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Inventor                         Chidambar Ganesh  
                                      Kai F. Gong

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2  
3 FUZZY LOGIC BASED MODEL ASSESSMENT SYSTE  
4 AND METHOD FOR CONTACT TRACKING

5  
6 STATEMENT OF GOVERNMENT INTEREST

7 The invention described herein may be manufactured and used  
8 by or for the Government of the United States of America for  
9 governmental purposes without the payment of any royalties  
10 thereon or therefore.

11  
12 BACKGROUND OF THE INVENTION

13 (1) Field Of The Invention

14 The present invention relates generally to the scientific  
15 field of optimal estimation, and more particularly, relates to a  
16 model assessment system and method used in the area of contact  
17 tracking or target motion analysis that is based on fuzzy logic  
18 inferencing methods.

19 (2) Description of the Prior Art

20 Expert systems can be used to identify likely models of  
21 physical phenomena in response to information about the state of  
22 the phenomena. One type of physical phenomena that can be

1 modeled is the motion of a signal source moving in a medium where  
2 the signal propagated through the medium is corrupted by noise.

3 In an underwater environment, for example, localization and  
4 tracking of an acoustic contact from sonar measurements are of  
5 considerable interest. Several estimation techniques have been  
6 applied to the tracking problem with varying results. The  
7 differences in techniques involve (1) the modeling of the  
8 process, and (2) the selection and formulation of the estimation  
9 algorithm. Sources of uncertainty in the modeling process  
10 include assumptions on contact kinematics, acoustic propagation  
11 mechanisms and measurement noise characteristics. Understanding  
12 and conveying the impact of these uncertainties on overall system  
13 performance is a critical issue. Model assessment is a crucial  
14 phase of contact tracking, leading to an appraisal of the system  
15 performance in the presence of modeling uncertainties. Model  
16 assessment involves identification of features from measurement  
17 residuals for formulation of possible causes of mismodeling  
18 associated with the system models employed in the tracking  
19 process.

20 A hierarchical approach to filtering and estimation for  
21 contact tracking was first proposed by A.G. Lindgren, et al.,  
22 "Nonlinear Parameter Estimation With Segmented Data: Trajectory

1 Estimation With Biased Measurements", *Proceedings of the 19th*  
2 *IEEE Asilomar Conference on Signals, Systems and Computers*, pp.  
3 349-353, November, 1985, incorporated herein by reference, and  
4 has been developed for generation of a tactical picture, as  
5 disclosed by K.F. Gong et al., "Intelligent Data Integration for  
6 Tactical Picture Generation: Performance Analysis of Advanced  
7 Techniques", *TTCP Subgroup G Symposium on Shallow Water Undersea*  
8 *Warfare*, Nova Scotia, October, 1996, incorporated herein by  
9 reference. The hierarchical model of intelligent data  
10 integration for generation of the tactical picture is shown  
11 generally in FIG. 1. This process entails (1) data conditioning,  
12 which associates and characterizes available data, and provides  
13 uncertainty descriptions; (2) data processing, which processes  
14 the conditioned data to form and maintain contact tracks,  
15 propagates the uncertainties, and provides for uncertainty  
16 descriptions associated with the resulting tracks; (3) model  
17 assessment, which detects, interprets and resolves anomalies due  
18 to uncertainties in modeling assumptions; and (4) the process  
19 controller, which provides for scenario driven adaptive  
20 processing by appropriate selection of data, models and  
21 algorithms.

1           Conventional approaches for propagation of uncertainty in  
2 contract tracking have primarily focused on probabilistic  
3 techniques, as disclosed by V.J. Aidala, "Kalman Filter Behavior  
4 in Bearings-Only Tracking Applications", *IEEE Transactions on*  
5 *Aerospace and Electronic Systems*, Vol. AES-15, No. 1, pp. 29-39,  
6 January, 1979, incorporated herein by reference. In particular,  
7 Bayesian methods have been used. The quality of the estimated  
8 track is evaluated based on a *a priori* knowledge of statistical  
9 uncertainties associated with the sensor measurements and the  
10 process model, i.e., input and modeling uncertainties. These  
11 uncertainties are typically represented as additive white  
12 Gaussian noise and are propagated through the conditional  
13 covariance matrix to form containment regions that indicate the  
14 final uncertainty associated with the contact state estimate, as  
15 described in S.C. Nardone et al., "Fundamental Properties and  
16 Performance of Conventional Bearings-Only Target Motion  
17 Analysis", *IEEE Transactions on Automatic Control*, Vol. AC-29,  
18 No. 9, pp. 775-787, September, 1984, incorporated herein by  
19 reference. Mismodeling in the tracking process has a severe  
20 impact on the integrity of the estimate and the uncertainties  
21 associated with those estimates. This includes erroneous  
22 assumptions, such as constant contact velocity, known acoustic

1 propagation path and Gaussian noise distributions, as well as  
2 erroneous model-order approximation.

3 To alleviate these difficulties in modeling, a contact  
4 management model assessment algorithm using the Dempster-Shafer  
5 approach has been developed, as disclosed in U.S. Patent No.  
6 5,581,490 issued to Ferkinhoff et al., and incorporated herein by  
7 reference. The Dempster-Shafer Theory of Evidential Reasoning  
8 represents a generalization of Bayesian probability for producing  
9 inferences from uncertain information. The results using this  
10 approach, however, can be inconclusive if there is a high degree  
11 of conflict in the evidence.

#### 12 13 SUMMARY OF THE INVENTION

14 It is therefore an object of the invention to provide a  
15 model assessment system and method for contact tracking that uses  
16 fuzzy logic.

17 The present invention features a fuzzy logic based model  
18 assessment system for assessing at least one model of physical  
19 phenomena using measurement residual values representing a  
20 difference between a measured data sequence corresponding to the  
21 physical phenomena and an expected data sequence corresponding to  
22 the model to be assessed. The system comprises a feature

1 identification module that identifies one or more features  
2 present in the measurement residual values and generates one or  
3 more feature amplitude values and feature amplitude standard  
4 deviation values. The system also comprises an anomaly  
5 characterization module that characterizes the features in one or  
6 more membership classes based upon the feature amplitude value  
7 and generates class membership interval values for each  
8 membership class based upon the feature amplitude standard  
9 deviation value. The class membership interval values represent  
10 a range of degrees of membership in each of the membership  
11 classes. The system further comprises a hypothesis formulation  
12 and evaluation module for determining at least one mismodeling  
13 hypothesis by applying fuzzy inferencing to the class  
14 memberships, and generates at least one hypothesis certainty  
15 interval value representing a range of degree of certainty of the  
16 mismodeling hypothesis.

17       According to one example, the physical phenomena includes a  
18 moving contact, the model is a contact tracking model, and the  
19 one or more features include one or more tracking anomalies.  
20 Examples of the tracking anomalies include a jump feature  
21 representing a discontinuity in a measured tracking signal and a  
22 drift feature representing a generally-linear drift of the

1 measured tracking signal. Examples of the membership classes  
2 include null, weak, moderate and strong. The class membership  
3 interval values preferably include an upper limit value  
4 representing the greatest possible extent to which the feature  
5 belongs to the membership class and includes a lower limit value  
6 representing the smallest necessary extent to which the feature  
7 belongs to the membership class. The hypothesis certainty value  
8 also preferably includes hypothesis certainty interval values  
9 representing a range of certainty for the mismodeling hypotheses.

10       According to one embodiment, the hypothesis formulation and  
11 evaluation module includes a knowledge base and an inferencing  
12 module. The knowledge base includes a plurality of rules for  
13 inferring one or more mismodeling hypotheses based upon features  
14 and their corresponding membership classes. The inferencing  
15 module applies one or more rules from the knowledge base to the  
16 class memberships, selects one or more mismodeling hypotheses  
17 based upon the rule, and generates hypothesis certainty interval  
18 values representing a range of certainty for the selected  
19 mismodeling hypothesis based on the class membership interval  
20 values. The hypothesis formulation and evaluation module can  
21 also include an aggregation module. Where the inferencing module  
22 applies a plurality of rules that results in the same mismodeling

1 hypothesis with different hypothesis certainty interval values,  
2 the aggregation module aggregates the hypothesis certainty  
3 interval values to generate a composite hypothesis certainty  
4 interval value for the mismodeling hypothesis.

5       The present invention also features a fuzzy inference system  
6 for use with a model assessment system comprising the anomaly  
7 characterization module and the hypothesis formulation and  
8 evaluation module as described above. According to one  
9 embodiment, the feature identification module, anomaly  
10 characterization module, and hypothesis formulation and  
11 evaluation module are implemented on a computer.

12       The present invention also features a method of assessing  
13 one or more models of physical phenomena in response to a  
14 measured data sequence representing a signal caused by the  
15 physical phenomena in the presence of noise. The method  
16 comprises providing measurement residual values representing a  
17 difference between the measured data sequence and an expected  
18 data sequence corresponding to the model to be assessed. One or  
19 more features are then identified in the measurement residual  
20 values, and one or more feature amplitude values and feature  
21 amplitude standard deviation values are generated for the  
22 identified feature. The feature is then characterized in one or

1 more membership classes based upon the feature amplitude value,  
2 and class membership interval values are generated for each of  
3 the membership classes based upon the feature amplitude standard  
4 deviation value. One or more mismodeling hypotheses are then  
5 determined by applying fuzzy inferencing to the class memberships  
6 and one or more hypotheses certainty interval values are  
7 generated, representing a degree of certainty of the mismodeling  
8 hypothesis. The method can also include the step of using the  
9 mismodeling hypothesis and the hypothesis certainty values to  
10 assess the model and generate a tactical picture.

#### 11 12 BRIEF DESCRIPTION OF THE DRAWINGS

13 These and other features and advantages of the present  
14 invention will be better understood in view of the following  
15 description of the invention taken together with the drawings  
16 wherein:

17 FIG. 1 is a functional block diagram of a hierarchical model  
18 of intelligent data integration for tactical picture generation,  
19 according to the prior art;

20 FIG. 2 is a functional block diagram of a fuzzy logic based  
21 model assessment system, according to the present invention;

1           FIG. 3 is a functional block diagram of a fuzzy inference  
2 system for use in the model assessment system, according to one  
3 embodiment of the present invention;

4           FIG. 4 is a flow chart illustrating the fuzzy logic based  
5 assessment method, according to the present invention;

6           FIG. 5 is a graphical representation of measurement residual  
7 data used to identify features or anomalies, according to one  
8 example of the present invention;

9           FIG. 6 is a graphical representation of identified features  
10 with respective amplitudes and standard deviations, according to  
11 one example of the present invention;

12          FIGS. 7A and 7B are graphical representations of normalized  
13 distributions of the identified features, according to one  
14 example of the present invention;

15          FIGS. 8A and 8B are graphical representations of class  
16 memberships of the identified feature, according to one example  
17 of the present invention;

18          FIGS. 9A and 9B are graphical representations of class  
19 membership interval values for an identified feature, according  
20 to one example of the present invention;

21          FIG. 10 is a graphical representation of a map of rules used  
22 to infer mismodeling hypotheses based upon the membership classes

1 of the identified features, according to one example of the  
2 present invention;

3 FIGS. 11A and 11B are graphical representations of  
4 mismodeling hypotheses and hypotheses certainty values determined  
5 based upon membership class values, according to one example of  
6 the present invention; and

7 FIGS. 12A and 12B are graphical representations of  
8 mismodeling hypotheses certainty interval values derived from  
9 membership class interval values, according to one example of the  
10 present invention.

11

12 DESCRIPTION OF THE PREFERRED EMBODIMENT

13 A fuzzy logic based model assessment system 10, FIG. 2, is  
14 used to assess one or more models of physical phenomena, such as  
15 a moving acoustic signal source. In one application, the model  
16 assessment system 10 is used for contact tracking or target  
17 motion analysis, for example, in military applications. The  
18 fuzzy logic based model assessment system uses fuzzy logic  
19 inferencing techniques to formulate possible causes of  
20 mismodeling associated with the models employed in the tracking  
21 process or other physical phenomena. The present invention also  
22 contemplates using the fuzzy logic based model assessment system

1 10 to assess models of other types of physical phenomena that can  
2 be measured.

3 The fuzzy logic based model assessment system 10 generally  
4 includes a feature identification module 12, an anomaly  
5 characterization module 14, and a hypothesis formulation and  
6 evaluation module 16. The anomaly characterization module 14 and  
7 the hypothesis formulation and evaluation module 16 together form  
8 a fuzzy inference system 18. The various modules of the present  
9 invention can be implemented using special purpose hardware  
10 and/or one or more suitably programmed general purpose computers.

11 The feature identification module 12 generates evidence for  
12 use in model assessment by identifying features or tracking  
13 anomalies present in measurement residuals. In the exemplary  
14 embodiment, measurement residuals are obtained by detecting the  
15 acoustic signal emitted by the contact or target and generating a  
16 measured data sequence. The difference values between the  
17 measured data sequence and an expected data sequence  
18 corresponding to the model being assessed form a measurement  
19 residual sequence. In the exemplary embodiment, the features  
20 identified in the measurement residuals represent tracking  
21 anomalies, such as jump, drift and curvature. A jump feature  
22 represents a discontinuity in a measured tracking signal. A

1 drift feature represents a generally linear drift of the measured  
2 tracking signal. A curvature feature represents a non-linear  
3 drift of the signal.

4 The measurement residuals are assumed to have a zero-mean  
5 Gaussian distribution when the correct tracking model is  
6 employed. Thus, deviations from a random white noise sequence in  
7 the measurement residuals indicates the presence of mismodeling.  
8 The evidence generated by the feature identification module 12  
9 includes the amplitudes of the identified features, representing  
10 the strength of the features and includes the standard deviation  
11 of the amplitudes, representing a probabilistic description of  
12 the uncertainty associated with the feature strength.

13 The fuzzy inference system 18 then applies fuzzy logic based  
14 inferencing to characterize and interpret this evidence and to  
15 formulate possible causes of mismodeling in the system models  
16 (i.e., mismodeling hypotheses) and to generate fuzzy measures of  
17 certainty in the mismodeling hypotheses. The fuzzy measure of  
18 certainty is used to evaluate the confidence associated with the  
19 different mismodeling hypotheses and can be used, for example, to  
20 generate a tactical picture.

21 The anomaly characterization module 14 within the fuzzy  
22 inference system 18 characterizes the features or anomalies in

1 terms of fuzzy input class memberships. The input class  
2 memberships represent the strength of the feature or tracking  
3 anomaly and include null (feature not present), weak, moderate  
4 and strong. The uncertainty in the feature amplitudes, as  
5 described by the standard deviation, results in a membership  
6 function of amplitude as opposed to a finite value. Thus, the  
7 anomaly characterization module 14 uses interval-valued fuzzy  
8 logic to handle the possible variability in the input data to the  
9 fuzzy inference system 18. The uncertainty in the input data  
10 results in an interval-valued set membership where the feature  
11 amplitude belongs to a particular class within a membership  
12 interval, as opposed to a finite membership value, as will be  
13 described in greater detail below.

14 The hypothesis formulation and evaluation module 16 within  
15 the fuzzy inference system 18 determines mismodeling hypotheses  
16 through the application of fuzzy inferencing to the anomaly  
17 characterizations, or input class memberships. The hypothesis  
18 formulation and evaluation module 16 also computes certainties  
19 associated with the various possible hypotheses and preferably  
20 provides fuzzy measures of confidence in each particular  
21 hypothesis.

1           According to the preferred embodiment, the hypothesis  
2 formulation and evaluation module 16, FIG. 2, is a fuzzy  
3 inference engine having a knowledge base 20 including a plurality  
4 of heuristic rules that are derived from problem-domain  
5 experience and expertise. Each rule is an IF-THEN relationship  
6 that infers possible causes of mismodeling (i.e., mismodeling  
7 hypotheses) based on combinations of observed effects (i.e.,  
8 features or tracking anomalies). In one example, the heuristics  
9 for fuzzy inferencing are formulated based on prior work and  
10 model assessment using, for example, a combination of  
11 perturbation analysis (both numerical and analytical) and expert  
12 knowledge to form compatibility maps for Dempster-Shafer  
13 evidential reasoning methods. The rules in the knowledge base 20  
14 are then derived from the compatibility maps.

15           An inferencing module 22 triggers one or more of the rules  
16 in the knowledge base 20 based upon the input class memberships  
17 and selects one or more mismodeling hypotheses by applying the  
18 rules to the input class memberships. A given combination of  
19 inputs, such as input class memberships and class membership  
20 intervals, can trigger several rules. An aggregation module 24  
21 combines the outputs of the rules applied by the inferencing

1 module 22 to evaluate the possible hypotheses in terms of their  
2 associated certainty.

3 The operation of the fuzzy logic based model assessment  
4 system 10 will be described in greater detail in connection with  
5 FIGS. 4 through 12. The method of assessing a model using the  
6 fuzzy logic based model assessment system 10, FIG. 4, begins by  
7 providing measurement residual values to the feature  
8 identification module 12, step 102. The feature identification  
9 module 12 then identifies the features present in the measurement  
10 residual values, step 104, and generates a feature amplitude  
11 value and feature amplitude standard deviation value for each  
12 feature identified, step 106.

13 According to one example, statistical methods are used to  
14 identify the features present in the measurement residual  
15 sequence. The features are extracted from a regression fit of a  
16 second-order polynomial to the measurement residuals, as  
17 disclosed in greater detail in U.S. Patent No. 5,581,490 to  
18 Ferkinhoff et al., incorporated herein by reference. The  
19 coefficients of the regression fit are the jump, drift and  
20 curvature features, together with their associated uncertainties  
21 as represented by the covariance matrix.

22 One example of a measurement residual sequence representing

1 the difference between a measured data sequence and an expected  
2 data sequence is shown in FIG. 5. When the measurement residual  
3 sequence, according to this example, is processed by the feature  
4 identification module 12, jump and drift features are identified  
5 in the measurement residual sequence having respective amplitudes  
6  $j=0.11$  and  $d=0.12$ , and respective standard deviations of  $\sigma_j=0.01$   
7 and  $\sigma_d=0.02$ . A graphical illustration of the amplitude values  
8 and standard deviations for the identified jump and drift  
9 features is shown in FIG. 6.

10 The peak value of the Gaussian distribution for the features  
11 of  $N(\text{mean}, \text{std\_dev})$  is then normalized to unity according to the  
12 equation:

$$13 \quad \eta(\bar{\chi}, \sigma) = N(\bar{\chi}, \sigma) * \sqrt{2\pi\sigma} \quad (1)$$

14 The resulting normalized anomaly distributions for the jump  
15 feature  $\mu_j(j) = \eta(0.11, 0.01)$  and the drift feature  $\mu_d(d) = \eta(0.12, 0.03)$  are  
16 shown in FIGS. 7A and 7B respectively.

17 The feature amplitude values and the feature amplitude  
18 standard deviation values constitute the tracking anomaly  
19 evidence that is input to the fuzzy inference system 18. The  
20 anomaly characterization module 14 characterizes the identified  
21 features in one or more membership classes based upon the feature

1 amplitude values, step 108. In a conventional Boolean logic  
2 approach, the membership classes or term sets are separated by  
3 hard limits or "crisp" boundaries in that a particular feature  
4 amplitude value belongs to one and only one class, as shown in  
5 FIG. 8A. In the fuzzy logic approach of the present invention,  
6 the amplitude values can belong to more than one class with  
7 varying degrees of membership, as shown in FIG. 8B. In the  
8 example shown, the jump feature having amplitude value  $j=0.11$  has  
9 memberships  $\mu_{NULL}(j)=0.4$  in the set null and  $\mu_{WEAK}(j)=0.6$  in the set  
10 weak, respectively.

11 The anomaly characterization module 14 also generates class  
12 membership interval values for each membership class based upon  
13 the feature amplitude standard deviation values, step 110. The  
14 class membership interval values include a lower limit  $N$ , denoted  
15 as necessity, which represents the smallest necessary extent to  
16 which the feature amplitude belongs to the membership class, and  
17 an upper limit  $P$ , denoted as possibility, which represents the  
18 greatest possible extent to which the feature amplitude belongs  
19 to the membership class. The lower limit  $N$  and upper limit  $P$  are  
20 calculated as follows:

1 Let  $\mu_M(\chi)$  represent the membership function of input data M over  
 2 variable  $\chi \in X$ . Then membership interval of data M in term set T  
 3 is

$$4 \quad \mu_T(M) = [N, P] = [N_T(M), P_T(M)] \quad (2)$$

5 where

$$6 \quad \text{possibility } P = P_T(M) \equiv \sup_{\forall \chi \in X} [\min(\mu_M(\chi), \mu_T(\chi))] \quad (3)$$

7 represents the greatest possible extent to which data M  
 8 belongs to term set T; and

$$9 \quad \text{necessity } N = N_T(M) \equiv \inf_{\forall \chi \in X} [\max(\mu_{\bar{M}}(\chi), \mu_T(\chi))] \quad (4)$$

10 represents the smallest necessary extent to which data M  
 11 belongs to term set T.

12 Here,  $\bar{M}$  is defined as the complement of set M:

$$13 \quad \mu_{\bar{M}}(\chi) = 1 - \mu_M(\chi) \quad (5)$$

14 In the example having the jump distribution  $\mu_j(j) = \eta(0.11, 0.01)$ ,  
 15 the membership interval values include  $\mu_{NULL}(J) = [0.31, 0.52]$  in the  
 16 set null (compared with membership 0.4 in null for the discrete  
 17 value of  $j=0.11$ ), and  $\mu_{WEAK}(J) = [0.48, 0.68]$  in the set weak (compared  
 18 with membership 0.6 in weak for the discrete value of  $j=0.11$ ).  
 19 The possibility values according to this example are shown in

1 FIG. 9A and the necessity values according to this example as  
2 shown in FIG. 9B.

3 The hypothesis formulation and evaluation module 16 then  
4 determines one or more mismodeling hypotheses by applying fuzzy  
5 inferencing to the class memberships, step 112. According to one  
6 example, the knowledge base 20 includes rules for a sphere-  
7 bearing measurement type. A sphere-bearing is the azimuthal  
8 angle from an observer to a contact or target with the direction  
9 north as a zero reference measured, for example, by sonar on a  
10 submarine hull. For a sphere-bearing measurement type, the  
11 possible mismodeling hypotheses include a null hypothesis (H0), a  
12 base frequency shift (BF) where the fundamental acoustic  
13 frequency of sound waves emitted by the contact has shifted, a  
14 propagation path change (PP) where the mode of traversal of the  
15 sound waves from the contact to the observer (e.g., the direct  
16 path or bottom bounce path) has changed, and contact maneuver  
17 (CM) where the contact has changed in course and/or speed, and  
18 unknown (UK). Examples of the fuzzy inference rules that infer  
19 one or more of these mismodeling hypotheses based upon the  
20 features or tracking anomalies are as follows:

21 1. IF ((jump is strong) OR (drift is strong)) THEN  
22 (hypothesis is UK)

- 1 2. IF (((jump is moderate) OR (jump is weak)) AND ((drift is  
2 moderate) OR (drift is weak))) THEN (hypothesis is CM).
- 3 3. IF (((jump is moderate) OR (jump is weak) AND (drift is  
4 null)) THEN (hypothesis is CM)
- 5 4. IF ((jump is null) AND ((drift is moderate) OR (drift is  
6 weak))) THEN (hypothesis is CM)
- 7 5. IF ((jump is null) AND (drift is null)) THEN ((hypothesis  
8 is HO) OR (hypothesis is PP) or (hypothesis is BF))

9 The mapping of these rules applied to sphere-bearing  
10 measurement types is shown in FIG. 10. Note that the output  
11 hypotheses boundaries are not crisp as shown, rather they  
12 represent the crossover lines in the transition from one class to  
13 the next.

14 The hypothesis formulation and evaluation module 16 also  
15 generates one or more certainty values representing a degree of  
16 certainty in the mismodeling hypotheses, step 114. Processing a  
17 sphere-bearing measurement residual sequence, for example, using  
18 anomaly amplitudes only with the conventional Boolean approach  
19 results in the CM hypothesis with a probability of 1, as shown in  
20 FIG. 11A. The fuzzy logic approach of the present invention  
21 results in 2 alternative hypotheses: CM with certainty 0.6 and  
22 (HO or BF or PP) with certainty 0.3, as shown in FIG. 11B. The

1 computational process from single-valued fuzzy logic is as  
2 follows:

3 Let  $\mu_{T_1}(m_1)$  be the membership value of data-point  $m_1$  in term  
4 set  $T_1$ .

5 Let  $\mu_{T_2}(m_2)$  be the membership value of data-point  $m_2$  in term  
6 set  $T_2$ .

7 Consider the heuristic rule: IF (( $m_1$  is  $T_1$ ) .AND. ( $m_2$  is  $T_2$ ))  
8 THEN (hypothesis is  $H_1$ )

9 Then premise  $A=(m_1$  is  $T_1$ ) .AND. ( $m_2$  is  $T_2$ )) has the strength  
10 value:

$$11 \quad \nu(A) \equiv [AND(\mu_{T_1}(m_1), \mu_{T_2}(m_2))] \quad (6)$$

12 And conclusion  $B=($ hypothesis is  $H_1)$  has the certainty value:

$$13 \quad \nu(B) \equiv [AND(\nu(A), \nu(A \rightarrow B))] \quad (7)$$

14 where  $\nu(A \rightarrow B)$  denotes the strength of the rule sufficiency: IF  
15 (premise  $A$ ) THEN (conclusion  $B$ ).

16 Typically the logical AND operator is the *min* function, while  
17 the rule sufficiency  $\nu(A \rightarrow B)=1$ . This results in the certainty  
18 of *conclusion B* being equal to the strength of *premise A*; that  
19 is,  $\nu(B) = \nu(A)$ .

20 In the fuzzy logic based model assessment system 10 of the  
21 present invention, the anomaly distributions are preferably

1 handled using an interval-valued fuzzy logic approach. The class  
 2 membership interval values for a particular anomaly distribution  
 3 in an input class are propagated through the fuzzy inference  
 4 engine 16 to provide certainty intervals pertaining to the  
 5 feasible mismodeling hypotheses, as shown in FIG. 12B. The  
 6 certainty interval is a range of certainty on a particular  
 7 mismodeling hypothesis and indicates the fuzzy confidence in that  
 8 hypothesis.

9 The method for propagating membership class interval values  
 10 through the inferencing module 22 of the fuzzy inference engine  
 11 to generate certainty interval values is as follows:

12 Let  $\mu_{T_1}(M_1) = [N_{T_1}(M_1)P_{T_1}(M_1)]$  be the membership interval of data-  
 13 set M1 in term set T1.

14 Let  $\mu_{T_2}(M_2) = [N_{T_2}(M_2)P_{T_2}(M_2)]$  be the membership interval of data-  
 15 set M2 in term set T2.

16 Consider the heuristic rule: IF ((M1 is T1) .AND. (M2 is T2))  
 17 THEN (hypothesis is H1).

18 This rule is of the form: IF (premise A) THEN (conclusion B).

19 The premise A = ((M1 is T1) .AND. (M2 is T2)) has the strength  
 20 interval:

21 
$$[\nu_L(A), \nu_U(A)] \equiv [AND(N_{T_1}(M_1), N_{T_2}(M_2)), AND(P_{T_1}(M_1), P_{T_2}(M_2))] \quad (8)$$

1 The conclusion B=(hypothesis is H1) has the certainty  
2 interval:

$$3 \quad [\nu_L(B), \nu_U(B)] \equiv [AND(\nu_L(A), \nu(A \rightarrow B)), OR(\nu_U(A), 1 - \nu(B \rightarrow A))] \quad (9)$$

4 where  $\nu(A \rightarrow B)$  denotes the strength of the rule *sufficiency*:

5 IF (premise A) THEN (conclusion B)

6 and  $\nu(B \rightarrow A)$  denotes the strength of the rule *necessity*: IF

7 (conclusion B) THEN (premise A)

8 Typically, the logical AND and OR operators are implemented  
9 with the *min* and *max* functions, while the rule sufficiency

10  $\nu(A \rightarrow B) = \text{necessity } \nu(B \rightarrow A) = 1$ . This results in a simplified

11 expression for the certainty interval of *conclusion B*;

12 Equation (9) reduces to the equivalent of the strength of

13 *premise A*. That is,  $[\nu_L(B), \nu_U(B)] = [\nu_L(A), \nu_U(A)]$ .

14 When multiple rules are triggered to give the same  
15 conclusion or *mismodeling hypothesis* with different levels of  
16 certainty, the certainty values are aggregated by the aggregation  
17 module 24 to provide a composite certainty value on the output  
18 conclusion. Using single-valued fuzzy logic (FIG. 11B), the  
19 logical OR is used to aggregate the different certainties, i.e.,  
20  $C = \max(C1, C2, C3 \dots)$ . Where certainty intervals  $[L1, U1]$ ,  $[L2,$   
21  $U2]$ ,  $[L3, U3] \dots$  are generated using interval valued fuzzy logic

1 and interval valued membership inputs (FIG. 12B), the aggregated  
2 certainty interval on the output conclusion is [L, U] where the  
3 lower limit,  $L = \max(L_1, L_2, L_3 \dots)$  and the upper limit  $U = \max(U_1,$   
4  $U_2, U_3 \dots)$ .

5 In the example above, the jump amplitude distribution of  
6  $\mu_j(j) = \eta(0.11, 0.01)$  results in fuzzy input class membership intervals  
7 of  $\mu_{NULL}(J) = [0.31, 0.52]$  and  $\mu_{WEAK}(J) = [0.48, 0.68]$  and the drift amplitude  
8 distribution of  $\mu_D(d) = \eta(0.12, 0.03)$  results in membership intervals  
9 of  $\mu_{NULL}(D) = [0.14, 0.60]$  and  $\mu_{WEAK}(D) = [0.40, 0.86]$ . The propagation of  
10 these interval valued memberships through the fuzzy inference  
11 engine gives the hypothesis CM with certainty interval [.40,  
12 0.68] and the hypothesis (HO OR BF OR PP) with certainty interval  
13 [0.14, 0.52]. The hypotheses and certainty intervals for this  
14 example are shown in FIG. 12B. In contrast, conventional  
15 Bayesian analysis results in a hypothesis CM with probability  
16 0.96 and hypothesis (HO OR BF OR PP) with probability 0.04, as  
17 shown in FIG. 12A.

18 Accordingly, the fuzzy logic based model assessment system  
19 of the present invention uses heuristic domain knowledge and  
20 fuzzy logic reasoning to assess a model of a physical process or  
21 phenomena even if there is a high degree of conflict in the

1 evidence. Input data uncertainty as represented by the standard  
2 deviation of the anomaly or feature amplitudes is characterized  
3 by interval-valued memberships in fuzzy input classes and is  
4 propagated to output information certainty, expressed in terms of  
5 certainty intervals on the mismodeling hypothesis.

6 In light of the above, it is therefore understood that  
7 , the invention may be  
8 practiced otherwise than as specifically described.

1 Attorney Docket No. 78610

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3

FUZZY LOGIC BASED MODEL ASSESSMENT SYSTEM

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AND METHOD FOR CONTACT TRACKING

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ABSTRACT OF THE DISCLOSURE

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A fuzzy logic based model assessment system assesses models

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of physical phenomena and in one example, is used for contact

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tracking. The system uses measurement residual values

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representing the difference between a measured data sequence

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corresponding to the physical phenomena and an expected data

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sequence corresponding to the model to be assessed. The system

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includes a feature identification module for identifying one or

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more features or tracking anomalies in the measurement residual

15

values, such as jump and drift, and for generating feature

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amplitude values and feature amplitude standard deviation values.

17

An anomaly characterization module characterizes the features in

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one or more membership classes representing the strength of the

19

identified feature and generates class membership intervals

20

representing a range of degrees of membership in each of the

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classes (e.g., null, weak, moderate or strong). A hypothesis

22

formulation and evaluation module determines one or more possible

1 causes of mismodeling by applying fuzzy inferencing to the class  
2 memberships, and generates hypothesis certainty intervals  
3 representing a range of degrees of certainty of the mismodeling  
4 hypothesis based on the class membership intervals. A knowledge  
5 base of heuristic rules are used to infer the mismodeling  
6 hypotheses based upon the membership classes.

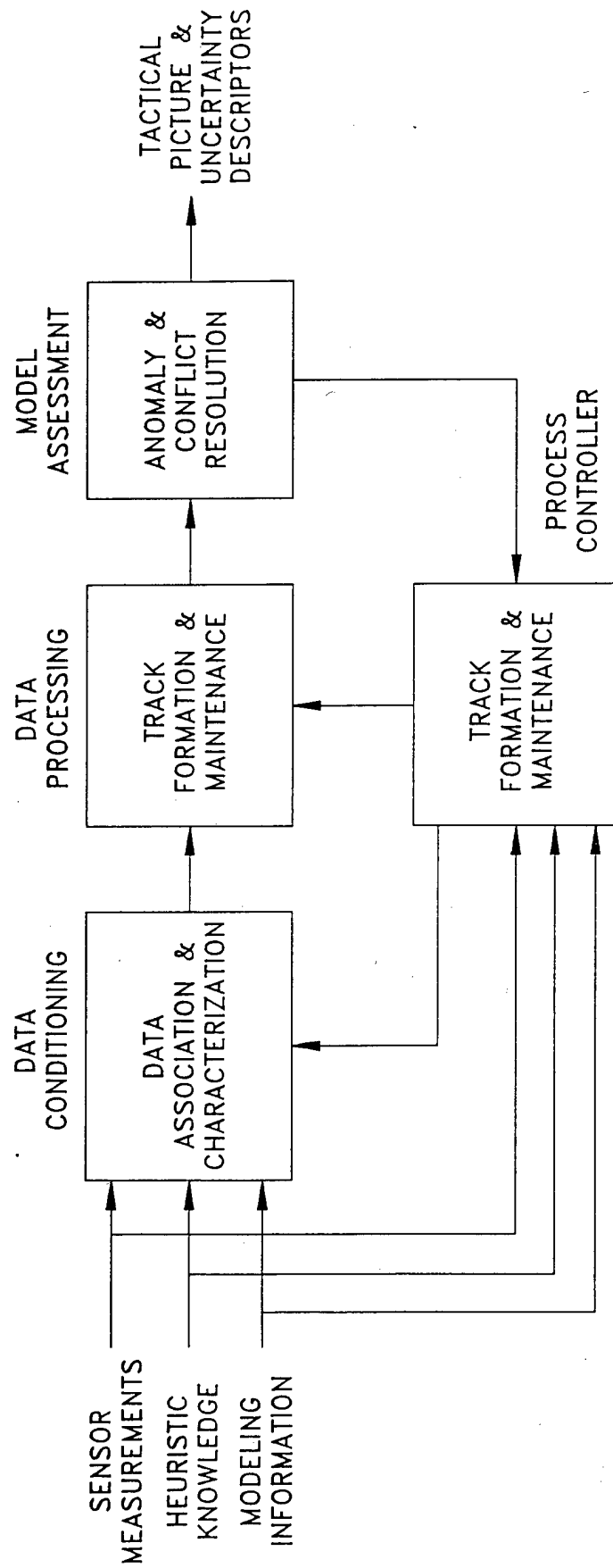


FIG. 1  
(PRIOR ART)

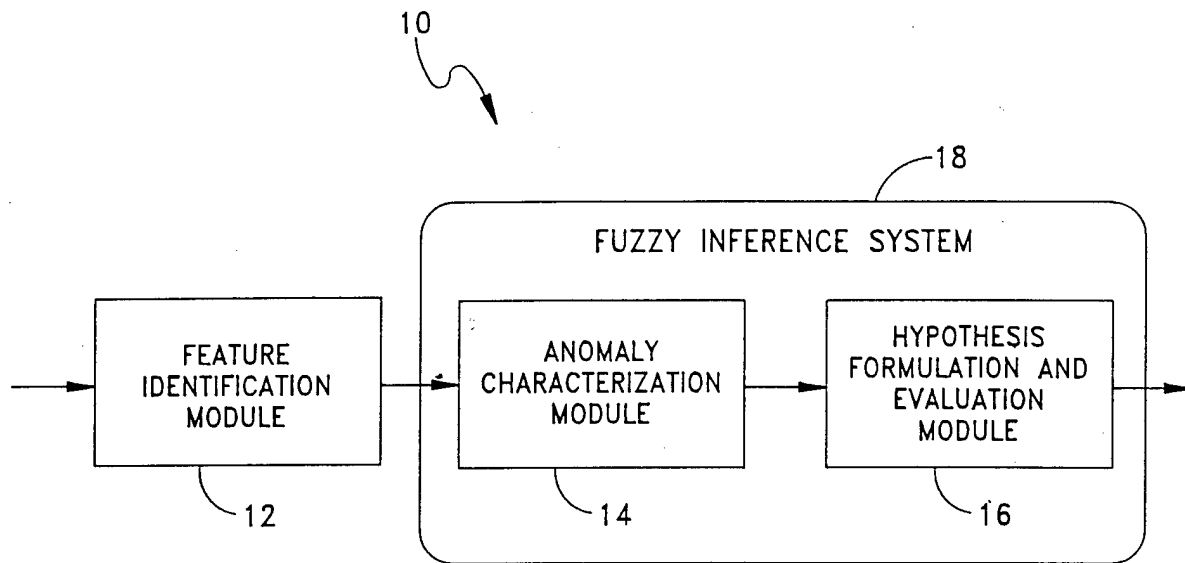


FIG. 2

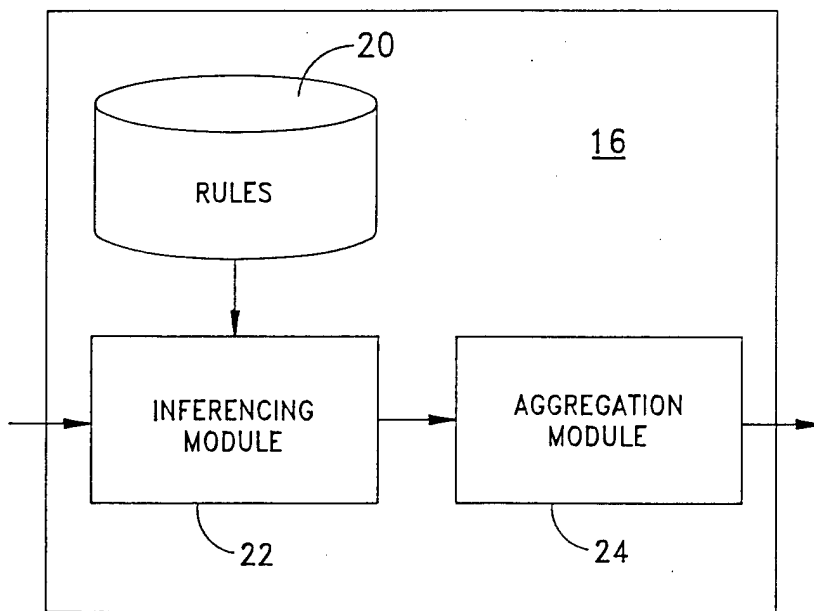


FIG. 3

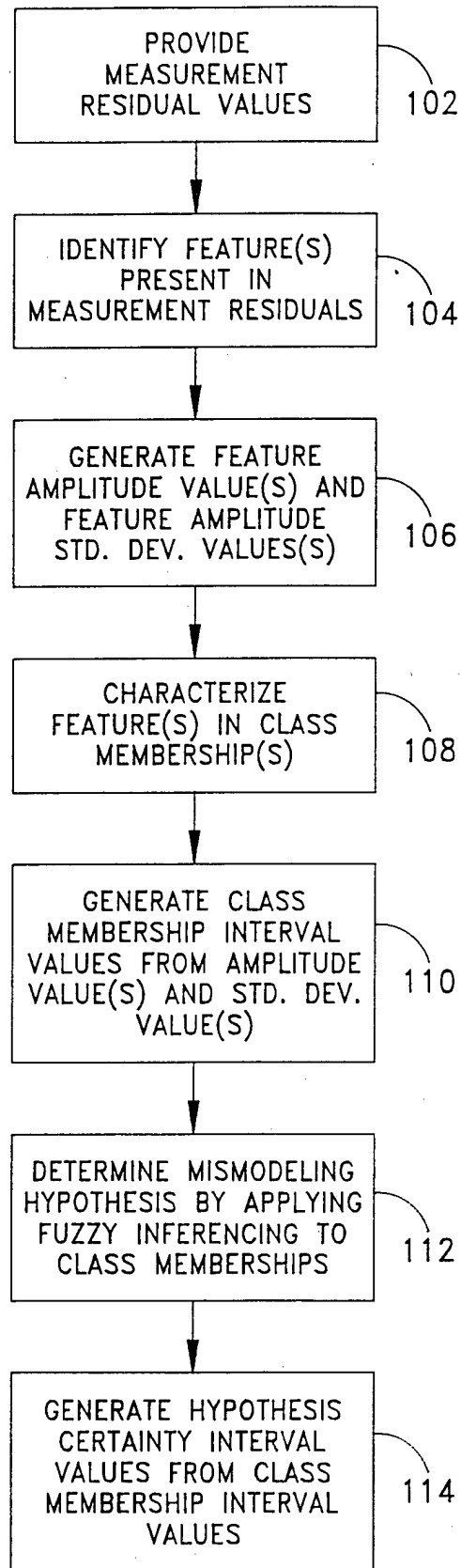


FIG. 4

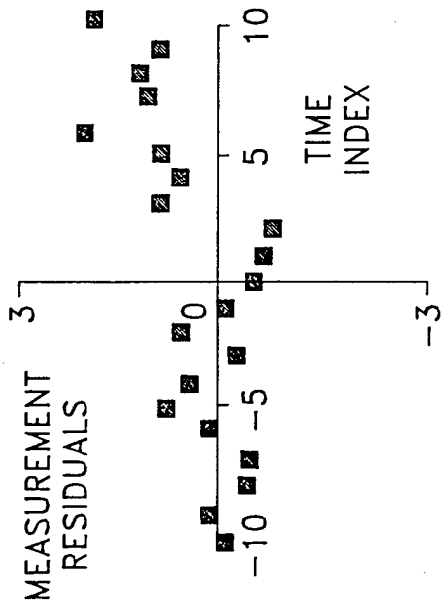


FIG. 5

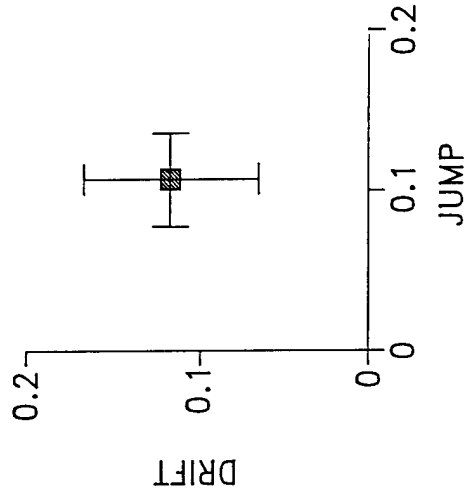


FIG. 6

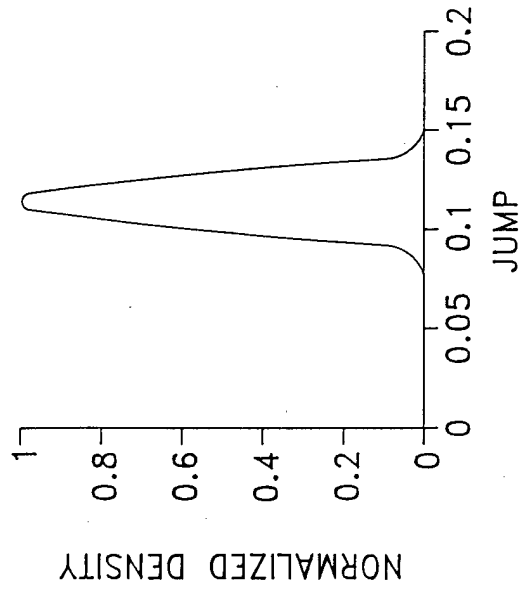


FIG. 7A

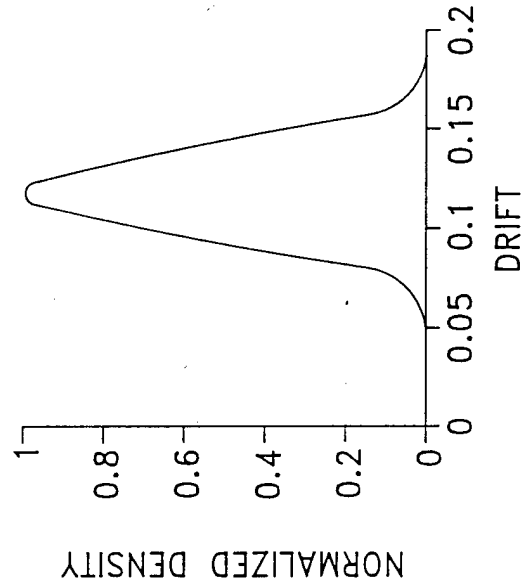


FIG. 7B

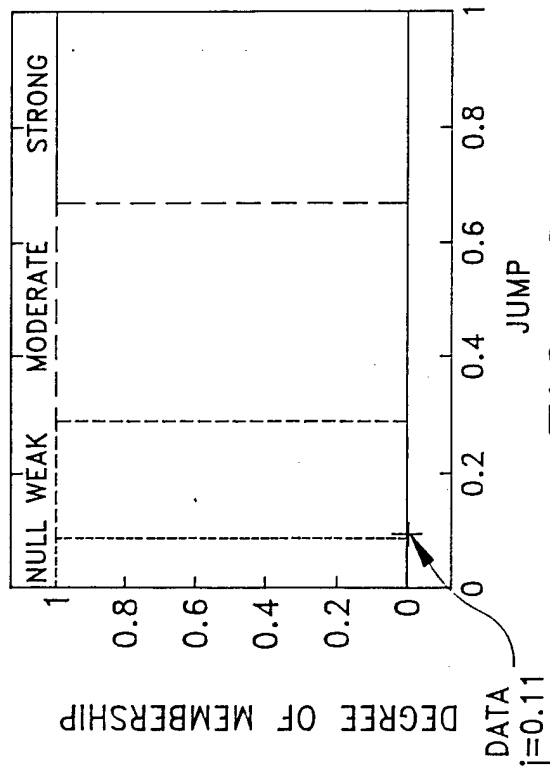


FIG. 8A

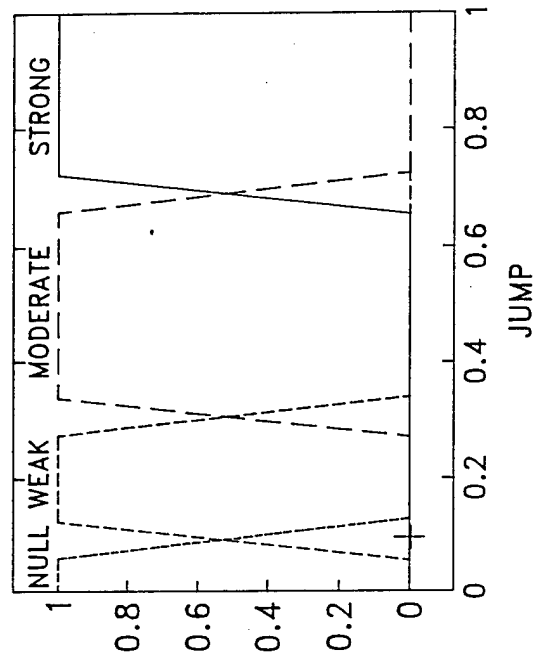


FIG. 8B

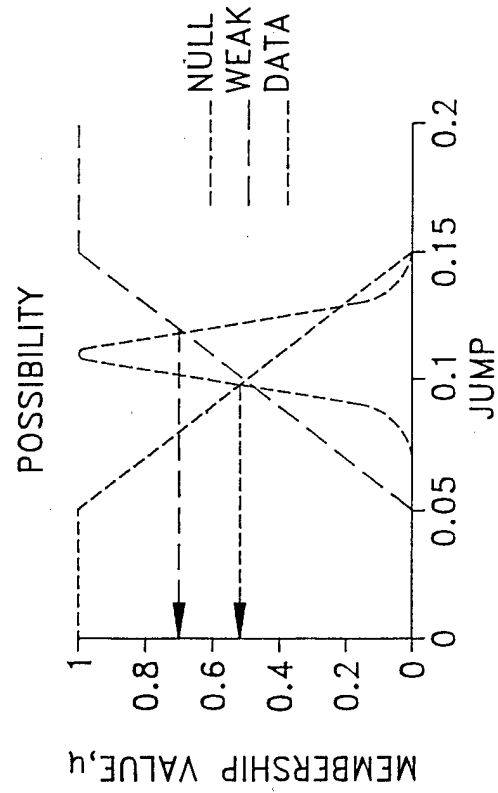


FIG. 9A

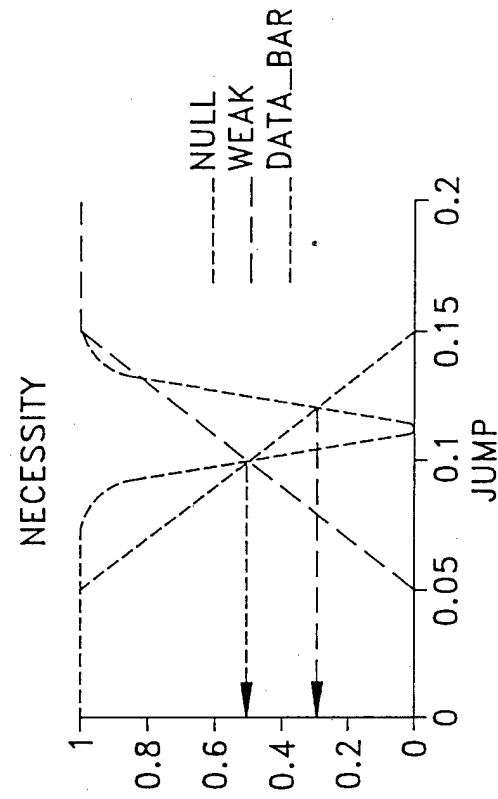


FIG. 9B

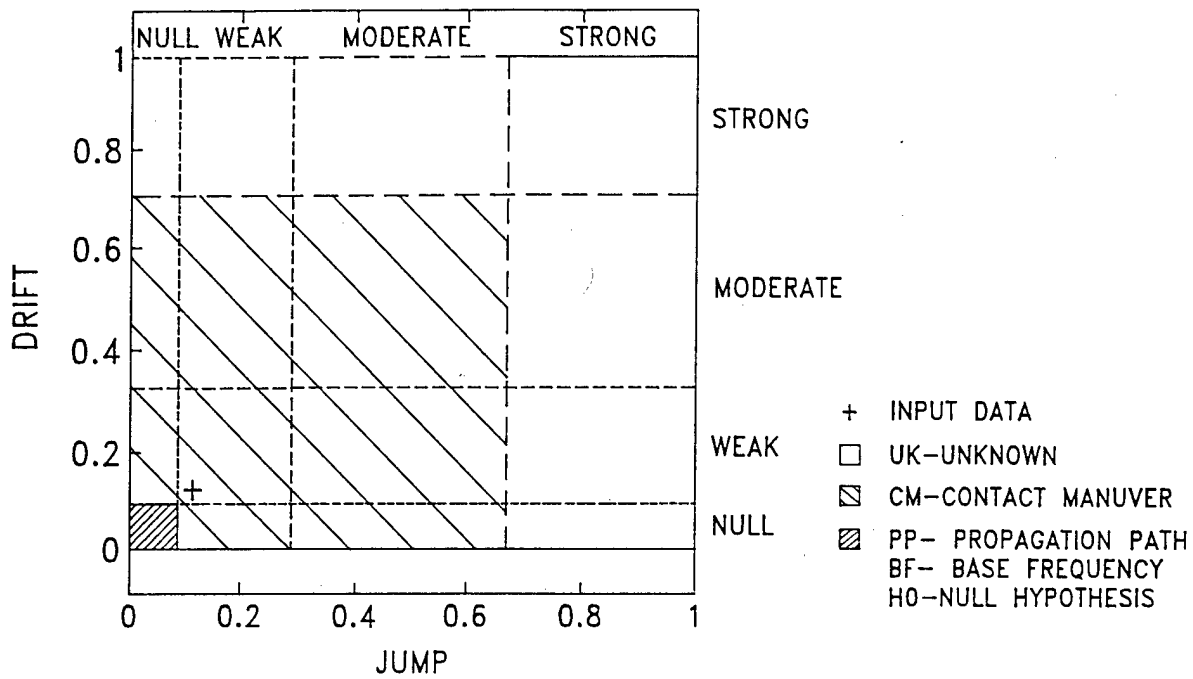


FIG. 10

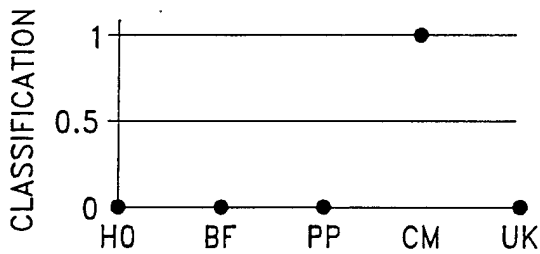


FIG. 11A

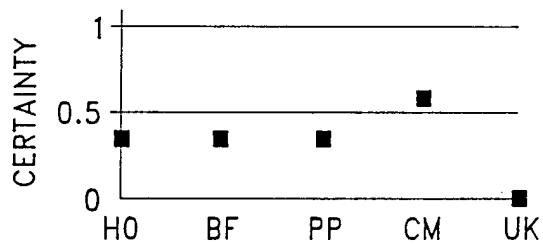


FIG. 11B

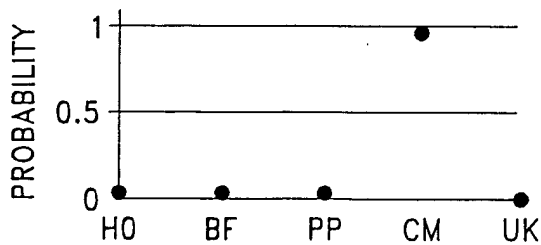


FIG. 12A

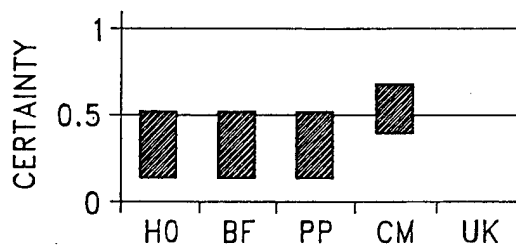


FIG. 12B