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# COMPUTER PROGRAM (NOLAST) FOR NON-LINEAR ANALYSIS OF COMPOSITE LAMINATES

TECHNICAL REPORT AFFDL-TR-76-1

FEBRUARY 1976

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response of the laminate is determined by ply-wise application of an energy based failure criterion.

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## FOREWORD

This work was performed by R. S. Sandhu of the Design and Analysis Branch, Structures Division, Air Force Flight Dynamics Laboratory under Project 1467, "Structural Analysis Methods," Task No. 146702, "Structural Analysis Methods for Aerospace Vehicles," and Work Unit 14670246, "Automated Design of Advanced Aerospace Structures".

The manuscript was released in November 1975.

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## SECTION I

### INTRODUCTION

Composite laminates are increasingly being used in the design of structural components of flight vehicles. To evolve an efficient design of components, it is necessary to know behavior of the laminates under various combinations of loads. This behavior can be determined experimentally but this is both expensive and inconvenient. The alternative to the purely experimental technique is to determine the analytical response of laminates based upon the mechanical properties of unidirectional laminae and to conduct some limited experimental verification. Analytical technique relating the properties of the unidirectional laminae to those of the laminates is documented in References 1 and 2.

The concepts developed in References 1 and 2 form the basis of a Nonlinear Laminate Strength (NOLAST) analysis computer program which is the subject of this report. The NOLAST program predicts the response of multidirectional laminates subjected to in-plane loads.

A general description of the program is included in Section II while Sections III and IV contain user's instructions and program modifications along with sample problems. The Fortran listing of the program and examples of output appear in Appendices A and B respectively.

## SECTION II

### PROGRAM DESCRIPTION

The program NOLAST is designed to analyze multidirectional laminates subjected to monotonically increasing proportional in-plane loads to failure. In the prediction process, it uses the following:

1. The incremental constitutive relationship for a unidirectional lamina

$$d\epsilon_i = S_{ij}(\epsilon_i) d\sigma_j \quad (i, j = 1, 2, 6) \quad (1)$$

where  $d\epsilon_i$ ,  $d\sigma_j$ ,  $S_{ij}(\epsilon_i)$  are stress and strain components and elements of the compliance matrix. For accurate determination of  $S_{ij}$  etc., experimentally obtained basic stress-strain data (uniaxial tension and compression along and transverse to the material axes and longitudinal shear) of the unidirectional lamina are represented by piecewise cubic spline interpolation functions to yield smooth composite stress-strain curves. The spacing of the stress-strain points of the experimental data can be chosen arbitrarily.

2. In paragraph 1, elements of the compliance matrix,  $S_{ij}(\epsilon_i)$ , are functions of strains ( $\epsilon_i$ ) resulting from simple load conditions. In case the stress-strain curves of the lamina are highly nonlinear, the use of strain components under biaxial stresses would have significant effect on the predicted behavior of the laminate. The presence of a compressive stress in the transverse direction in combination with a tensile stress in the longitudinal direction is likely to result in the reduction of the

apparent longitudinal tensile tangent modulus. The reverse situation would occur if the transverse stress were tensile. The quantitative influence on the tangent modulus relative to one material axis due to the presence of stresses in the other material axis is not known. This information is not available due to the lack of experimental data under biaxial stress states. Consequently the use of components of strains under biaxial stress fields to determine  $S_{ij}(\epsilon_i)$  is erroneous. For the determination of the tangent moduli in this program the effect of the presence of transverse stresses (or longitudinal) is allowed for. For this purpose it is assumed that simple equivalent strain increments can be computed from the following Equations.

$$d\epsilon_1 \Big|_{Eq.} = d\epsilon_1 / (1 - \nu_{12} B) \quad (2)$$

$$d\epsilon_2 \Big|_{Eq.} = d\epsilon_2 / (1 - \nu_{21} / B) \quad (3)$$

where

$\nu_{12}$  = Major Poisson's Ratio and

$B = d\sigma_2 / d\sigma_1$

3. In order to compute laminate strain increments, Equation 24 of Reference 1 is used. This Equation is

$$[d\epsilon^*] = [A]^{-1} [dN] \quad (4)$$

where  $[d\epsilon^o]$  = Laminate Strain Increments

$[A]^{-1}$  = Laminate Compliance Matrix

$[dN]$  = Increments of Stress Resultants

The compliance matrix  $[A]^{-1}$  in Equation 4 represents the average compliance properties during the application of (n+1)-th load increment. However, these properties are not known beforehand. This difficulty is overcome by using the elastic properties corresponding to those at the end of the n-th load increment to compute laminate strain increments. These are then used to compute current stresses and strains in the plies. Based upon the current strains in the plies, average elastic properties are determined. A new compliance matrix is computed and laminate strain increments determined. This procedure is repeated until the difference between two laminate strain increments in two consecutive cycles is smaller than the prescribed error bound. This predictor-corrector and iterative procedure renders the method of analysis practically independent of the size of the load increment.

4. Incremental loading of the laminate cannot continue indefinitely without affecting the load carrying capability of the plies. To determine the onset of degradation of the plies, a criterion is used. The criterion used in this program (Equations 21, and 22 of Reference 2) is a function of both stress and strain states. Specialized for plane stress conditions, it can be written as

$$K_i \left[ \int_{\epsilon_i} \sigma_i d\epsilon_i \right]^{m_i} = 1 \quad (i = 1, 2, 6) \quad (5)$$

where

$$K_i = \left[ \int_{\epsilon_{iu}} \sigma_i d\epsilon_i \right]^{-m_i} \quad (i = 1, 2, 6) \quad (6)$$

In Equations 5 and 6,  $\hat{\epsilon}_i, \epsilon_{iu}$  are current and ultimate normal (tensile or compressive) and shear components of strains.

In plywise application of Equation 5, the program NOLAST allows for two modes of failure i.e. fiber failure and matrix failure modes. To distinguish between the two modes, it is assumed that if

$$K_1 \left[ \int_{\epsilon_1} \sigma_1 d\epsilon_1 \right]^{m_1} / K_1 \left[ \int_{\epsilon_1} \sigma_1 d\epsilon_1 \right]^{m_1} \geq 0.1 \quad (7)$$

the failure mode of the ply corresponds to that of the fiber. When the ply reaches a degradation state, the ply is assumed to unload while the laminate loads are maintained. In the case of a matrix failure mode, both transverse and shear loads of the affected lamina are set to zero. If the failure corresponds to that of the fiber, total unloading of the affected plies is assumed.

5. Strain components corresponding to biaxial stress states are used to satisfy Equations 5 to 7, while equivalent strain components are used to determine tangent moduli. In the absence of experimental data, it is assumed that these strain components cannot be in excess of the ultimate strains obtained under simple load conditions. For this reason, these two type of strain components are checked at the end of application of each load increment. If the difference between ultimate

experimental strain components and equivalent and/or biaxial strain components is less than a prescribed value, the ply is assumed to have failed. The mode of failure would depend upon the nature of the strain component. The exceedance of longitudinal strains results in the fiber failure mode while the others cause a matrix mode of failure.

6. Once the ply failure and its associated mode have been established (Point B in Figure 1), there still remains a question of the influence of the failed ply upon the laminate. Some of the possible responses of the laminate subsequent to the initial ply failure are shown in Figure 1. They are the following:

a. The affected ply unloads completely at B giving rise to a instantaneous increase in strain  $BB_1$  or a drop in stress  $BB_2$  depending upon the nature loading process. Under constant loading rate, the path  $B_1$  would be obtained, while the path  $BB_2$  would result under constant displacement application. After  $B_1$  or  $B_2$ , the stress strain response would be along  $B_1A_1$  or  $B_2A_2$ .

b. An other extreme response corresponding to paragraph 6.a. could be obtained by assuming that the ply continues to carry failure loads (Path  $BA_4$ ) but can sustain no additional loads. This will correspond to an elastic perfectly plastic material.

c. Between the two extremes discussed in paragraphs 6.a. and 6.b., other paths could result depending upon the nature of unloading of the affected ply.

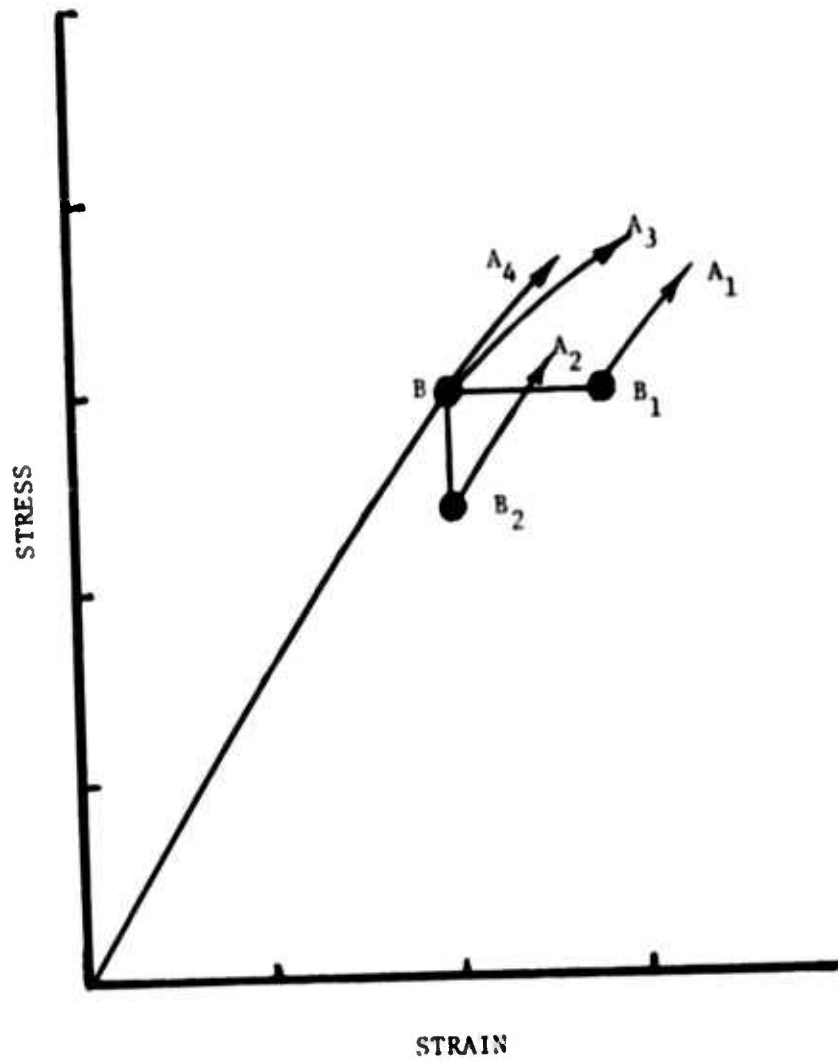


Figure 1. Laminate Response Subsequent to Initial Failure

d. The affected ply may unload gradually. This would correspond to the path  $BA_3$ .

In the NOLAST program, the unloading option of the affected ply corresponds to the path  $BB_1A_1$ . Introduction of other options into the program is not a problem. This is discussed in Section IV.

The structure of the program 'NOLAST' is shown in Figure 2. The main program calls Subroutines INPUT and SPLIN1 only once. Thereafter for every increment of loads, it calls Subroutines ELCON, ITER and OUTPUT in succession.

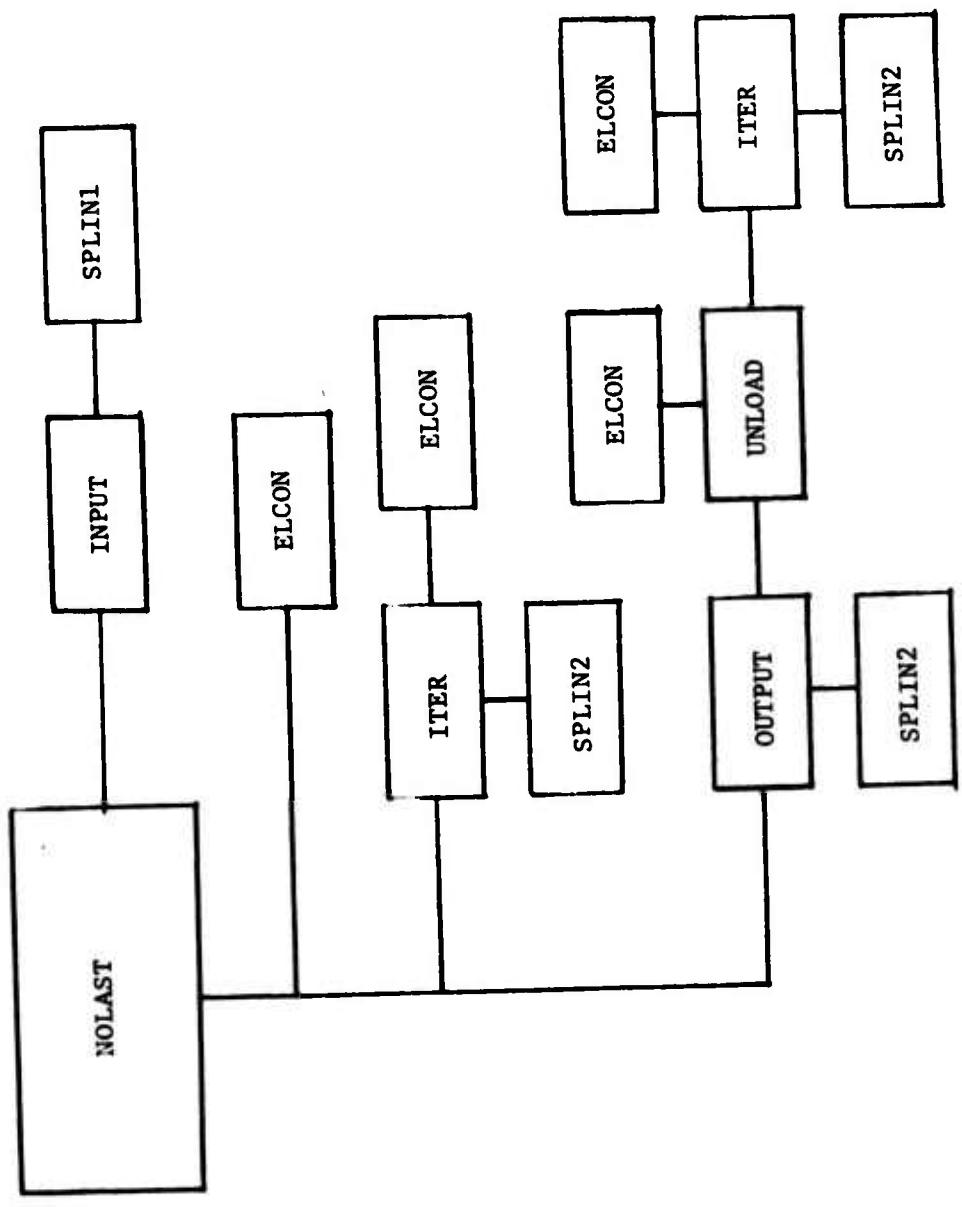


Figure 2. Computer Program Structure

### SECTION III

#### USER'S INSTRUCTIONS FOR DATA PREPARATION

The following sequence of punched cards will be necessary for conducting strength analysis of laminates:

Card 1	HED CARD (12A6)
Col	1-72 Any alphanumeric information
Card 2	MATERIALS (15)
Col	1-5 MATYPE - number of material systems, (maximum = 5)
Cards 3	NUMBER OF NODAL POINTS FOR STRESS-STRAIN PLOTS (715)
Col	1-5 NEPOT - 0° tensile
	6-10 NEPOC - 0° compressive
	11-15 NEP90T - 90° tensile
	16-20 NEP90C - 90° compressive
	21-25 NIP12 - shear
	26-30 NPNUT - tensile Poisson's ratio
	31-35 NPNUC - Compressive Poisson's ratio

Note 1. The above nodal points data includes the fictitious nodal point A (Figure 3). This is done to improve the accuracy of the curves in the last segment. Maximum number of nodal points for a stress-strain plot is limited to 30.

Cards 4	MATERIAL PROPERTY DATA (6F10.0)
Col	1-10 Strain Repeat until all stress-strain
	11-20 Stress data corresponding to 0° tension,
	21-30 Strain 0° compression, 90° tension, 90°
	31-40 Stress compression, shear, tensile Poisson's
	41-50 Strain ratio and compression Poisson's ratio
	51-60 Stress in sequence is accounted for.

Cards 5	INITIAL ELASTIC PROPERTIES (6F10.0)
Col	1-10 E1T Elastic modulus of 0° lamina in tension
	11-20 E1C Elastic modulus of 0° lamina in compression
	21-30 E2T Elastic modulus of 90° lamina in tension
	31-40 E2C Elastic modulus of 90° lamina in compression
	41-50 G12 Shear modulus of 0° lamina

Note 2. One set of (Cards 3 to 5) this data is required for each material system.

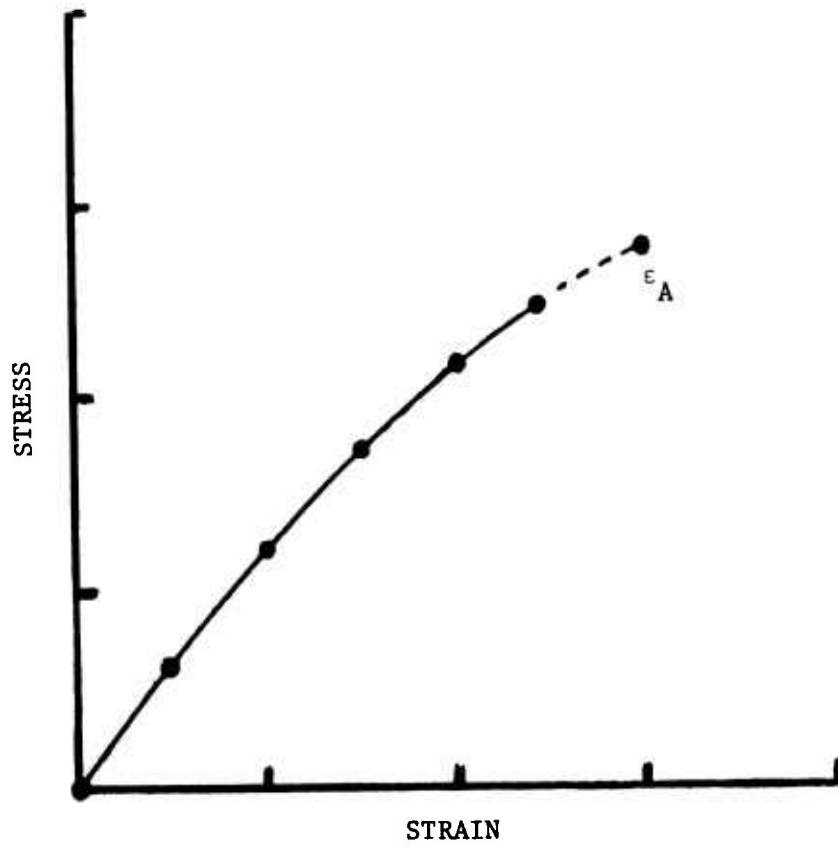


Figure 3. Fictitious Nodal Point A

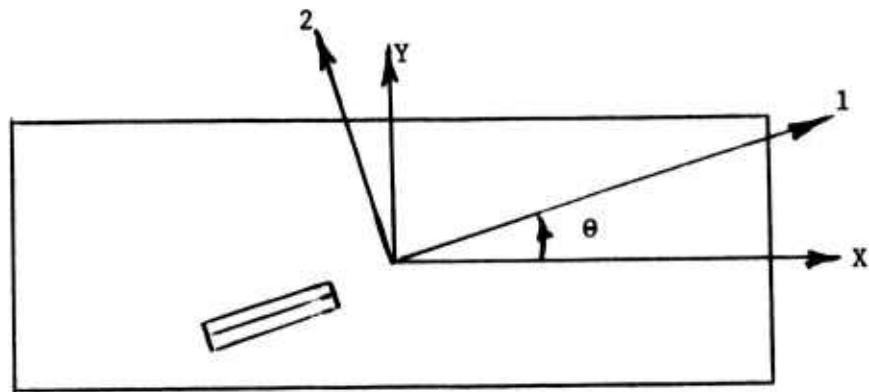


Figure 4. Transformation of Axes

Card 6	NUMBER OF LAMINATES (1415)		
Col	1-5	NUMLAM	- number of laminates
Cards 7	CONTROL CARDS FOR EACH LAMINATE (1415)		
Col	1-5	LAMINA	- number of plies in a laminate (maximum = 15)
	6-10	NN	- number of load combinations (maximum = 10)
	11-15	MLT	- Exponents in Equations 5 to 7. - Until further experimentation, - they may be assumed to be unity.
	16-20	MLC	
	21-25	MTT	
	26-30	MTC	
	31-35	MSH	
	36-40	NPRINT	- Print output for each NPRINT increment (e.g. if NPRINT = 3, the output would be printed 3rd, 6th, 9th etc. increments) except the output for first increment and every increment after initial failure.
	41-45	NOPSHN	- Unloading option. It is to be taken equal to unity until additional options of unloading are added. For NOPSHN = 1, the affected ply or plies are unloaded in one step and loads transferred to the remaining plies.
Cards 8	BOUNDARIES OF PLYS OF THE LAMINATE (6F10.0)		
Col	1-10	H(1)	These are the distances of the boundaries of the plies from a reference line as defined in Figure 5.
	11-20	H(2)	
	21-30	H(3)	
	31-40	H(4)	
		⋮	
		H(LAMINA + 1)	
Cards 9	ORIENTATION OF PLYS (6F10.0)		
Col	1-10	TH(1)	Orientation angle in degrees of the first ply (Figure 4)
	11-20	TH(2)	Orientation angle in degrees of the second ply (Figure 4)
		⋮	
		TH(LAMINA)	Orientation angle in degrees of the last ply (Figure 4)
Cards 10	MATERIAL TYPES ASSOCIATED WITH PLYS (1415)		
Col	1-5	MAT(1)	Material number of the first ply
	6-10	MAT(2)	Material number of the second ply
		⋮	
		MAT(LAMINA)	Material number of the last ply

Cards 11	LOAD CONDITIONS (3F10.0)	
Col	1-10 A1(1)	Stress resultant $\Delta NX$ in x-direction (Figure 4) for the first load condition.
	11-20 A2(1)	Stress resultant $\Delta NY$ in y-direction (Figure 4) for the first load condition.
	21-30 A3(1)	Stress resultant $\Delta NXY$ in xy-direction (Figure 4) for the first load condition.

Note 3.1 Repeat for all the number of load conditions NN of the Card 7.

Note 3.2 The components of stress resultants are computed by estimating strengths (NX, NY, and NXY) of the laminate and dividing the same by the number of desired increments. Experience indicates that 10-20 increments are adequate.

Note 3.3  $\Delta NX$ ,  $\Delta NY$ ,  $\Delta NXY$  of Cards 11 represent the maximum size of the increments. In the program the increment size get reduced as the failure points based upon strains are approached.

Note 4. Prepare other sets of cards from Card 7 to Card 11 for other laminates defined by Card 6.

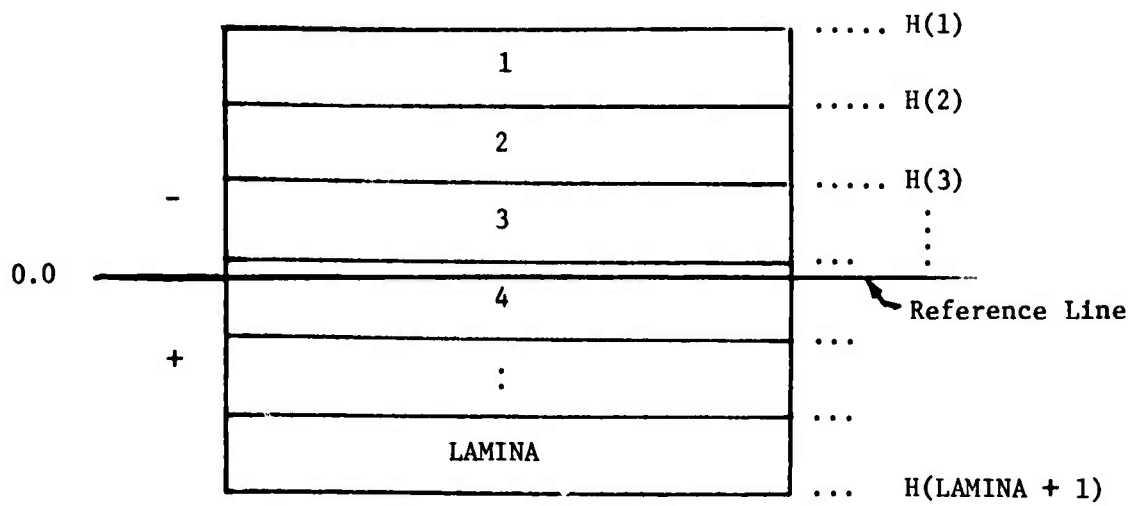


Figure 5. Distances of Boundaries of Plies of a Laminate from a Reference Line

## SECTION IV

### PROGRAM MODIFICATIONS AND SAMPLE PROBLEMS

#### 1. MODIFICATIONS

NOLAST is the experimental computer program. It is being made available to designated recipients in the interest of timely exchange of technical information. Therefore user's experience communicated to AFFDL/FBR would be valuable for improving the program and would be appreciated. In the meantime, it is likely that the program would be modified by the users to suit their requirements. To help them in making modifications, the following comments are pertinent:

- a. The program, in the present form, allows for five material systems (isotropic and anisotropic), thirty nodal points (including the fictitious one) of stress-strain curves, fifteen plies in a laminate, and ten combinations of loads for each of the laminates. These maxima can be modified by changing the dimensions of the program.
- b. The program incorporates the criterion represented by Equations 5 to 7. Any other criterion, with constraints if any, may be introduced by insertion of suitable Fortran Statements in the Subroutine OUTPUT (cards 118 to 250).
- c. Additional unloading options may be added to cards 373 and 374 by assigning a suitable number to NOPSHN on card 297 in the Subroutine OUTPUT.
- d. For additional changes reference may be made to AFFDL/FBR.

## 2. SAMPLE PROBLEMS

In the present form, NOLAST is an in-core program requiring less than 60K octal. It was used to generate stress-strain responses of the following laminates reported herein:

- a.  $(0/\underline{+45}/90)_8$  laminate with all the plies of one material and subjected to two combinations of loads.
- b.  $(0/90)_{48}$  laminate with all the plies of one material subjected to one load combination.
- c.  $(0/0/\underline{+45}/90)_8$  laminate with  $(0/\underline{+45}/90)$  plies of one material and  $0^\circ$  ply of the second material subjected to one load combination.

Generation of the responses of the laminates (a, b, and c) required compilation and execution times of 8.28 seconds and 4.13 seconds respectively, on CYBER 7400 computer.

The stress-strain data of both materials appears on pages 49 and 50. The relevant input information for the three laminates (a, b, and c) is printed on pages 51, 58, and 63 respectively.

The output information on each of the printed pages consists of the following:

- (i) Load Increment, Load Combination, Laminate No. and NOPSIN No.
- (ii) Average laminate elastic constants (EX, EY, UXY, GXY, ETA1 and ETA2) during the load increment.
- (iii) Components of the laminate strain increment.

(iv) Components of the laminate strain, stress resultant and stress.

(v) Components of biaxial lamina strains and stresses.

(vi) Components of equivalent lamina strains and corresponding stresses.

(vii) Total energies due only to longitudinal tension and compression, transverse tension and compression, and shear for each of the material systems. This information is printed only for the first load increment.

(viii) Energy ratios (longitudinal, transverse and shear), their sums for all plies and the sum of sums.

(ix) Moduli of elasticity of all plies at the end of the load increment.

(x) Information about failing plies and their nodes.

(xi) At the time of the failure of a ply or plies (e.g.

page 53, Load Increment 12, Load Combination 1, Laminate No. 1, NOPSIN No. 1) additional information consists of the moduli of elasticity of all the plies and stress resultants of the affected plies during unloading and iterative process. The unloading process was indicated by the total contribution (1.010665) of the fourth ply exceeding unity. The present program does not have a provision to refine the laminate stresses corresponding to the total contribution (1.010665) to those pertaining to the total contribution of unity. This can easily be done by interpolating the results of the current load increment and the previous one. These

remarks also apply to the final failure of the laminate.

(xii) Final failure of the laminate (e.g. page 55, Load Increment 18, Load Combination 1, Laminate No. 1, NOPSIN No. 1) occurs when the stress resultants of the failing plies cannot be imposed upon the intact plies without being reduced or without the stiffness matrix  $A$  becoming singular.

(xiii) Additional information about  $C_{ij}$  of the plies and  $A_{ij}$  of the laminate may be obtained by deleting the letter C in the beginning of the card numbers 245 and 247 of the Subroutine OUTPUT.

APPENDIX A

FORTRAN LISTING OF COMPUTER

PROGRAM (NOLAST)

PROGRAM NOLAST

```

1      PROGRAM NOLAST(INPUT,TAPES=INPUT,OUTPUT,TAPE6=OUTPUT)
COMMON/PROP/ NEPJT(5),EPJT(3,5),SIGGT(3,5),NEPJC(5),EPJC(3,5),
2      SIGGC(3,5),NEPJT(5),EP90T(3,5),SIG90T(3,5),
3      NEP90C(5),EP90C(3,5),SIG90C(3,5),NEP12(5),
4      EP12(3,5),SIG12(3,5),NPNUT(5),EPNUT(3,5),
5      PNUC(3,5),NPNUC(5),EPNUC(3,5),PNUC(3,5),
6      SUM1(5),SUM12(5),SUM21(5),SUM22(5),SUM3(5),SUM0,
COMMON/SPLN/ SP2(7,30,5),SP3(7,30,5),DELSY(7,30,5)
COMMON/CNST/ MATYPE,NULAM,LAMINA,NN,NTURN,NFAIL,NOFF,LCAD,
1      NTERM,EX,EY,UXY,GXY,VXY,WXY,SIGXX,SIGYY,SIGXY,
2      EPXX,EPYY,EPXY,DA,EDIFF,KL,KM,MLT,MLC,MTT,MTC,MSH,
3      NPRINT
COMMON/4AIN/ H(15),TH(15),MAT(15),S1(15),S2(15),S3(15),S4(15),
4      S5(15),S6(15),S7(15),S8(15),C(3,3,15),SIG(15,3),
5      SIGDR(15,3),DELL(15),DETT(15),DELT(15),E11(15),
6      E22(15),GG(15),UNN(15),SUMOLL(15),SUMOTT(15),
7      SUMDLT(15),ENER(15,3),EPN(15,3),DEPN(15,3),
8      STRESS(15,3),XX(15),XL(15),XT(15),XS(15),NLONG(15),
9      NTRAN(15),NSHEAR(15),STRSS(15,3),A(3,3),DELEP(3),
10     DLEP(3),A1(10),A2(10),A3(10),AA1(10),AA2(10),
11     AA3(10),NALTER(15),STRAIN(15),SUM1(15),SUM2(15),
12     SUMS(15),SIGDR1(15,3)
REAL M(15),N(15)
PRINT 100
100  FORMAT(1HT)
CALL INPUT(MATYPE)
READ(5,50) NUMLAM
50  FORMAT(14I5)
KM=1
1000 WRITE(6,60) KM
60  FORMAT(1H1,/,53X,13HLAMINATE NO. ,I2)
READ(5,50) LAMINA,NN,MLT,MLC,MTT,MTC,MSH,NPRINT,NOPSHN
KK=LAMINA+1
READ(5,22) (M(K),K=1,KK)
22  FORMAT(6F10.0)
READ(5,22) (TH(K),K=1,LAMINA)
READ(5,50) (MAT(K),K=1,LAMINA)
READ(5,23) (A1(K),A2(K),A3(K),K=1,NN)
23  FORMAT(3F10.0)

```

PROGRAM NOLAST

```

45      WRITE(6,312) KK,(K,H(K),K=1,KK)
312  FORMAT(15X,25HNO. OF BOUNDING SURFACES-,I5/
1      (15X,11HUISTANCE OF,I4,11H-BOUNDARY -,F10.4))
602  WRITE(6,502) (I,TH(I),MAT(I),I=1,LAMINA)
      FOKMAT(/,15X,5HLAMINA,4X,11HORIENTATION,4X,10HMATERIAL /
1      (17X,I2,7X,F8.3,8X,I2))
313  WRITE(6,313) (I,41(I),A2(I),A3(I),I=1,NN)
      FORMAT(/,15X,32HLOAD COMBINATION -----,I4/
1      15X,32HSTRESS RESULTANT INCREMENT NX-----,E17.8/
2      15X,32HSTRESS RESULTANT INCREMENT NY-----,E17.8/
3      15X,32HSTRESS RESULTANT INCREMENT NX-----,E17.8/)
50      DO 700 I=1,NN
55      AA1(I)=A1(I)
      AA2(I)=A2(I)
      AA3(I)=A3(I)
700  CONTINUE

21      DO 556 I=1,LAMINA
60      TH(I)=TH(I)*3.1415926536/180.
      M(I)=COS(TH(I))
      N(I)=SIN(TH(I))
      S1(I)=M(I)**4
65      S2(I)=M(I)**2*N(I)**2
      S3(I)=M(I)**3*N(I)
      S4(I)=N(I)**4
      S5(I)=M(I)*N(I)**3
      S6(I)=M(I)**2
      S7(I)=N(I)**2
70      S8(I)=M(I)*N(I)
556  CONTINUE
      KL=1
      META=0
      LOAD=0
      NPR=0
      NFAIL=0
      SIGXX=0.
      SIGYY=0.
75

```

PROGRAM NOLAST

```

80  SIGXY=0.
    EPXX=0.
    EPYY=0.
    EPXY=J.
    DO 330 I=1,LAMINA
    SUMOLL(I)=J.
    SUMOTT(I)=0.
    SUMOLT(I)=J.
    K=MAT(I)
    E11(I)=E1T(K)
    E22(I)=E2T(K)
    GG(I)=G12(K)
    UNW(I)=PMUT(1,K)
    NLONG(I)=0.
    NTRAN(I)=0
    NSHEAR(I)=0
    NALTER(I)=0
    DO 330 J=1,3
    OLEP(J)=0.
    ENER(I,J)=0.
    SIGORI(I,J)=0.
    EPN(I,J)=0.
    DEPN(I,J)=0.
    330 CONTINUE
    601 CONTINUE
    CALL ELCON
    NDD=0
    NFR0=J
    IF(DA.LE.0.) GO TO 30
    CALL ITER
    IF(DA.LE.0.) GO TO 30
    CALL OUTPUT(NOPSHN,NPR)
    IF(INTERM.GE.LAMINA) GO TO 30
    IF(EODIFF.LE.0.) GO TO 30
    IF(DA.LE.0.) GO TO 30
    IF(NTURN-1) 601,30,601
    30  KL=KL+1
    40  IF(KL-NH) 20,20,60
    40  KM=KM+1
    45  IF(KH-NUMLAM) 1000,1000,45
    END
105  110
115  115

```

SUBROUTINE INPUT

```

1      SUBROUTINE INPUT(MATYPE)
      COMMON/PROP/ NEPOT(5),EPOT(30,5),SIGOT(30,5),NEPJC(5),EPJC(30,5),
      SIGOC(50,5),NEP9OT(5),EP9OT(30,5),SIG9OT(30,5),
      NEP9OC(5),EP9OC(30,5),SIG9OC(30,5),NEP12(5),
      EP12(30,5),SIG12(30,5),NPNUT(5),EPNUT(30,5),
      PNUT(30,5),NPNUC(5),EPNUC(30,5),PNUC(30,5),
      SUM11(5),SUM12(5),SUM21(5),SUM22(5),SUM3(5),SUM4,
      E1T(5),E2T(5),G12(5),E1C(5),E2C(5),MED(12)
      COMMON/SPLN/ SP2(7,30,5),SP3(7,30,5),DELSY(7,30,5)

10     DIMENSION X(3J),Y(3J)
      READ(5,10) MED
15     FORMAT(12A6)
      READ(5,19) MATYPE
19     FORMAT(7I5)
      DO 1000 I=1,MATYPE
      READ(5,19) NEPJT(I),NEPJC(I),NEP9OT(I),NEP9JC(I),NEP12(I),
      NPNUT(I),NPNUC(I)
1      J1=NEPJT(I)
      J2=NEPJC(I)
      J3=NEP9OT(I)
      J4=NEP9OC(I)
      J5=NEP12(I)
      J6=NPNUT(I)
      J7=NPNUC(I)
      READ(5,20) (EPOT(J,I),SIGOT(J,I),J=1,J1)
      READ(5,21) (EP9OC(J,I),SIG9OC(J,I),J=1,J2)
      READ(5,23) (EP9OT(J,I),SIG9OT(J,I),J=1,J3)
      READ(5,23) (EP9OC(J,I),SIG9OC(J,I),J=1,J4)
      READ(5,20) (EP12(J,I),SIG12(J,I),J=1,J5)
      READ(5,20) (EPNUT(J,I),PNUT(J,I),J=1,J6)
      READ(5,20) (EPNUC(J,I),PNUC(J,I),J=1,J7)
      READ(5,2 ) E1T(I),E1C(I),E2T(I),E2C(I),G12(I)
20     FORMAT(6F10.4)
      L=MAX(J1,J2)
      L1=MAX(J3,J4,J5)
      L2=MAX(J6,J7)
      WRITE(6,3 )
35     L=MAX(L,L1,L2)
      300 FORMAT(1H1)
40

```

SUBROUTINE INPUT

```

45      WRITE(6,11) HED
11      FORMAT( 12A6)
        WRITE(6,315) I
305     FORMAT( /53X,8HMATERIAL,I2)
        WRITE(6,311) (EPJT(J,I),SIGJT(J,I),EPUC(J,I),SIGUC(J,I),J=1,L)
310     FORMAT( /15X,6H STRAIN DEG.(TEN) STRESS / DEG.(TEN) STRAIN
1DEG.(COM) STRESS / DEG.(COM) / (15X,4E20.8))
        WRITE(6,315) (EP90T(J,I),SIG9T(J,I),EP9C(J,I),SIG9C(J,I),
1      EP12(J,I),SIG12(J,I),J=1,L)
315     FORMAT( / 5X,6H STRAIN 90DEG.(TEN) STRESS 90DEG.(TEN) STRAIN 9
1DEG.(COM) STRESS 90DEG.(COM),6X,12HSHEAR STRAIN,9X,
2      12HSHEAR STRESS / (5X,6E2 .8))
        WRITE(6,325) (EPNUT(J,I),PNUC(J,I),EPNUC(J,I),PNUC(J,I),J=1,L2)
325     FORMAT( /15X,8H STRAIN DEG.(TEN) TEN. POISSONS RATIO STRAIN
1DEG.(COM) COM. POISSONS RATIO / (15X,4E20.8))
        WRITE(6,331) E1T(I),E1C(I),E2T(I),E2C(I),G12(I)
331     FORMAT(15X,3.HINITIAL MODULI OF ELASTICITY /
1      15X,4HE1T=,E15.8,6H E1C=,E15.8,6H E2T=,E15.8,
2      6H E2C=,E15.8,6H G12=,E15.8)
        DO 801 J=1,J1
        X(J)=EPJT(J,I)
        Y(J)=SIGJT(J,I)
801     CALL SPLINI(J1,X,Y,1,XY,I)
        SUM11(I)=XY
        DO 802 J=1,J2
        X(J)=EPUC(J,I)
        Y(J)=SIGUC(J,I)
802     CALL SPLINI(J2,X,Y,2,XY,I)
        SUM12(I)=XY
        DO 803 J=1,J3
        X(J)=EP90T(J,I)
        Y(J)=SIG90T(J,I)
803     CALL SPLINI(J3,X,Y,3,XY,I)
        SUM22(I)=XY
        DO 804 J=1,J4
        X(J)=EP90C(J,I)
        Y(J)=SIG90C(J,I)
804     CALL SPLINI(J4,X,Y,4,XY,I)
        SUM21(I)=XY

```

SUBROUTINE INPUT

```
80      DO 805 J=1,J5
      C
      X(J)=EP12(J,I)
      Y(J)=SI 12(J,I)
      805 CALL SPLIN1(J5,X,Y,5,XY,I)
      SUM3(I)=XY
      DO 806 J=1,J6
      X(J)=EPNUT(J,I)
      Y(J)=PNUT(J,I)
      806 CALL SPLIN1(J6,X,Y,6,XY,I)
      DO 807 J=1,J7
      X(J)=EPNUC(J,I)
      Y(J)=PNUT(J,I)
      807 CALL SPLIN1(J7,X,Y,7,XY,I)
      1000 CONTINUE
      RETURN
      95  END
```

SUBROUTINE SPLIN1

```

1      C      SUBROUTINE SPLIN1(N,X,Y,M,PROXIN,K)
COMMON/SPLN/ SPL(7,3J,5),SP3(7,3J,5),DELSY(7,3J,5)
5      C      DIMENSION 4 X(N),Y(N),H(3J),DELY(3J),H2(3J),B(3J),DELSOY(3J),
1      EPSLN=0.1
2 N1=N-1
3 DO 51 I=1,N1
4 H(I)=X(I+1)-X(I)
51 DELY(I)=(Y(I+1)-Y(I))/H(I)
4 DO 52 I=2,N1
H2(I)=H(I-1)+H(I)
8(I)=.5*H(I-1)/H2(I)
DELSOY(I)=(DELY(I)-DELY(I-1))/H2(I)
S2(I)=2.*DELSOY(I)
52 C(I)=3.*DELSOY(I)
S2(I)=0.
S2(N)=0.
OMEGA=1.0717958
5 ETA=0.
6 DO 10 I=2,N1
7 W=(C(I)-3(I))*S2(I-1)-(.5-B(I))*S2(I+1)-S2(I)*OMEGA
8 IF(ABS(W)-ETA) 10,10,9
9 ETA=ABS(W)
10 S2(I)=S2(I)+W
13 IF(ETA=EPSLN) 14,5,5
14 DO 53 I=1,N1
53 S3(I)=(S2(I+1)-S2(I))/H(I)
DO 1J0 I=1,N
SP2(M,I,K)=S2(I)
SP3(M,I,K)=S3(I)
DELSY(M,I,K)=DELY(I)
100 CONTINUE
20 PROXIN=0.
35 N1=N1-1
DO 62 I=1,N1
62 PROXIN=PROXIN+.5*H(I)*(Y(I)+Y(I+1))-H(I)**3*(S2(I)+S2(I+1))/24.
RETURN
END
40

```

SUBROUTINE ELCON

```

1      C
      SUBROUTINE ELCON
COMMON/PROP/ NEPJT(5), EPJT(30,5), SIGOT(3,5), NEPJC(5), EPQC(30,5),
SIGUC(30,5), NEP9T(5), EP9T(3,5), SIG9T(30,5), SIG9UT(30,5),
NEP9OC(5), EP9JC(30,5), SIG9JC(30,5), NEP12(5),
EP12(30,5), SIG12(30,5), NPNUT(5), EPNUT(30,5),
PNUT(30,5), NPNUC(5), EPNUC(30,5), PNUC(30,5),
SUM11(5), SUM12(5), SUM21(5), SUM22(5), SUM3(5), SUM4,
E1T(5), E2T(5), G12(5), E1C(5), E2C(5), HED(12)
COMMON/CNST/
      MATYPE,NULAM,LAMINA,NN,NTURN,NFAIL,NOFF,LOAD,
      NTERM,EX,EY,UXY,GXY,VXY,WXY,SIGXX,SIGYY,SIGXY,
      EPXX,EPYY,EPXY,DA,EDIFF,KL,KM,MLT,MLC,MTT,MTC,MSH,
      NPRINT
COMMON/MAIN/
      H(16), TH(15), MAT(15), S1(15), S2(15), S3(15), S4(15),
      S5(15), S6(15), S7(15), S8(15), C(3,3,15), SIG(15,3),
      SIGDR(15,3), DELL(15), DETT(15), DELT(15), E11(15),
      E22(15), GG(15), UNN(15), SUMOLL(15), SUMDTT(15),
      SUMDLT(15), ENER(15,3), EPN(15,3), DEPI(15,3),
      STRESS(15,3), XX(15), XL(15), XT(15), XS(15), NLONG(15),
      NTRAN(15), NSHEAR(15), STRSS(15,3), A(3,3), DELEP(3),
      ULEP(3), A1(10), A2(10), A3(10), AA1(10), AA2(10),
      AA3(10), NALTER(15), STRAIN(15), SUM1(15), SUM2(15),
      SUMS(15), SIGDR1(15,3)
      DIMENSION X1(15), X2(15), X3(15), XX1(15), XX2(15), XX3(15)
      IF(NOFF.EQ.1) WRITE(6,652) (E11(I), E22(I), GG(I), UNN(I), I=1, LAMINA)
      /
      FORMAT(30H ELCON CALLED FROM *UNLOAD* /
      1 33X, 21HMODULI OF ELASTICITY / (10X, 4E20.8)
      IF(NOFF.EQ.1) WRITE(6,651) A1(KL), A2(KL), A3(KL)
      / (11X, 3E20.8)
      FORMAT(30X, 10HSTRESS RESULTANTS
      NTURN=C
      NLIMIT=0
      KK=LAMINA+1
      801 DO 27 L=1, LAMINA
      IF(E11(L).EQ.J...OR.E22(L).EQ.0.) GO TO 33
      UN=UNN(L)*E22(L)/E11(L)
      GO TO 32
      33 UN=0.
      32 UNU=1./ (1.-UN*UNN(L))
      C11=E11(L)*UNU

```

SUBROUTINE ELCON

```

45      C12=E22(L)*UNN(L)*UNU
        C16=C.
        C22=E22(L)*UNU
        C26=G.
        C66=G(L)
        C21=C12
        C61=C16
        C62=C26
50      C(1,1,L)=S1(L)*C11+2.*S2(L)*C12+4.*S3(L)*C16+S4(L)*C22+4.*S5(L)
        *C26+4.*S2(L)*C66
        1 C(1,2,L)=S2(L)*C11+(S1(L)+S4(L))*C12+2.*S5(L)-S3(L)*C16+S2(L)
        *C22+2.*S3(L)-S5(L)*C26-4.*S2(L)*C66
        C(2,1,L)=C(1,2,L)
55      C(1,3,L)=-S3(L)*C11+(S3(L)-S5(L))*C12+(S1(L)-3.*S2(L))*C16+S5(L)
        *C22+(3.*S2(L)-S4(L))*C26+2.*S3(L)-S5(L)*C66
        1 C(3,1,L)=C(1,3,L)
        C(2,2,L)=S4(L)*C11+2.*S2(L)*C12-4.*S5(L)*C16+S1(L)*C22-
        4.*S3(L)*C26+4.*S2(L)*C66
        1 C(2,3,L)=-S5(L)*C11+(S5(L)-S3(L))*C12+(3.*S2(L)-S4(L))*C16+
        S3(L)*C22+(S1(L)-3.*S2(L))*C26+(S5(L)-S3(L))*2.*C66
60      C(3,2,L)=C(2,3,L)
        C(3,3,L)=S2(L)*C11-2.*S2(L)*C12+2.*S5(L)-S3(L)*C16
        +S2(L)*C22+2.*S3(L)-S5(L)*C26+(S6(L)-S7(L))*2.*C66
        1 27 CONTINUE
65      DO 35 I=1,3
        DO 36 J=1,3
        A(I,J)=0.
        DO 37 K=1,LAMINA
        KO=K+1
        A(I,J)=A(I,J)+C(I,J,K)*(H(KO)-H(K))
37 CONTINUE
36 CONTINUE
35 CONTINUE
70      DA =A(1,1)*A(2,2)*A(3,3)-A(2,3)*A(3,2)+A(1,2)*A(2,3)*A(3,1)-
        A(2,1)*A(3,3)+A(1,3)*A(2,1)*A(3,2)-A(2,2)*A(3,1)
75      1 IF(DA) 30,30,31
        31 CONTINUE
        AL11=(A(2,2)*A(3,3)-A(2,3)*A(3,2))/DA
        AL12=(A(1,3)*A(2,3)-A(1,2)*A(3,3))/DA
        AL13=(A(1,2)*A(2,3)-A(1,3)*A(2,2))/DA
80

```

SUBROUTINE ELCON

```

AL21=AL12
AL22=(A(1,1)*A(3,3)-A(1,3)*A(2,3))/DA
AL23=(A(1,2)*A(1,3)-A(1,1)*A(2,3))/DA
AL31=AL13
AL32=AL23
AL33=(A(1,1)*A(2,2)-A(1,2)*A(2,1))/DA
HK=H(HK)-H(1)
EX=1./(AL11*HK)
EY=1./(AL22*HK)
GXY=1./(AL33*HK)
UXY=-AL12*EX*HK
VXY=AL13*EX*HK
WXY=AL23*EY*HK
IF(NOFF.EQ.0) GO TO 100
IF(NFAIL.EQ.0) GO TO 100
DO 101 I=1,NN
A1(I)=A11(I)
A2(I)=A12(I)
A3(I)=A13(I)
101 CONTINUE
100 NFAIL=0
100 CONTINUE
DELEP(1)=A1(KL)*AL11+A2(KL)*AL12+A3(KL)*AL13
DELEP(2)=A1(KL)*AL21+A2(KL)*AL22+A3(KL)*AL23
DELEP(3)=A1(KL)*AL31+A2(KL)*AL32+A3(KL)*AL33
DO 110 I=1,LAMINA
SIG(I,1)=C(1,1,I)*DELEP(1)+C(1,2,I)*DELEP(2)+C(1,3,I)*DELEP(3)
SIG(I,2)=C(2,1,I)*DELEP(1)+C(2,2,I)*DELEP(2)+C(2,3,I)*DELEP(3)
SIG(I,3)=C(3,1,I)*DELEP(1)+C(3,2,I)*DELEP(2)+C(3,3,I)*DELEP(3)
SIGOR(I,1)=SIG(I,1)*S6(I)+SIG(I,2)*S7(I)-2.*SIG(I,3)*S8(I)
SIGOR(I,2)=SIG(I,1)*S7(I)+SIG(I,2)*S6(I)+2.*SIG(I,3)*S8(I)
SIGOR(I,3)=SIG(I,1)*S6(I)-SIG(I,2)*S6(I)+SIG(I,3)*S8(I)
DELL(I)=DELEP(1)*S6(I)+DELEP(2)*S7(I)-DELEP(3)*S3(I)
DELT(I)=DELEP(1)*S7(I)+DELEP(2)*S6(I)+DELEP(3)*S3(I)
DELT(I)=DELEP(1)*2.*S6(I)-DELEP(2)*2.*S3(I)+DELEP(3)*S6(I)-S7(I)
110 CONTINUE
ZZZ=C.
DO 110 I=1,3
ZZZ=ZZZ+DELEP(I)**2
ZZZ=SQRT(ZZZ)
120

```

SUBROUTINE ELGON

```

125 IF(ZZZ.GE.1.) DA=0.
    IF(ZZZ.GE.1.) GO TO 30
    DO 150 I=1,LAMINA
    K=MAT(I)
    K1=NEPOT(K)-1
    K2=NEP0C(K)-1
    K3=NEP90T(K)-1
    K4=NEP90C(K)-1
    K5=NEP12(K)-1
    T1=EP0T(K1,K)
    T1C=EP0C(K2,K)
    T2=EP90T(K3,K)
    T2C=EP90C(K4,K)
    T12=EP12(K5,K)
    XX1(I)=SUMDL(I)+DELL(I)
    XX2(I)=SUMDT(I)+DETT(I)
    XX3(I)=SUMOLT(I)+DELT(I)
    TT1=ABS(XX1(I))
    TT2=ABS(XX2(I))
    TT3=ABS(XX3(I))
    Y1=SIGDR(I,1)+SIGDR1(I,1)
    Y2=SIGDR(I,2)+SIGDR1(I,2)
    IF(E11(I).LE.J.) GO TO 150
    IF(ABS(SIGDR(I,1)).LE.0.1) B1=1.
    IF(ABS(SIGDR(I,1)).LE.0.1) GO TO 92
    B=SIGDR(I,2)/SIGDR(I,1)
    B1=(1.-UNN(I)*B)
    92 DEPN(I,1)=DELL(I)/B1
    X1(I)=EPN(I,1)+DEPN(I,1)
    T1=ABS(X1(I))
    IF(Y1) 70,71,71
    70 IF(T1.GE.T1C) GO TO 500
    IF(TT1.GE.T1C) GO TO 500
    GO TO 80
    71 IF(T1.GE.T1T) GO TO 500
    IF(TT1.GE.T1T) GO TO 500
    80 IF(E22(I).LE.J.) GO TO 150
    IF(ABS(SIGDR(I,1)).LE.0.1) B2=1.
    IF(ABS(SIGDR(I,1)).LE.0.1) GO TO 93
    IF(ABS(SIGDR(I,2)).LE.0.1) B2=1.
130
135
140
145
150
155
160

```

SUBROUTINE ELCON

```

165 IF (ABS(SIGDR(I,2)).LE.0.1) GO TO 93
    B2=(1.-UNN(I)*E22(I))/(E11(I)*B1)
    93 DEPN(I,2)=DETT(I)/B2
    X2(I)=EPN(I,2)+DEPN(I,2)
    T2=ABS(X2(I))
    IF(Y2) 72,73,73
    72 IF(T2.GE.T2C) GO TO 500
    IF(TT2.GE.T2C) GO TO 500
    GO TO 81
    170 IF(T2.GE.T2T) GO TO 500
    IF(TT2.GE.T2T) GO TO 500
    81 IF(GG(I).LE.0.) GO TO 150
    DEPN(I,3)=DELT(I)
    X3(I)=EPN(I,3)+DEPN(I,3)
    T3=ABS(X3(I))
    IF(T3.GE.T12) GO TO 500
    IF(TT3.GE.T12) GO TO 500
    150 CONTINUE
    RETURN
    500 CONTINUE
    A1(KL)=0.5*A1(KL)
    A2(KL)=J.5*A2(KL)
    A3(KL)=0.5*A3(KL)
    NLIMIT=NLIMIT+1
    IF(NLIMIT-10) +00,400,40
    40 NTURN=1
    400 WRITE(6,104)
    104 FORMAT(10X,10HREDUCE
    IF(NOFF.EQ.1.AND.NLIMIT.GT.0) DA=0.
    IF(NOFF.EQ.1.AND.NLIMIT.GT.0) WRITE(6,200)
    200 FORMAT(//5X,+8H *** UNLOADING LEADS TO FAILURE OF LAMINATE ***
    1 10X,20H PROGRAM TERMINATED
    )
    RETURN
    30 WRITE(6,620) EX,EY,UXY,GXY,VXY,WXY
    620 FORMAT(//10X,3HEX=,E15.8,3X,3HEY=,E15.8,3X,+HUXY=,E15.8,3X,4HGXY=
    1 ,E15.8,//10X,5HETA1=,E15.8,3X,5HETA2=,E15.8,//
    2 10X, 25H MATRIX *A* IS SINGULAR
    )
    RETURN
    END

```

## SUBROUTINE ITER

```

1          C
          SUBROUTINE ITER
          COMMON/PROF/ NEPJT(5), EPJT(30,5), SIGJT(30,5), NEPJC(5), EPJC(30,5),
2          SIGOC(30,5), NEPOT(5), EPOT(30,5), SIGOT(30,5), SIG9UT(30,5),
3          NEPJC(5), EPJC(30,5), SIG9JC(30,5), NEP12(5),
4          EP12(30,5), SIG12(30,5), NPNT(5), EPNT(30,5),
5          PNUT(30,5), NPNUC(5), EPNUC(30,5), PNUC(30,5),
6          SUM1(5), SUM12(5), SUM21(5), SUM22(5), SUM3(5), SUM4,
7          E1T(5), E2T(5), G12(5), E1C(5), E2C(5), HED(12)
          COMMON/SPLN/ SP2(7,30,5), SP3(7,30,5), DELSY(7,30,5)
          COMMON/CNST/ MATYPE,NULAM,LAMINA,NN,NTURN,NFAIL,NOFF,LOAD,
10          NTERM,EX,EY,UXY,GXY,VXY,WXY,SIGXX,SIGYY,SIGXY,
11          EPXX,EPYY,EPXY,DA,EDIFF,KL,KM,MLT,MLC,MTT,HTC,MSH,
12          NPRINT
          COMMON/MAIN/ H(16),TH(15),MAT(15),S1(15),S2(15),S3(15),S4(15),
13          S5(15),S6(15),S7(15),S8(15),C(3,3,15),SIG(15,3),
14          SIGOR(15,3),DELL(15),DETT(15),DELT(15),E11(15),
15          E22(15),GG(15),UNN(15),SUMDLL(15),SUMOTT(15),
16          SUMDLT(15),ENER(15,3),EPN(15,3),DEPN(15,3),
17          STRESS(15,3),XX(15),XL(15),XT(15),XS(15),NLONG(15),
18          NTRAN(15),NSHEAR(15),STRSS(15,3),A(3,3),DELEP(3),
19          OLEP(3),A1(10),A2(10),A3(10),AA1(10),AA2(10),
20          AA3(10),NALTER(15),STRAIN(15),SUM1(15),SUM2(15),
21          SUMS(15),SIGDR1(15,3)
          C
          DIMENSION X1(2),X2(2),X3(2),XX1(2),XX2(2),XX3(2),
25          EEL(15),EE2(15),GG12(15),UNU(15),
26          V1(15),Y2(15),Y3(15),T(2),ST(2),SST(2),PT(2),
27          PST(2),PSST(2),X(30),Y(30)
          C
          ZD1=0.
          DO 100 I=1,3
          ZB=(1000.*DELEP(I))
          ZD1=ZD1+ZB*ZB
          C
          MM=0
          ZD1=SQRT(ZD1)
          DO 130 I=1,LAMINA
          IF(NOFF.EQ.1.AND.MM.GE.6) GO TO 125
          IF(E11(I).LE.0.) GO TO 130
          Y1(I)=SIGOR(I,1)+SIGDR1(I,1)

```

## SUBROUTINE ITER

```
45 Y2(I)=SIGDR(I,2)+SIGDR1(I,2)
   Y3(I)=SIGDR(I,3)+SIGDR1(I,3)
   IF (ABS(SIGDR(I,1)).LE.0.1) B1=1.
   IF (ABS(SIGDR(I,1)).LE.0.1) GO TO 92
   B=SIGDR(I,2)/SIGDR(I,1)
   B1=(1.-UNN(I))*B)
92 DEPN(I,1)=DELL(I)/B1
   XX1(1)=EPN(I,1)+DEPN(I,1)*J.5
   X1(1)=EPN(I,1)+DEPN(I,1)
   T(1)=ABS(XX1(1))
   T(2)=ABS(X1(1))
   K=MAT(I)
   IF(Y1(I)) 70,200,71
70 KP=NEP0C(K)
   DO 201 J=1,KP
   X(J)=EP0C(J,K)
201 Y(J)=SIG0C(J,K)
   SGN=-1.
   CALL SPLIN2(KP,X,Y,2,T,ST,SST,2,ZY,1,K)
   IF(E22(I).EQ.0.) GO TO 200
   KP=NPNUC(K)
   DO 202 J=1,KP
   X(J)=EPNUC(J,K)
202 Y(J)=PNUC(J,K)
   CALL SPLIN2(KP,X,Y,2,T,PST,PSST,7,ZY,1,K)
   GO TO 73
71 KP=NEP0T(K)
   DO 203 J=1,KP
   X(J)=EP0T(J,K)
203 Y(J)=SIG0T(J,K)
   SGN=1.
   CALL SPLIN2(KP,X,Y,2,T,ST,SST,1,ZY,1,K)
   IF(E22(I).EQ.0.) GO TO 200
   KP=NPNUC(K)
   DO 204 J=1,KP
   X(J)=EPNUT(J,K)
204 Y(J)=PNUT(J,K)
   CALL SPLIN2(KP,X,Y,2,T,PST,PSST,6,ZY,1,K)
73 E11(I)=SST(1)
   STRESS(I,1)=ST(2)*SGN
80
```

## SUBROUTINE ITER

```

85      IF (ABS (STRESS (I, 1)), LE, 0.1) STRESS (I, 1) = 0.
      EE1 (I) = SST (2)
      IF (E22 (I), LE, 0.) GO TO 200
      UNN (I) = PST (2)
      UNN (I) = PST (1)
      200 CONTINUE
      IF (E22 (I), LE, 0.) GO TO 131
      IF (ABS (SIGDR (I, 1)), LE, 0.1) R2 = 1.
      IF (ABS (SIGDR (I, 1)), LE, 0.1) GO TO 93
      IF (ABS (SIGDR (I, 2)), LE, 0.1) R2 = 1.
      IF (ABS (SIGDR (I, 2)), LE, 0.1) GO TO 93
      B2 = (1. - UNN (I) * E22 (I)) / (E11 (I) * B)
      93 DEPN (I, 2) = DETT (I) / B2
      XX2 (1) = EPN (I, 2) + DEPN (I, 2) * 0.5
      X2 (1) = EPN (I, 2) + DEPN (I, 2)
      T (1) = ABS (XX2 (1))
      T (2) = ABS (X2 (1))
      IF (Y2 (I)) 75, 131, 76
      75 KP = NEP90C (K)
      00 205 J = 1, KP
      X (J) = EP90C (J, K)
      205 Y (J) = SIG90C (J, K)
      SGN = -1.
      CALL SPLIN2 (KP, X, Y, 2, T, ST, SST, 4, ZY, 1, K)
      GO TO 77
      76 KP = NEP90T (K)
      00 206 J = 1, KP
      X (J) = EP90T (J, K)
      206 Y (J) = SIG90T (J, K)
      SGN = 1.
      CALL SPLIN2 (KP, X, Y, 2, T, ST, SST, 3, ZY, 1, K)
      77 E22 (I) = SST (1)
      STRESS (I, 2) = ST (2) * SGN
      IF (ABS (STRESS (I, 2)), LE, 0.1) STRESS (I, 2) = 0.
      EE2 (I) = SST (2)
      131 IF (GG (I), LE, 0.) GO TO 130
      DEPN (I, 3) = DELT (I)
      XX3 (1) = EPN (I, 3) + DEPN (I, 3) * 0.5
      X3 (1) = EPN (I, 3) + DEPN (I, 3)
      T (1) = ABS (XX3 (1))
      120

```

SUBROUTINE ITER

```

125 T(2)=ABS(X3(1))
    IF(Y3(I).EQ.0.) GO TO 130
    KP=NEP12(K)
    DO 267 J=1,KP
    X(J)=EP12(J,K)
267 Y(J)=SIG12(J,K)
    CALL SPLIN2(KP,X,Y,2,I,SST,5,ZY,1,K)
    STRESS(I,3)=ST(2)*Y3(I)/ABS(Y3(I))
    IF(ABS(STRESS(I,3)).LE.0.1) STPESS(I,3)=..
130 GG(I)=SST(I)
    GG12(I)=SST(2)
130 CONTINUE
    IM=MM+1
    CALL ELCON
    IF(OA.LE.0.) RETURN
    ZD2=C.
    DO 85 I=1,3
    Z0=(1/J)*DELEP(I)
    ZD2=ZD2+ZB*ZB
85 CONTINUE
    ZD2=SQRT(ZD2)
    OCHEK=A3S(ZD1-ZD2)
    RATIO=OCHEK/ZD1
    ZD1=ZD2
    IF(RATIO.LE.0.001.OR.MM.GE.10) GO TO 125
    GO TO 132
125 DO 150 I=1,LAMINA
    IF(E11(I).LE.0.) GO TO 150
    IF(Y1(I).EQ.0.) GO TO 150
    UNN(I)=UNU(I)
    E11(I)=E1(I)
    IF(E22(I).EQ.0.) AND.(NOFF.EQ.1) UNN(I)=0.
    IF(E22(I).LE.0.) GO TO 150
    IF(Y2(I).EQ.0.) GO TO 150
    E22(I)=E2(I)
    IF(Y3(I).EQ.0.) GO TO 150
    GG(I)=GG12(I)
150 CONTINUE
    RETURN
    END
160

```

SUBROUTINE SPLIN2

```

1      C
      SUBROUTINE SPLIN2(N,X,Y,I,T,SS,SS1,L,PROXIN,NI,K)
      COMMON/SPLN/ SP2(7,3),5,SP3(7,3),5,DELSY(7,3),5)
      DIMENSION: X(N),Y(N),T(4),SS(M),SS1(4),SS2(3),
5      PROXIN=J,
      15 00 61 J=1,M
      16 I=1
      54 IF(T(J)-X(I)) 58,17,55
      55 IF(T(J)-X(N)) 57,59,58
      56 IF(T(J)-X(I)) 63,17,57
      57 I=I+1
      GO TO 55
      58 WRITE(6,*) T(J),NI,X(N)
      44 FORMAT(15X,2.4**ARGUMENT OUT OF RANGE,F15.8,2X,11HCALLED FROM,I,
1      ,74 X(N)=,F15.8)
      GO TO 61
      59 I=N
      60 I=I-1
      17 HT1=T(J)-X(I)
      HT2=T(J)-X(I+1)
      PROO=HT1*HT2
      SS2(J)=SP2(L,I,K)+HT1*SP3(L,I,K)
      DELSOS=(SP2(L,I,K)+SP2(L,I+1,K)+SS2(J))/6.
      SS(J)=Y(I)+HT1*DELSY(L,I,K)+PROO*DELSGS
      SS1(J)=DELSY(L,I,K)+(HT1+HT2)*DELSQS+PROO*SP3(L,I,K)/6.
      61 CONTINUE
      IF(M.GT.1) RETURN
      I=1
      10 IF(T(M)-X(I)) 30,80,d1
      81 HT1=X(I+1)-X(I)
      YY=Y(I+1)+Y(I)
      YZ=SP2(L,I,K)+SP2(L,I+1,K)
      PROXIN=PROXIN+C.5*HT1*YY-HT1**3*YZ/24.
      I=I+1
      GO TO 10
      80 HT1=X(I)-T(4)
      YY=Y(I)+SS(M)
      YZ=SP2(L,I,K)+SS2(M)
      PROXIN=PROXIN-0.5*HT1*YY+HT1**3*YZ/24.
      RETURN
      END

```

SUBROUTINE OUTPUT

```

1      C      SUBROUTINE OUTPUT(NOPSHN,NPR)
COMMON/PROP/ NEPT(5),EPJT(30,5),SIGGT(30,5),NEPJC(5),EPOC(30,5),
SIGOC(30,5),NEP9GT(5),EP9GT(30,5),SIG9GT(30,5),SIG9JT(30,5),
NEP9JC(5),EP9JC(30,5),SIG9JC(30,5),NEP12(5),
EP12(30,5),SIG12(30,5),NPNU(5),EPNU(30,5),
PNUT(30,5),NPNUC(5),EPNUC(30,5),PNUC(30,5),
SUM11(5),SUM12(5),SUM21(5),SUM22(5),SUM3(5),SUM4,
E11(5),E2T(5),G12(5),E1C(5),E2C(5),HED(12)
COMMON/SPLN/ SP2(7,30,5),SP3(7,30,5),DELSY(7,30,5)
COMMON/CNST/ MATYPE,NULAM,LAMINA,NN,NTURN,NFAIL,NOFF,LOAD,
NTERM,EX,EY,UXY,GXY,WXY,SIGXX,SIGYY,SIGXY,
EPXX,EPYY,EPXY,DA,EDIFF,KL,KM,MLT,MLC,MTT,MTC,MSH,
NPRINT
15     C      COMMON/MAIN/ H(16),TH(15),MAT(15),S1(15),S2(15),S3(15),S4(15),
S5(15),S6(15),S7(15),S8(15),S9(15),C(3,3,15),SIG(15,3),
SIGDR(15,3),DELL(15),DETT(15),DELT(15),E11(15),
E22(15),GG(15),UNN(15),SUMULL(15),SUMDIT(15),
SUMDLT(15),ENER(15,3),EPN(15,3),DEPN(15,3),
STRESS(15,3),XX(15),XL(15),XT(15),XS(15),NLONG(15),
NTRAN(15),NSHEAR(15),STRSS(15,3),A(3,3),DELEP(3),
OLEP(3),A1(10),A2(10),A3(10),AA1(10),AA2(10),
AA3(10),NALTER(15),STRAIN(15),SUM1(15),SUM2(15),
SUMS(15),SIGDR1(15,3)
20     C      DIMENSION NSIGN1(3),NSIGN2(3),X(30),Y(30),T(2),ST(2),SST(2)
LOAD=LOAD+1
DO 110 I=1,LAMINA
K=MAT(I)
SIGDR1(I,1)=SIGDR(I,1)+SIGDR1(I,1)
SIGDR1(I,2)=SIGDR(I,2)+SIGDR1(I,2)
SIGDR1(I,3)=SIGDR(I,3)+SIGDR1(I,3)
IF(ABS(SIGDR1(I,1)).LE.C.1) SIGDR1(I,1)=J.
IF(ABS(SIGDR1(I,2)).LE.C.1) SIGDR1(I,2)=J.
IF(ABS(SIGDR1(I,3)).LE.C.1) SIGDR1(I,3)=0.
SUMDLL(I)=SUMDLL(I)+DELL(I)
SUMDIT(I)=SUMDIT(I)+DETT(I)
SUMDLT(I)=SUMDLT(I)+DELT(I)
IF(E11(I).GT.3.) STRSS(I,1)=SIGDR1(I,1)
IF(E22(I).GT.3.) STRSS(I,2)=SIGDR1(I,2)
30     C
35     C
40     C

```

SUBROUTINE OUTPUT

```

45      IF(GG(I).GT.0.) STRSS(I,J)=SIGDR1(I,3)
      IF(E11(I).LE.J.) GO TO 110
      T(1)=ABS(SUMD1(I))
      IF(SIGDR1(I,1)) 45,200,46
      45      KP=NEP9JC(K)
           00 701 J=1,KP
           X(J)=EP9JC(J,K)
           Y(J)=SIG9JC(J,K)
           M1=MLC
50      CALL SPLIN2(KP,X,Y,1,T,ST,SST,2,ZY,2,K)
           SUM1(I)=SUM12(K)
           GO TO 73
           46      KP=NEP0T(K)
           00 702 J=1,KP
           X(J)=EP0T(J,K)
           Y(J)=SIG0T(J,K)
           M1=MLT
70      CALL SPLIN2(KP,X,Y,1,T,ST,SST,1,ZY,2,K)
           SUM1(I)=SUM11(K)
           ENER(I,1)=ZY
           GO TO 2J1
           73      SUM1(I)=SUM11(K)
           IF(E22(I).EQ.J.) DEPN(I,2)=DETT(I)
           IF(E22(I).EQ.J.) DEPN(I,1)=DELL(I)
           IF(E22(I).LE.J.) GO TO 111
           T(1)=ABS(SUMDT(I))
           IF(SIGDR1(I,2)) 75,112,76
           75      KP=NEP9JC(K)
           00 703 J=1,KP
           X(J)=EP9JC(J,K)
           Y(J)=SIG9JC(J,K)
           M2=MLC
70      CALL SPLIN2(KP,X,Y,1,T,ST,SST,4,ZY,2,K)
           SUM2(I)=SUM21(K)
           GO TO 77
           76      KP=NEP9JT(K)
           00 704 J=1,KP
           X(J)=EP9JT(J,K)
           Y(J)=SIG9JT(J,K)
           M2=MTT
80

```

SUBROUTINE OUTPUT

```

85      CALL SPLIN2(KP,X,Y,1,T,ST,SST,3,ZY,2,K)
        SUM2(I)=SUM22(K)
        77 ENER(I,2)=ZY
           GO TO 111
        112 SUM2(I)=SUM22(K)
        111 IF( GG(I).EQ.J.) DEPN(I,3)=DELT(I)
           IF( GG(I).LE.J.) GO TO 110
           T(1)=ABS(SUMDLT(I))
           SUMS(I)=SUM3(K)
           IF(SIGOR1(I,3).EQ.0.) GO TO 110
           KP=NEP12(K)
           DO 705 J=1,KP
             X(J)=EP12(J,K)
           705 Y(J)=SIG12(J,K)
           M3=MSH
           95      CALL SPLIN2(KP,X,Y,1,T,ST,SST,5,ZY,2,K)
             ENER(I,3)=ZY
           110 CONTINUE
           DO 60 I=1,LAMINA
             DO 60 J=1,3
               EPN(I,J)=EPN(I,J)+DEPN(I,J)
           60 CONTINUE
           EFF1=2./SQRT(3.)*(EPXX*EPXX+EPYY*EPYY+EPXX*EPYY+J*.25*EPXY*EPXY)**
           1 0.5
           EPXX=EPXX+DELEP(1)
           EPYY=EPYY+DELEP(2)
           EPXY=EPXY+DELEP(3)
           EFF2=2./SQRT(3.)*(EPXX*EPXX+EPYY*EPYY+EPXX*EPYY+J*.25*EPXY*EPXY)**
           1 0.5
           EDIFF=EFF2-EFF1
           SIGXX=SIGXX+A1(KL)
           SIGYY=SIGYY+A2(KL)
           SIGXY=SIGXY+A3(KL)
           511 HK=H(LAMINA+1)-H(1)
             SGXX=SIGXX/HK
             SGYY=SIGYY/HK
             SGXY=SIGXY/HK
           DO 78 I=1,LAMINA
             K=MAT(I)
             K1=NEP0T(K)-1
           120

```

SUBROUTINE OUTPUT

```

125 K2=NEP0C(K)-1
    K3=NEP90T(K)-1
    K4=NEP90C(K)-1
    K5=NEP12(K)-1
    T1T=EP0T(K1,K)
    T1C=EP0C(K2,K)
    T2T=EP90T(K3,K)
    T2C=EP90C(K4,K)
    T12=EP12(K5,K)
    T1=ABS(EPN(I,1))
    T2=ABS(EPN(I,2))
    T3=ABS(EPN(I,3))
    TT1=ABS(SUMD1(I))
    TT2=ABS(SUMD2(I))
    TT3=ABS(SUMD3(I))
    IF(E11(I).EQ.0.) GO TO 78
    XL(I)=ENER(I,1)/SUM1(I)
    IF(GG(I).EQ.0.) GO TO 7
    XS(I)=ENER(I,3)/SUMS(I)
7  IF(E22(I).EQ.0.) GO TO 8
    XT(I)=ENER(I,2)/SUM2(I)
8  IF(XL(I).EQ.0.) GO TO 2
    XL(I)=XL(I)+M1
2  IF(XT(I).EQ.0.) GO TO 3
    XT(I)=XT(I)+M2
    IF(XT(I).LE.0.) XT(I)=0.
3  IF(XS(I).EQ.0.) GO TO 4
    XS(I)=XS(I)+M3
    IF(XS(I).LE.0.) XS(I)=0.
4  XX(I)=XL(I)+XT(I)+XS(I)
    IF(XX(I)-1.) +02,79,79
79 NFAIL=NFAIL+1
    XR=XL(I)/XX(I)
    IF(XR-0.1) 240,250,250
250 CONTINUE
    E11(I)=0.
    UNN(I)=0.
240 CONTINUE
    UNN(I)=1.
160

```



SUBROUTINE OUTPUT

```

205      TYYT=TYY/T2T
        IF(TYT.LE.0.0J1) GO TO 214
        IF(TYYT.GE.0.0J1) GO TO 216
214      NTRAN(I)=I
        UNN(I)=0.
        E22(I)=0.
        SG(I)=0.
        NALTER(I)=1
        NSHEAR(I)=I
        NFAIL=NFAIL+1
        NPR=1
216      IF(NSHEAR(I).EQ.1) GO TO 79
        IF(GG(I).EQ.0.) GO TO 78
        TXY=ABS(T3-T12)
        TXYT=TXY/T12
        TXXY=ABS(T3-T12)
        TXXYT=TXXY/T12
        IF(T3.E1.0.) GO TO 78
        IF(TXYT-0.0J1) 215,215,230
230      IF(TXXYT-0.0J1) 215,215,75
215      NSHEAR(I)=I
        NALTER(I)=1
        NTRAN(I)=I
        GG(I)=0.
        E22(I)=0.
        UNN(I)=0.
        NPR=1
        NFAIL=NFAIL+1
        78      CONTINUE
        ENTL=0.
235      DO 178 I=1,LAMINA
        ENTL=ENTL+XX(I)
        LB=MOO(LOAD,NPRINT)
        IF(LOAD.EQ.1) GO TO 80
        IF(NPR.EQ.1) GO TO 90
        IF(LB) 90,80,80
        80      WRITE(6,300)
        300      FORMAT(1H1)
        WRITE(6,314)
        314      FORMAT(119X/119X)

```



## SUBROUTINE OUTPUT

```

C      WRITE(6,352) (I,(ENER(I,J),J=1,3),I=1,LAMINA)
352  FORMAT(2X,5HLAYER,8X,7HENER-LL,11X,7HENER-TT,11X,7HENER-LT/
1      (3X,I2,3E18.8))
205  WRITE(6,902) (I,XL(I),XT(I),XS(I),XX(I),I=1,LAMINA)
902  FORMAT(/7H LAYER,5X,14HENERGY RATIO-L,4X,14HENERGY RATIO-T,4X,
1      14HENERGY RATIO-S,4X,18HTOTAL CONTRIBUTION ,/
2      (3X,I2,2X,4E18.8))
390  WRITE(6,910) ENLE
910  FORMAT(/53X,27HTOTAL ENERGY OF ALL LAYERS ,E15.8,/ /)
290  WRITE(6,100) (I,E11(I),E22(I),GG(I),UNN(I),I=1,LAMINA)
100  FORMAT(33H MODULI AT THE END OF INCREMENT
1      7H LAYER,9X,3HE11,15X,3HE22,15X,3HG12,15X,3HU12, /
2      (3X,I2,2X,4E18.8))
101  FORMAT(/22X,5HLONG.,5X,5HTRAN.,5X,5HSHEAR, / )
800  CONTINUE
GO TO (810,820,830) ,NOPSHN
810  CONTINUE
GX=0.
GY=0.
GXX=0.
DO 89 I=1,LAMINA
KK=NLONG(I)
LL=NTRAN(I)
MM=NSHEAR(I)
IF(NPR.EQ.1.OR.LB.EQ.0) WRITE(6,99) NLONG(I),NTRAN(I),NSHEAR(I)
83  HK=H(I+1)-H(I)
GX =GX +HK*(SIGDR1(I,1)*S6(I)+SIGDR1(I,2)*S7(I)+2.*S8(I)*
1      SIGDR1(I,3))
310  GY =GY +HK*(SIGDR1(I,1)*S7(I)+SIGDR1(I,2)*S6(I)-2.*S8(I)*
1      SIGDR1(I,3))
1      GXX=GXX+HK*((SIGDR1(I,2)-SIGDR1(I,1))*S3(I)+SIGDR1(I,3))*
1      S6(I)-S7(I))
315  SIGDR1(I,1)=0.
SIGDR1(I,2)=0.
SIGDR1(I,3)=0.
GO TO 83
82  IF(LL-I) 189,85,189
85  GO TO(86,87),NALTER(I)
320

```

## SUBROUTINE OUTPUT

```

86 HK=H(I+1)-H(I)
GX=GX+HK*(SIGDR1(I,2)*S7(I)+2.*S8(I)*SIGDR1(I,3))
GY=GY+HK*(SIGDR1(I,2)*S6(I)-2.*S8(I)*SIGDR1(I,3))
GXX=GXX+HK*(SIGDR1(I,2)*S8(I)+SIGDR1(I,3)*(S6(I)-S7(I)))
SIGDR1(I,2)=0.
SIGDR1(I,3)=0.
GO TO 89

87 HK=H(I+1)-H(I)
GX=GX+HK*SIGDR1(I,2)*S7(I)
GY=GY+HK*SIGDR1(I,2)*S6(I)
GXX=GXX+HK*SIGDR1(I,2)*S8(I)
SIGDR1(I,2)=0.
IF(MM-I) 89,190,89
189 IF(MM-I) 89,190,89
190 HK=H(I+1)-H(I)
GX=GX+2.*S8(I)*SIGDR1(I,3)
GY=GY-2.*S8(I)*SIGDR1(I,3)
GXX=GXX+(S6(I)-S7(I))*SIGDR1(I,3)
SIGDR1(I,3)=0.
89 CONTINUE
XYZ=ABS(GX)+ABS(GY)+ABS(GXX)
IF(XYZ.GT.1.) NOFF=1
IF(NOFF.EQ.0) GO TO 401
AB1=A1(KL)
AB2=A2(KL)
AB3=A3(KL)
SIGXX=SIGXX-A1(KL)
SIGYY=SIGYY-A2(KL)
SIGXY=SIGXY-A3(KL)
LOAD=LOAD-1
A1(KL)=GX
A2(KL)=GY
A3(KL)=GXX
CALL UNLOAD(DA)
NOFF=0
A1(KL)=AB1
A2(KL)=AB2
A3(KL)=AB3
IF(EFF1.GE.0.5.OR.EFF2.GE.0.5) DA=0.
IF(EFF1.GE.0.5.OR.EFF2.GE.0.5) WRITE(6,*)51 EFF1,EFF2
451 FORMAT(/10X,17HLOADING UNSTABLE ,18HEFFECTIVE STRAINS=,2E18.8)

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SUBROUTINE OUTPUT

```

365 IF(DA.LE.0.) GO TO 401
      GO TO 20
      401 CONTINUE
      IF(EDIFF.LE.0.) WRITE(6,45J) EDIFF
      450 FORMAT(/10X,17HLOADING UNSTABLE
                1 E18.8)
      IF(NPR.NE.1.OR.LB.NE.0) RETURN
      IF(NOFF.EQ.0) WRITE(6,103) (I,E11(I),E22(I),GG(I),UWN(I),I=1,
                1 LAMINA)
      103 FORMAT(/ 41H MODULI AFTER THE OF CALL FOR *UNLOAU* //
                1 7H LAYER,9X,3HE11,15X,3HE22,15X,3HG12,15X,3HU12, /
                2 (3X,I2,2X,4E18.8))
      820 CONTINUE
      830 CONTINUE
      RETURN
      END
375

```

SUBROUTINE UNLOAD

```

1 C SUBROUTINE UNLOAD(DA)
      CALL ELCON
      IF(DA.LE.0.) RETURN
      CALL ITER
      RETURN
      END
5 C

```

**APPENDIX B**

**EXAMPLES OF OUTPUT**





LAMINATE NO. 1

NO. OF BOUNDING SURFACES - 5  
 DISTANCE OF 1-BOUNDARY - 0.0000  
 DISTANCE OF 2-BOUNDARY - .0052  
 DISTANCE OF 3-BOUNDARY - .0104  
 DISTANCE OF 4-BOUNDARY - .0156  
 DISTANCE OF 5-BOUNDARY - .0208

LAMINA	ORIENTATION	MATERIAL
1	0.0000	1
2	45.0000	1
3	-45.0000	1
4	90.0000	1

LOAD COMBINATION 1 .10000000E+03  
 STRESS RESULTANT INCREMENT NX--  
 STRESS RESULTANT INCREMENT NY--  
 STRESS RESULTANT INCREMENT NXY--

LOAD COMBINATION 2 .10000000E+03  
 STRESS RESULTANT INCREMENT NX--  
 STRESS RESULTANT INCREMENT NY--  
 STRESS RESULTANT INCREMENT NXY--

LOAD INCREMENT 1 LOAD COMBINATION 1 LAMINATE NO. 1 NOPSHN NO. 1  
 EX = .11640661E+02 EY = .13019960E+08 UXY = .28648981E+00 GXY = .43883820E+07

ETA1 = .28571242E-11 ETA2 = -.96623602E-11

ST. INCR. DELEP(1) DELEP(2) DELEP(3)  
 .41159420E-03 -.11791754E-03 .11759758E-14

LAYER	STRAIN-LL	STRAIN-LT	STRAIN-TT	STRAIN-XX	STRAIN-YY	STRAIN-XY	STRESS-LL	STRESS-LT	STRESS-TT	STRESS-XX	STRESS-YY	STRESS-XY	RESULT-XX	RESULT-YY	RESULT-XY
1	.41159420E-03	.11791754E-03	.11759758E-14	.41159420E-03	.11791754E-03	.11759758E-14	.48076923E+04	.12283370E+05	.12283370E+05	.10000000E+03	.0	.0	.0	.0	.0
2	.14683833E-03	.4683833E-03	.14683833E-03	.14683833E-03	.4683833E-03	.14683833E-03	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04
3	.14683833E-03	.4683833E-03	.14683833E-03	.14683833E-03	.4683833E-03	.14683833E-03	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04
4	.11791754E-03	.41159420E-03	.41159420E-03	.11791754E-03	.41159420E-03	.41159420E-03	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04	.48076923E+04

STRESSES IN LAMINAE OBTAINED FROM STRESS-STRAIN CURVES

LAYER	STRAIN-L	STRAIN-T	STRAIN-TT	ENERGY-LLT	ENERGY-LTC	ENERGY-TTC	ENERGY-LT	ENERGY-LT	ENERGY-LT
1	.41091093E-03	.11759758E-14	.11759758E-14	.27557636E+04	.24052808E+02	.82257247E+04	.51666040E+03	.21850173E+03	.21850173E+03
2	.15021467E-03	.52951174E-03	.52951174E-03	.17838349E-03	.17838349E-03	.56541447E-03	.44901433E+04	.48068740E+03	.48068740E+03
3	.15021467E-03	.52951174E-03	.52951174E-03	.17838349E-03	.17838349E-03	.56541447E-03	.44901433E+04	.48068740E+03	.48068740E+03
4	.11128479E-03	.38655511E-03	.38655511E-03	.82257247E+04	.82257247E+04	.82257247E+04	.39480479E+04	.10448409E+04	.10448409E+04

ENERGY RATIO-L ENERGY RATIO-T ENERGY RATIO-S ENERGY RATIO-S TOTAL CONTRIBUTION

1	.39266397E-02	.41390728E-04	.0	.39680304E-02
2	.48974949E-03	.12071370E-02	.56541447E-03	.22723010E-02
3	.49974949E-03	.12071370E-02	.56541447E-03	.22723010E-02
4	.88054649E-04	.95327860E-02	.0	.95908427E-02

MODULI AT THE END OF INCREMENT E11 E22 E33 E44 U12

1	.29882131E+08	.30756695E+07	.88160701E+06	.21000260E+00
2	.59892131E+08	.56991665E+07	.87848296E+06	.21000112E+00
3	.59892131E+08	.56991665E+07	.87848296E+06	.21000112E+00
4	.35400535E+08	.27238996E+07	.86160701E+06	.22500017E+00

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LOAD INCREMENT 12 LOAD COMBINATION 1 LAMINATE NO. 1 NOPSMM NO. 1  
 EX = .10650562E+00 EY = .12288350E+00 UXY = .30373102E+00 GXY = .43657981E+07

ETA1 = .27430199E-11 ETA2 = -.92279364E-11  
 ST. INCR. DELEP(1) .28212667E-04 DELEP(2) .77387908E-16 DELEP(3)

STRAINS - STRESS RESULTANTS / STRESSES  
 STRAIN-XX .44499220E-02 STRAIN-YY .13944604E-02 STRAIN-XY .10562500E+04  
 STRAIN-LL .44992200E-02 STRAIN-TT .12460480E-13 STRAIN-LT .13220026E+06  
 STRAIN-LR .44727308E-02 STRAIN-LR .15727308E-02 STRAIN-LR .48077480E+05  
 STRAIN-LR .13757308E-02 STRAIN-LR .15727308E-02 STRAIN-LR .48077480E+05  
 STRAIN-LR .13044604E-02 STRAIN-LR .44499220E-02 STRAIN-LR .93775769E+04

STRESSES IN LAMINAE OBTAINED FROM STRESS-STRAIN CURVES  
 STRAIN-LR .44727308E-02 STRAIN-LR .15727308E-02 STRAIN-LR .48077480E+05  
 STRAIN-LR .13757308E-02 STRAIN-LR .15727308E-02 STRAIN-LR .48077480E+05  
 STRAIN-LR .13044604E-02 STRAIN-LR .44499220E-02 STRAIN-LR .93775769E+04

ENERGY RATIO-L  
 ENERGY RATIO-T  
 ENERGY RATIO-S  
 ENERGY RATIO-S

MODULI AT THE END OF INCREMENT  
 MODULI AT THE END OF INCREMENT  
 MODULI AT THE END OF INCREMENT

LONG. TRAN. SHEAR  
 LONG. TRAN. SHEAR  
 LONG. TRAN. SHEAR

ELCON CALLED FROM \*UNLOAD\*  
 ELCON CALLED FROM \*UNLOAD\*  
 ELCON CALLED FROM \*UNLOAD\*

LOAD INCREMENT 12 AD COMBINATION 1 LAMINATE NO. 1 NOPSIN NO. 1  
 EX = .10342132E+08 EY = .272840E+08 UXY = .29819101E+00 GXY = .41409282E+07

ETA1 = .2361663E-11 G2 = -.10414787E-10  
 ST. INCR. (1) DELEP(2) DELEP(3)  
 . . . . . 03 -.67595087E-04 -.21516968E-14

STRAIN-XX STRAIN-YY STRAIN-XY STRAIN-LT STRAIN-TT STRAIN-TT  
 .46766059E-02 -.13720555E-02 .10308791E-13 .13308791E-13 .13308791E-13 .13308791E-13

STRESS-XX STRESS-YY STRESS-XY STRESS-LT STRESS-TT STRESS-TT  
 .1652227355E-02 .1652227355E-02 .1652227355E-02 .1652227355E-02 .1652227355E-02 .1652227355E-02

STRESSES IN LAMINAE OBTAINED FROM STRESS-STRAIN CURVES  
 STRAIN-LT-13 STRAIN-TT-13 STRAIN-TT-13  
 .13308791E-13 .13308791E-13 .13308791E-13

ENERGY RATIO-L ENERGY RATIO-T ENERGY RATIO-S  
 .11025376E-01 .11025376E-01 .11025376E-01

MODULI AT THE END OF INCREMENT  
 E11 98E+08 E22 99997E+07 G12 1007001E+00  
 E12 98E+08 E23 99997E+07 G13 1007001E+00  
 E31 98E+08 E32 99997E+07 G23 1007001E+00  
 E33 98E+08 E34 99997E+07 G34 1007001E+00

LAYER FAILING LAYER FAILING LAYER FAILING LAYER FAILING  
 MODULI AFTER THE OF CALL FOR \*UNLOAD\*

LONG. TRAN. SHEAR  
 0 0 0  
 0 0 0  
 0 0 0

RESUL.-XX RESUL.-YY RESUL.-XY  
 0. 0. 0.  
 0. 0. 0.  
 0. 0. 0.

STRESS-LT STRESS-TT STRESS-TT  
 0. 0. 0.  
 0. 0. 0.  
 0. 0. 0.

TOTAL CONTRIBUTION TOTAL ENERGY OF ALL LAYERS  
 .51237355E+00 .20885570E+01  
 .28219525E+00 .20885570E+01  
 .101117930E+01 .20885570E+01



LOAD INCREMENT 1    LOAD COMBINATION 2    LAMINATE NO. 1    NDFSHN NO. 1  
 EX= .11561033E+08    EY= .11561033E+08    UXY= .31710922E+00    GXY= .43867904E+07  
 ETA1= .26574733E-11    ETA2= -.80699692E-11  
 ST. INCR.    DELEP(1)    .28398231E-03    DELEP(2)    .28398231E-03    DELEP(3)    -.22508037E-14

STRAIN-XX    .28398231E-03    STRAIN-YY    .28398231E-03    STRAIN-TT    .28398231E-03  
 STRAIN-LL    .28398231E-03    STRAIN-LT    .28398231E-03    STRAIN-LT    .28398231E-03  
 STRAIN-LL    .28398231E-03    STRAIN-LT    .28398231E-03    STRAIN-LT    .28398231E-03  
 STRAIN-LL    .28398231E-03    STRAIN-LT    .28398231E-03    STRAIN-LT    .28398231E-03

STRESSES IN LAMINAE OBTAINED FROM STRESS-STRAIN CURVES  
 STRAIN-TT    .28398231E-03    STRAIN-LT    .28398231E-03    STRAIN-LT    .28398231E-03  
 STRAIN-LT    .28398231E-03    STRAIN-LT    .28398231E-03    STRAIN-LT    .28398231E-03  
 STRAIN-LT    .28398231E-03    STRAIN-LT    .28398231E-03    STRAIN-LT    .28398231E-03  
 STRAIN-LT    .28398231E-03    STRAIN-LT    .28398231E-03    STRAIN-LT    .28398231E-03

ENERGY-LLT    .64483175E+03    ENERGY-TTC    .51666040E+03    ENERGY-LT    .21850173E+03  
 ENERGY-LLT    .64483175E+03    ENERGY-TTC    .51666040E+03    ENERGY-LT    .21850173E+03  
 ENERGY-LLT    .64483175E+03    ENERGY-TTC    .51666040E+03    ENERGY-LT    .21850173E+03  
 ENERGY-LLT    .64483175E+03    ENERGY-TTC    .51666040E+03    ENERGY-LT    .21850173E+03

ENERGY RATIO-L    .18692169E-02    ENERGY RATIO-T    .45184981E-02    ENERGY RATIO-S    0.  
 ENERGY RATIO-L    .18692169E-02    ENERGY RATIO-T    .45184981E-02    ENERGY RATIO-S    0.  
 ENERGY RATIO-L    .18692169E-02    ENERGY RATIO-T    .45184981E-02    ENERGY RATIO-S    0.  
 ENERGY RATIO-L    .18692169E-02    ENERGY RATIO-T    .45184981E-02    ENERGY RATIO-S    0.

MODULI AT THE END OF INCREMENT E22    G12    U12  
 LAYER 1    .29893694E+08    .271747225E+07    .88180701E+06  
 LAYER 2    .29893694E+08    .271747225E+07    .88180701E+06  
 LAYER 3    .29893694E+08    .271747225E+07    .88180701E+06  
 LAYER 4    .29893694E+08    .271747225E+07    .88180701E+06

TOTAL ENERGY OF ALL LAYERS    .25550860E-01  
 TOTAL CONTRIBUTION  
 .63877150E-02  
 .63877150E-02  
 .63877150E-02  
 .63877150E-02



LAMINATE NO. 2

NO. OF BOUNDING SURFACES - 3  
DISTANCE OF 1-BOUNDARY - .0052  
DISTANCE OF 2-BOUNDARY - 0.0003  
DISTANCE OF 3-BOUNDARY - .0052

LAMINA	ORIENTATION	MATERIAL
1	0.000	1
2	90.000	1

LOAD COMBINATION	-----
STRESS RESULTANT	INCREMENT NXX---
STRESS RESULTANT	INCREMENT NYY---
STRESS RESULTANT	INCREMENT NXY---
	1 .50000000E+02
	0.
	0.

LOAD INCREMENT 1 LOAD COMBINATION 1 LAMINATE NO. 2 NOPS MN NO. 1  
 EX= .16341277E+08 EY= .19105132E+08 UXY= .30765999E-01 GXY= .00100701E+06  
 ETA1= .39165544E-11 ETA2= -.95904621E-10  
 ST. INCR. DELEP(1) DELEP(2) DELEP(3)  
 .29420543E-03 -.90515230E-05 .11522716E-14

	STRAIN-XX	STRAIN-YY	STRAIN-XY	STRAINS - STRESS RESULTANTS / STRESSES	RESUL.-XX	RESUL.-YY	RESUL.-XY
	.29420543E-03	-.90515230E-05	.11522716E-14	.50000003E+02	0.	0.	0.
LAYER	STRAIN-LL	STRAIN-TT	STRAIN-LT	STRESS-LL	STRESS-TT	STRESS-LT	
1	.29420543E-03	-.90515230E-05	.11522716E-14	.0243575E+04	.14255307E+03	.79102711E+03	
2	-.90515230E-03	.29420543E-03	-.4243523E-14	-.14255307E+03			
LAYER	STRESSES IN LAMINAE OBTAINED FROM STRESS-STRAIN CURVES			STRESS-L	STRESS-T	STRESS-LT	
1	.29520690E-03	.52342251E-04	.11522716E-14	.00109302E+04	.00109302E+03	.79102711E+03	
2	-.40255391E-05	.29329960E-03	-.4243523E-14	-.16591043E+03	.13096313E+03	.79102711E+03	
MAT 1	ENERGY-LLI	ENERGY-LLC	ENERGY-TT	ENERGY-TTC	ENERGY-LT		
	.64483175E+03	.27957636E+04	.24352000E+02	.51666040E+03	.21050173E+03		
MAT 2	.02257247E+04	.02257247E+04	.02257247E+04	.02257247E+04	.21050173E+03		

LAYER	ENERGY RATIO-L	ENERGY RATIO-T	ENERGY RATIO-S	TOTAL CONTRIBUTION
1	.23062213E-02	.45956370E-05	0.	.20100069E-02
2	.51007830E-06	.40500505E-02	0.	.48505694E-02
			TOTAL ENERGY OF ALL LAYERS	.60613763E-02

58 MODULI AT THE END OF INCREMENT E22 G12 U12  
 LAYER E11 E12 G12 U12  
 1 .29093764E+08 .26930346E+07 .00100701E+06 .21000205E+00  
 2 .35412163E+08 .27105475E+07 .00100701E+06 .225000001E+00

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LOAD INCREMENT 18 LOAD COMBINATION 1 LAMINATE NO. 2 NOPSIN NO. 1  
 EX= .14335106E+08 EY= .19050216E+08 UXY= .14904289E-01 GXY= .44090351E+06  
 ETA1= .30500087E-11 ETA2= -.20463967E-09  
 ST. INCR. DELEP(1) DELEP(2) DELEP(3)  
 .33927839E-03 -.50567030E-05 -.55182300E-13

STRAIN-XX STRAIN-YY STRAIN-TT STRAIN-LT STRAIN-LL STRAIN-LT  
 .47860241E-02 -.12936535E-03 -.47460241E-02 -.4973560E-13  
 .12936535E-03 -.47460241E-02 -.4973560E-13  
 STRESSES IN LAMINAE OBTAINED FROM STRESS-STRAIN CURVES  
 STRAIN-L STRAIN-T STRAIN-LT STRAIN-LL STRAIN-LT  
 .47860241E-02 .07932072E-03 .47719610E-02 .4973560E-13  
 .67595561E-04 .47719610E-02 .47719610E-02 .4973560E-13  
 ENERGY RATIO-L ENERGY RATIO-T ENERGY RATIO-S  
 .51057450E+00 .93688519E+03 .99868115E+00  
 .10936055E-03 0. 0.

STRESS RESULTANTS / STRESSES  
 RESULT-XX RESULT-YY RESULT-XY  
 .74140625E+03 0. 0.  
 .71289063E+05 0. 0.  
 STRESS-LL STRESS-TT STRESS-LT  
 .4257857E+06 .23923369E+04 0. 0.  
 .23923369E+04 0. 0.  
 STRESS-L STRESS-T STRESS-LT  
 .4257857E+06 .23923369E+04 0. 0.  
 .23923369E+04 .57265550E+04 0. 0.

TOTAL CONTRIBUTION  
 .53151198E+00  
 .99878713E+00  
 TOTAL ENERGY OF ALL LAYERS .15302985E+01

MODULI AT THE END OF INCREMENT E22 U12  
 LAYER 1 20853300E+08 0. 88160701E+06 0. 20970730E+00  
 LAYER 2 35408525E+08 0. 88160701E+06 0. 20970730E+00

LAYER FAILING LONG. TRAN. SHEAR  
 LAYER 1 0 0 0  
 LAYER 2 0 2 2

MODULI AFTER THE OF CALL FOR \*UNLOAD\*  
 E11 E22 G12  
 LAYER 1 .20853300E+08 .26735439E+07 0. 88160701E+06 0. 20970730E+00  
 LAYER 2 .35408525E+08 .26735439E+07 0. 88160701E+06 0. 20970730E+00

LOAD INCREMENT 27 LOAD COMBINATION 1 LAMINATE NO. 2 NOPSMM NO. 1  
 EX = .13008964E+08 EY = .18935335E+08 UXY = .12393778E-01 GXY = .44090351E+06  
 ETA1 = .25362586E-11 ETA2 = -.20463967E-09

ST. INCR. DELEP(1) DELEP(2) DELEP(3)  
 .11548989E-04 -.14313560E-06 .23291222E-16

STRAIN-XX STRAIN-YY STRAIN-XY STRESS RESULTANTS / STRESSES RESULT.-YY RESULT.-XY  
 .65706278E-02 .15401633E-03 -.65706278E-02 -.38928993E-13 .98984375E+03 0.  
 .57177204E+05 0.

LAYER STRAIN-LL STRAIN-TT STRAIN-LT STRAIN-LL STRAIN-LL STRAIN-TT STRAIN-TT STRAIN-LT  
 1 .65706278E-02 .15401633E-03 -.65706278E-02 -.38928993E-13 .98984375E+03 0.  
 2 .15401633E-03 .65706278E-02 -.29612703E-13 .19035457E+06 .32651916E+04 0.

LAYER STRESSES IN LAMINAE OBTAINED FROM STRESS-STRAIN CURVES STRESS-L STRESS-L STRESS-T STRESS-T  
 1 .65545937E-02 .12207610E-02 -.65565647E-02 .90351256E+06 .32651170E+04  
 2 -.92210537E-04 .65565647E-02 -.29612703E-13 -.22132662E+04 .97265520E+04  
 ENERGY RATIO-L ENERGY RATIO-T ENERGY RATIO-S TOTAL CONTRIBUTION  
 .99134005E+09 .13280776E-02 0. .99268133E+00  
 .15021399E-09 .99668115E+08 0. .99883136E+00

TOTAL ENERGY OF ALL LAYERS .19914995E+01

MODULI AT THE END OF INCREMENT E22 G12 U12  
 LAYER 0. .35408525E+08 0. 0. .22500010E+00  
 2 .35408525E+08 0. 0.

LAYER FAILING LONG. TRAN. SHEAR MODULI OF ELASTICITY  
 1 0 0 0  
 2 0 0 0  
 ELCON CALLED FROM \*UNLOAD\* MODULI OF ELASTICITY 0. 0. 0.  
 .35408525E+08 STRESS RESULTANTS .16978997E+02 0.  
 .98984375E+03 .16978997E+02 0.

EX = .13008964E+08 EY = .18935335E+08 UXY = .12393778E-01 GXY = .44090351E+06  
 ETA1 = .25362586E-11 ETA2 = -.20463967E-09

MATRIX \*A\* IS SINGULAR

MODULI AFTER THE OF CALL FOR \*UNLOAD\* MODULI OF ELASTICITY  
 LAYER 0. .35408525E+08 0. 0. 0. 0.  
 1 .35408525E+08 0. 0. 0. 0.  
 2 .35408525E+08 0. 0. 0. 0.

LAMINATE NC. 3

NO. OF BOUNDING SURFACES--	6	--.1050
DISTANCE OF 1-BOUNDARY - -		--.0575
DISTANCE OF 2-BOUNDARY - -		--.0263
DISTANCE OF 3-BOUNDARY - -		--.0158
DISTANCE OF 4-BOUNDARY - -		--.0053
DISTANCE OF 5-BOUNDARY - -		0.0000
DISTANCE OF 6-BOUNDARY - -		0.0000

LAMINA	ORIENTATION	MATERIAL
1	0.000	2
2	0.000	1
3	-45.000	1
4	45.000	1
5	90.000	1

LOAD COMBINATION	INCREMENT	INCREMENT	INCREMENT
STRESS RESULTANT	STRESS RESULTANT	STRESS RESULTANT	STRESS RESULTANT
STRESS RESULTANT	STRESS RESULTANT	STRESS RESULTANT	STRESS RESULTANT
1	.40000000E+03	0.	0.

LOAD INCREMENT 1 LOAD COMBINATION 1 LAMINATE NO. 3 NOPSHN NO. 1  
 EX = .15001257E+08 EY = .90661721E+07 UXY = .33795739E+00 GXY = .36959545E+07  
 ETA1 = .79606761E-12 ETA2 = -.22919376E-11

ST. INCR. DELEP(1) DELEP(2) DELEP(3)  
 .25394698E-03 -.85833414E-04 .20215896E-15

LAYER	STRAIN-LL-03	STRAIN-TT-04	STRAIN-XY-15	STRAIN-LL-04	STRAIN-TT-04	STRAIN-XY-15	STRAIN-LL-04	STRAIN-TT-04	STRAIN-XY-15	STRAIN-LL-04	STRAIN-TT-04	STRAIN-XY-15
1	.25394698E-03	-.85833414E-04	.20215896E-15	.38095238E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03
2	.25394698E-03	-.85833414E-04	.20215896E-15	.38095238E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03
3	.25394698E-03	-.85833414E-04	.20215896E-15	.38095238E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03
4	.25394698E-03	-.85833414E-04	.20215896E-15	.38095238E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03
5	.25394698E-03	-.85833414E-04	.20215896E-15	.38095238E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03

STRESSES IN LAMINAE OBTAINED FROM STRESS-STRAIN CURVES

LAYER	STRAIN-LL-03	STRAIN-TT-04	STRAIN-XY-15	STRAIN-LL-04	STRAIN-TT-04	STRAIN-XY-15	STRAIN-LL-04	STRAIN-TT-04	STRAIN-XY-15	STRAIN-LL-04	STRAIN-TT-04	STRAIN-XY-15
1	.25394698E-03	-.85833414E-04	.20215896E-15	.38095238E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03
2	.25394698E-03	-.85833414E-04	.20215896E-15	.38095238E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03
3	.25394698E-03	-.85833414E-04	.20215896E-15	.38095238E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03
4	.25394698E-03	-.85833414E-04	.20215896E-15	.38095238E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03
5	.25394698E-03	-.85833414E-04	.20215896E-15	.38095238E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03	.26093133E+04	.1037679E+03	.1037679E+03

MAT	ENERGY-LLT	ENERGY-LLC	ENERGY-TTC	ENERGY-TTC	ENERGY-TTC	ENERGY-TTC	ENERGY-TTC
1	.64483175E+03	.27957636E+04	.24052808E+02	.51666040E+03	.82257247E+04	.82257247E+04	.82257247E+04
2	.82257247E+04	.82257247E+04	.82257247E+04	.82257247E+04	.82257247E+04	.82257247E+04	.82257247E+04

LAYER	ENERGY RATIO-L	ENERGY RATIO-T	ENERGY RATIO-S	ENERGY RATIO-S	ENERGY RATIO-S	ENERGY RATIO-S	ENERGY RATIO-S
1	.40780779E-04	.46598200E-05	.00	.454099E-04	.1516266E-02	.7321809E-02	.36591449E-02
2	.14947242E-02	.21930465E-04	.00	.23290184E-03	.23290184E-03	.23290184E-03	.23290184E-03
3	.16376338E-03	.39549544E-03	.00	.39549544E-03	.39549544E-03	.39549544E-03	.39549544E-03
4	.16376338E-03	.39549544E-03	.00	.39549544E-03	.39549544E-03	.39549544E-03	.39549544E-03
5	.16376338E-03	.39549544E-03	.00	.39549544E-03	.39549544E-03	.39549544E-03	.39549544E-03

MODULI AT THE END OF INCREMENT	E11	E22	G12	U12	TOTAL ENERGY OF ALL LAYERS
1	.10405170E+08	.10405170E+08	.40020924E+07	.30000000E+00	.68055741E-02
2	.29899107E+08	.30056745E+07	.80160701E+06	.210000181E+00	
3	.29899107E+08	.30056745E+07	.80160701E+06	.210000181E+00	
4	.29899107E+08	.30056745E+07	.80160701E+06	.210000181E+00	
5	.29899107E+08	.30056745E+07	.80160701E+06	.210000181E+00	

LONG. TRAN. SHEAR

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LOAD INCREMENT 19      LOAD COMBINATION 1      LAMINATE NO. 3      NOPSIN NO. 1  
 EX= .14315702E+08      EY= .88591778E+07      UXY= .34758233E+00      GXY= .36457514E+07  
 ETA1= .63327826E-12      ETA2= -.23779272E-11  
 DELEP(1)      DELEP(2)      DELEP(3)  
 ST. INCR. .32472585E-04      -.11286894E-04      -.62276867E-15

STRAIN-XX      STRAIN-YY      STRAIN-XY      STRAIN-TT      STRAIN-LT      STRAIN-LT  
 .44781477E-02      -.15343599E-02      .28107195E-14      .28107195E-14      .28107195E-14      .28107195E-14  
 .4787477E-02      .13343298E-02      .28107195E-14      .28107195E-14      .28107195E-14      .28107195E-14  
 .4787477E-02      .13343298E-02      .28107195E-14      .28107195E-14      .28107195E-14      .28107195E-14  
 .4787477E-02      .13343298E-02      .28107195E-14      .28107195E-14      .28107195E-14      .28107195E-14  
 .4787477E-02      .13343298E-02      .28107195E-14      .28107195E-14      .28107195E-14      .28107195E-14

STRESSES IN LAMINAE OBTAINED FROM STRESS-STRAIN CURVES  
 STRAIN-LE-02      STRAIN-LE-03      STRAIN-LE-04      STRAIN-LE-05  
 .44781477E-02      .20955291E-02      .28107195E-14      .28107195E-14  
 .4787477E-02      .17888338E-02      .28107195E-14      .28107195E-14  
 .4787477E-02      .17888338E-02      .28107195E-14      .28107195E-14  
 .4787477E-02      .17888338E-02      .28107195E-14      .28107195E-14  
 .4787477E-02      .17888338E-02      .28107195E-14      .28107195E-14

ENERGY RATIO-L      ENERGY RATIO-T      ENERGY RATIO-S  
 .12680590E-01      .14888081E-02      .10577800E-02  
 .42495922E-01      .12121822E+00      .12121822E+00  
 .50248909E-01      .19944905E+00      .19944905E+00  
 .14763140E-01      .99449050E+00      .99449050E+00

MODULI AT THE END OF INCREMENT      TRAN.      SHEAR  
 LAYER 1      0      0  
 LAYER 2      0      0  
 LAYER 3      0      0  
 LAYER 4      0      0  
 LAYER 5      0      0

TOTAL CONTRIBUTION      TOTAL ENERGY OF ALL LAYERS  
 .14169398E-01      .19748643E+01  
 .47202707E+00      .30000000E+00  
 .23777079E+00      .21028450E+00  
 .10132536E+01      .209993139E+00  
 .10132536E+01      .209993139E+00

RESULT--XY      RESULT--YY      RESULT--TT      RESULT--LT  
 0.      0.      0.      0.  
 0.      0.      0.      0.  
 0.      0.      0.      0.  
 0.      0.      0.      0.  
 0.      0.      0.      0.

STRESS-LT      STRESS-TT      STRESS-LE-02      STRESS-LE-03      STRESS-LE-04      STRESS-LE-05  
 0.      0.      0.      0.      0.      0.  
 0.      0.      0.      0.      0.      0.  
 0.      0.      0.      0.      0.      0.  
 0.      0.      0.      0.      0.      0.  
 0.      0.      0.      0.      0.      0.



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