	02300
	WRITE(LUNO, 920) 1, (IOUT(J), J=1, 6)	02310
920	FORMAT(1X, 14, 2X, 3(3X, 2110))	02320
930	CONTINUE	02330
	GO TO 100	02340
990	RETURN	02350
	END	02360

FIGURE B-2

ATACM2 LISTING

```

PROGRAM ATACM2 (OUTPUT,TAPE4=65,TAPE5,TAPE6=OUTPUT,TAPE7=65,
1TAPE8=65,TAPE9=65)
C
C      /ATACM2/ AND ASSOCIATED SUBROUTINES ARE USED TO EVALUATE
C      TRIAL AIRWARS USING THE OPTIMAL STRATEGIES AND GAME VALUES
C      INPUT FROM A TRIAL-TAPE WRITTEN DURING A PREVIOUS RUN
C      OF /ATACM1/.
C
COMMON /INPUT/ IMISS(8,4,2),IGRID(11,4,2),LASTP,NALOC(8,4),
1NFRAC(4,2),NSHL(2),NSTAGE,NDAPST,CASF(4,2),IPRINT(8),
1ITITLE(6),VALU(4,2),PKBC(4,4,2),PKBDES(4,4,2),XGRID(11,4,2),
1PKAD(4,4,2),PKADES(4,4,2),PKBA(4,4,2),PKAA(4,4,2),
1PKESBD(4,4,2),PKESAD(4,4,2),PKSH(4,2),PKNS(4,2),REIN(4,2,100),
1WGHT(100,2),XSORT(8,4,2),NOIV(2),OWGHT(5),NRSAM(2),NFSAM(2),
1PKRS(4,2),PKFS(4,2),ABAF(8,4,2),DIVFP(2),PKWAFS(4,2),
1PKAAS(4,2),PKAARS(4,2),PKAEFS(4,2),PKAERS(4,2),PKBEFS(4,2),
1PKFAFS(4,2),PKRAFS(4,2),PKRAHS(4,2),DFPRED(4,2),FEBA(2,28),
1REINF(4,2,100)
COMMON /WORKN/ NTYPE(2),NMISS(4,2),NMISST(2),NGRID(4,2),
11BLURD(2),NSTRAT(4,2),NFULST(2),NSTAT,NINGAM,IMPNT(32,2),
1ITPNT(32,2),IOEM(8),NSTRTC(2),IRA(100),JRA(100),LUNI,LUNO,
1NWORK,NSTAT2,ISINT(500,2),IDINT(100,2),INPNT(32,2)
COMMON /WORKL/ LOCST(500,2),LOCBG,LOCEG,KOCHG,KOCEG,LOCBVR,
1LOCBVB,LOCEVR,LOCEVB,LOCBPR,LOCBPB,LOCEPR,LOCEPB,
1KOCBVB,KOCEVB,KOCBVR,KOCEVR,JOCBVB,JOCEVB,JOCBVR,JOCEVR,
1IOCBVB,IOCEVB,IOCBVR,IOCEVR
COMMON /WORK/ XARRAY(25000)
COMMON /ERROR/ IERR
DIMENSION INPUTZ(2680),WORKNZ(1640),WORKLZ(1024),WORKZ(25000)
DIMENSION IARRAY(10000)
DIMENSION JGRID(11,8),JPRINT(8)
EQUIVALENCE (IMISS,INPUTZ),(NTYPE,WORKNZ),(LOCST,WORKLZ)
EQUIVALENCE (IGRID,JGRID)
EQUIVALENCE (XARRAY,IARRAY,WORKZ)
BUFFER IN (4,1) (INPUTZ,INPUTZ(2680))
IF(UNIT(4)) 200,150,150
150 CALL ERR(22)
200 BUFFER IN (4,1) (WORKNZ,WORKNZ(1640))
IF(UNIT(4)) 300,150,150
300 BUFFER IN (4,1) (WORKLZ,WORKLZ(1024))
IF(UNIT(4)) 400,150,150
400 BUFFER IN (4,1) (WORKZ,WORKZ(NWORK))
IF(UNIT(4)) 410,150,150
410 DO 480 I=1,NSTAGE
BUFFER IN (4,1) (IARRAY(LOCBVB),IARRAY(LOCEVR))
IF(UNIT(4)) 415,450,450
415 BUFFER OUT (7,1) (IARRAY(LOCBVB),IARRAY(LOCEVR))
IF(UNIT(7)) 420,460,460
420 BUFFER IN (4,1) (IARRAY(LOCBPB),IARRAY(LOCEPR))
IF(UNIT(4)) 425,450,450
425 BUFFER OUT (8,1) (IARRAY(LOCBPB),IARRAY(LOCEPR))
IF(UNIT(8)) 480,470,470
450 CALL ERR(22)
460 CALL ERR(12)
470 CALL ERR(13)
480 CONTINUE
READ(LUNI,490) IKEY,(JPRINT(1),I=1,8)
490 FORMAT(A3,7X,8I1)
IF(IKEY.NE.3HRUN) CALL ERR(16)

```

FIGURE B-2 (cont'd)

500	IF(JPRINT(1) .EQ. 0) CALL PRNTIN	00700
	IF(JPRINT(2) .NE. 0) GO TO 700	00710
	DO 560 K=1,2	00720
	IM13=NMISS(K)	00730
	IM11=NFULST(K)	00740
	DO 560 I=1,IM11	00750
	ILO2=LOCST(I,K)	00760
	IM12=ILO2+NMISS(K)-1	00770
	IF((I-1)/50*50 .NE. I-1) GO TO 538	00780
	WRITE(LUNO,530) 1BLORD(K), (IIFNT(J,K), IMPNT(J,K), J=1, IM13)	00790
530	FORMAT(1H1///, 17X, A5, 15HPURE STRATEGIES//, 6H STRAT, 4X, 4H LAST,	00800
	112X, 18H PLANE TYPE/MISSION/, 7H NUMBER, 3X, 5H STAGE, 5X,	00810
	14(10(11, 1H/, 11, 2X)/20X))	00820
	WRITE(LUNO,535)	00830
535	FORMAT(1H)	00840
538	WRITE(LUNO,540) I, ISINT(I,K), (XARRAY(J), J=ILO2, IM12)	00850
540	FORMAT(1X, 15, 5X, 13, 4X, 4(10F5.2/, 18X))	00860
560	CONTINUE	00870
700	IF(JPRINT(3) .NE. 0) GO TO 800	00880
	ICNT=0	00890
	NG1=NGRID(1,1)	00900
	NG2=NGRID(2,1)	00910
	NG3=NGRID(3,1)	00920
	NG4=NGRID(4,1)	00930
	NG5=NGRID(1,2)	00940
	NG6=NGRID(2,2)	00950
	NG7=NGRID(3,2)	00960
	NG8=NGRID(4,2)	00970
	DO 730 I1=1, NG1	00980
	DO 730 I2=1, NG2	00990
	DO 730 I3=1, NG3	01000
	DO 730 I4=1, NG4	01010
	DO 730 I5=1, NG5	01020
	DO 730 I6=1, NG6	01030
	DO 730 I7=1, NG7	01040
	DO 730 I8=1, NG8	01050
	ICNT=ICNT+1	01060
	IF((ICNT-1)/50*50 .EQ. ICNT-1) WRITE(LUNO,710)	01070
710	FORMAT(1H1///, 18X, 27H LIST OF ALL POSSIBLE STATES//, 6H STATE,	01080
	115X, 4H BLUE, 27X, 3H RED, 7H NUMBER, 7X, 2(19H1 2 3 4,	01090
	111X)/)	01100
	WRITE(LUNO,720) ICNT, JGRID(11,1), JGRID(12,2), JGRID(13,3),	01110
	JGRID(14,4), JGRID(15,5), JGRID(16,6), JGRID(17,7), JGRID(18,8)	01120
720	FORMAT(1X, 15, 4X, 2(416, 6X))	01130
730	CONTINUE	01140
800	CALL TRIALS	01150
	END	01160

In addition, ATACM2 uses subroutines

BATTLE
 BETAS
 ERR
 ISTATE
 PRNTIN
 TRIALS
 PKILLS

all of which are listed under ATACM1.

TABLE B-3

VARIABLES MOST FREQUENTLY USED
IN ATACM1 AND ATACM2

<u>Variable</u>	<u>Subroutine or COMMON</u>	<u>Description</u>
ABAF(i,j,k)	INPUT	Fraction of type j aircraft on side k assigned to the ith mission which is vulnerable to airbase attack.
ALPHA	GAMES	Coefficient used in the linear interpolation algorithm to weight the objective function value corresponding to that point in the state space currently being examined.
ATTK	BATTLE	Number of ABA sorties flown against the opponent's airbase during the current one-cycle battle.
BETA(·,j)	INTERP	Weights used to linearly interpolate an objective function value for a point lying between two adjacent grid levels in dimension j. BETA(1,j) is the weight for the value corresponding to the lower level; BETA(2,j) the weight for the higher level.
BMIN(i)	GAMES	Minimum value in the ith row of the game matrix for the current state.
BOBJ	INIT TRIALS	Value of Blue's contribution to the objective function.
BTFP	BATTLE	Total ground firepower delivered by Blue during the current one-cycle battle.
CASF(j,k)	INPUT	Firepower per CAS sortie for an aircraft of type j on side k.
CASO(k)	BATTLE	Total CAS firepower delivered by side k during the current one-cycle battle.
CHECK	GAMES	Objective function value resulting from using specified Blue/Red strategies for one stage followed by the use of optimal conservative strategies by both sides for all subsequent stages. Used to compute MAXMIN/MINMAX bounds.
CHECKB	GAMES	Analogous to CHECK. Used to compute Blue's optimal MAXMIN play.
CHECKR	GAMES	Analogous to CHECK. Used to compute Red's optimal MINMAX play.
CNP(j,k)	BPARM	Current number of planes of type j on side k.

TABLE B-3 (Cont'd)

<u>Variable</u>	<u>Subroutine or COMMON</u>	<u>Description</u>
CNPV(j)	BATTLE	Current number of planes of type j vulnerable to the opponent's airbase attackers.
DELTA(j)	IPARM	Distance between adjacent "fine" grid levels in dimension j.
DFPRED(j,k)	INPUT	Division firepower reduction produced by a CAS sortie flown by aircraft type j on side k.
DIVFP(k)	INPUT	Firepower produced by a ground division of type k.
FEBA(i,j)	INPUT	i-th coordinate of the j-th point in the set of points which define FEBA movement as a function of Blue/Red force ratios.
FRACN	STRAT	Denominator of the minimum allocation fraction for the current aircraft type.
FRATIO	BATTLE	Ratio of Blue ground firepower to Red ground firepower for the current one-cycle battle.
IARRAY(.)	WORK	Work array used to store strategies, battle assessments, and MAXMIN/MINMAX plays and objective function values. EQUIVALENCED to XARRAY.
IB	BPARM	Index of the strategy employed by Blue in the current one-stage battle.
IBETA(.,j)	INTERP	Indices of grid levels lying on either side of an interpolation point in dimension j. IBETA(1,j) is one less than the subscript corresponding to the lower grid level; IBETA(2,j) is one less than the subscript corresponding to the higher.
IBH	INIT	High bound on the range of stages over which the current Blue strategy can be played.
IBIT(i)	IPARM	Rightmost bit in the i-th 7-bit byte of the word used to store the results of a one-stage battle assessment. From left to right, bytes 1-4 are used to store levels of Blue aircraft of types 1-4; bytes 5-8 levels of Red aircraft of types 1-4.
IBL	INIT	Low bound on the range of stages over which the current Blue strategy can be played.
IBLURD(k)	WORKN	Hollerith constant equal to "BLUE" if k=1 or "RED" if k=2.

TABLE B-3 (Cont'd)

<u>Variable</u>	<u>Subroutine or COMMON</u>	<u>Description</u>
IBPLAY	GAMES	Index of Blue's optimal MAXMIN strategy.
IBR(k)	BPARM	Index of the strategy employed by side k in the current one-stage battle.
IDEM(*)	WORKN	Array of constants used to compute the number of the state corresponding to a set of grid-level indices. Constants are assigned in INIT.
IDINT(t,k)	WORKN	Latest stage for which the set of strategies available to side k during stage t are applicable.
IDUMMY(*)	READIN	Array used for temporary storage of input parameters prior to their being decoded.
IERR	ERROR	Flag indicating the severity of the last diagnostic message printed.
IETYPE(i)	ERR	Severity code associated with diagnostic i. Codes 1, 2, and 3 correspond to "INFO", "ERROR", and "ABORT" respectively.
IGRID(i,j,k)	INPUT	ith grid level assigned to aircraft type j on side k.
IHEAD(.,.)	PRNTIN	Array of explanatory titles used to print input parameters in an easy-to-read format.
IKEY	READIN	Card key on the current input card.
IMAX	TRIALS	Rounded MINMAX bound on the value of the objective function for the current trial.
IMESSG(.,i)	ERR	Diagnostic message associated with error code i.
IMIN	TRIALS	Rounded MAXMIN bound on the value of the objective function for the current trial.
IMISS(i,j,k)	INPUT	Code of the ith mission assigned to aircraft type j on side k.
IMPNT(i,k)	WORKN	ith mission code assigned to aircraft types on side k.
INPNT(i,k)	WORKN	Index, within an aircraft type, of the ith mission code assigned to all aircraft types on side k.
INPUTZ(*)	INPUT	Single array EQUIVALENCED to COMMON block INPUT.
IOBJ	GAMES INIT	Blue's contribution to the value of the objective function resulting from a one-stage battle.

TABLE B-3 (Cont'd)

<u>Variable</u>	<u>Subroutine or COMMON</u>	<u>Description</u>
IOBJF	TRIALS	Rounded cumulative value of the objective function produced by playing optimal MAXMIN strategies against optimal MINMAX strategies during the current trial.
IOCBVB	WORKL	Beginning location of the area used in XARRAY to store current-stage MAXMIN values for Blue.
IOCBVR	WORKL	Beginning location of the area used in XARRAY to store current-stage MINMAX values for Red.
IOCEVB	WORKL	End location of the area used in XARRAY to store current-stage MAXMIN values for Blue.
IOCEVR	WORKL	End location of the area used in XARRAY to store current-stage MINMAX values for Red.
IOPTN(I)	TRIALS	Value of the Ith print option specified on the current TRIAL card.
IPLAL(t,k)	TRIALS	Beginning location in XARRAY of the optimal allocation fractions used by side k during stage t of the current trial war.
IPNT(I)	SPARM	Index of the Ith strategy for which an allocation fraction is not specified.
IPPNT(I)	TEMP	Pointer indicating the dimension in the state space which corresponds to the Ith aircraft type assigned.
IPRINT(I)	INPUT	Value of the control parameter specified for the Ith print option on the RUN card.
IR	BPARM	Index of the strategy employed by Red in the current one-stage battle.
IRA(•)	WORKN	Array of indices used in conjunction with the random access file TAPE2.
IRHI(I)	SINTVL	High bound on the range of Red strategies which can be played against the Ith strategy of Blue.
IRLO(I)	SINTVL	Low bound on the range of Red strategies which can be played against the Ith strategy of Blue.
IRPLAY	GAMES	Index of Red's optimal MINMAX strategy.
ISINT(I,k)	WORKN	Latest stage for which the Ith strategy available to side k is applicable.

TABLE B-3 (Cont'd)

<u>Variable</u>	<u>Subroutine or COMMON</u>	<u>Description</u>
ISTAT	GAMES	Number of the state corresponding to a set of grid levels.
ITITLE(·)	INPUT	Array used to store the run title as specified on the RUN card.
ITP	READIN	Flag to indicate whether the parameters on the current card are for Blue or Red. ITP=1 corresponds to Blue, ITP=2 to Red.
ITPNT(1,k)	WORKN	Aircraft type to which the 1th mission on side k is assigned.
ITYPE	SPARM	Aircraft type for which the current strategies are being generated.
IVERT(·,j)	GAMES	An NPTT-tuple of 1's and 2's representing the jth vertex of a "cube" in the state space. The number of possible tuples equals LPTT.
IWORD	GAMES INIT	Word containing both Blue and Red contributions to the value of the objective function resulting from a one-stage battle. Blue's contribution is packed into the leftmost 30 bits, Red's in the rightmost 30 bits.
JBETA(·,j,k)	IPARM	Indices of grid levels lying on either side of the kth "fine" grid level in dimension j. JBETA(1,j,k) is one less than the subscript corresponding to the lower grid level; JBETA(2,j,k) is one less than the subscript corresponding to the higher.
JDEX(·,·,k)	ROUND	Array of grid-level indices used to compute the state resulting from rounding the numbers of aircraft on side k down and the numbers opposing side k up.
JOBJ	GAMES INIT	Red's contribution to the value of the objective function resulting from a one-stage battle.
JOGBVB	WORKL	Beginning location of the area used in XARRAY to store next-stage MAXMIN values for Blue.
JOGBVR	WORKL	Beginning location of the area used in XARRAY to store next-stage MINMAX values for Red.
JOCEVB	WORKL	End location of the area used in XARRAY to store next-stage MAXMIN values for Blue.

TABLE B-3 (Cont'd)

<u>Variable</u>	<u>Subroutine or COMMON</u>	<u>Description</u>
JOCEVR	WORKL	End location of the area used in XARRAY to store next-stage MINMAX values for Red.
JOPTN(I)	TRIALS	Value of the Ith print option specified on the previous TRIAL card.
JPRINT(I)	ATACM2	Value of the control parameter specified for the Ith print option on the RUN card.
JRA(.)	WORKN	Array of indices used in conjunction with the random access file TAPE3.
JWORD	GAMES INIT	Word containing "fine" grid-level indices indicating the numbers of planes remaining after a one-stage battle.
KEVEL(.)	INIT	Array of "fine" grid-level indices indicating the numbers of planes remaining after a one-stage battle.
KEY(.)	READIN	Array of valid card keys recognized by READIN.
KOCBG	WORKL	Beginning location of the area used in IARRAY to store numbers of planes available after one-stage battle assessments.
KOCBVB	WORKL	Beginning location of the area used in XARRAY to store interpolated current-stage MAXMIN values for Blue.
KOCBVR	WORKL	Beginning location of the area used in XARRAY to store interpolated current-stage MINMAX values for Red.
KOCEG	WORKL	End location of the area used in IARRAY to store numbers of planes available after one-stage battle assessments.
KOCEVB	WORKL	End location of the area used in XARRAY to store interpolated current-stage MAXMIN values for Blue.
KOCEVR	WORKL	End location of the area used in XARRAY to store interpolated current-stage MINMAX values for Red.
LASTP	INPUT	Last stage thru which the current STRT card is applicable.
LEVEL	GAMES INIT	Index of the "fine" grid-level corresponding to the numbers of planes remaining after a one-stage battle.

TABLE B-3 (Cont'd)

<u>Variable</u>	<u>Subroutine or COMMON</u>	<u>Description</u>
LOCBG	WORKL	Beginning location of the area used in IARRAY to store objective function values resulting from one-stage battle assessments.
LOCBPB	WORKL	Beginning location of the area used in IARRAY to store the indices of optimal MAXMIN plays for Blue.
LOCBPR	WORKL	Beginning location of the area used in IARRAY to store the indices of optimal MINMAX plays for Red.
LOCBVB	WORKL	Beginning location of the area used in XARRAY to store interpolated next-stage MAXMIN values for Blue.
LOCBVR	WORKL	Beginning location of the area used in XARRAY to store interpolated next-stage MINMAX values for Red.
LOCEG	WORKL	End location of the area used in IARRAY to store objective function values resulting from one-stage battle assessments.
LOCEPB	WORKL	End location of the area used in IARRAY to store the indices of optimal MAXMIN plays for Blue.
LOCEPR	WORKL	End location of the area used in IARRAY to store indices of optimal MINMAX plays for Red.
LOCEVB	WORKL	End location of the area used in XARRAY to store interpolated next-stage MAXMIN values for Blue.
LOCEVR	WORKL	End location of the area used in XARRAY to store interpolated next-stage MINMAX values for Red.
LOCST(i,k)	WORKL	Beginning location in XARRAY of the allocation fractions which define the <i>i</i> th strategy of side <i>k</i> .
LOCWD	INIT	Location within IARRAY where the results of the next one-stage battle will be stored.
LPTT	GAMES	Total number of vertices on a "cube" in the state space. Equals 2 raised to the NPTT power.
LUNI	WORKN	Logical unit number of the primary input device (card reader). In the current version LUNI=5.
LUNO	WORKN	Logical unit number of the primary output device (line printer). In the current version LUNO=6.

TABLE B-3 (Cont'd)

<u>Variable</u>	<u>Subroutine or COMMON</u>	<u>Description</u>
MALOC(·)	INPUT	Input array used for temporary storage of STRT card parameters.
MFRAC	SPARM	Numerator of the fraction of aircraft unspecified on the current STRT card for the current aircraft type.
MISSN	STRAT	Number of missions assigned to the current aircraft type.
MMISS	SPARM	Number of missions assigned to the current aircraft type for which allocation fractions are not specified.
MSLOC	GAMES TRIALS	Number of the stage for which current calculations are being made.
MSTAGE	TRIALS	Number of stages specified on the current TRIAL card.
MSTOR(I)	STRAT	Numerator of the allocation fraction for the Ith mission assigned to the current aircraft type.
MVEC(·)	ROUND	Array of grid-level indices used to compute the number of the corresponding state.
NALOC(I,J)	INPUT	Numerator of the allocation fraction specified on the current STRT card for the Ith mission assigned to aircraft type J.
NBATLS	TIMER	Total number of battle evaluations required for each stage, state, and cycle.
NDAPST	INPUT	Number of cycles per stage.
NDIV(k)	INPUT	Number of ground divisions specified for side k.
NFRAC(j,k)	INPUT	Denominator of the minimum allocation fraction specified for aircraft type j on side k.
NFSAM(k)	INPUT	Number of forward SAMs specified for side k.
NFULST(k)	WORKN	Total number of strategies available to side k.
NGRID(j,k)	WORKN	Number of grid-levels specified for aircraft type j on side k.
NINGAM	WORKN GAMES	Number of elements in each one-stage/one-state game matrix.
NKEYS	READIN	Number of valid card keys recognized by READIN.

TABLE B-3 (Cont'd)

<u>Variable</u>	<u>Subroutine or COMMON</u>	<u>Description</u>
NMISS(j,k)	WORKN	Number of missions assigned to aircraft type j on side k.
NMISST(k)	WORKN	Total number of missions assigned to all aircraft types on side k.
NPNTS	TIMER	Total number of vertices on a "cube" in the state space. Equals 2 raised to the NTP power.
NPTT	GAMES	Total number of aircraft types assigned to Blue and Red.
NRSAM(k)	INPUT	Number of rear SAMs specified for side k.
NSHL(k)	INPUT	Number of aircraft shelters assigned to side k.
NSKIP	TRIALS	Number of records to be skipped on TAPE7 and TAPE8 before reading optimal plays and values for the first stage of the current trial war.
NSLOC	GAMES TRIALS	Number of the next stage for which calculations will be made. Equals MSLOC + 1.
NSTAGE	INPUT	Number of stages in the campaign.
NSTAT	WORKN	Total number of states for which optimal plays and objective function values are explicitly computed.
NSTOR(i)	SPARM	Numerator of the allocation fraction specified for the i-th mission assigned to the current aircraft type.
NSTRAT(k)	WORKN	Total number of strategies available to side k.
NSTRIC(k)	WORKN	Number of STRT cards submitted for side k.
NTARG	BATTLE	Total number of planes vulnerable to the opponent's airbase attackers during the current one-cycle battle.
NTP	TIMER	Total number of aircraft types assigned to Blue and Red.
NTRIAL	TRIALS	Number of the current trial.
NTYPE(k)	WORKN	Number of aircraft types specified for side k.
NVEC(-)	ROUND	Array of grid-level indices used to compute the number of the corresponding state.
NWORK	WORKN	Length, in words, of the array XARRAY.

TABLE B-3 (Cont'd)

<u>Variable</u>	<u>Subroutine or COMMON</u>	<u>Description</u>
OBJEC(k,i)	BPARM	Contribution of side k to the value of the ith objective function f_i (see Equation A-1).
OBJF	TRIALS	Value of the objective function for the current stage produced by playing the optimal MAXMIN strategy against the optimal MINMAX strategy.
OWGHT(i)	INPUT	Weight w_i specified on the OWGHT card to be used as a multiplier on f_i (see Equation A-1).
PKAA(i,j,k)	INPUT	Probability an airbase attacker of type j on side k is killed by an opposing airbase defender of type i.
PKAAFS(j,k)	INPUT	Probability an airbase attacker of type j on side k is killed by an opposing forward SAM.
PKAARS(j,k)	INPUT	Probability an airbase attacker of type j on side k is killed by an opposing rear SAM.
PKAD(i,j,k)	INPUT	Probability an airbase defender of type j on side k is killed by an opposing airbase attacker of type i.
PKADES(i,j,k)	INPUT	Probability an airbase defender of type j on side k is killed by an opposing airbase attack escort of type i.
PKAEFS(j,k)	INPUT	Probability an airbase attack escort of type j on side k is killed by an opposing forward SAM.
PKAERS(j,k)	INPUT	Probability an airbase attack escort of type j on side k is killed by an opposing rear SAM.
PKBA(i,j,k)	INPUT	Probability a battlefield attacker of type j on side k is killed by an opposing battlefield defender of type i.
PKBAFS(j,k)	INPUT	Probability a battlefield attacker of type j on side k is killed by an opposing forward SAM.
PKBD(i,j,k)	INPUT	Probability a battlefield defender of type j on side k is killed by an opposing battlefield attacker of type i.
PKBDES(i,j,k)	INPUT	Probability a battlefield defender of type j on side k is killed by an opposing battlefield attack escort of type i.
PKBEFS(j,k)	INPUT	Probability a battlefield attack escort of type j on side k is killed by an opposing forward SAM.

TABLE B-3 (Cont'd)

<u>Variable</u>	<u>Subroutine or COMMON</u>	<u>Description</u>
PKESAD(i,j,k)	INPUT	Probability an airbase attack escort of type j on side k is killed by an opposing airbase defender of type i.
PKESBD(i,j,k)	INPUT	Probability a battlefield attack escort of type j on side k is killed by an opposing battlefield defender of type i.
PKFAFS(j,k)	INPUT	Probability a forward SAM attacker of type j on side k is killed by an opposing forward SAM.
PKFS(i,k)	INPUT	Probability a forward SAM on side k is killed by an opposing forward SAM attacker of type i.
PKNS(i,k)	INPUT	Probability a vulnerable, non-sheltered aircraft on side k is killed by an opposing airbase attacker of type i.
PKRAFS(j,k)	INPUT	Probability a rear SAM attacker of type j on side k is killed by an opposing forward SAM.
PKRARS(j,k)	INPUT	Probability a rear SAM attacker of type j on side k is killed by an opposing rear SAM.
PKRS(i,k)	INPUT	Probability a rear SAM on side k is killed by an opposing rear SAM attacker of type i.
PKSH(i,k)	INPUT	Probability a vulnerable, sheltered aircraft on side k is killed by an opposing airbase attacker of type i.
REIN(j,k,t)	INPUT	Number of reinforcement planes of type j on side k introduced at the beginning of stage t.
REINF(j,k,t)	INPUT	1.0 plus the fraction of reinforcement planes of type j on side k introduced at the beginning of stage t.
REMP(j,k)	BATTLE	Number of remaining planes of type j on side k after attrition.
RFSAM(k)	BATTLE	Number of undamaged forward SAMs on side k during the current one-cycle battle.
RMAX(j)	GAMES	Maximum value in the jth column of the game matrix for the current state.
ROBJ	INIT TRIALS	Value of Red's contribution to the objective function.
RRSAM(k)	BATTLE	Number of undamaged rear SAMs on side k during the current one-cycle battle.

TABLE B-3 (Cont'd)

<u>Variable</u>	<u>Subroutine or COMMON</u>	<u>Description</u>
RTFP	BATTLE	Total ground firepower delivered by Red during the current one-cycle battle.
STRATS(i,k,j)	WORK	Allocation fraction in strategy k for the ith mission assigned to aircraft type j. STRATS makes temporary use of part of the area occupied by XARRAY.
TARG	BATTLE	Total number of planes vulnerable to the opponent's airbase attackers during the current one-cycle battle.
TARGN	BATTLE	Number of unsheltered planes vulnerable to the opponent's airbase attackers during the current one-cycle battle.
TARGS	BATTLE	Number of sheltered planes vulnerable to the opponent's airbase attackers during the current one-cycle battle.
TCASO(k)	BATTLE	Total CAS firepower delivered by side k during the current one-stage battle.
TFIRE(k)	BATTLE	Total ground firepower delivered by side k during the current one-cycle battle.
TIMEC(k)	TIMER	Estimated CPU time required for the ith phase of calculations performed by ATACM1. Phases 1, 2, and 3 are SETUP, BATTLES, and GAMES respectively.
TIMEI(i)	TIMER	Estimated I/O time required for the ith phase of calculations performed by ATACM1. Phases 1, 2, and 3 are SETUP, BATTLES, and GAMES respectively.
TMOVE	BATTLE	Total FEBA movement during the current one-stage battle.
TNNK	BATTLE	Total number of unsheltered aircraft not killed by opposing airbase attackers during the current one-cycle battle.
TNP(i,k)	BATTLE	Total number of sorties assigned to be flown by planes prosecuting mission i for side k during the one-cycle battle.
TOBJF	TRIALS	Cumulative value of the objective function produced by playing optimal MAXMIN strategies against optimal MINMAX strategies during the current trial.

TABLE B-3 (Cont'd)

<u>Variable</u>	<u>Subroutine or COMMON</u>	<u>Description</u>
TOTFP(k)	BATTLE	Total firepower delivered by side k during the current one-stage battle.
TSNK	BATTLE	Total number of sheltered aircraft not killed by opposing airbase attackers during the current one-cycle battle.
TXOBJF(i)	TRIALS	Cumulative value of objective function i produced by playing the optimal MAXMIN strategy against the optimal MINMAX strategy during the current trial.
VALU(j,k)	INPUT	Residual value of an undamaged plane of type j available to side k at the end of the war.
WGHT(t,k)	INPUT	Value of weight b_t if $k=1$ or r_t if $k=2$ as specified on the WGHT card (see Equations A-3 thru A-5).
WORKLZ(•)	WORKL	Single array EQUIVALENCED to COMMON block WORKL.
WORKNZ(•)	WORKN	Single array EQUIVALENCED to COMMON block WORKN.
WORKZ(•)	WORK	Single array EQUIVALENCED to COMMON block WORK.
XARRAY(•)	WORK	Work array used to store strategies, battle assessments, and MAXMIN/MINMAX plays and objective function values. EQUIVALENCED to IARRAY.
XATT	BATTLE	Number of attack sorties during the current phase of the one-cycle battle.
XBETA(•,j,k)	IPARM	Weights used to linearly interpolate an objective function value for the kth "fine" grid-level lying between two adjacent grid-levels in dimension j. XBETA(1,j,k) is the weight for the value corresponding to the lower level, XBETA(2,j,k) the weight for the higher level.
XFSAM	BATTLE	Number of forward SAMs available to the defending side during the current one-cycle battle.
XGRID(i,j,k)	INPUT	i-th grid-level assigned to aircraft type j on side k.
XMOVE	BATTLE	FEBA movement during the current one-cycle battle.

TABLE B-3 (Cont'd)

<u>Variable</u>	<u>Subroutine or COMMON</u>	<u>Description</u>
XNENG	BATTLE	Number of one-on-one engagements between attackers and opponents during the current phase of a one-cycle battle.
XNP(i,j,k)	BPARM	Number of successful sorties flown by planes of type j prosecuting mission i for side k during the current one-cycle battle.
XOBJF(i,t)	TRIALS	Value of objective function i produced by playing the optimal MAXMIN strategy against the optimal MINMAX strategy during stage t.
XOPP	BATTLE	Number of sorties opposing the attackers during the current phase of the one-cycle battle.
XRSAM	BATTLE	Number of rear SAMs available to the defending side during the current one-cycle battle.
XSORT(i,j,k)	INPUT	Sortie rate for aircraft of type j on side k assigned to the ith mission.

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#20 (continued)

campaign. The model permits multiple aircraft types with user-assigned missions, numerical and fractional reinforcements as a function of stage, and user selection of the objective function used to generate the optimal strategies.

Descriptions of the problem formulation and the engagement and optimization methodologies used to solve it are presented along with a user's guide and CDC 6600 FORTRAN listings.

Unclassified