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Plasma Phase Transition in Dense Hydrogen and Electron-Hole Plasmas

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Plasma phase transitions (PPT) in dense hydrogen and electron-hole plasmas are investigated by direct path integral Monte Carlo methods (DPIMC). The phase boundary of the electron-hole liquid in Germanium is calculated and is found to agree reasonably well with the known experimental results. Analogous results are found for high-density hydrogen. For a temperature of $T = 10,000\text{K}$ it is shown that the internal energy is lowered due to droplet formation for densities between 10^{23}cm^{-3} and 10^{24}cm^{-3} .

1. Path integral Monte Carlo simulations

All thermodynamic properties of a two-component plasma are defined by the partition function Z which, for the case of N_e electrons and N_p protons, is given by $Z(N_e, N_p, V, \beta) = \frac{Q(N_e, N_p, \beta)}{N_e! N_p!}$, with $Q(N_e, N_p, \beta) = \sum_{\sigma} \int d\mathbf{q} d\mathbf{r} \rho(\mathbf{q}, \mathbf{r}, \sigma; \beta)$, where $\beta = 1/k_B T$. The exact density matrix is, for a quantum system, in general, not known but can be constructed using a path integral representation $[1, 2] \int_V dR^{(0)} \sum_{\sigma} \rho(R^{(0)}, \sigma; \beta) = \int_V dR^{(0)} \dots dR^{(n)} \rho^{(1)} \cdot \rho^{(2)} \dots \rho^{(n)} \times \sum_{\sigma} \sum_P (\pm 1)^{\kappa_P} S(\sigma, \hat{P}\sigma') \hat{P} \rho^{(n+1)}$, where $\rho^{(i)} \equiv \rho(R^{(i-1)}, R^{(i)}; \Delta\beta) \equiv \langle R^{(i-1)} | e^{-\Delta\beta \hat{H}} | R^{(i)} \rangle$, whereas $\Delta\beta \equiv \beta/(n+1)$ and $\Delta\lambda_a^2 = 2\pi\hbar^2 \Delta\beta/m_a$, $a = p, e$. $\hat{H}$ is the Hamilton operator, $\hat{H} = \hat{K} + \hat{U}_c$, containing kinetic and potential energy contributions, $\hat{K}$ and $\hat{U}_c$, respectively, with $\hat{U}_c = \hat{U}_p^e + \hat{U}_e^e + \hat{U}_e^p$ being the sum of the Coulomb potentials between protons (p), electrons (e) and electrons and protons (ep). Further, σ comprises all particle spins, and

the particle coordinates are denoted by $R^{(i)} = (q^{(i)}, r^{(i)}) \equiv (R_p^{(i)}, R_e^{(i)})$, for $i = 1, \dots, n+1$, $R^{(0)} \equiv (q, r) \equiv (R_p^{(0)}, R_e^{(0)})$, and $R^{(n+1)} \equiv R^{(0)}$ and $\sigma' = \sigma$. This means, the particles are represented by fermionic loops with the coordinates (beads) $[R] \equiv [R^{(0)}; R^{(1)}; \dots; R^{(n)}; R^{(n+1)}]$, where q and r denote the electron and proton coordinates, respectively. The spin gives rise to the spin part of the density matrix S , whereas exchange effects are accounted for by the permutation operator $\hat{P}$, which acts on the electron coordinates and spin projections, and the sum over the permutations with parity κ_P . To compute thermodynamic functions, the logarithm of the partition function has to be differentiated with respect to thermodynamic variables, so for internal energy E we have $\beta E = -\beta \ln Q / \partial \beta$

2. Numerical Results

Since the PPT in dense hydrogen is still hypothetical and has not been observed experimentally, it is reasonable to look for other systems where similar conditions exist. A suitable example is electron-hole plasma in low-temperature semiconductors, for which droplet formation is well established and observed ex-

perimentally three decades ago [3]. We, therefore, performed DPIMC simulations for electron hole plasmas. Below the critical temperature the simulations exhibit anomalously large fluctuations and an unstable behavior of the pressure. The e-h-plasma is found to phase separate and form large droplets. The phase boundary of the electron-hole liquid (e-h-droplets) in Germanium obtained by our DPIMC method is presented in Fig. 1 together with the experimental data. We observe good agreement. Deviations may be connected with complex band structure of Germanium approximated in our simulations by a two-band parabolic mass model.

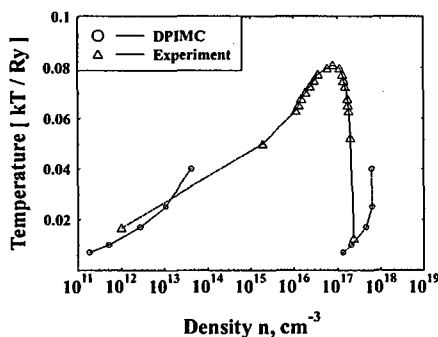


Figure 1: Phase boundary of the electron-hole liquid in bulk Germanium. Experiment - [3]. Temperature is presented in units of the exciton binding energy.

Fig.2 presents results of our calculations for pressure and energy of hydrogen at $T = 10,000K$, which is well below the critical point of the PPT predicted by chemical models (around $T = 15,000K$). In our calculations between $10^{22}cm^{-3}$ and $10^{24}cm^{-3}$ calculated pressure becomes negative. We find also that in this region plasma energy is systematically lower than the RPIMC results [4]. If average distance be-

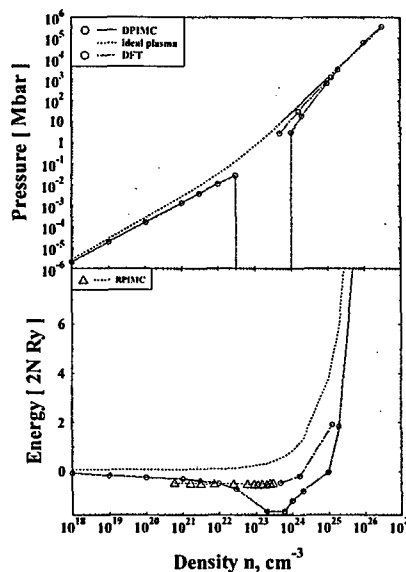


Figure 2: Pressure and energy of hydrogen for $T = 10,000K$, DFT - [5], RPIMC - [4].

tween plasma particles is of the order of the size of a hydrogen molecule the homogeneous plasma state becomes unstable, and many-particle clusters appear. Results of one independent well tested method based on density functional theory (DFT) are presented on Fig. 2, where PPT was obtained at smaller density [5].

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